Assignment 3

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Download all python codes from

https://github.com/Dontha−Aarthi/AI1103/tree/main/Assignment3/Codes

and latex-tikz codes from

https://github.com/Dontha−Aarthi/AI1103/blob/main/Assignment3/main.tex

1 Problem

(GATE 2019-XE Q.no 1 (Page Number:4)

Let X be the Poisson random variable with parameter $\lambda = 1$. Then, the probability $\Pr(2 \le X \le 4)$ equals .....

2 solution

Let

$$X \in \{0, 1, 2, 3, 4, 5...\} \tag{2.0.1}$$

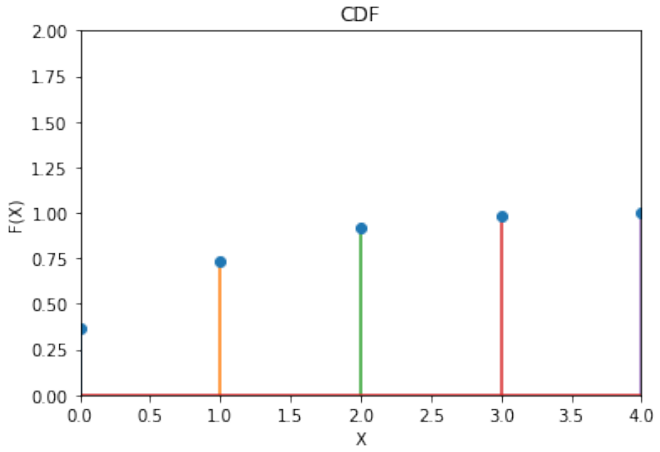
We know that, for a poisson random variable X with a given parameter λ, probability of $X = k$ is:

$$\Pr(X = k) = \left(\frac{\lambda^k e^{-\lambda}}{k!}\right) \tag{2.0.2}$$

The graph of CDF is shown below

x	0	1	2	3	4
$F(X)$	1/e	2/e	5/2e	8/3e	65/24e

TABLE 0: CDF



And also,

$$\Pr(x < X \le y) = F(y) - F(x) \tag{2.0.3}$$

So, now we can find the value of $\Pr(2 \le X \le 4)$ and also its given that λ=1.
We can represent the value of $\Pr(2 \le X \le 4)$ as $\Pr(1 \le X \le 4)$.

Now by using 2.0.3,

$$\begin{aligned}\Pr(2 \le X \le 4) &= \Pr(1 < X \le 4)\\ &= F(4) - F(1)\\ &= \frac{65}{24e} - \frac{2}{e}\\ &= \frac{17}{24e}\end{aligned} \tag{2.0.4}$$

The graph for theoretical result vs simulation is given below