Before you turn this problem in, make sure everything runs as expected. First, **restart the kernel** (in the menubar, select Kernel→Restart) and then **run all cells** (in the menubar, select Cell→Run All).

Make sure you fill in any place that says "Write your answer here.", as well as your name and NetID below:

```
In [1]:
```

```
NAME = "Ma Zicheng"
NetID = "zicheng5"
```

Submission Instructions

- This lab has two components: the coding component as well as a report (text written) component.
- The coding component comprises Q1.1, Q1.2, Q1.3. You will be writing the code for these questions in the file lab4.py. The grading for this component will take place through the gradescope autograder by submitting the lab4.py file to the **NLP Lab4 Code** assignment on Gradescope.
- The report component comprises Q1.4, Q1.5, Q2.1, Q2.2, Q2.3, Q2.4, Q2.5, Q2.6, Q2.7, Q2.8.
- The report component comprises three kinds of questions: Code+Plot, Code+Written and Written. For the Code+Plot (e.g Q1.4) type you will be graded for the code you write and the corresponding plot produce. For the Code+Written(e.g Q2.7) type you will be graded for the code you write and the corresponding written response. For the Written(e.g Q2.8) type you will be graded for the written response. You can enter the written responses in the corresponding space provided in the jupyter notebook itself, by editing the corresponding markdown cell. Make sure you fill in any place that says "Write your answer here."
- To submit the questions that comprise the report section, you can either convert the jupyter notebook to a pdf by following one of two methods described in the next cell (choose whichever method that produces the best pdf render) or you can take screenshots of the corresponding section of the jupyter notebook, paste the screenshots onto a document (eg .doc) file and then convert to pdf. For the Code+Written and Code+Plot questions, make sure the code cell as well as the written/plot cell is included in the screenshot. For the Written questions, you can only include the written response in your screenshot.
- Once you have prepared the report using either the direct PDF or the screenshot route, submit the
 corresponding file to the Gradescope assignment called NLP Lab4 Report.
- It is extremely important that you tag the corresponding pages of the report to the appropriate
 question outline on gradescope. Failure to tag the appropriate/correct pages can lead to deduction
 of points.

Converting Jupyter Notebook to PDF [Method 1]

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly.

Converting Jupyter Notebook to PDF [Method 2]

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).

- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, run Cmd+P (Ctrl+P on windows) -> Save as PDF.
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly.

Lab4: Word Vectors

```
In [2]:
```

```
# All Import Statements Defined Here
# Note: Do not add to this list.
# All the dependencies you need, can be installed by running.
# Make sure to have scikit-learn version 0.21.3, otherwise you might run into import problems.
# I found it best to create a new conda environment with scikit-learn 0.21.3 installed using the com
# conda create -n lab4_env python=3 scikit-learn==0.21.3
import sys
assert sys. version info[0]==3
assert sys.version_info[1] >= 5
from gensim. models import KeyedVectors
from gensim. test. utils import datapath
import pprint
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = [10, 5]
import nltk
nltk. download('reuters')
from nltk.corpus import reuters
import numpy as np
import random
import scipy as sp
from sklearn.decomposition import TruncatedSVD
from sklearn. decomposition import PCA
START TOKEN = '<START>'
END TOKEN = '<END>'
np. random. seed (0)
random. seed (0)
```

```
[nltk_data] Error loading reuters: <urlopen error [Errno 11004]
[nltk_data] getaddrinfo failed>
```

```
In [3]:
```

```
from importlib import reload import lab4
```

Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from *co-occurrence matrices*, and those derived via *word2vec*.

Assignment Notes: Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

Note on Terminology: The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia (https://en.wikipedia.org/wiki/Word_embedding) states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

Part 1: Count-Based Word Vectors (50 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (<u>Firth, J. R. 1957:11</u> (<u>https://en.wikipedia.org/wiki/John_Rupert_Firth</u>))

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, *co-occurrence matrices* (for more information, see here (https://medium.com/data-science-group-iitr/word-embedding-2d05d270b285)).

Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word w_i occurring in the document, we consider the *context window* surrounding w_i . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document, i.e. words $w_{i-n} \dots w_{i-1}$ and $w_{i+1} \dots w_{i+n}$. We build a *co-occurrence matrix* M, which is a symmetric word-by-word matrix in which M_{ij} is the number of times w_i appears inside w_i 's window.

Example: Co-Occurrence with Fixed Window of n=1:

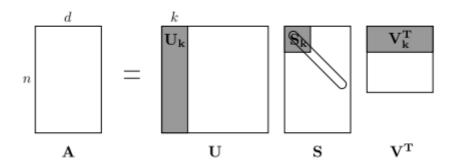
Document 1: "all that glitters is not gold"

Document 2: "all is well that ends well"

*	START	all	that	glitters	is	not	gold	well	ends	END
START	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0
gold	0	0	0	0	0	1	0	0	0	1
well	0	0	1	0	1	0	0	0	1	1
ends	0	0	1	0	0	0	0	1	0	0
END	0	0	0	0	0	0	1	1	0	0

Note: In NLP, we often add START and END tokens to represent the beginning and end of sentences, paragraphs or documents. In thise case we imagine START and END tokens encapsulating each document, e.g., "START All that glitters is not gold END", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on word-word co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run *dimensionality reduction*. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is A with n rows corresponding to n words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal S matrix, and our new, shorter length-k word vectors in U_k .



This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. *doctor* and *hospital* will be closer than *doctor* and *dog*.

Notes: If you can barely remember what an eigenvalue is, here's <u>a slow, friendly introduction to SVD (https://davetang.org/file/Singular_Value_Decomposition_Tutorial.pdf)</u>. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing pre-programmed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k— known as $\underline{Truncated\ SVD}$ (https://en.wikipedia.org/wiki/Singular_value_decomposition#Truncated_SVD)— then there are reasonably scalable techniques to compute those iteratively.

Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see https://www.nltk.org/book/ch02.html (https://www.nltk.org/book/ch02.html). We provide a read_corpus function below that pulls out only articles from the "crude" (i.e. news articles about oil, gas, etc.) category. The function also adds START and END tokens to each of the documents, and lowercases words. You do **not** have to perform any other kind of pre-processing.

In [4]:

```
def read_corpus(category="crude"):
    """ Read files from the specified Reuter's category.
    Params:
        category (string): category name
    Return:
        list of lists, with words from each of the processed files
    """
    files = reuters.fileids(category)
    return [[START_TOKEN] + [w.lower() for w in list(reuters.words(f))] + [END_TOKEN] for f in files.
```

Let's have a look what these documents are like....

In [5]:

```
reuters_corpus = read_corpus()
pprint.pprint(reuters_corpus[:3], compact=True, width=100)
```

```
[['<START>', 'japan', 'to', 'revise', 'long', '-', 'term', 'energy', 'demand', 'd
ownwards', 'the',
  'ministry', 'of', 'international', 'trade', 'and', 'industry', '(', 'miti',
')', 'will', 'revise',
 'its', 'long', '-', 'term', 'energy', 'supply', '/', 'demand', 'outlook', 'by',
  'meet', 'a', 'forecast', 'downtrend', 'in', 'japanese', 'energy', 'demand',
  ', 'ministry',
'officials', 'said', '.', 'miti', 'is', 'expected', 'to', 'lower', 'the', 'proj
ection', 'for',
  'primary', 'energy', 'supplies', 'in', 'the', 'year', '2000', 'to', '550', 'ml
n', 'kilolitres',
  '(', 'kl', ')', 'from', '600', 'mln', ',', 'they', 'said', '.', 'the', 'decisio
n', 'follows', 'the', 'emergence', 'of', 'structural', 'changes', 'in', 'japanese', 'industr
y', 'following',
   the', 'rise', 'in', 'the', 'value', 'of', 'the', 'yen', 'and', 'a', 'decline',
'in', 'domestic',
  'electric', 'power', 'demand', '.', 'miti', 'is', 'planning', 'to', 'work', 'ou
   'a', 'revised',
  'energy', 'supply', '/', 'demand', 'outlook', 'through', 'deliberations', 'of',
'committee',
  meetings', 'of', 'the', 'agency', 'of', 'natural', 'resources', 'and', 'energ
y', ',', 'the',
'officials', 'said', '.', 'they', 'said', 'miti', 'will', 'also', 'review', 'th
e', 'breakdown',
  of', 'energy', 'supply', 'sources', ',', 'including', 'oil', ',', 'nuclear',
 ', 'coal', 'and',
'natural', 'gas', '.', 'nuclear', 'energy', 'provided', 'the', 'bulk', 'of', 'j
apan', "'", 's',
  'electric', 'power', 'in', 'the', 'fiscal', 'year', 'ended', 'march', '31',
  ', 'supplying',
  'an', 'estimated', '27', 'pct', 'on', 'a', 'kilowatt', '/', 'hour', 'basis',
  ', 'followed',
 'by', 'oil',
               '(', '23', 'pct', ')', 'and', 'liquefied', 'natural', 'gas', '(',
'21', 'pct', '),'
  'they', 'noted', '.', '<END>'],
 ['<START>', 'energy', '/', 'u', '.', 's', '.', 'petrochemical', 'industry', 'che
ap', 'oil',
  'feedstocks', ',', 'the', 'weakened', 'u', '.', 's', '.', 'dollar', 'and', 'a',
'plant',
  'utilization', 'rate', 'approaching', '90', 'pct', 'will', 'propel', 'the', 'st
  '.', 's', '.', 'petrochemical', 'industry', 'to', 'record', 'profits', 'this',
year',
  'with', 'growth', 'expected', 'through', 'at', 'least', '1990', ',', 'major',
'company',
  'executives', 'predicted', '.', 'this', 'bullish', 'outlook', 'for', 'chemica
1', 'manufacturing',
  'and', 'an', 'industrywide', 'move', 'to', 'shed', 'unrelated', 'businesses',
'has', 'prompted',
 'gaf', 'corp', '&', 'lt', ';', 'gaf', '>,', 'privately', '-', 'held', 'cain',
'chemical', 'inc',
  ,', 'and', 'other', 'firms', 'to', 'aggressively', 'seek', 'acquisitions', 'o
f', 'petrochemical',
```

```
'plants', '.', 'oil', 'companies', 'such', 'as', 'ashland', 'oil', 'inc', '&',
'lt', ';', 'ash',
      , 'the', 'kentucky', '-', 'based', 'oil', 'refiner', 'and', 'marketer',
  ', 'are', 'also',
  'shopping', 'for', 'money', '-', 'making', 'petrochemical', 'businesses', 'to',
'buy', '.', '"',
'i', 'see', 'us', 'poised', 'at', 'the', 'threshold', 'of', 'a', 'golden', 'per
iod', ', "', 'said',
          'oreffice', ',', 'chairman', 'of', 'giant', 'dow', 'chemical', 'co',
  'paul',
'&', '1t', ';
'dow', '>,'
         , ; ,
'>,', 'adding', ',', '"', 'there', "'", 's', 'no', 'major', 'plant', 'ca
        'being´,
pacity',
  'added', 'around', 'the', 'world', 'now', '.', 'the', 'whole', 'game', 'is', 'b
ringing', 'out',
  'new', 'products', 'and', 'improving', 'the', 'old', 'ones', '."', 'analysts',
'say', 'the'
  'chemical', 'industry', "'", 's', 'biggest', 'customers', ',', 'automobile', 'm
anufacturers',
  'and', 'home', 'builders', 'that', 'use', 'a', 'lot', 'of', 'paints', 'and', 'p
lastics', ',',
  'are', 'expected', 'to', 'buy', 'quantities', 'this', 'year', '.', 'u', '.',
's', '.',
 'petrochemical', 'plants', 'are', 'currently', 'operating', 'at', 'about', '9
0', 'pct',
  'capacity', ',', 'reflecting', 'tighter', 'supply', 'that', 'could', 'hike', 'p
roduct', 'prices'
  'by', '30', 'to', '40', 'pct', 'this', 'year', ',', 'said', 'john', 'dosher',
 ,', 'managing',
 \tt 'director', 'of', 'pace', 'consultants', 'inc', 'of', 'houston', '.', 'demand',
'for', 'some'
  products', 'such', 'as', 'styrene', 'could', 'push', 'profit', 'margins', 'u
p', 'by', 'as',
   \mbox{much}',
          'as', '300', 'pct', ',', 'he', 'said', '.', 'oreffice', ',', 'speakin
   meeting', 'of', 'chemical', 'engineers', 'in', 'houston', ',', 'said', 'dow',
'would', 'easily'
        'the', '741', 'mln', 'dlrs', 'it', 'earned', 'last', 'year', 'and', 'pre
  'top',
dicted', 'it',
  'would', 'have', 'the', 'best', 'year', 'in', 'its', 'history', '.', 'in', '198
         'when',
   oil', 'prices', 'were', 'still', 'above', '25', 'dlrs', 'a', 'barrel', 'and',
'chemical',
  'exports', 'were', 'adversely', 'affected', 'by', 'the', 'strong', 'u', '.',
s', '.', 'dollar', ',', 'dow', 'had', 'profits', 'of', '58', 'mln', 'dlrs', '.', '"', 'i', 'believ
  the',
e', 'the', 'entire', 'chemical', 'industry', 'is', 'headed', 'for', 'a', 'record', 'year',
'or', 'close',
  'to', 'it', ',"', 'oreffice', 'said', '.', 'gaf', 'chairman', 'samuel', 'heyma
n', 'estimated',
  'that', 'the', 'u', '.', 's', '.', 'chemical', 'industry', 'would', 'report',
'a', '20', 'pct',
  'gain', 'in', 'profits', 'during', '1987', '.', 'last', 'year', ',', 'the', 'do
   industry', 'earned', 'a', 'total', 'of', '13', 'billion', 'dlrs', ',', 'a', '5
4', 'pct', 'leap',
  'from', '1985', '.', 'the', 'turn', 'in', 'the', 'fortunes', 'of', 'the', 'onc
e', '-', 'sickly',
  chemical', 'industry', 'has', 'been', 'brought', 'about', 'by', 'a', 'combinat
ion', 'of', 'luck',
  'and', 'planning', ',', 'said', 'pace', "'", 's', 'john', 'dosher', '.', 'doshe
```

```
'last',
r', 'said',
  'year', "'", 's', 'fall', 'in', 'oil', 'prices', 'made', 'feedstocks', 'dramati
cally', 'cheaper',
  'and', 'at', 'the', 'same', 'time', 'the', 'american', 'dollar', 'was', 'weaken
ing', 'against',
  'foreign', 'currencies', '.', 'that', 'helped', 'boost', 'u', '.', 's', '.', 'c
hemical',
  'exports', '.', 'also', 'helping', 'to', 'bring', 'supply', 'and', 'demand', 'i
nto', 'balance'
  'has', 'been', 'the', 'gradual', 'market', 'absorption', 'of', 'the', 'extra',
'chemical',
  'manufacturing', 'capacity', 'created', 'by', 'middle', 'eastern', 'oil', 'prod
ucers', 'in',
  'the', 'early', '1980s', '.', 'finally', ',', 'virtually', 'all', 'major', 'u',
 .', 's',
  'chemical', 'manufacturers', 'have', 'embarked', 'on', 'an', 'extensive', 'corp
orate',
  restructuring, 'program', 'to', 'mothball', 'inefficient', 'plants', ',', 'tr'
im', 'the',
  'payroll', 'and', 'eliminate', 'unrelated', 'businesses', '.', 'the', 'restruct
uring', 'touched',
'off', 'a', 'flurry', 'of', 'friendly', 'and', 'hostile', 'takeover', 'attempt s', '.', 'gaf', ',',
  'which', 'made', 'an', 'unsuccessful', 'attempt', 'in', '1985', 'to', 'acquir
e', 'union',
   carbide', 'corp', '&', 'lt', ';', 'uk', '>,', 'recently', 'offered', 'three',
'billion', 'dlrs'
  'for', 'borg', 'warner', 'corp', '&', 'lt', ';', 'bor', '>,', 'a', 'chicago',
'manufacturer',
  'of', 'plastics', 'and', 'chemicals', '.', 'another', 'industry', 'powerhouse',
 ,',','w','.',
'r',',','grace','&','lt',';','gra','>','has','divested','its','retai
  'restaurant', 'and', 'fertilizer', 'businesses', 'to', 'raise', 'cash', 'for',
'chemical',
  'acquisitions', '.', 'but', 'some', 'experts', 'worry', 'that', 'the', 'chemica
l', 'industry'
  'may', 'be', 'headed', 'for', 'trouble', 'if', 'companies', 'continue', 'turnin
g', 'their',
  'back', 'on', 'the', 'manufacturing', 'of', 'staple', 'petrochemical', 'commodi
ties', ',', 'such',
'as', 'ethylene', ',', 'in', 'favor', 'of', 'more', 'profitable', 'specialty',
'chemicals',
  'that', 'are', 'custom', '-', 'designed', 'for', 'a', 'small', 'group', 'of',
'buyers', '.',
               'like', 'dupont', '&', 'lt', ';', 'dd', '>', 'and', 'monsanto', 'c
  'companies',
o', '&', 'lt', ';',
  'mtc', '>', 'spent', 'the', 'past', 'two', 'or', 'three', 'years', 'trying', 't
o', 'get', 'out',
  'of', 'the', 'commodity', 'chemical', 'business', 'in', 'reaction', 'to', 'ho
w', 'badly', 'the',
   'market', 'had', 'deteriorated', ',"', 'dosher', 'said', '.', '"', 'but', 'i',
  hink
'will', ever
'in',
'think', 'they',
          'eventually', 'kill', 'the', 'margins', 'on', 'the', 'profitable', 'che
micals,
  'the', 'niche', 'market', '."', 'some', 'top', 'chemical', 'executives', 'shar
e', 'the', 'concern', '.', '"', 'the', 'challenge', 'for', 'our', 'industry', 'is', 'to',
'keep', 'from',
   getting', 'carried', 'away', 'and', 'repeating', 'past', 'mistakes', ',"', 'ga
```

```
'heyman', 'cautioned', '.', '"', 'the', 'shift', 'from', 'commodity', 'chemical
s', 'may', 'be',
'ill', '-', 'advised', '.', 'specialty', 'businesses', 'do', 'not', 'stay', 'sp
        'long',
ecial', 'long',
'."', 'houston', '-', 'based', 'cain', 'chemical', ',', 'created', 'this', 'mon
th', 'by', 'the',
   sterling', 'investment', 'banking', 'group', ',', 'believes', 'it', 'can', 'ge
nerate', '700',
  'mln', 'dlrs', 'in', 'annual', 'sales', 'by', 'bucking', 'the', 'industry', 'tr
end', '.',
  'chairman', 'gordon', 'cain', ',', 'who', 'previously', 'led', 'a', 'leverage
d', 'buyout', 'of',
   'dupont', "'", 's', 'conoco', 'inc', "'", 's', 'chemical', 'business', ',', 'ha
s', 'spent', '1',
'.', '1', 'billion', 'dlrs', 'since', 'january', 'to', 'buy', 'seven', 'petroch
emical', 'plants',
  'along', 'the', 'texas', 'gulf', 'coast', '.', 'the', 'plants', 'produce', 'onl
y', 'basic',
   commodity', 'petrochemicals', 'that', 'are', 'the', 'building', 'blocks', 'o
f', 'specialty',
               '.', '"', 'this', 'kind', 'of', 'commodity', 'chemical', 'busines
  'products',
s', 'will', 'never',
  'be', 'a', 'glamorous', ',', 'high', '-', 'margin', 'business', ',"', 'cain',
'said', ',
  'adding', 'that', 'demand', 'is', 'expected', 'to', 'grow', 'by', 'about', 'thr
ee', 'pct',
  'annually', '.', 'garo', 'armen', ',', 'an', 'analyst', 'with', 'dean', 'witte
r', 'reynolds',
   said', 'chemical', 'makers', 'have', 'also', 'benefitted', 'by', 'increasing',
'demand', 'for',
   plastics', 'as', 'prices', 'become', 'more', 'competitive', 'with', 'aluminu
m', ',', 'wood',
        , 'steel', 'products', '.', 'armen', 'estimated', 'the', 'upturn', 'in',
   and',
'the', 'chemical',
  'business', 'could', 'last', 'as', 'long', 'as', 'four', 'or', 'five', 'years',
   , 'provided',
 'the', 'u', '.', 's', '.', 'economy', 'continues', 'its', 'modest', 'rate', 'o
f', 'growth',
  '<END>'],
 ['<START>', 'turkey', 'calls', 'for', 'dialogue', 'to', 'solve', 'dispute', 'tur
key', 'said',
  'today', 'its', 'disputes', 'with', 'greece', ',', 'including', 'rights', 'on',
'the',
  'continental', 'shelf', 'in', 'the', 'aegean', 'sea', ',', 'should', 'be', 'sol
ved', 'through',
  'negotiations', '.', 'a', 'foreign', 'ministry', 'statement', 'said', 'the', 'l
atest', 'crisis',
  'between', 'the', 'two', 'nato', 'members', 'stemmed', 'from', 'the', 'continen
tal', 'shelf',
  'dispute', 'and', 'an', 'agreement', 'on', 'this', 'issue', 'would', 'effect',
the', 'security',
',', 'economy', 'and', 'other', 'rights', 'of', 'both', 'countries', '.', '"',
',', 'economy', 'and', 'other', 'rights', 'of', both, countries, ., , 'as', 'the',
  'issue', 'is', 'basicly', 'political', ',', 'a', 'solution', 'can', 'only', 'b
e', 'found', 'by',
  'bilateral', 'negotiations', ',"', 'the', 'statement', 'said', '.', 'greece',
'has', 'repeatedly',
  'said', 'the', 'issue', 'was', 'legal', 'and', 'could', 'be', 'solved', 'at',
  international', 'court', 'of', 'justice', '.', 'the', 'two', 'countries', 'app'
roached', 'armed',
```

```
'confrontation', 'last', 'month', 'after', 'greece', 'announced', 'it', 'planne
d', 'oil',
  'exploration', 'work', 'in', 'the', 'aegean', 'and', 'turkey', 'said', 'it', 'w
ould', 'also',
  'search', 'for', 'oil', '.', 'a', 'face', '-', 'off', 'was', 'averted', 'when',
'turkey',
  'confined', 'its', 'research', 'to', 'territorrial', 'waters', '.', '"', 'the',
'latest',
  'crises', 'created', 'an', 'historic', 'opportunity', 'to', 'solve', 'the', 'di
sputes', 'between',
'the', 'two', 'countries', ',"', 'the', 'foreign', 'ministry', 'statement', 'sa id', '.', 'turkey',
"", 's', 'ambassador', 'in', 'athens', ',', 'nazmi', 'akiman', ',', 'was', 'du
e', 'to', 'meet',
'prime', 'minister', 'andreas', 'papandreou', 'today', 'for', 'the', 'greek',
'reply', 'to', 'a',
'message', 'sent', 'last', 'week', 'by', 'turkish', 'prime', 'minister', 'turgu t', 'ozal', '.',
   the', 'contents', 'of', 'the', 'message', 'were', 'not', 'disclosed', '.', 'E
ND>']]
```

Question 1.1: Implement distinct_words [code] (5 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with for loops, but it's more efficient to do it with Python list comprehensions. In particular, this (https://coderwall.com/p/rcmaea/flatten-a-list-of-lists-in-one-line-in-python) may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information (https://python-3-patterns-idioms-test.readthedocs.io/en/latest/Comprehensions.html).

You may find it useful to use <u>Python sets (https://www.w3schools.com/python/python_sets.asp)</u> to remove duplicate words.

```
In [6]:
```

```
reload(lab4);
```

In [7]:

```
# Run this sanity check
# Note that this not an exhaustive check for correctness.
# Define toy corpus
test_corpus = ["START All that glitters isn't gold END".split(" "), "START All's well that ends well
test_corpus_words, num_corpus_words = lab4.distinct_words(test_corpus)
# Correct answers
ans_test_corpus_words = sorted(list(set(["START", "All", "ends", "that", "gold", "All's", "glitters'
ans num_corpus_words = len(ans_test_corpus_words)
# Test correct number of words
assert (num_corpus_words == ans_num_corpus_words), "Incorrect number of distinct words. Correct: {}.
# Test correct words
assert (test_corpus_words == ans_test_corpus_words), "Incorrect corpus_words. \nCorrect: {}\nYours:
# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
                                                                                                   Þ
```

Passed All Tests!

Question 1.2: Implement compute_co_occurrence_matrix [code] (15 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use numpy (np) to represent vectors, matrices, and tensors.

```
In [8]:
```

reload(lab4);

```
In [9]:
# Run this sanity check
# Note that this is not an exhaustive check for correctness.
# Define toy corpus and get student's co-occurrence matrix
test_corpus = ["START All that glitters isn't gold END".split(" "), "START All's well that ends well
M_test, word2Ind_test = lab4.compute_co_occurrence_matrix(test_corpus, window_size=1)
# Correct M and word2Ind
M test ans = np. array(
         [[0., 0., 0., 1., 0., 0., 0., 0., 1., 0.,],
           [0., 0., 0., 1., 0., 0., 0., 0., 0., 1.,],
           [0., 0., 0., 0., 0., 0., 1., 0., 0., 1.,],
           [1., 1., 0., 0., 0., 0., 0., 0., 0., 0., 0., ],
           [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
           [0., 0., 0., 0., 0., 0., 0., 1., 1., 0.,],
           [0., 0., 1., 0., 0., 0., 0., 1., 0., 0.,],
           [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
           [1., 0., 0., 0., 1., 1., 0., 0., 0., 1.,],
           [0., 1., 1., 0., 1., 0., 0., 0., 1., 0.,]]
word2Ind ans = {'All': 0, "All's": 1, 'END': 2, 'START': 3, 'ends': 4, 'glitters': 5, 'gold': 6, "is
# Test correct word2Ind
assert (word2Ind_ans == word2Ind_test), "Your word2Ind is incorrect:\nCorrect: {}\nYours: {}".formation of the correct is a second of the correct is a secon
# Test correct M shape
assert (M test.shape == M test ans.shape), "M matrix has incorrect shape.\nCorrect: {}\nYours: {}".
# Test correct M values
for w1 in word2Ind ans.keys():
         idx1 = word2Ind_ans[w1]
         for w2 in word2Ind ans.keys():
                  idx2 = word2Ind ans[w2]
                 student = M test[idx1, idx2]
                 correct = M test ans[idx1, idx2]
                  if student != correct:
                          print("Correct M:")
                          print(M test ans)
                          print("Your M: ")
                           print(M test)
                           raise AssertionError("Incorrect count at index ({}, {})=({}, {}) in matrix M. Yours has
# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

```
Passed All Tests!
```

Question 1.3: Implement reduce_to_k_dim [code] (10 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

Note: All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD (https://scikit-learn.org/stable/modules/generated/sklearn.decomposition.TruncatedSVD.html).

In [10]:

```
reload(lab4);
```

In [11]:

```
# ------
# Run this sanity check
# Note that this not an exhaustive check for correctness
# In fact we only check that your M_reduced has the right dimensions.
# -------

# Define toy corpus and run student code
test_corpus = ["START All that glitters isn't gold END".split(" "), "START All's well that ends well
M_test, word2Ind_test = lab4.compute_co_occurrence_matrix(test_corpus, window_size=1)
M_test_reduced = lab4.reduce_to_k_dim(M_test, k=2)

# Test proper dimensions
assert (M_test_reduced.shape[0] == 10), "M_reduced has {} rows; should have {} ".format(M_test_reduced)
assert (M_test_reduced.shape[1] == 2), "M_reduced has {} columns; should have {} ".format(M_test_reduced)
# Print Success
print ("-" * 80)
print ("Passed All Tests!")
print ("-" * 80)
```

```
Running Truncated SVD over 10 words...

Done.

Passed All Tests!
```

Question 1.4: Implement plot_embeddings [code+plot] (10 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code

(https://www.pythonmembers.club/2018/05/08/matplotlib-scatter-plot-annotate-set-text-at-label-each-point/). In the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at the future, a good way to make a plot is to look at <a href="mailto:the-matplotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scatter-plotlib-scat

(https://matplotlib.org/gallery/index.html), find a plot that looks somewhat like what you want, and adapt the code they give.

While submitting this question for the report, include the code cell as well as the corresponding plot produced by your code.

In [12]:

```
def plot embeddings(M reduced, word2Ind, words):
     """ Plot in a scatterplot the embeddings of the words specified in the list "words".
        NOTE: do not plot all the words listed in M reduced / word2Ind.
        Include a label next to each point.
        Params:
            M_reduced (numpy matrix of shape (number of unique words in the corpus , k)): matrix of
            word2Ind (dict): dictionary that maps word to indices for matrix M
            words (list of strings): words whose embeddings we want to visualize
    # Write your implementation here.
   plt.figure()
    index_list = [word2Ind[word] for word in words]
    words_vector_list = [M_reduced[i] for i in index list]
    for i in range(len(words)):
        word = words[i]
        vec = words_vector_list[i]
        plt.scatter(vec[0], vec[1], marker="x", color="red")
        plt.text(vec[0], vec[1], word)
    plt. show()
```

In [12]:

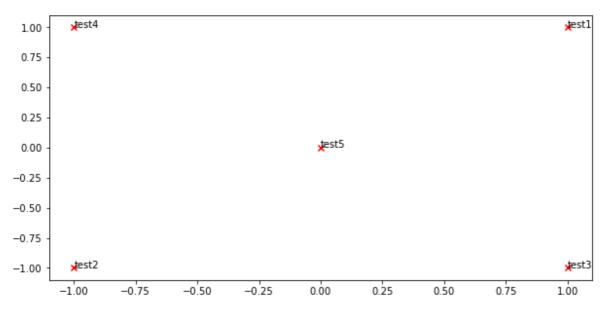
```
# ------
# Run this sanity check
# Note that this not an exhaustive check for correctness.
# The plot produced should look like the "test solution plot" depicted below.
# ------

print ("-" * 80)
print ("Outputted Plot:")

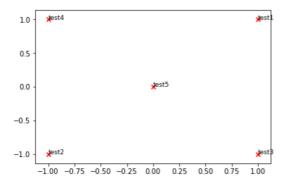
M_reduced_plot_test = np.array([[1, 1], [-1, -1], [1, -1], [-1, 1], [0, 0]])
word2Ind_plot_test = {'test1': 0, 'test2': 1, 'test3': 2, 'test4': 3, 'test5': 4}
words = ['test1', 'test2', 'test3', 'test4', 'test5']
plot_embeddings(M_reduced_plot_test, word2Ind_plot_test, words)

print ("-" * 80)
```

Outputted Plot:



Test Plot Solution



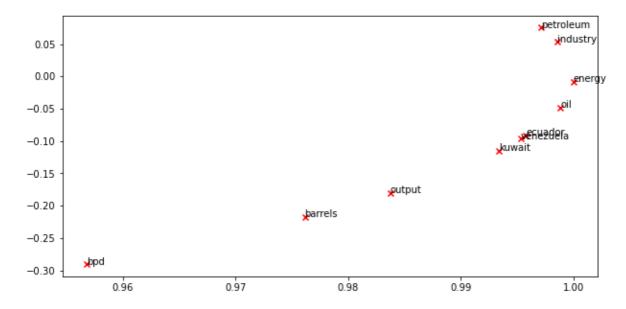
Question 1.5: Co-Occurrence Plot Analysis [written] (10 points)

Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4, over the Reuters "crude" corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns U*S, so we normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness). **Note**: The line of code below that does the normalizing uses the NumPy concept of *broadcasting*. If you don't know about broadcasting, check out <u>Computation on Arrays: Broadcasting by Jake VanderPlas</u> (https://jakevdp.github.io/PythonDataScienceHandbook/02.05-computation-on-arrays-broadcasting.html).

Run the below cell to produce the plot. It'll probably take a few seconds to run. What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? **Note:** "bpd" stands for "barrels per day" and is a commonly used abbreviation in crude oil topic articles.

In [13]:

Running Truncated SVD over 8185 words... Done.



Cluster together:

(petroleum,industry-tight related)
(venezuela,kuwait,ecuador-top oil producing country)
(oil,energy-oil is kind of energy)
(output,barrels-the way to count output)

things not cluster but I think they should be:

```
'bpd','barrels'
'bpd','energy'
'oil', 'petroleum'
```

Part 2: Prediction-Based Word Vectors (50 points)

More recently prediction-based word vectors have come into fashion, e.g. word2vec. Here, we shall explore the embeddings produced by word2vec. If you're feeling adventurous, challenge yourself and try reading the <u>original paper (https://papers.nips.cc/paper/5021-distributed-representations-of-words-and-phrases-and-their-compositionality.pdf)</u>.

Then run the following cells to load the word2vec vectors into memory. **Note**: This might take several minutes.

In [13]:

In [14]:

```
# -----
# Run Cell to Load Word Vectors
# Note: This may take several minutes
# ------
wv_from_bin = load_word2vec()
```

Loaded vocab size 3000000

Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly.

Reducing dimensionality of Word2Vec Word Embeddings

Let's directly compare the word2vec embeddings to those of the co-occurrence matrix. Run the following cells to:

- 1. Put the 3 million word2vec vectors into a matrix M
- 2. Run reduce_to_k_dim (your Truncated SVD function) to reduce the vectors from 300-dimensional to 2-dimensional.

```
In [15]:
```

```
def get matrix of vectors (wv from bin, required words=['barrels', 'bpd', 'ecuador', 'energy', 'indu
       Put the word2vec vectors into a matrix M.
            wv from bin: KeyedVectors object; the 3 million word2vec vectors loaded from file
        Return:
            M: numpy matrix shape (num words, 300) containing the vectors
            word2Ind: dictionary mapping each word to its row number in M
    import random
   words = list(wv from bin.vocab.keys())
    print("Shuffling words ...")
    random. shuffle (words)
    words = words[:10000]
    print ("Putting %i words into word2Ind and matrix M..." % len(words))
    word2Ind = \{\}
   M = []
    curInd = 0
    for w in words:
        try:
            M. append (wv_from_bin.word_vec(w))
            word2Ind[w] = curInd
            curInd += 1
        except KeyError:
            continue
    for w in required words:
        try:
            M. append (wv from bin. word vec (w))
            word2Ind[w] = curInd
            curInd += 1
        except KeyError:
            continue
    M = np. stack(M)
    print ("Done.")
    return M, word2Ind
```

In [16]:

```
# -----
# Run Cell to Reduce 300-Dimensinal Word Embeddings to k Dimensions
# Note: This may take several minutes
# -----
M, word2Ind = get_matrix_of_vectors(wv_from_bin)
M_reduced = lab4.reduce_to_k_dim(M, k=2)
```

```
Shuffling words ...
Putting 10000 words into word2Ind and matrix M...
Done.
Running Truncated SVD over 10010 words...
Done.
```

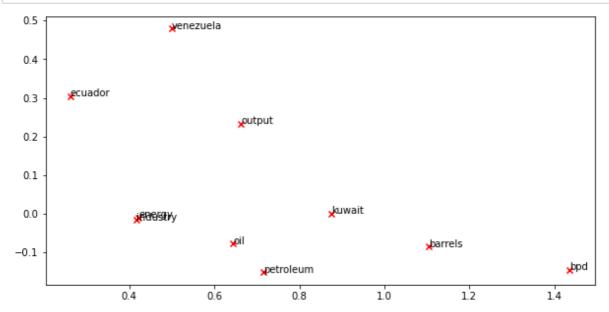
Question 2.1: Word2Vec Plot Analysis [written] (5 points)

```
Run the cell below to plot the 2D word2vec embeddings for ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output', 'petroleum', 'venezuela'].
```

What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? How is the plot different from the one generated earlier from the co-occurrence matrix?

In [17]:

```
words = ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output', 'petroleum',
plot_embeddings(M_reduced, word2Ind, words)
```



Write your answer here.

things cluster together:

(industry,energy)

(oil,petroleum)

(bpd,barrels)

things not cluster but I think they should be:

'ecuador', 'kuwait', 'venezuela'

'bpd', 'output'

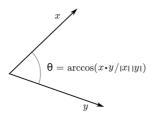
Compared to the one generated earlier from the co-occurrence matrix:

Changes in relative distance and position make the plot different, note that we can see the three country kuwait, ecuador and venezuela are not cluster together.

Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective L1 and L2 Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:



Instead of computing the actual angle, we can leave the similarity in terms of $similarity = cos(\Theta)$. Formally the <u>Cosine Similarity (https://en.wikipedia.org/wiki/Cosine_similarity)</u> s between two vectors p and q is defined as:

$$s = \frac{p \cdot q}{\|p\| \|q\|}, \text{ where } s \in [-1, 1]$$

Question 2.2: Polysemous Words (5 points) [code + written]

Find a <u>polysemous (https://en.wikipedia.org/wiki/Polysemy)</u> word (for example, "leaves" or "scoop") such that the top-10 most similar words (according to cosine similarity) contains related words from *both* meanings. For example, "leaves" has both "vanishes" and "stalks" in the top 10, and "scoop" has both "handed_waffle_cone" and "lowdown". You will probably need to try several polysemous words before you find one. Please state the polysemous word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous words you tried didn't work?

Note: You should use the $wv_from_bin.most_similar(word)$ function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance please check the **GenSim documentation**

(https://radimrehurek.com/gensim/models/keyedvectors.html#gensim.models.keyedvectors.FastTextKeye

```
In [18]:
```

```
# -----
# Write your polysemous word exploration code here.

wv_from_bin.most_similar("right")
# ------
```

Out[18]:

```
[('Right', 0.5703941583633423),
  ('wrong', 0.5534271597862244),
  ('##.Help_us', 0.5502839684486389),
  ('Goodwill_Catanese', 0.5159174203872681),
  ('left', 0.49213990569114685),
  ('fielder_Joe_Borchard', 0.48948541283607483),
  ('NOTE_Xactly_Incent', 0.4886630177497864),
  ('fielder_Ambiorix_Concepcion', 0.4841775894165039),
  ('now', 0.4794555902481079),
  ('fielder_Jeromy_Burnitz', 0.4771837890148163)]
```

Write your answer here.

I find the word "right", with three meanings here:

Direction

Correctness

Signal of time now

The reason might be that some meaning of these words may not exist in this corpus, or too sparse compared with another meaning.

Question 2.3: Synonyms & Antonyms (5 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words (w1,w2,w3) where w1 and w2 are synonyms and w1 and w3 are antonyms, but Cosine Distance(w1,w3) < Cosine Distance(w1,w2). For example, w1="happy" is closer to w3="sad" than to w2="cheerful".

Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the $wv_from_bin. distance(w1, w2)$ function here in order to compute the cosine distance between two words. Please see the **GenSim documentation**

(https://radimrehurek.com/gensim/models/keyedvectors.html#gensim.models.keyedvectors.FastTextKeye for further assistance.

```
→
```

```
In [19]:
```

Synonyms true, authentic have cosine distance: 0.641054093837738 Antonyms true, false have cosine distance: 0.6290567517280579

Write your answer here.

True and false are very frequently used in daily life, and often comes in pairs(especially in exams), so they are more likely to occur together. While for 'authentic', obviously it is longer, harder to think of when writing and reading(not convenient), thus its use frequency is quite low. Based on this, the antonyms get much closer cosine distance.

Solving Analogies with Word Vectors

Word2Vec vectors have been shown to sometimes exhibit the ability to solve analogies.

As an example, for the analogy "man: king:: woman: x", what is x?

In the cell below, we show you how to use word vectors to find x. The $most_similar$ function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list. The answer to the analogy will be the word ranked most similar (largest numerical value).

Note: Further Documentation on the <code>most_similar</code> function can be found within the **GenSim documentation** (https://radimrehurek.com/gensim/models/keyedvectors.html#gensim.models.keyedvectors.FastTextKeye

```
In []:

# Run this cell to answer the analogy -- man : king :: woman : x

pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'king'], negative=['man']))
```

Question 2.4: Finding Analogies [code + written] (10 Points)

Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y :: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

Note: You may have to try many analogies to find one that works!

```
In [34]:
```

```
[('grandma', 0.6901211738586426),
('granddad', 0.6659698486328125),
('Grandpa', 0.6597509384155273),
('grandfather', 0.6559692621231079),
('dad', 0.6350705623626709),
('grandkids', 0.6302976608276367),
('granddaughter', 0.6056955456733704),
('grandson', 0.6052547097206116),
('grandmother', 0.6042029857635498),
('Grandma', 0.5968949794769287)]
```

Write your answer here.

female:grandma::male:grandma

Question 2.5: Incorrect Analogy [code + written] (5 point)

Find an example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the (incorrect) value of b according to the word vectors.

Write your answer here.

It was supposed to see China:Russia::Beijing:Moscow, while we do not see any words implies Moscow the city, but word 'Ukraine' the country.

Question 2.6: Guided Analysis of Bias in Word Vectors [written] (5 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit to our word embeddings.

Run the cell below, to examine (a) which terms are most similar to "woman" and "worker" and most dissimilar to "man", and (b) which terms are most similar to "man" and "worker" and most dissimilar to "woman". What do you find in the top 10?

```
In [40]:
```

```
# Run this cell
# Here `positive` indicates the list of words to be similar to and `negative` indicates the list of
# most dissimilar from.
pprint.pprint(wv from bin.most similar(positive=['woman', 'worker'], negative=['man']))
print()
pprint.pprint(wv from bin.most similar(positive=['man', 'worker'], negative=['woman']))
[('workers', 0.6582455635070801),
 ('employee', 0.5805294513702393),
 ('nurse', 0.5249922275543213),
 ('receptionist', 0.5142490267753601),
 ('migrant_worker', 0.5001609921455383),
 ('Worker', 0.4979270100593567),
 ('housewife', 0.48609834909439087),
 ('registered nurse', 0.4846190810203552),
 ('laborer', 0.48437264561653137),
 ('coworker', 0.48212409019470215)]
[('workers', 0.5590359568595886),
 ('laborer', 0.54481041431427),
 ('foreman', 0.5192232131958008),
 ('Worker', 0.5161596536636353),
 ('employee', 0.5094279646873474),
 ('electrician', 0.49481213092803955),
 ('janitor', 0.48718899488449097),
 ('bricklayer', 0.4825313687324524),
 ('carpenter', 0.47499001026153564),
 ('workman', 0.4642517566680908)]
```

Write your answer here.

(a)Words like nurse,receptionist,migrant_worker,housewife,registered_nurse are most similar to "woman" and "worker" while most dissimilar to "man"

(b)Words like foreman, electrician, janitor, bricklayer, carpenter are most similar to "man" and "worker" while most dissimilar to "woman"

The results reflect gender bias, with men stereotyped as more inclined to manual labor while women attached to jobs more about caring, tidying or interpersonal work.

Question 2.7: Independent Analysis of Bias in Word Vectors [code + written] (10 points)

Use the $most_similar$ function to find another case where some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

```
In [39]:
# Write your bias exploration code here.
pprint.pprint(wv from bin.most similar(positive=['hispanic', 'director'], negative=['white']))
print()
pprint.pprint(wv from bin.most similar(positive=['white', 'director'], negative=['hispanic']))
[('coordinator', 0.5700598359107971),
 ('Director', 0.5223729014396667),
 ('Executive_Director', 0.5200456976890564),
 ('di_rector', 0.5067609548568726),
 ('vp', 0.5009108781814575),
 ('vice_president', 0.47591227293014526),
 ('co ordinator', 0.4571147561073303),
 ('direc_tor', 0.45574527978897095),
 ('directorof', 0.44874030351638794),
 ('manager', 0.44786566495895386)]
[('vice_president', 0.5175800919532776),
 ('executive', 0.5020480751991272),
 ('managing_director', 0.4879714846611023),
 ('manager', 0.43419456481933594),
 ('Director', 0.4320756196975708),
 ('vicepresident', 0.4178272485733032),
 ('direc_tor', 0.41616371273994446),
 ('directorof', 0.41518113017082214),
 ('codirector', 0.4112960696220398),
 ('associate', 0.4028768539428711)]
```

Write your answer here.

In many companies in various countries, black employees are in the minority in the management ranks, which is a form of color, or racial bias.

Question 2.8: Thinking About Bias [written] (5 point)

What might be the cause of these biases in the word vectors?

Write your answer here.

The frequency of words produces word vectors, and we know that all the corpus come from our daily life materials like papers, articles, news and so on,they are generated by people, and nobody can get rid of bias and become absolutely fair, so they made word selections according to their own values, which makes frequency of word pairs that take in bias increase.

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In [ ]:
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