# **3T2:** Fourier Transform properties (2 of 2)

Xavier Serra

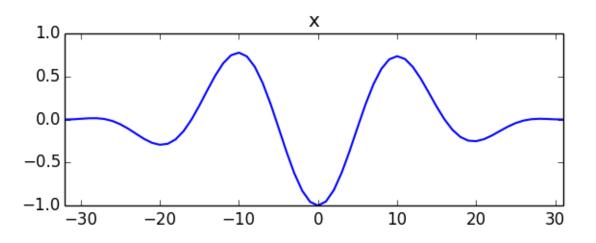
Universitat Pompeu Fabra, Barcelona

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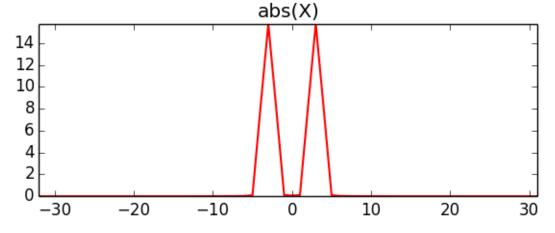
- Energy conservation & decibels
- Phase unwrapping
- Zero padding
- Fast Fourier Transform (FFT)
- FFT and zero-phase windowing
- Analysis/synthesis

## **Energy conservation**

$$\sum_{n=-N/2}^{N/2-1} |x[n]|^2 = \frac{1}{N} \sum_{k=-N/2}^{N/2-1} |X[k]|^2$$

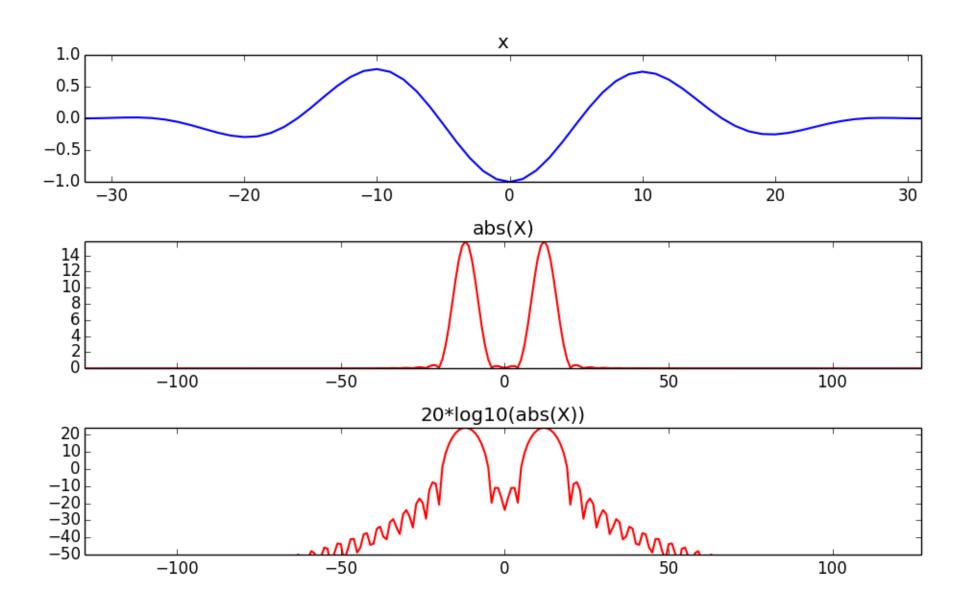


$$\sum_{n=N/2}^{N/2-1} |x[n]|^2 = 11.81182$$

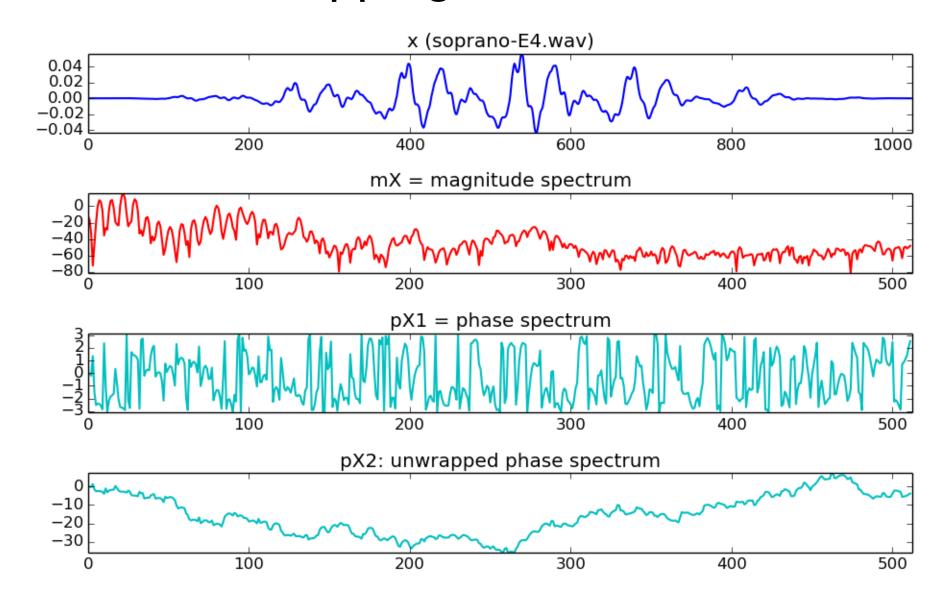


$$\frac{1}{N} \sum_{k=N/2}^{N/2-1} |X[k]|^2 = 11.81182$$

## Amplitude in decibels (dB)

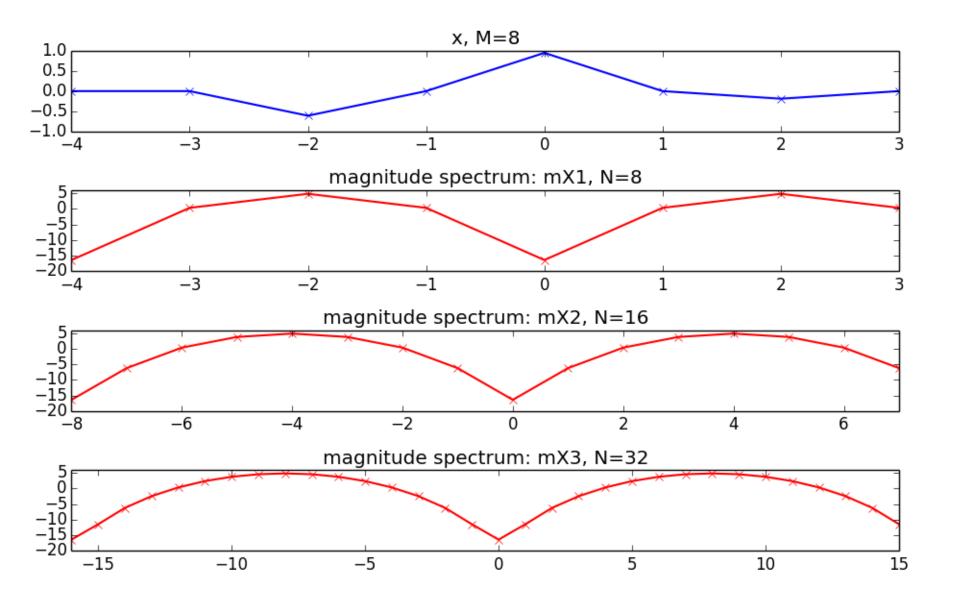


## Phase unwrapping



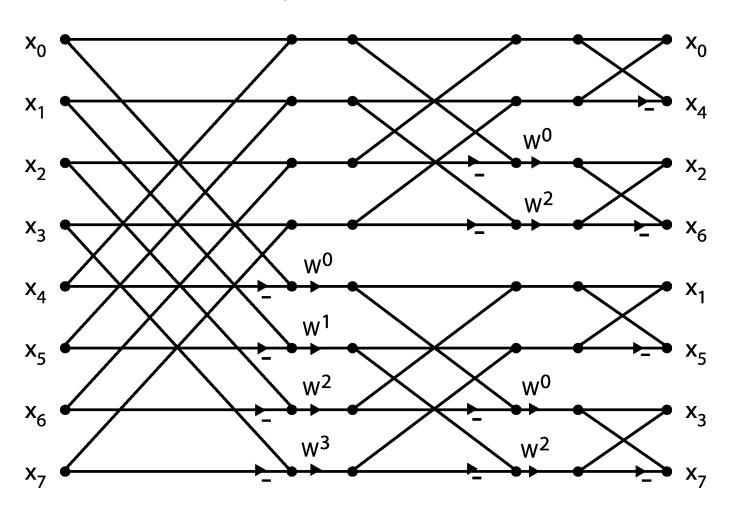
# Zero-padding

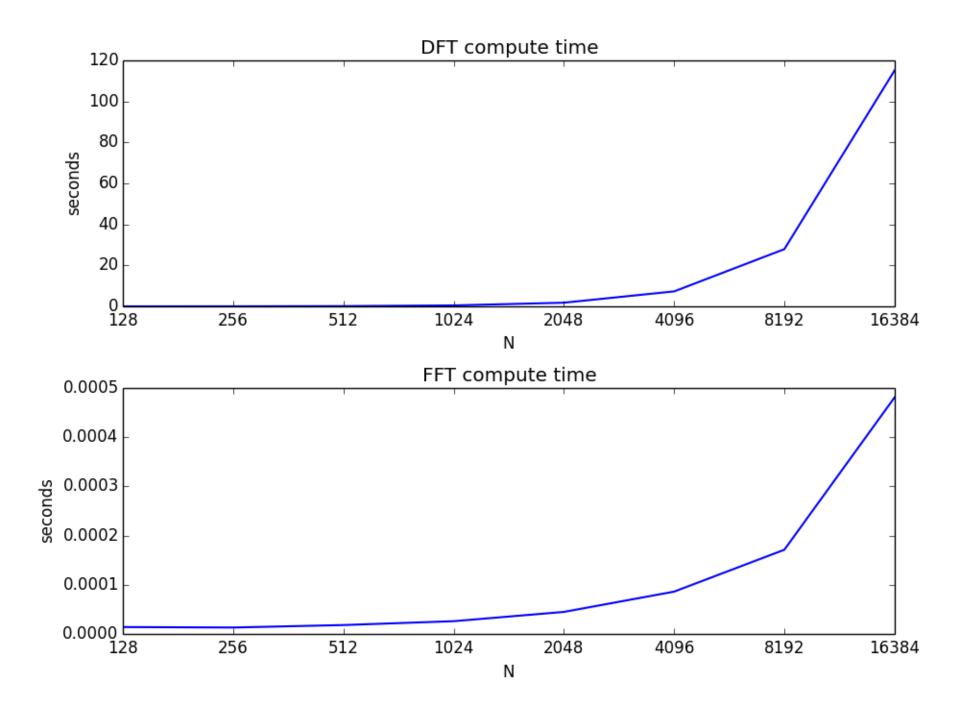
#### zero padding $\leftrightarrow$ interpolation



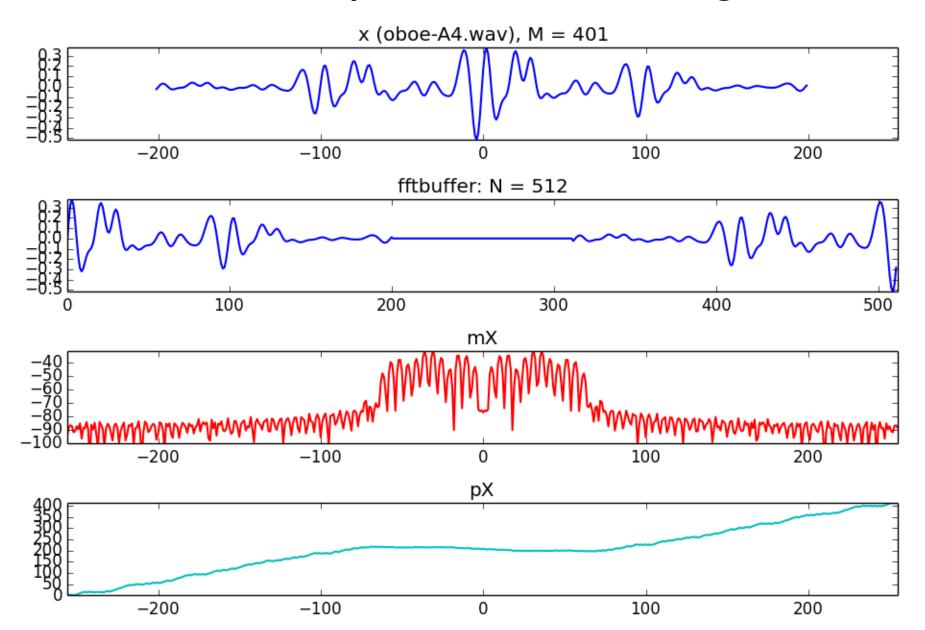
## **Fast Fourier Transform**

Cooley-Tukey algorithm: breaks down recursively the DFT of a power of 2 size into two pieces of size N/2.

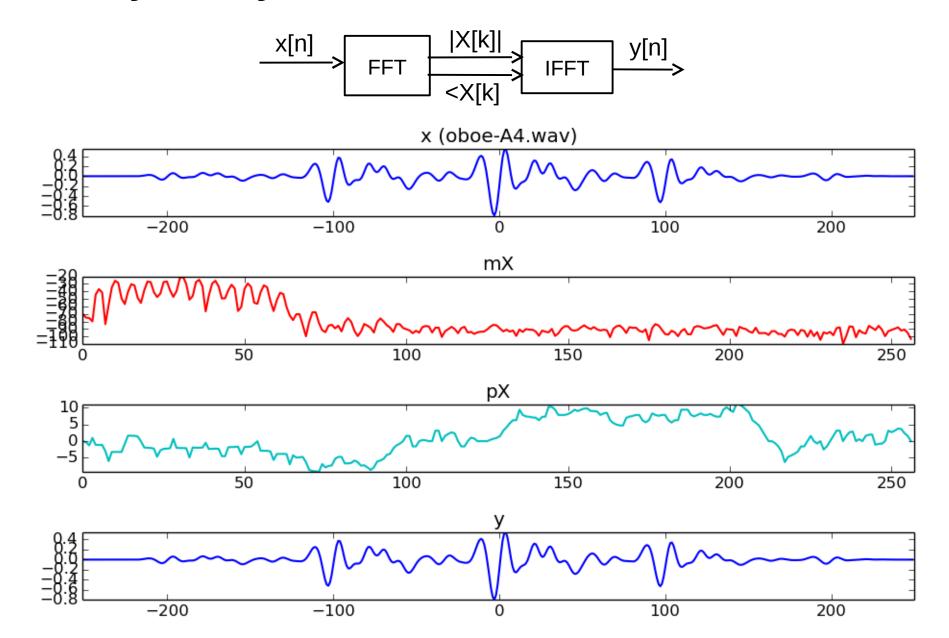




## FFT and zero-phase windowing



## Analysis/synthesis



### References and credits

- More information on: https://en.wikipedia.org/wiki/Discrete\_Fourier\_transform https://en.wikipedia.org/wiki/Fast\_Fourier\_transform
- Sounds from: http://www.freesound.org/people/xserra/packs/13038/
- Reference for the DFT by Julius O. Smith: https://ccrma.stanford.edu/~jos/mdft/
- Slides released under CC Attribution-Non Commercial-Share Alike license and code under Affero GPL license; available from https://github.com/MTG/sms-tools

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