



Assumptions :-

$$\vec{p}_1 = -4.84 - 6.37i;$$

$$\vec{p}_2 = -7.75 - 6.6i;$$

$$\vec{p}_3 = -12.39 - 7.09i;$$

$$\vec{p}_4 = -11.02 - 4.68i;$$

$$\vec{p}_5 = -8.08 - 4.36i;$$

$$\theta_2^{o1} = 1.39$$

$$\theta_2^{o2} = 3.14$$

$$\theta_2^{o3} = 3.92$$

$$\theta_2^{o4} = 4.88$$

$$L_1 = 50 \text{ P}(0.26)$$

Loop closure equation

Loop 1:-

$$\vec{l}_1 + \vec{l}_2 + \vec{l}_3 - \vec{l}_4 = 0$$

$$\vec{l}_4 = \vec{l}_1 + \vec{l}_2 + \vec{l}_3$$

$$\begin{aligned} \vec{l}_4 \cdot \vec{l}_4 &= (\vec{l}_1 + \vec{l}_2 + \vec{l}_3) \cdot (\vec{l}_1 + \vec{l}_2 + \vec{l}_3) \\ &= \vec{l}_1 \cdot \vec{l}_1 + \vec{l}_1 \cdot \vec{l}_2 + \vec{l}_1 \cdot \vec{l}_3 + \vec{l}_2 \cdot \vec{l}_1 + \vec{l}_2 \cdot \vec{l}_2 + \vec{l}_2 \cdot \vec{l}_3 + \\ &\quad \vec{l}_3 \cdot \vec{l}_1 + \vec{l}_3 \cdot \vec{l}_2 + \vec{l}_3 \cdot \vec{l}_3 = 0 \end{aligned}$$

$$\vec{l}_4 e^{i\theta_4^{01}} = \vec{l}_1 + \vec{l}_2 e^{i\theta_2^{01}} + \vec{l}_3 e^{i\theta_3^{01}}$$

$$\begin{aligned} \vec{l}_4 \cdot \vec{l}_4 &= (\vec{l}_1 + \vec{l}_2 e^{i\theta_2^{01}} + \vec{l}_3 e^{i\theta_3^{01}}) \cdot (\vec{l}_1 + \vec{l}_2 e^{-i\theta_2^{01}} + \vec{l}_3 e^{-i\theta_3^{01}}) \\ &= \vec{l}_1 \cdot \vec{l}_1 + \vec{l}_1 \cdot \vec{l}_2 e^{-i\theta_2^{01}} + \vec{l}_1 \cdot \vec{l}_3 e^{-i\theta_3^{01}} + \vec{l}_2 e^{i\theta_2^{01}} \cdot \vec{l}_1 \\ &\quad + \vec{l}_2 \cdot \vec{l}_2 + \vec{l}_2 \cdot \vec{l}_3 e^{i(\theta_2^{01} - \theta_3^{01})} + \vec{l}_3 e^{i\theta_3^{01}} \cdot \vec{l}_1 + \\ &\quad \vec{l}_3 \cdot \vec{l}_2 e^{i(\theta_3^{01} - \theta_2^{01})} + \vec{l}_3 \cdot \vec{l}_3 = 0 \end{aligned}$$

$$\vec{l}_4 e^{i\theta_4^{02}} = \vec{l}_1 + \vec{l}_2 e^{i\theta_2^{02}} + \vec{l}_3 e^{i\theta_3^{02}}$$

$$\begin{aligned} \vec{l}_4 \cdot \vec{l}_4 &= (\vec{l}_1 + \vec{l}_2 e^{i\theta_2^{02}} + \vec{l}_3 e^{i\theta_3^{02}}) \cdot (\vec{l}_1 + \vec{l}_2 e^{-i\theta_2^{02}} + \vec{l}_3 e^{-i\theta_3^{02}}) \\ &= \vec{l}_1 \cdot \vec{l}_1 + \vec{l}_1 \cdot \vec{l}_2 e^{-i\theta_2^{02}} + \vec{l}_1 \cdot \vec{l}_3 e^{-i\theta_3^{02}} + \vec{l}_2 e^{i\theta_2^{02}} \cdot \vec{l}_1 \\ &\quad + \vec{l}_2 \cdot \vec{l}_2 + \vec{l}_2 \cdot \vec{l}_3 e^{i(\theta_2^{02} - \theta_3^{02})} + \vec{l}_3 e^{i\theta_3^{02}} \cdot \vec{l}_1 + \\ &\quad \vec{l}_3 \cdot \vec{l}_2 e^{i(\theta_3^{02} - \theta_2^{02})} + \vec{l}_3 \cdot \vec{l}_3 = 0 \end{aligned}$$

$$\begin{aligned}
 \textcircled{2} - \textcircled{1} \Rightarrow & \vec{l}_1 \vec{l}_3 (e^{-i\theta_3^{01}} - 1) + \vec{l}_1 \vec{l}_3 (e^{-i\theta_3^{01}} - 1) + \vec{l}_1 \vec{l}_2 (e^{i\theta_2^{01}} - 1) \\
 & + \vec{l}_1 \vec{l}_3 (e^{i\theta_3^{01}} - 1) + \vec{l}_2 \vec{l}_3 (e^{i(\theta_2^{01} - \theta_3^{01})} - 1) + \vec{l}_3 \vec{l}_2 (e^{i(\theta_3^{01} - \theta_2^{01})} - 1) = 0
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{3} - \textcircled{1} \Rightarrow & \vec{l}_1 \vec{l}_3 (e^{-i\theta_3^{02}} - 1) + \vec{l}_1 \vec{l}_3 (e^{-i\theta_3^{02}} - 1) + \vec{l}_1 \vec{l}_2 (e^{i\theta_2^{02}} - 1) \\
 & + \vec{l}_1 \vec{l}_3 (e^{i\theta_3^{02}} - 1) + \vec{l}_2 \vec{l}_3 (e^{i(\theta_2^{02} - \theta_3^{02})} - 1) + \vec{l}_3 \vec{l}_2 (e^{i(\theta_3^{02} - \theta_2^{02})} - 1) \\
 & = 0
 \end{aligned}$$

$$\vec{l}_4 e^{i\theta_4^{03}} = \vec{l}_1 + \vec{l}_2 e^{i\theta_2^{03}} + \vec{l}_3 e^{i\theta_3^{03}}$$

$$\begin{aligned} \vec{l}_4 \vec{l}_4 &= (\vec{l}_1 + \vec{l}_2 e^{i\theta_2^{03}} + \vec{l}_3 e^{i\theta_3^{03}}) (\vec{l}_1 + \vec{l}_2 e^{i\theta_2^{03}} + \vec{l}_3 e^{i\theta_3^{03}}) \\ &= \vec{l}_1 \vec{l}_1 + \vec{l}_1 \vec{l}_2 e^{-i\theta_2^{03}} + \vec{l}_1 \vec{l}_3 e^{-i\theta_3^{03}} + \vec{l}_2 e^{i\theta_2^{03}} \vec{l}_2 \\ &\quad + \vec{l}_2 \vec{l}_3 e^{i(\theta_2^{03} - \theta_3^{03})} + \vec{l}_3 e^{i\theta_3^{03}} \vec{l}_3 \\ &\quad + \vec{l}_3 \vec{l}_2 e^{i(\theta_3^{03} - \theta_2^{03})} + \vec{l}_3 \vec{l}_3 \quad \text{--- (4)} \end{aligned}$$

$$\begin{aligned} \text{(4)} - \text{(4)} &\Rightarrow \vec{l}_1 \vec{l}_3 (e^{-i\theta_3^{03}} - 1) + \vec{l}_1 \vec{l}_3 (e^{-i\theta_3^{03}} - 1) + \\ &\quad \vec{l}_1 \vec{l}_2 (e^{i\theta_2^{03}} - 1) + \vec{l}_1 \vec{l}_3 (e^{i\theta_3^{03}} - 1) + \vec{l}_2 \vec{l}_3 \\ &\quad (e^{i(\theta_2^{03} - \theta_3^{03})} - 1) + \vec{l}_2 \vec{l}_2 (e^{i(\theta_3^{03} - \theta_2^{03})} - 1) \\ &= 0 \end{aligned}$$



Loop 2:

$$c_1 = p_1 - l_2 - l_3$$

$$c_2 = p_2 - l_2 e^{i\theta_2^{01}} - l_3 e^{i\theta_3^{01}}$$

$$c_3 = p_3 - l_2 e^{i\theta_2^{02}} - l_3 e^{i\theta_3^{02}}$$

$$a_3 \cos \alpha + w \cos \beta = \operatorname{Re}(c_1)$$

$$a_3 \sin \alpha + w \sin \beta = \operatorname{Im}(c_1)$$

$$a_3 \cos (\theta_3^{01} + \alpha) + w \cos (\beta + \theta_6^{01}) = \operatorname{Re}(c_2)$$

$$a_3 \sin (\theta_3^{01} + \alpha) + w \sin (\beta + \theta_6^{01}) = \operatorname{Im}(c_2)$$

$$a_3 \cos (\theta_3^{02} + \alpha) + w \cos (\beta + \theta_6^{02}) = \operatorname{Re}(c_3)$$

$$a_3 \sin (\theta_3^{02} + \alpha) + w \sin (\beta + \theta_6^{02}) = \operatorname{Im}(c_3)$$

used vpasolve to solve the above equations.

loop 3:

$$\vec{l}_4 + \vec{a}_3 - \vec{l}_6 - \vec{l}_5 - \vec{a}_1 \vec{l}_1 = 0$$

$$\vec{l}_6 + \vec{l}_5 - \vec{a}_1 \vec{l}_1 = \vec{l}_4 + \vec{a}_3 \quad (1)$$

$$\vec{l}_6 e^{i\theta_6^{01}} + \vec{l}_5 e^{i\theta_5^{01}} - \vec{a}_1 \vec{l}_1 = \vec{l}_4 e^{i\theta_4^{01}} + \vec{a}_3 e^{i\theta_3^{01}} \quad (2)$$

$$\vec{l}_6 e^{i\theta_6^{02}} + \vec{l}_5 e^{i\theta_5^{02}} - \vec{a}_1 \vec{l}_1 = \vec{l}_4 e^{i\theta_4^{02}} + \vec{a}_3 e^{i\theta_3^{02}} \quad (3)$$

$$\vec{l}_6 e^{i\theta_6^{03}} + \vec{l}_5 e^{i\theta_5^{03}} - \vec{a}_1 \vec{l}_1 = \vec{l}_4 e^{i\theta_4^{03}} + \vec{a}_3 e^{i\theta_3^{03}} \quad (4)$$

$$\vec{l}_6 e^{i\theta_6^{04}} + \vec{l}_5 e^{i\theta_5^{04}} - \vec{a}_1 \vec{l}_1 = \vec{l}_4 e^{i\theta_4^{04}} + \vec{a}_3 e^{i\theta_3^{04}} \quad (5)$$

$$(2) - (1) \Rightarrow \vec{l}_6 (e^{i\theta_6^{01}} - 1) + \vec{l}_5 (e^{i\theta_5^{01}} - 1) - \vec{l}_4 (e^{i\theta_4^{01}} - 1) + \vec{a}_3 (e^{i\theta_3^{01}} - 1)$$

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$$\textcircled{3} - \textcircled{1} \Rightarrow \vec{L}_6 (e^{i\theta_6^{02}} - 1) + \vec{L}_5 (e^{i\theta_5^{02}} - 1) = \vec{L}_4 (e^{i\theta_4^{02}} - 1) + \vec{a}_3 (e^{i\theta_3^{02}} - 1)$$

$$\textcircled{4} - \textcircled{1} \Rightarrow \vec{L}_6 (e^{i\theta_6^{03}} - 1) + \vec{L}_5 (e^{i\theta_5^{03}} - 1) = \vec{L}_4 (e^{i\theta_4^{03}} - 1) + \vec{a}_3 (e^{i\theta_3^{03}} - 1)$$

$$\textcircled{5} - \textcircled{1} \Rightarrow \vec{L}_6 (e^{i\theta_6^{04}} - 1) + \vec{L}_5 (e^{i\theta_5^{04}} - 1) = \vec{L}_4 (e^{i\theta_4^{04}} - 1) + \vec{a}_3 (e^{i\theta_3^{04}} - 1)$$

used vpsolve to solve the above equations.