

# Lecture 05: Relationships between 2 variables

January 31 2020

Relationships between two  
quantitative variables

Looking at relationships  
visually: Scatterplots

Exploratory analysis using  
scatterplots

Participation

Assessing a relationship  
between two variables with  
a number: Pearson's  
correlation

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# Recap of chapters 1 and 2

Mostly looking at a single variable:

- ▶ Graphs to explore the distribution of single variables (histograms, bar charts)
- ▶ Summary numbers to describe our distributions:
  - ▶ Measures of central tendency (mean, median)
  - ▶ Measures of spread (standard deviation, IQR)

One example of two variables:

- ▶ Time plots to examine what happens to a variable over time

Relationships between two quantitative variables

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# Learning objectives for today

## Lecture 05: Relationships between 2 variables

- ▶ Explore the relationship between two quantitative variables
  - ▶ Directionality
  - ▶ Association vs causation
- ▶ Make scatter plots to look at relationships visually
  - ▶ using `geom_point()`
- ▶ Use the correlation coefficient to quantify the strength of linear relationships
  - ▶ calculate correlations using `cor()`

Relationships between two quantitative variables

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**Relationships between two  
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## Relationships between two quantitative variables

# Explanatory (X) and response (Y) variables

## Relationships between two quantitative variables

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## Bi-directional:

- ▶ “X predicts Y”, or “Y predicts X”
- ▶ “X is associated with Y”, or “Y is associated with X”

## Unidirectional:

- ▶ “X causes Y”

# Which variable is x and which is y?

In prediction we generally use  $X$  to denote the variable we are using to predict the variable of interest ( $Y$ )

In causation we generally use  $X$  to denote the explanatory (independent) and  $Y$  to denote the response (dependent)

Graphically the  $X$  variable is on the  $X$  (horizontal) axis and the  $Y$  variable is the  $Y$  (vertical) axis

# Which variable is x and which is y?

1. Each hospital's rate of hospital-acquired infections, and whether the hospital has implemented a hand-washing intervention as part of a cluster randomized trial.
2. The weight in kilograms and height in centimeters of a person
3. Inches of rain in the growing season and the yield of corn in bushels per day
4. A person's leg length and arm length, in centimeters



# How to investigate causation?

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- ▶ Randomized controlled trials (RCTs) to randomize individuals to different levels
- ▶ Observational study that is *designed* to investigate causation and reduce the risk of bias

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## Looking at relationships visually: Scatterplots

# Scatterplots

## Lecture 05: Relationships between 2 variables

- ▶ Scatterplots are a good way to visualize a relationship between two variables
- ▶ When we look at a scatterplot we want to evaluate:
- ▶ The overall Pattern of the dots
- ▶ Any notable exceptions to the pattern
- ▶ Direction (positive or negative)
- ▶ Form (straight line or curved)
- ▶ Strength (how closely the points follow a line)
- ▶ Are there any obvious outliers

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# Scatterplot Syntax in R

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```
name of plot <- ggplot(data = dataset, aes(x = xvariable, y = yvariable)) +  
geom_point(na.rm=TRUE) + theme_minimal(base_size = 15)+  
labs(x = "xlabel", y = "ylabel", title = "Title")
```

# Bi-directional relationships ex: systolic and diastolic BP

Read in NHANES dataset

```
nhanes_dataNA <- read_csv("nhanes.csv")
nhanes_data <- nhanes_dataNA[rowSums(is.na(nhanes_dataNA[, 15:18])) == 0, ]
names(nhanes_data)
```

```
## [1] "ridageyr" "agegroup" "gender" "military" "born"
## [6] "citizen" "drinks" "drinkscat" "bmxt" "bmxt"
## [11] "bmxhmi" "bmicat" "bpxpls" "bpxsy1" "bpxsy2"
## [16] "sys1d" "sys2d" "bpxdi1" "bpxdi2" "dias1d"
## [21] "dias2d" "bpcat" "chest" "fs1" "fs2"
## [26] "fs3" "lbdhdd" "hdlcat" "highhdl" "hi"
## [31] "asthma" "vwa" "vra" "va" "aspirin"
## [36] "sleep" "is" "hs" "lbdldl" "highldl"
```

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# Bi-directional relationships ex: systolic and diastolic BP

Relationships between two  
quantitative variables

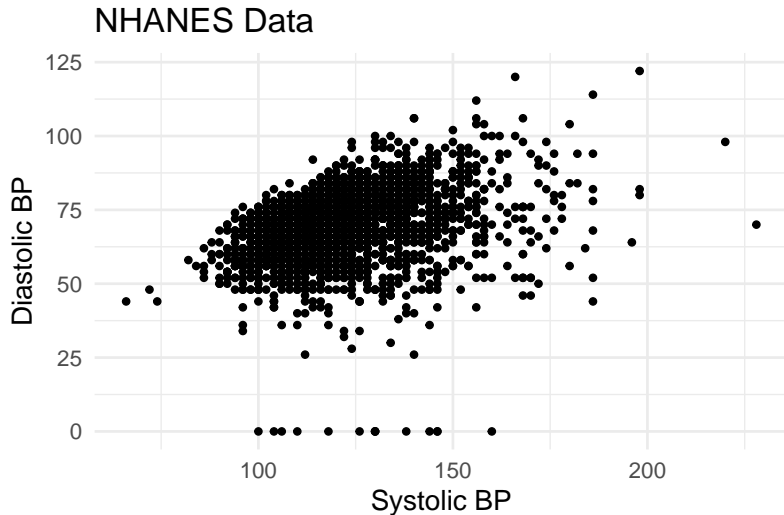
Looking at relationships  
visually: Scatterplots

Exploratory analysis using  
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Participation  
in a study: relationship  
between two variables with  
a number: Pearson's  
correlation

```
nhanes_scatter <- ggplot(data = nhanes_data, aes(x = bpxsy1, y = bpxdi1)) +  
  geom_point(na.rm=TRUE) + theme_minimal(base_size = 15)+  
  labs(x = "Systolic BP",  
       y = "Diastolic BP",  
       title = "NHANES Data")
```

# Bi-directional relationships ex: systolic and diastolic BP



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# Bi-directional relationships ex: systolic and diastolic BP

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What do we notice from the plot?

- ▶ Is there a visible association?
- ▶ Any notable exceptions to the pattern
- ▶ Direction (positive or negative)
- ▶ Form (straight line or curved)
- ▶ Strength (how closely the points follow a line)
- ▶ Are there any obvious outliers

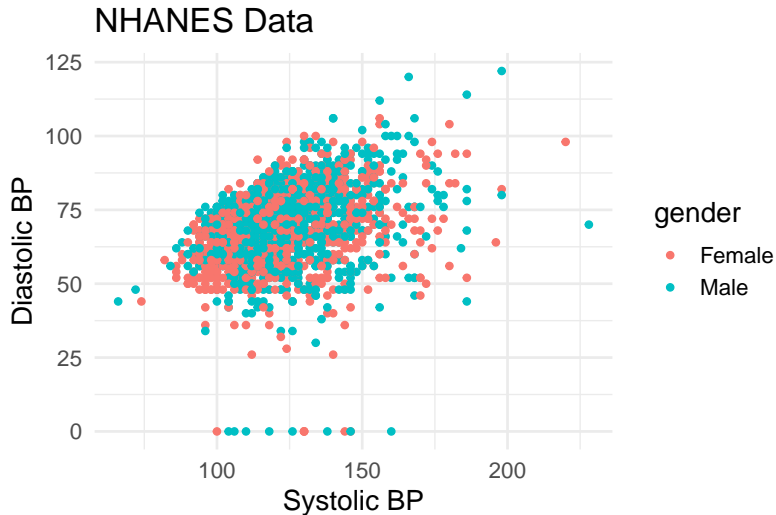


# Bi-directional relationships ex: systolic and diastolic BP

We can add a third variable to our graph by coloring the dots

```
nhanes_scatter <- ggplot(data = nhanes_data, aes(x = bpxsy1, y = bpxdi1)) +  
  geom_point(aes(col=gender), na.rm=TRUE) + theme_minimal(base_size = 15) +  
  labs(x = "Systolic BP",  
        y = "Diastolic BP",  
        title = "NHANES Data")
```

# Bi-directional relationships ex: systolic and diastolic BP



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# Association with a plausible direction

Manatee data set from your textbook:

```
mana_data <- read_csv("Ch03_Manatee-deaths.csv")  
head(mana_data)
```

```
## # A tibble: 6 x 3  
##   year powerboats deaths  
##   <dbl>      <dbl>   <dbl>  
## 1  1977         447     13  
## 2  1987         645     39  
## 3  1997         755     54  
## 4  2007        1027     73  
## 5  1978         460     21  
## 6  1988         675     43
```

# Power boats and Manatees

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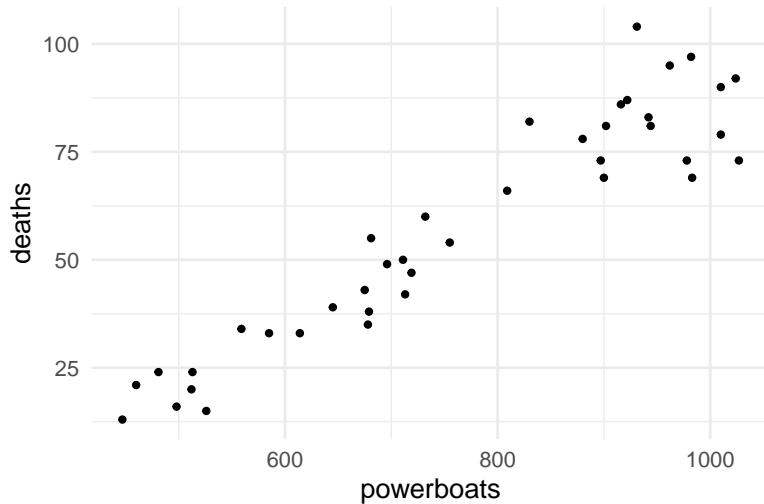
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Assessing a relationship  
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a number: Pearson's  
r

```
mana_scatter <- ggplot(data = mana_data, aes(x = powerboats, y = deaths)) +  
  geom_point() + theme_minimal(base_size = 15)
```

# Power boats and Manatees



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What do we notice from the plot?

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# Power boats and Manatees

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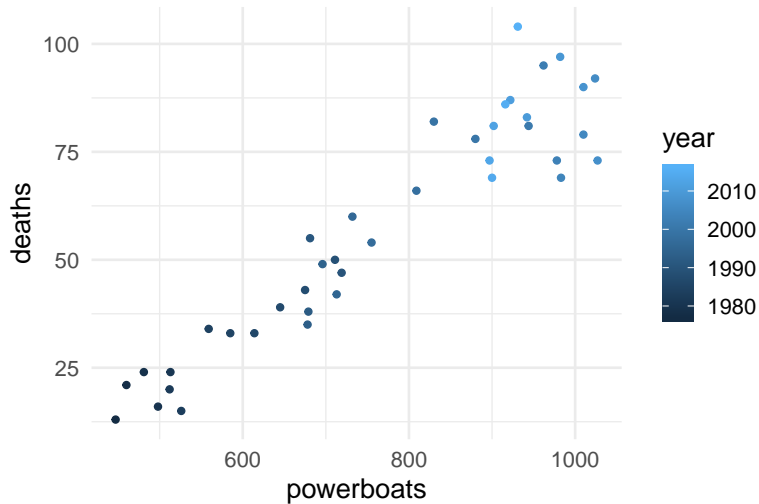
Participation

Assessing a relationship  
between two variables with  
a number: Pearson's  
correlation

What if we layer in a continuous third variable?

```
mana_scatter <- ggplot(data = mana_data, aes(x = powerboats, y = deaths)) +  
  geom_point(aes(col=year)) + theme_minimal(base_size = 15)
```

# Power boats and Manatees



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# Enzyme activity and temperature

Also from your book: A study examined the activity rate (in micromoles per second) of a digestive enzyme at varying temperatures.

```
## # A tibble: 6 x 2
##   temperature rate
##         <dbl> <dbl>
## 1         298  0.04
## 2         298  0.05
## 3         298  0.05
## 4         303  0.08
## 5         303  0.08
## 6         303  0.08
```

Relationships between two  
quantitative variables

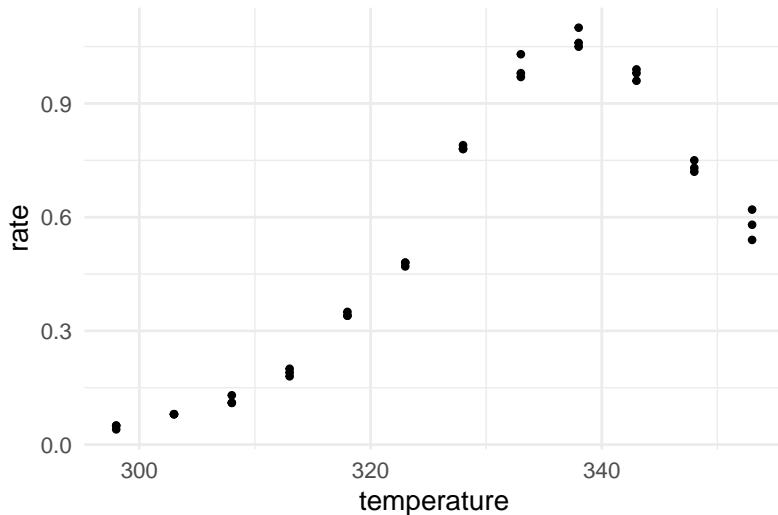
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# Enzyme activity and temperature



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# Enzyme activity and temperature

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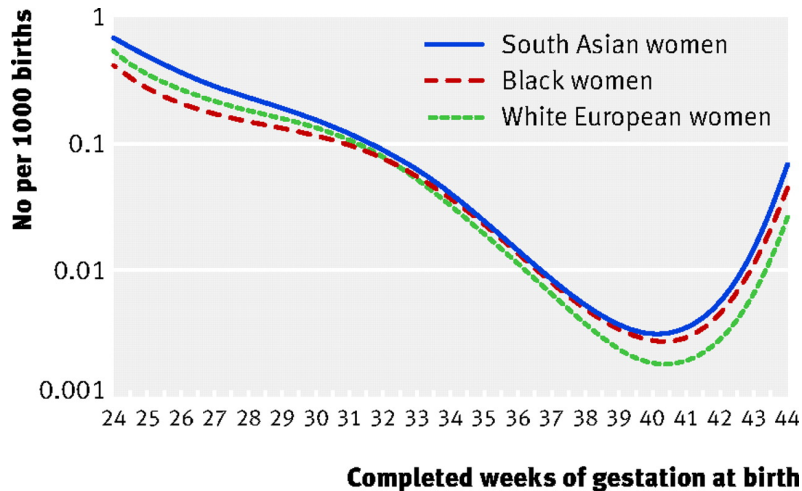
Assessing a relationship  
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What do we notice from the plot?

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# Another non-linear example

## Gestational age and perinatal mortality



Source: Balchin et al. BMJ. 2007.

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## Exploratory analysis using scatterplots

# Lean body mass and metabolic rate: Problem and Plan

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**Problem:** Is lean body mass (person's weight after removing the fat) associated with metabolic rate (kilocalories burned in 24 hours)?

**Plan:** A diet study was conducted on 12 women and 7 men that measured lean body weight and metabolic rate for each individual.

# Lean body mass and metabolic rate: DATA

Data: In the textbook

| Subject | Sex | Mass (kg) | Rate (Cal) | Subject | Sex | Mass (kg) | Rate (Cal) |
|---------|-----|-----------|------------|---------|-----|-----------|------------|
| 1       | M   | 62.0      | 1792       | 11      | F   | 40.3      | 1189       |
| 2       | M   | 62.9      | 1666       | 12      | F   | 33.1      | 913        |
| 3       | F   | 36.1      | 995        | 13      | M   | 51.9      | 1460       |
| 4       | F   | 54.6      | 1425       | 14      | F   | 42.4      | 1124       |
| 5       | F   | 48.5      | 1396       | 15      | F   | 34.5      | 1052       |
| 6       | F   | 42.0      | 1418       | 16      | F   | 51.1      | 1347       |
| 7       | M   | 47.4      | 1362       | 17      | F   | 41.2      | 1204       |
| 8       | F   | 50.6      | 1502       | 18      | M   | 51.9      | 1867       |
| 9       | F   | 42.0      | 1256       | 19      | M   | 46.9      | 1439       |
| 10      | M   | 48.7      | 1614       |         |     |           |            |

What would the corresponding data frame look like? How many variables would it have? How many rows?

Relationships between two quantitative variables

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# Lean body mass and metabolic rate: DATA

*# Note: you won't be tested on writing code using tibble::tribble()*

*# Do be able to look at the code and recognize that it is creating a data set*

```
weight_data <- tibble::tribble(  
  ~subject, ~gender, ~mass, ~rate,  
  1, "M", 62.0, 1792,  
  2, "M", 62.9, 1666,  
  3, "F", 36.1, 995,  
  4, "F", 54.6, 1425,  
  5, "F", 48.5, 1396,  
  6, "F", 42.0, 1418,  
  7, "M", 47.4, 1362,  
  8, "F", 50.6, 1502,  
  9, "F", 42.0, 1256,  
  10, "M", 48.7, 1614,  
  11, "F", 40.3, 1189,  
  12, "F", 33.1, 913
```



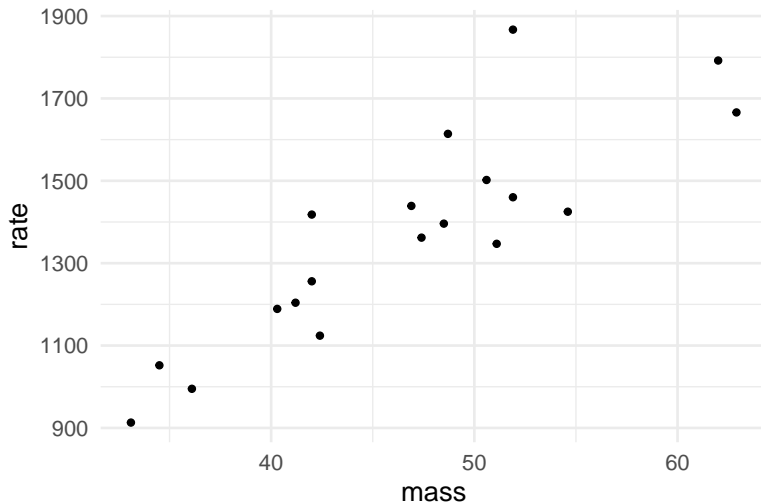
# Lean body mass and metabolic rate: Analysis

## Exploratory data analysis using scatter plots

```
weight_scatter <- ggplot(weight_data, aes(x = mass, y = rate)) +  
  geom_point() +  
  theme_minimal(base_size = 15)
```

# Lean body mass and metabolic rate: Analysis

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Assessing a relationship between two variables with a number: Pearson's correlation

# Analysis: Colour the points by gender

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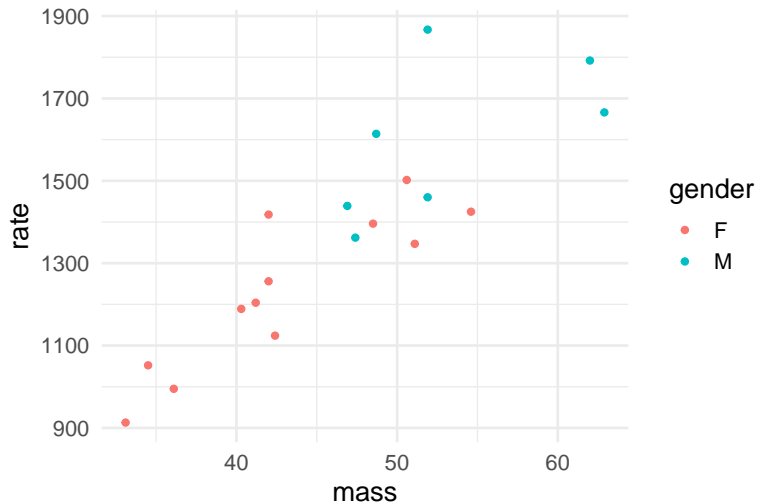
**Exploratory analysis using  
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Participation

Assessing a relationship  
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correlation

```
weight_scatter <- ggplot(weight_data, aes(x = mass, y = rate)) +  
  geom_point(aes(col=gender)) +  
  theme_minimal(base_size = 15)
```

# Analysis: Colour the points by gender



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## Analysis: Create separate plots for men and women

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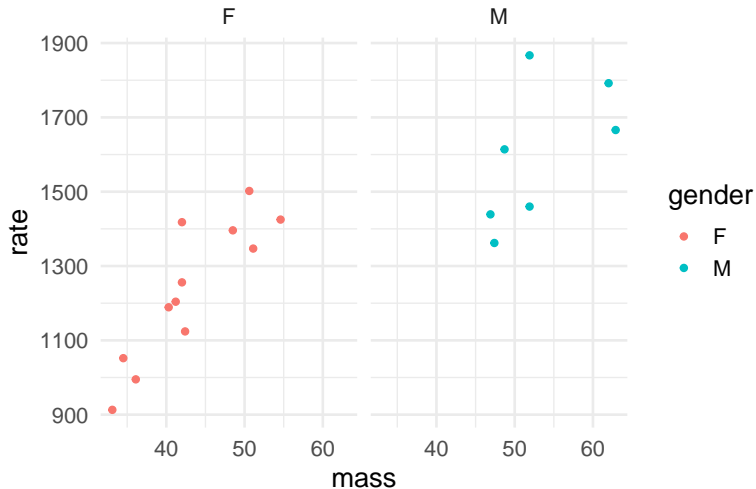
Participation

Assessing a relationship  
between two variables with  
a number: Pearson's  
correlation

```
weight_scatter <- ggplot(weight_data, aes(x = mass, y = rate)) +  
  geom_point(aes(col=gender)) +  
  theme_minimal(base_size = 15)+  
  facet_wrap(~ gender)
```

# Analysis: Create separate plots for men and women

weight\_scatter



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## Participation

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**Assessing a relationship  
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## Assessing a relationship between two variables with a number: Pearson's correlation



# Pearson's correlation

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Using just our eyes, we can often say something about whether an association between two variables is weak or strong.

But we can also use a numeric value to describe the direction and strength of an association

# Pearson's correlation

- ▶ For linear associations, we can use Pearson's correlation coefficient (denoted by  $r$ ) to quantify the strength of a linear relationship between two variables.
- ▶ The correlation between  $x$  and  $y$  is:

$$r = \frac{1}{n-1} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{s_x} \right) \left( \frac{y_i - \bar{y}}{s_y} \right)$$

Notice that because we are dividing by the standard deviation the values become unitless

Relationships between two quantitative variables

Looking at relationships visually: Scatterplots

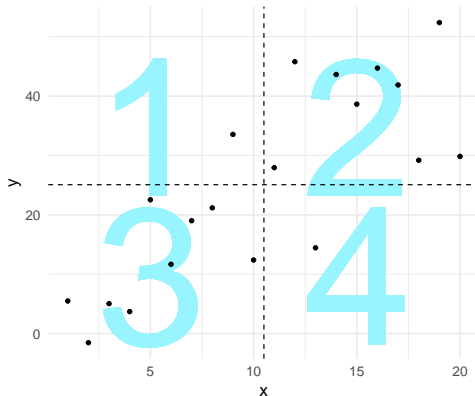
Exploratory analysis using scatterplots

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Assessing a relationship between two variables with a number: Pearson's correlation

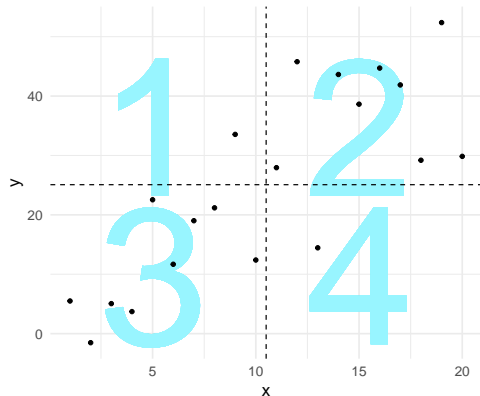
# Intuition about Pearson's correlation

To understand this formula, first only consider the numerators of the fractions (i.e.,  $x_i - \bar{x}$  and  $y_i - \bar{y}$ ). If you imagine a scatter plot of  $x$  and  $y$ , we can also add a dashed line at the mean  $x$  value of  $\bar{x}$  and a dashed line at the mean  $y$  value ( $\bar{y}$ ):



# Intuition about Pearson's correlation

$$r = \frac{1}{n-1} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{s_x} \right) \left( \frac{y_i - \bar{y}}{s_y} \right)$$



- Points in Q2 and Q3 contribute positive products to  $r$
- Points in Q1 and Q4 contribute negative products to  $r$

Relationships between two  
quantitative variables

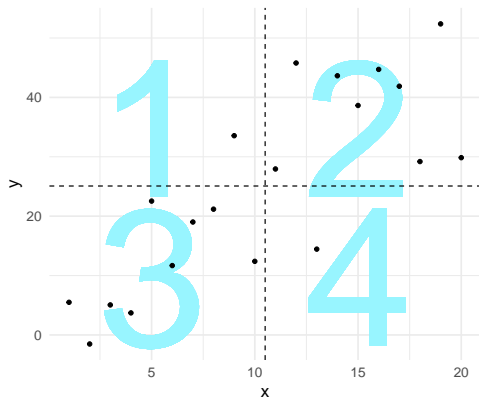
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# Intuition about Pearson's correlation



- ▶ The more there are points in Q2 and Q3 vs. Q1 and Q4, the more the value of the correlation coefficient will be higher and positive
- ▶ If you want even more of an explanation see the response to this [stack overflow post](#)

# Properties of the correlation coefficient

- ▶ Always a number between -1 and 1.
  - ▶ -1: A perfect, negative linear association
  - ▶ 1: A perfect, positive linear association
  - ▶ 0: No linear association
- ▶ Is used to measure the association between two *quantitative* variables.
- ▶ Only useful for *linear* associations!

# Corellation and direction

Relationships between two  
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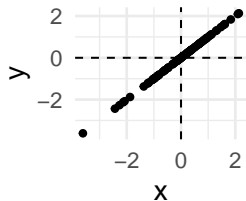
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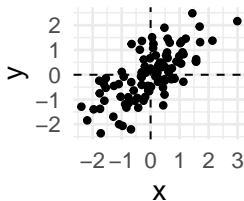
Participation

Assessing a relationship  
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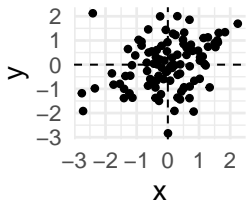
Correlation = 1



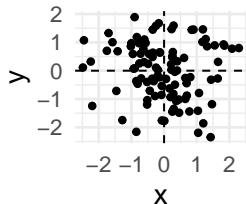
Correlation = 0.7



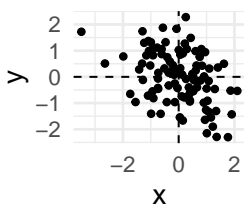
Correlation =



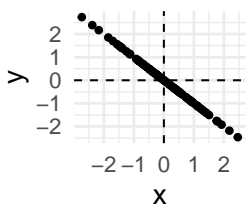
Correlation = -0.1



Correlation = -0.4



Correlation =



# Syntax: Pearson's correlation using `cor()`

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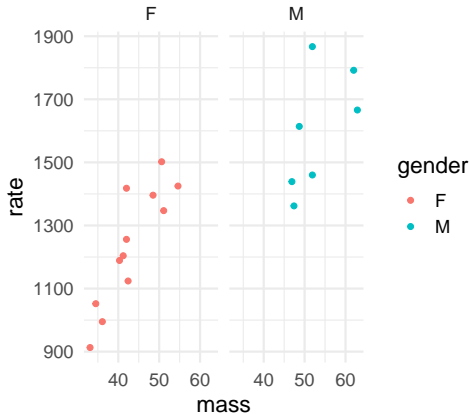
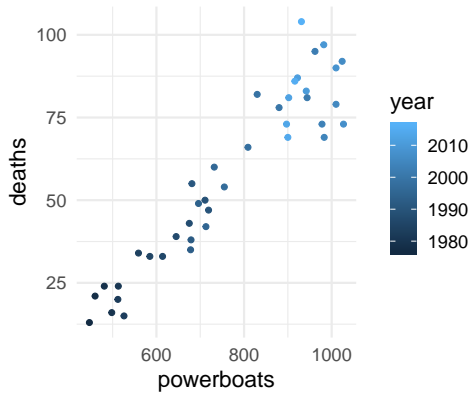
```
correlation coefficient <- dataset %>%
```

```
summarize(newvar = cor(xvar, yvar))
```



# Syntax: Pearson's correlation using `cor()`

Remember the manatee plot and the weight plot:



Relationships between two  
quantitative variables

Looking at relationships  
visually: Scatterplots

Exploratory analysis using  
scatterplots

Participation

Assessing a relationship  
between two variables with  
a number: Pearson's  
correlation

## Syntax: Pearson's correlation using cor()

Now, calculate the correlations between X and Y for manatees:

```
mana_cor <- mana_data %>%  
  summarize(corr_mana = cor(powerboats, deaths))  
mana_cor
```

```
## # A tibble: 1 x 1  
##   corr_mana  
##   <dbl>  
## 1      0.945
```

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# Syntax: Pearson's correlation using cor()

And for the weight data:

```
weight_cor <- weight_data %>%  
  summarize(corr_weight = cor(mass, rate))  
weight_cor
```

```
## # A tibble: 1 x 1  
##   corr_weight  
##         <dbl>  
## 1         0.865
```

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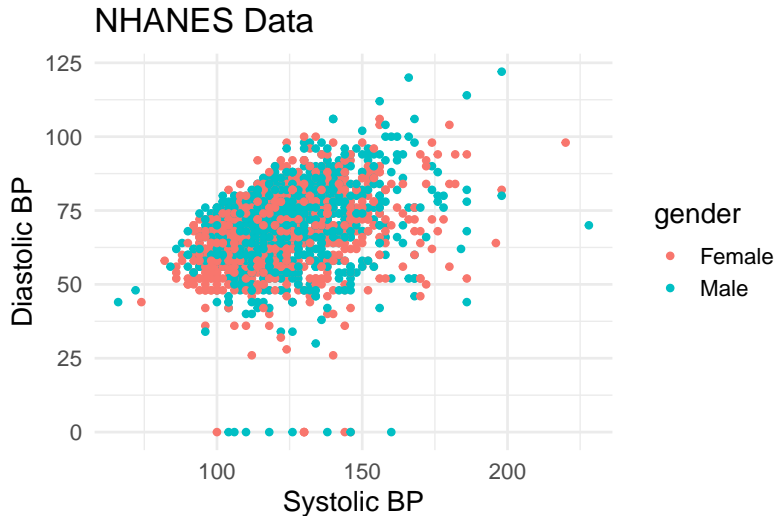
Exploratory analysis using  
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correlation

## Syntax: Pearson's correlation using `cor()`

What about our blood pressure data from NHANES?



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correlation

## Syntax: Pearson's correlation using cor()

```
bp_cor <- nhanes_data %>%  
  summarize(corrbp = cor(bpxsy1, bpxdi1))  
bp_cor
```

```
## # A tibble: 1 x 1  
##   corrbp  
##   <dbl>  
## 1  0.322
```

Relationships between two  
quantitative variables

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visually: Scatterplots

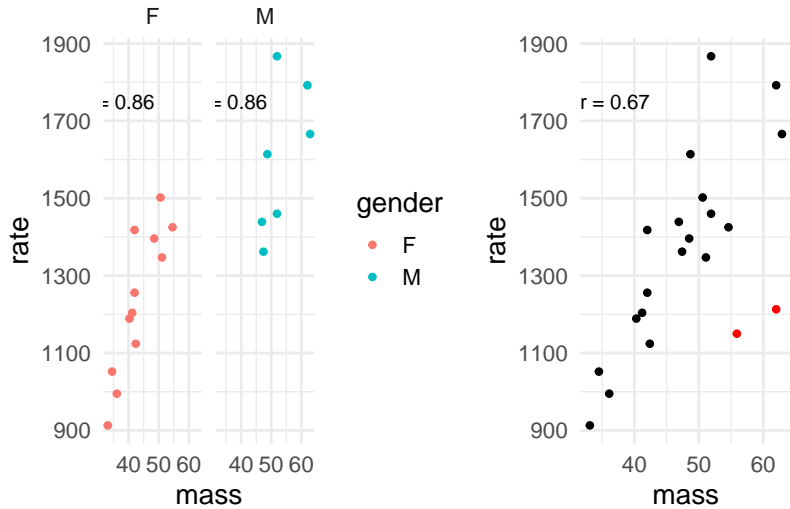
Exploratory analysis using  
scatterplots

Participation

Assessing a relationship  
between two variables with  
a number: Pearson's  
correlation

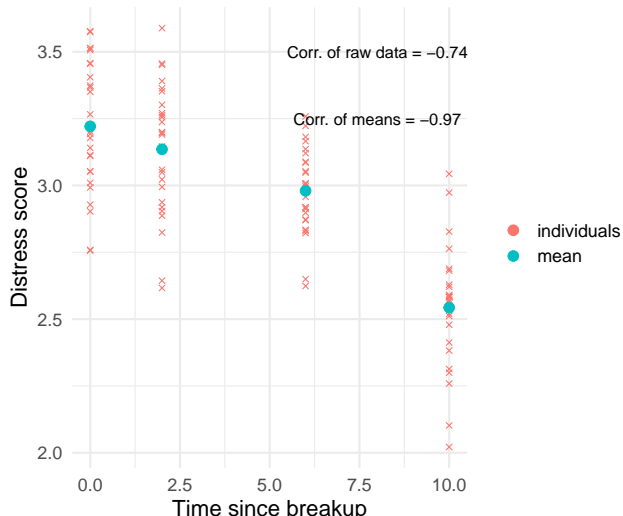
# Properties of the correlation coefficient

The correlation coefficient is not resistant to outliers, notice what happens when we add two outliers (in red) to the weight\_data and recalculate correlation



# Properties of the correlation coefficient

- ▶ Correlations for average measures is typically stronger than correlations for individual data



# Important concepts

## Lecture 05: Relationships between 2 variables

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Assessing a relationship  
between two variables with  
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correlation

- ▶ Determine which variable is explanatory and which is response, or when it doesn't matter
- ▶ Visually describe the relationship between two variables (form, direction, strength, and outliers)
- ▶ Numerically describe the relationship with the correlation coefficient  $r$



## R Recap: What functions did we use?

- ▶ `geom_point()`,
- ▶ `aes(col = gender)` to color points by levels of gender
- ▶ `summarize()` to calculate correlation using `cor(var1, var2)`

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correlation

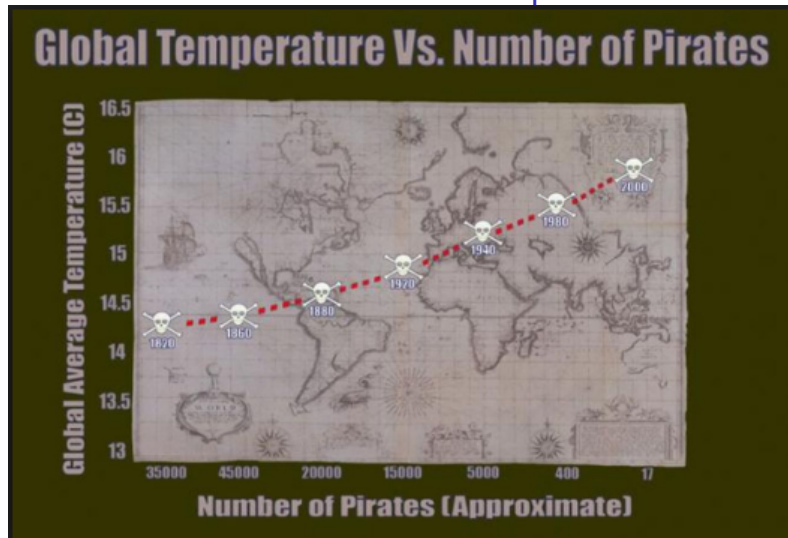
# Reminder: Association does not equal causation

Remember that just because two variables are associated, does not mean there is a causal relationship

The correlation coefficient measures association *not* causation.

Even a very strong association doesn't mean that one variable causes the other.

## Reminder: Association does not equal causation



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This image is one from a Forbes.com article but this example pops up in lots of places