# 1sttheory: An R Package for Fast Computation of State Trait Models

Axel Mayer University of Jena

Christian Geiser Utah State University Rolf Steyer University of Jena

David A. Cole Vanderbilt University

December 22, 2013

#### Abstract

This R (?, ?) package is a supplement for the article 'A Theory of States and Traits' (Steyer, Geiser, Cole, & Mayer, 2013). It is based on the structural equation modeling R package lavaan (Rosseel, 2012) and provides a convenient interface to compute some common models of the revised latent state-trait theory (LST-R theory). The main function of the package allows for easy specification of multistate, multistate-singletrait, and multistate-multitrait models. It automatically generates lavaan syntax for these models, runs the models, and returns model estimates together with reliability, occasion specificity, and consistency coefficients for the respective models. There is also an additional package called lsttheoryGUI, which depends on lsttheory. The lsttheoryGUI provides a graphical user interface, i.e., a click menu, for users who are not familiar with R. lsttheoryGUI works best with the JGR console for R (Markus Helbig, Simon Urbanek, & Ian Fellows, 2013).

**Keywords:** states, traits, reliability, occasion specificity, consistency

Cautionary Note: The package is currently under development and some things may change in the future. We are at an early stage of development and it is likely that the structure and key aspects of the two packages will change. The latest versions can be downloaded from metheval.uni-jena.de. We also plan to release the package on CRAN, once we are a bit further in the development process. Please report any bugs.

# Contents

1	Inti	roduction	3				
<b>2</b>	Installation						
	2.1	Windows Installation	3				
	2.2	Linux Installation	3				
	2.3	Loading the Package	4				
3	Mu	ltistate Models	5				
	3.1	Multistate Model with $\eta_t$ -Congenericity	5				
	3.2	Multistate Model with Essential $\eta_t$ -Equivalence	9				
	3.3	Multistate Model with $\eta_t$ -Equivalence	10				
	3.4	Multistate Models with Scale Invariance	11				
	3.5	Multistate Models with Method Factors	12				
4	Mu	ltistate-Singletrait Models	13				
	4.1	Multistate-Singletrait Models with $\theta$ -Congenericity	13				
	4.2	Multistate-Singletrait Models with $\theta\textsc{-}\textsc{Equivalence}$	14				
5	Mu	ltistate-Doubletrait Models	16				
	5.1	Multistate-Double trait Models with $\theta_1, \theta_2$ -Congenericity	16				
6	Plo	t LST-R Theory Models with semPlot	18				
7	Gra	phical User Interface 1sttheoryGUI	19				

## 1 Introduction

1sttheory allows for easy specification of multistate, multistate-singletrait, and multistate-multitrait models. This vignette is structured as follows: We first describe the installation process in detail for nonexperienced users of R. Users who are familiar with package installation from local .zip files may wish to skip this section. We then present various kinds of LST-R theory models with syntax and model results.

#### 2 Installation

The R package 1sttheory will most likely be installed from a local file. Therefore, we need to install the dependencies first. The installation has been tested under Windows 7 and under Linux (Ubuntu 11.10). It should also work under Mac OS X using the JGR console — but we haven't tested it yet. Please make sure that you are using R version 3.0.1 or higher.

#### 2.1 Windows Installation

For a Windows installation (without Rtools) we suggest installing the dependencies from a CRAN mirror first by executing

```
install.packages("lavaan") ## for lsttheory
install.packages("Deducer") ## for lsttheoryGUI
```

in the console (either the standard Roonsole or the JGR console) and then selecting a mirror next to you. After that, the R package lsttheory can be installed using the Windows binary file (with file ending .zip) as follows:

```
install.packages("D:/workspace/lsttheory_0.1-1.zip")
install.packages("D:/workspace/lsttheoryGUI_0.1-1.zip")
```

Please adjust the file path and version number accordingly. We recommend using the JGR console (http://rforge.net/JGR/). The JGR console can be called via a launcher or from with an R session by calling

```
library(JGR)
JGR()
```

#### 2.2 Linux Installation

We assume that Linux users are familiar with installing R packages from source. The source files are lsttheory\_0.1-1.tar.gz and lsttheoryGUI\_0.1-1.tar.gz.

Note that for the graphical user interface to work, the user may want to use the JGR console. The JGR console can be called from with an R session by calling

```
library(JGR)
JGR()
```

## 2.3 Loading the Package

After having succesfully installed the packages, we need to load them:

```
library("lsttheory")

## Loading required package: lavaan

## This is lavaan 0.5-16

## lavaan is BETA software! Please report any bugs.

# library('lsttheoryGUI')
```

If you are using the JGR console, you can click on default next to the lsttheory and lsttheoryGUI entry in the Package Installer. Then the packages and their dependencies are automatically loaded every time you open JGR.

#### 3 Multistate Models

The lsttheory pacakee contains several simulated example datasets. The first one that we use is the dataset multistate. It contains 9 manifest variables  $Y_{it}$ , where the index refers to the *i*th manifest variable assessed at occasion t.

```
data(multistate)
head(round(multistate, 2))
##
            y21
                  y31
                        y12
                              y22
                                    y32
                                           y13
                                                y23
                                                      y33
                 4.54
##
      3.88
           4.76
                       3.95
                             5.68
                                   2.53
                                          2.18
                                                3.74
                                                      3.29
           2.40
                 2.42
                       2.52
                             3.33
      0.02
                                   0.33
                                          0.08
                                                1.61
                                                      0.83
## 3
      0.06
           1.54 -0.86
                       0.12 - 1.19
                                   1.69
                                          1.59
                                                2.49
                                                     0.20
           3.41 3.31 2.63 1.83
                                   3.29
                                               2.05
     2.70
                                          2.47
## 5 0.30 2.03 -0.08 0.46 1.41 1.19 -1.58 -1.40 0.97
## 6 -5.13 -3.78 -3.23 -0.34 1.48 -1.64 -2.36 -3.27 -0.78
```

#### 3.1 Multistate Model with $\eta_t$ -Congenericity

First, we use this dataset to fit a multistate model with  $\eta_t$ -congenericity and conditional mean independence (see Box 4.1 of SGCM). The main function of our package to be called by the user is 1sttheory. See ?1sttheory for details. It is used to fit all models. The multistate model with  $\eta_t$ -congenericity can be specified as follows:

```
m1 <- lsttheory(neta = 3, data = multistate)</pre>
print(m1)
##
##
   Multistate Model
##
##
       rely spey cony
## y11 0.73
               NA
                    NA
## y21 0.83
               NA
                    NA
## y31 0.64
               NA
                    NA
## y12 0.77
               NA
                    NA
## y22 0.81
               NA
                    NA
## y32 0.65
               NA
                    NA
## y13 0.74
                    NA
               NA
## y23 0.79
               NA
                     NA
## y33 0.68
               NA
                    NA
##
##
```

The lsttheory function just requires two mandatory arguments: The number of common state variables  $\eta_t$  and the dataset to use. In the current version of our package, the dataset may only include the manifest variables  $Y_{it}$  and these should be ordered by occasion t and indicator i, i.e.,  $Y_{11}, Y_{21}, \ldots, Y_{12}, Y_{22}, \ldots, Y_{13}, Y_{23}, \ldots$ . The lsttheory function returns an object of class lsttheory for which several methods are available. print(m1) shows reliability, occasion specificity, and consistency coefficients (see Box 3.1 of SGCM). For the multistate model only reliability coefficients are available, because traits are not modeled.

The function lsttheory has automaticall generated lavaan input syntax:

```
cat(m1@lavaansyntax)
## eta1 =^{\sim} 1*y11
## eta1 =~ la211*y21
## eta1 =~ la311*y31
## eta2 =~ 1*y12
## eta2 =~ la221*y22
## eta2 =~ la321*y32
## eta3 =^{\sim} 1*y13
## eta3 =~ la231*y23
## eta3 =~ la331*y33
## y11 ~ 0*1
## y21 ~ la210*1
## v31 ~ la310*1
## y12 ~ 0*1
## y22 ~ la220*1
## y32 ~ la320*1
## y13 ~ 0*1
## y23 ~ la230*1
## y33 ~ la330*1
## eta1 ~ ga10*1
## eta2 ~ ga20*1
## eta3 ~ ga30*1
## y11 ~~ eps11*y11
## y21 ~~ eps21*y21
## y31 ~~ eps31*y31
## y12 ~~ eps12*y12
## y22 ~~ eps22*y22
## y32 ~~ eps32*y32
## y13 ~~ eps13*y13
## y23 ~~ eps23*y23
## y33 ~~ eps33*y33
## eta1 ~~ psi1*eta1
## eta2 ~~ psi2*eta2
## eta3 ~~ psi3*eta3
##
```

```
##
##
## vareta1 := psi1
## vareta2 := psi2
## vareta3 := psi3
## vary11 := 1^2 * vareta1 + eps11
## vary21 := la211^2 * vareta1 + eps21
## vary31 := la311^2 * vareta1 + eps31
## vary12 := 1^2 * vareta2 + eps12
## vary22 := la221^2 * vareta2 + eps22
## vary32 := la321^2 * vareta2 + eps32
## vary13 := 1^2 * vareta3 + eps13
## vary23 := la231^2 * vareta3 + eps23
## vary33 := la331^2 * vareta3 + eps33
## rely11 := 1^2 * vareta1 / vary11
## rely21 := la211^2 * vareta1 / vary21
## rely31 := la311^2 * vareta1 / vary31
## rely12 := 1^2 * vareta2 / vary12
## rely22 := la221^2 * vareta2 / vary22
## rely32 := la321^2 * vareta2 / vary32
## rely13 := 1^2 * vareta3 / vary13
## rely23 := la231^2 * vareta3 / vary23
## rely33 := la331^2 * vareta3 / vary33
```

and the lavaan output can be seen by calling:

```
summary(m1@lavaanres)
## lavaan (0.5-16) converged normally after 47 iterations
##
    Number of observations
                                                      1000
##
##
    Estimator
                                                        ML
##
    Minimum Function Test Statistic
                                                    32.025
##
    Degrees of freedom
                                                        24
##
    P-value (Chi-square)
                                                    0.126
##
## Parameter estimates:
##
##
    Information
                                                  Expected
##
    Standard Errors
                                                  Standard
##
                      Estimate Std.err Z-value P(>|z|)
## Latent variables:
```

##	eta1 =~						
##	y11		1.000				
##	y11 y21	(1211)	1.221	0.034	35.656	0.000	
	y21 y31	(1311)		0.034	30.166	0.000	
##	y31 eta2 =~	(1311)	0.801	0.021	30.100	0.000	
##			1 000				
##	y12	(1001)	1.000	0 020	27 420	0.000	
##	y22	(1221)	1.211	0.032	37.430	0.000	
##	y32 eta3 =~	(1321)	0.772	0.024	31.867	0.000	
##	y13		1 000				
##	y13 y23	(1231)	1.000 1.233	0.035	34.906	0.000	
##	y23 y33	(1231)	0.828	0.035	31.450	0.000	
##	y 3 3	(1331)	0.020	0.020	31.430	0.000	
	Covariances	a •					
##	eta1 ~~	<b>.</b>					
##	eta1		2.041	0.131	15.535	0.000	
##	eta2		1.856	0.126	14.769	0.000	
##	eta2 ~~		1.000	0.120	14.700	0.000	
##	eta3		2.039	0.131	15.523	0.000	
##	0000		2.000	0.101	10.020	0.000	
	Intercepts	:					
##	y11	•	0.000				
##	y21	(1210)	0.217	0.054	4.030	0.000	
##	y31	(1310)	0.570	0.044	12.812	0.000	
##	y12		0.000				
##	y22	(1220)	0.212	0.060	3.539	0.000	
##	y32	(1320)	0.578	0.047	12.358	0.000	
##	y13		0.000				
##	y23	(1230)	0.262	0.055	4.779	0.000	
##	у33	(1330)	0.574	0.043	13.466	0.000	
##	eta1	(ga10)	0.611	0.063	9.758	0.000	
##	eta2	(ga20)	1.071	0.063	17.010	0.000	
##	eta3	(ga30)	0.495	0.062	7.925	0.000	
##							
##	Variances:						
##	y11	(ep11)	1.070	0.068			
##	y21	(ep21)	0.874	0.079			
##	у31	(ep31)	1.029	0.057			
##	y12	(ep12)	0.932	0.063			
##	y22	(ep22)	1.036	0.082			
##	у32	(ep32)	0.956	0.053			
##	y13	(ep13)	1.028	0.067			
##	y23	(ep23)	1.146	0.089			
##	у33	(ep33)	0.944	0.055			
##	eta1	(psi1)	2.845	0.175			

```
##
        eta2
                (psi2)
                            3.035
                                      0.179
##
        eta3
                (psi3)
                            2.869
                                      0.175
##
##
   Defined parameters:
##
        vareta1
                            2.845
                                      0.175
                                               16.243
                                                           0.000
                            3.035
                                      0.179
                                               16.973
                                                           0.000
##
        vareta2
##
                            2.869
                                      0.175
                                                16.387
                                                           0.000
        vareta3
##
        vary11
                            3.914
                                      0.175
                                               22.361
                                                           0.000
##
        vary21
                            5.116
                                      0.229
                                               22.361
                                                           0.000
##
        vary31
                            2.853
                                      0.128
                                               22.361
                                                           0.000
##
        vary12
                            3.967
                                      0.177
                                               22.361
                                                           0.000
##
        vary22
                                      0.245
                                               22.361
                                                           0.000
                            5.483
                                      0.124
                                               22.361
##
        vary32
                            2.765
                                                           0.000
##
        vary13
                            3.897
                                      0.174
                                               22.361
                                                           0.000
##
        vary23
                            5.511
                                      0.246
                                               22.361
                                                           0.000
                                      0.130
                                               22.361
                                                           0.000
##
        vary33
                            2.912
##
        rely11
                            0.727
                                      0.019
                                               37.877
                                                           0.000
##
                                      0.017
        rely21
                            0.829
                                               49.704
                                                           0.000
##
        rely31
                            0.639
                                      0.022
                                               29.628
                                                           0.000
##
        rely12
                            0.765
                                      0.018
                                               43.377
                                                           0.000
##
        rely22
                            0.811
                                      0.016
                                               49.447
                                                           0.000
##
                                      0.021
        rely32
                            0.654
                                               31.323
                                                           0.000
                            0.736
                                      0.019
##
        rely13
                                                38.680
                                                           0.000
##
        rely23
                            0.792
                                      0.018
                                                45.000
                                                           0.000
##
        rely33
                            0.676
                                      0.021
                                               32.679
                                                           0.000
```

The slot lavaanres in the m1 object contains the fitted lavaan object of class lavaan. See ?"lavaan-class" for more information and available methods.

## 3.2 Multistate Model with Essential $\eta_t$ -Equivalence

The default setting of the lsttheory function is to assume  $\eta_t$ -congenericity. If we want to assume essential  $\eta_t$ -equivalence, we need to specify an additional argument, namely the equiv.assumption argument, which is a list of equivalence assumptions. For the multistate model, the xi argument will be ignored. By specifying tau="ess", we assume essential  $\eta_t$ -equivalence:

```
m1 <- lsttheory(neta = 3, data = multistate, equiv.assumption = list(tau = "ess",
    xi = "equi"))
coef(m1@lavaanres, type = "user")
                                                   eta2=~y22
##
    eta1=~y11
                eta1=~y21
                           eta1=~y31
                                       eta2=~y12
                                                               eta2=~y32
##
        1.000
                    1.000
                                1.000
                                            1.000
                                                       1.000
                                                                   1.000
##
    eta3=~y13
                eta3=~y23
                           eta3=~y33
                                                       la210
                                                                   1a310
                                           y11~1
##
        1.000
                    1.000
                                1.000
                                           0.000
                                                       0.352
                                                                   0.448
```

##	y12~1	la220	1a320	y13~1	la230	1a330
##	0.000	0.438	0.334	0.000	0.378	0.489
##	ga10	ga20	ga30	eps11	eps21	eps31
##	0.611	1.071	0.495	1.064	1.375	0.962
##	eps12	eps22	eps32	eps13	eps23	eps33
##	0.993	1.563	0.891	1.083	1.674	0.831
##	psi1	psi2	psi3	eta1~~eta2	eta1~~eta3	eta2~~eta3
##	2.721	2.747	2.715	1.946	1.794	1.909
##	vareta1	vareta2	vareta3	vary11	vary21	vary31
##	2.721	2.747	2.715	3.785	4.096	3.683
##	vary12	vary22	vary32	vary13	vary23	vary33
##	3.740	4.310	3.638	3.798	4.389	3.546
##	rely11	rely21	rely31	rely12	rely22	rely32
##	0.719	0.664	0.739	0.735	0.637	0.755
##	rely13	rely23	rely33			
##	0.715	0.619	0.766			

#### 3.3 Multistate Model with $\eta_t$ -Equivalence

Similarly, if we want to assume  $\eta_t$ -equivalence, we specify the equivalence assumption as follows:

```
m1 <- lsttheory(neta = 3, data = multistate, equiv.assumption = list(tau = "equi",
    xi = "equi"))
coef(m1@lavaanres, type = "user")
##
    eta1=~y11
                eta1=~y21
                            eta1=~y31
                                        eta2=~y12
                                                   eta2=~y22
                                                               eta2=~y32
##
        1.000
                    1.000
                                1.000
                                            1.000
                                                        1.000
                                                                    1.000
                            eta3=~y33
##
    eta3=~y13
                eta3=~y23
                                            y11~1
                                                        y21~1
                                                                    y31~1
##
        1.000
                    1.000
                                1.000
                                            0.000
                                                        0.000
                                                                    0.000
##
        y12~1
                    y22~1
                                y32~1
                                            y13~1
                                                        y23~1
                                                                    y33~1
##
        0.000
                    0.000
                                0.000
                                            0.000
                                                        0.000
                                                                    0.000
##
         ga10
                     ga20
                                 ga30
                                            eps11
                                                        eps21
                                                                    eps31
##
        0.885
                    1.316
                                0.803
                                            1.193
                                                        1.387
                                                                    0.992
##
        eps12
                    eps22
                                eps32
                                            eps13
                                                        eps23
                                                                    eps33
                                            1.240
##
        1.117
                    1.643
                                0.866
                                                        1.688
                                                                    0.869
                                 psi3 eta1~~eta2 eta1~~eta3 eta2~~eta3
##
         psi1
                     psi2
##
        2.705
                    2.696
                                2.697
                                            1.936
                                                        1.798
                                                                    1.898
##
      vareta1
                  vareta2
                              vareta3
                                           vary11
                                                       vary21
                                                                   vary31
##
        2.705
                    2.696
                                2.697
                                            3.897
                                                        4.092
                                                                    3.697
##
       vary12
                   vary22
                               vary32
                                           vary13
                                                       vary23
                                                                   vary33
##
        3.813
                    4.338
                                3.562
                                            3.937
                                                        4.385
                                                                    3.566
##
       rely11
                   rely21
                               rely31
                                           rely12
                                                       rely22
                                                                   rely32
##
        0.694
                    0.661
                                0.732
                                            0.707
                                                        0.621
                                                                    0.757
```

```
## rely13 rely23 rely33
## 0.685 0.615 0.756
```

#### 3.4 Multistate Models with Scale Invariance

In order to add scale invariance assumptions over time, we need to specify the scale.invariance argument. The default is not to assume scale invariance. The scale invariance argument is a list of four entries. For the multistate models, only the first and the second entry are relevant. The first entry refers to scale invariance of intercepts and the second entry refers to scale invariance of loadings. For example, if we want to specify a multistate model with  $\eta_t$ -congenericity and scale invariance of intercepts and loadings, the function call is:

```
m1 <- lsttheory(neta = 3, data = multistate, scale.invariance = list(lait0 = TRUE,
    lait1 = TRUE, gat0 = TRUE, gat1 = TRUE))
coef(m10lavaanres, type = "user")
##
    eta1=~y11
                    la211
                                 la311
                                        eta2=~y12
                                                         la211
                                                                     1a311
                     1.219
##
         1.000
                                 0.798
                                             1.000
                                                         1.219
                                                                     0.798
    eta3=~y13
                     la211
                                             y11~1
                                                         la210
                                                                     1a310
##
                                 la311
##
         1.000
                     1.219
                                 0.798
                                             0.000
                                                         0.229
                                                                     0.570
        y12~1
                                             y13~1
##
                     la210
                                 la310
                                                         la210
                                                                     1a310
##
         0.000
                     0.229
                                 0.570
                                             0.000
                                                         0.229
                                                                     0.570
##
         ga10
                      ga20
                                  ga30
                                             eps11
                                                         eps21
                                                                     eps31
         0.606
                                 0.515
##
                     1.056
                                             1.068
                                                         0.875
                                                                     1.030
##
         eps12
                     eps22
                                 eps32
                                             eps13
                                                         eps23
                                                                     eps33
         0.943
                     1.041
                                 0.945
                                             1.014
                                                                     0.960
##
                                                         1.142
##
         psi1
                     psi2
                                  psi3 eta1~~eta2 eta1~~eta3 eta2~~eta3
##
         2.853
                     2.973
                                 2.950
                                             2.024
                                                         1.883
                                                                     2.046
                                            vary11
                                                                    vary31
##
      vareta1
                  vareta2
                              vareta3
                                                        vary21
##
         2.853
                     2.973
                                 2.950
                                             3.922
                                                         5.116
                                                                     2.847
##
       vary12
                   vary22
                                vary32
                                            vary13
                                                        vary23
                                                                    vary33
##
        3.916
                     5.459
                                 2.838
                                             3.964
                                                         5.526
                                                                     2.838
##
       rely11
                   rely21
                                rely31
                                            rely12
                                                        rely22
                                                                    rely32
##
        0.728
                     0.829
                                 0.638
                                             0.759
                                                         0.809
                                                                     0.667
##
       rely13
                   rely23
                                rely33
##
        0.744
                     0.793
                                 0.662
```

Of course, the scale invariance argument can also be used for a multistate model with essential  $\eta_t$ -equivalence. Then, the lait1 entry is ignored.

```
m1 <- lsttheory(neta = 3, data = multistate, equiv.assumption = list(tau = "ess",
    xi = "equi"), scale.invariance = list(lait0 = TRUE, lait1 = TRUE, gat0 = TRUE,
    gat1 = TRUE))</pre>
```

For a multistate model with  $\eta_t$ -equivalence, all scale invariance settings are ignored.

# 3.5 Multistate Models with Method Factors

Section under development

# 4 Multistate-Singletrait Models

#### 4.1 Multistate-Singletrait Models with $\theta$ -Congenericity

The same function lst theory can also be used to fit multistate-single trait models in LST-R theory. We only need to specify that there is one  $\xi$  variable<sup>1</sup> in addition to the specification of the corresponding multistate model. The following syntax specifies a multistate-single trait model with the these assumptions:

- $\eta_t$ -congenericity (Box 4.1 of SGCM)
- conditional mean independence (Box 4.1 of SGCM)
- $\theta$ -congenericity (Box 5.1 of SGCM)

```
m1 <- lsttheory(neta = 3, nxi = 1, data = multistate)</pre>
print(m1)
##
##
    Singletrait-Multistate Model
##
       rely spey cony
## y11 0.73 0.25 0.47
## y21 0.83 0.29 0.54
## y31 0.64 0.22 0.42
## y12 0.77 0.20 0.57
## y22 0.81 0.21 0.60
## y32 0.65 0.17 0.48
## y13 0.74 0.26 0.48
## y23 0.79 0.28 0.51
## y33 0.68 0.24 0.44
##
##
```

We now also get estimates for the occasion specificity and consistency coefficients in addition to the reliability coefficients. To see all parameters of the model:

```
coef(m1@lavaanres, type = "user")
## eta1=~y11
                  la211
                            la311 eta2=~y12
                                                  la221
                                                             la321 eta3=~y13
##
       1.000
                  1.221
                            0.801
                                       1.000
                                                                        1.000
                                                  1.211
                                                             0.772
##
       la231
                  la331
                            y11~1
                                       la210
                                                  la310
                                                             y12~1
                                                                        1a220
##
       1.233
                  0.828
                             0.000
                                       0.217
                                                             0.000
                                                                        0.212
                                                  0.570
##
       1a320
                  y13~1
                             1a230
                                       1a330
                                                 eta1~1
                                                              ga20
                                                                         ga30
```

<sup>&</sup>lt;sup>1</sup>The names of the variables will be changed to be in line with SGCM

##	0.578	0.000	0.262	0.574	0.000	0.400	-0.115
##	eps11	eps21	eps31	eps12	eps22	eps32	eps13
##	1.070	0.874	1.029	0.932	1.036	0.956	1.028
##	eps23	eps33	psi1	psi2	psi3	xi1=~eta1	ga21
##	1.146	0.944	0.988	0.792	1.014	1.000	1.099
##	ga31	varxi1	mxi1	vareta1	vareta2	vareta3	vary11
##	0.999	1.857	0.611	2.845	3.035	2.869	3.914
##	vary21	vary31	vary12	vary22	vary32	vary13	vary23
##	5.116	2.853	3.967	5.483	2.765	3.897	5.511
##	vary33	rely11	rely21	rely31	rely12	rely22	rely32
##	2.912	0.727	0.829	0.639	0.765	0.811	0.654
##	rely13	rely23	rely33	spey11	spey21	spey31	spey12
##	0.736	0.792	0.676	0.252	0.288	0.222	0.200
##	spey22	spey32	spey13	spey23	spey33	cony11	cony21
##	0.212	0.171	0.260	0.280	0.239	0.474	0.541
##	cony31	cony12	cony22	cony32	cony13	cony23	cony33
##	0.417	0.565	0.599	0.483	0.476	0.512	0.437

## 4.2 Multistate-Singletrait Models with $\theta$ -Equivalence

We don't show all possible combinations of assumptions. We just give one more example of a multistate-singletrait model with this set of assumptions:

- essential  $\eta_t$ -equivalence (Box 4.1 of SGCM)
- scale invariance over time
- conditional mean independence (Box 4.1 of SGCM)
- $\theta$ -equivalence (Box 5.1 of SGCM)

```
m1 <- lsttheory(neta = 3, nxi = 1, data = multistate, equiv.assumption = list(tau = "ess",
    xi = "equi"), scale.invariance = list(lait0 = TRUE, lait1 = TRUE, gat0 = TRUE,
    gat1 = TRUE))
coef(m1@lavaanres, type = "user")
## eta1=~y11 eta1=~y21 eta1=~y31 eta2=~y12 eta2=~y22 eta2=~y32 eta3=~y13
##
       1.000
                 1.000
                            1.000
                                      1.000
                                                 1.000
                                                           1.000
                                                                      1.000
## eta3=~y23 eta3=~y33
                                                           y12~1
                            y11~1
                                      la210
                                                 la310
                                                                      la210
       1.000
                 1.000
                            0.000
                                      0.385
                                                 0.421
                                                           0.000
                                                                      0.385
##
                                                eta1~1
##
       la310
                 y13~1
                            la210
                                      la310
                                                          eta2~1
                                                                     eta3~1
       0.421
                 0.000
                            0.385
                                      0.421
                                                 0.000
                                                           0.000
                                                                      0.000
##
##
                 eps21
                                      eps12
                                                 eps22
                                                           eps32
                                                                      eps13
       eps11
                            eps31
       1.064
                 1.381
                            0.961
                                      1.004
                                                 1.591
                                                           0.878
                                                                      1.090
##
                                                  psi3 xi1=~eta1 xi1=~eta2
##
       eps23
                 eps33
                             psi1
                                       psi2
```

##	1.673	0.831	0.861	0.939	0.963	1.000	1.000
##	xi1=~eta3	varxi1	mxi1	vareta1	vareta2	vareta3	vary11
##	1.000	1.855	0.727	2.716	2.794	2.817	3.780
##	vary21	vary31	vary12	vary22	vary32	vary13	vary23
##	4.097	3.677	3.797	4.384	3.672	3.908	4.490
##	t vary33	rely11	rely21	rely31	rely12	rely22	rely32
##	3.648	0.719	0.663	0.739	0.736	0.637	0.761
##	rely13	rely23	rely33	spey11	spey21	spey31	spey12
##	0.721	0.627	0.772	0.228	0.210	0.234	0.247
##	spey22	spey32	spey13	spey23	spey33	cony11	cony21
##	0.214	0.256	0.246	0.214	0.264	0.491	0.453
##	cony31	cony12	cony22	cony32	cony13	cony23	cony33
##	0.504	0.488	0.423	0.505	0.475	0.413	0.508

#### 5 Multistate-Doubletrait Models

For the mulistate double trait models, we need to use a different data set, because we need at least two common state variables for each of the  $\theta$  variables. The simulated data set is called multitrait multistate and contains 8 manifest variables  $Y_{it}$  distributed across 4 occasions of measurement:

```
data(multitraitmultistate)
head(round(multitraitmultistate, 2))
##
      y11
            y21
                  y12
                        y22
                              y13
                                    y23
                                          y14
                                                y24
## 1
                 0.63
                      0.02
                                   2.26
     1.55
           1.99
                             1.61
                                         4.85
                                               3.55
     1.92
           3.43 -0.66 -0.58
                             2.81
                                   4.27
                                         1.58
                                               0.97
## 3 -0.07
           0.32 1.81 1.83 1.73
                                   4.05 0.70
                                               2.93
## 4 -0.67 -1.67
                 1.01 1.55 -1.79 -2.35 -0.67
                 0.11 -0.47 -1.10 -1.03
                                         2.91 - 0.56
## 5 0.53 0.65
## 6 -1.90 -2.47 1.46 3.04 1.02 -0.08 0.88 1.39
```

## 5.1 Multistate-Doubletrait Models with $\theta_1, \theta_2$ -Congenericity

The first model that we want to show with this dataset is a multistate-doubletrait model with these assumptions:

- $\eta_t$ -congenericity (Box 4.1 of SGCM)
- conditional mean independence (Box 4.1 of SGCM)
- $\theta_1$ -congenericity (Box 6.1 of SGCM)
- $\theta_2$ -congenericity (Box 6.1 of SGCM)

The model syntax is:

```
m1 <- lsttheory(neta = 4, nxi = 2, data = multitraitmultistate)
coef(m10lavaanres, type = "user")
## eta1=~y11
                  la211 eta2=~y12
                                       la221 eta3=~y13
                                                             la231 eta4=~y14
##
       1.000
                  1.203
                            1.000
                                       1.195
                                                  1.000
                                                             1.204
                                                                        1.000
##
       la241
                  y11~1
                            la210
                                       y12~1
                                                  la220
                                                             y13~1
                                                                        1a230
                  0.000
                                                             0.000
##
       1.080
                            0.313
                                       0.000
                                                  0.380
                                                                        0.307
##
       y14~1
                  la240
                           eta1~1
                                                 eta3~1
                                                                        eps11
                                        ga20
                                                              ga40
       0.000
                  0.382
                            0.000
                                       0.398
                                                  0.000
                                                             0.234
                                                                        0.941
##
                                       eps13
##
       eps21
                  eps12
                             eps22
                                                  eps23
                                                             eps14
                                                                        eps24
       1.020
                  1.136
                             0.857
                                       0.915
                                                  1.038
                                                             0.901
                                                                        1.158
##
                                        psi4 xi1=~eta1
                                                              ga21 xi2=~eta3
##
        psi1
                   psi2
                              psi3
##
       0.955
                  1.141
                             1.390
                                       0.681
                                                  1.000
                                                             0.649
                                                                        1.000
```

##	ga41	varxi1	varxi2	mxi1	mxi2	xi1~~xi2	vareta1
##	0.858	2.694	2.580	0.450	0.928	1.721	3.649
##	vareta2	vareta3	vareta4	vary11	vary21	vary12	vary22
##	2.277	3.970	2.583	4.590	6.303	3.413	4.106
##	vary13	vary23	vary14	vary24	rely11	rely21	rely12
##	4.885	6.795	3.484	4.173	0.795	0.838	0.667
##	rely22	rely13	rely23	rely14	rely24	spey11	spey21
##	0.791	0.813	0.847	0.741	0.722	0.208	0.219
##	spey12	spey22	spey13	spey23	spey14	spey24	cony11
##	0.334	0.397	0.284	0.297	0.196	0.191	0.587
##	cony21	cony12	cony22	cony13	cony23	cony14	cony24
##	0.619	0.333	0.395	0.528	0.551	0.546	0.532

6 Plot LST-R Theory Models with semPlot



# 7 Graphical User Interface 1sttheoryGUI

The graphical user interface is under development. It currently contains two menu items: One for loading the datasets included in the package and one for specifying the LST-R theory model. Figure 7 shows a screenshot of the dialog that can be used to load datasets.

Figure 7 shows a screenshot of the dialog for specifying the LST-R theory models. The dialog is a convenient graphical interface for the lsttheory function described previously. The graphical user interface provides easy access to almost all functionality described earlier in this vignette.

