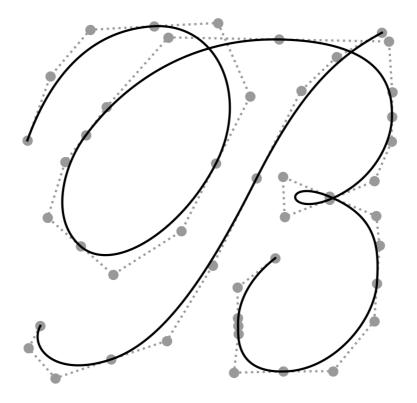
bsplyne

bsplyne





bsplyne is a Python library for working with N-dimensional B-splines. It implements the Cox-de Boor algorithm for basis evaluation, order elevation, knot insertion, and provides a connectivity class for multi-patch structures. Additionally, it includes visualization tools with export capabilities to Paraview.

Note: This library is not yet available on PyPI. To install, please clone the repository and install it manually.

Installation

Since **bsplyne** is not yet on PyPI, you can install it locally as follows:

```
git clone https://github.com/Dorian210/bsplyne
cd bsplyne
pip install -e .
```

Dependencies

Make sure you have the following dependencies installed:

- numpy
- numba
- scipy
- matplotlib
- meshio
- tqdm
- pathos

Main Modules

BSplineBasis

Implements B-spline basis function evaluation using the Cox-de Boor recursion formula.

• BSpline

Provides methods for creating and manipulating N-dimensional B-splines, including order elevation and knot

insertion.

• MultiPatchBSplineConnectivity

Manages the connectivity between multiple N-dimensional B-spline patches.

CouplesBSplineBorder (less documented)
 Handles and line between B and an elemented

Handles coupling between B-spline borders.

Examples

Several example scripts demonstrating the usage of **bsplyne** can be found in the examples/ directory. These scripts cover:

- Basis evaluation on a curved line
- Plotting with Matplotlib
- Order elevation
- Knot insertion
- Surface examples
- Exporting to Paraview

Documentation

The full API documentation is available in the docs/ directory of the project or via the online documentation portal.

Contributions

At the moment, I am not actively reviewing contributions. However, if you encounter issues or have suggestions, feel free to open an issue.

License

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• View Source

bsplyne.my_wide_product

View Source



```
@nb.njit(cache=True)
```

def wide_product_max_nnz(a_indptr: numpy.ndarray, b_indptr: numpy.ndarray, height: int) -> int:

• View Source

Compute the maximum number of nonzeros in the result.

Parameters

- a_indptr (np.ndarray): CSR pointer array for matrix A.
- **b_indptr** (np.ndarray): CSR pointer array for matrix B.
- height (int): Number of rows (must be the same for both A and B).

Returns

• max_nnz (int): Total number of nonzero elements in the resulting matrix.

```
@nb.njit(cache=True)
def wide_product_row(
   a_data: numpy.ndarray,
   a_indices: numpy.ndarray,
   b_data: numpy.ndarray,
   b_indices: numpy.ndarray,
   b_width: int,
   out_data: numpy.ndarray,
   out_indices: numpy.ndarray
) -> int:
```

View Source

Compute the wide product for one row.

For each nonzero in the row of A and each nonzero in the row of B, it computes: out_index = a_indices[i] * b_width + b_indices[j] out_value = a_data[i] * b_data[j]

Parameters

- a_data (np.ndarray): Nonzero values for the row in A.
- a_indices (np.ndarray): Column indices for the row in A.
- **b_data** (np.ndarray): Nonzero values for the row in B.
- **b_indices** (np.ndarray): Column indices for the row in B.
- **b_width** (int): Number of columns in B.
- out data (np.ndarray): Preallocated output array for the row's data.
- out_indices (np.ndarray): Preallocated output array for the row's indices.

Returns

• off (int): Number of nonzero entries computed for this row.

```
@nb.njit(cache=True)
def wide_product_numba(
height: int,
a_data: numpy.ndarray,
a_indices: numpy.ndarray,
a_indptr: numpy.ndarray,
a_width: int,
b_data: numpy.ndarray,
b_indices: numpy.ndarray,
b_indptr: numpy.ndarray,
b_indptr: numpy.ndarray,
b_width: int
):
```

View Source

Compute the row-wise wide (Khatri-Rao) product for two CSR matrices.

For each row i, the result[i, :] = kron(A[i, :], B[i, :]), i.e. the Kronecker product of the i-th rows of A and B.

Parameters

- height (int): Number of rows in A and B.
- a_data (np.ndarray): Data array for matrix A (CSR format).
- a indices (np.ndarray): Indices array for matrix A.
- a_indptr (np.ndarray): Index pointer array for matrix A.
- a_width (int): Number of columns in A.
- **b_data** (np.ndarray): Data array for matrix B (CSR format).
- **b_indices** (np.ndarray): Indices array for matrix B.
- **b_indptr** (np.ndarray): Index pointer array for matrix B.
- **b_width** (int): Number of columns in B.

Returns

- out_data (np.ndarray): Data array for the resulting CSR matrix.
- out_indices (np.ndarray): Indices array for the resulting CSR matrix.
- out_indptr (np.ndarray): Index pointer array for the resulting CSR matrix.
- total_nnz (int): Total number of nonzero entries computed.

def my_wide_product(

```
A: scipy.sparse._base.spmatrix,
B: scipy.sparse._base.spmatrix
) -> scipy.sparse._csr.csr_matrix:
```

View Source

Compute a "1D" Kronecker product row by row.

For each row i, the result C[i, :] = kron(A[i, :], B[i, :]). Matrices A and B must have the same number of rows.

Parameters

- A (scipy.sparse.spmatrix): Input sparse matrix A in CSR format.
- **B** (scipy.sparse.spmatrix): Input sparse matrix B in CSR format.

Returns

 C (scipy.sparse.csr_matrix): Resulting sparse matrix in CSR format with shape (A.shape[0], A.shape[1]*B.shape[1]).

base_cylinder = show

def new_cylinder(center_front, orientation, radius, length):

bsplyne.geometries_in_3D View Source def scale_rotate_translate(pts, scale_vector, axis, angle, translation_vector): View Source p = 2**knot** = array([0., 0., 0., 0.25, 0.5, 0.75, 1., 1., 1.]) C = array([1.00002282, 1.00002282, 0.84721156, 0.56754107, 0.19634954, 0.])base_quarter_circle = show def new_quarter_circle(center, normal, radius): View Source base_circle = show def new_circle(center, normal, radius): View Source base_disk = show def new_disk(center, normal, radius): View Source base_degenerated_disk = show def new_degenerated_disk(center, normal, radius): View Source base_quarter_pipe = show def new_quarter_pipe(center_front, orientation, radius, length): View Source base_pipe = show def new_pipe(center_front, orientation, radius, length): View Source base_quarter_cylinder = show def new_quarter_cylinder(center_front, orientation, radius, length): View Source

View Source



bsplyne.multi_patch_b_spline

View Source



```
@nb.njit(cache=True)
def find(parent, x):

@nb.njit(cache=True)
def union(parent, rank, x, y):

@nb.njit(cache=True)
def get_unique_nodes_inds(nodes_couples, nb_nodes):

• View Source

• View Source

• View Source
```

class MultiPatchBSplineConnectivity:

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Contains all the methods to link multiple B-spline patches. It uses 3 representations of the data:

- a unique representation, possibly common with other meshes, containing only unique nodes indices,
- · a unpacked representation containing duplicated nodes indices,
- a separated representation containing duplicated nodes indices, separated between patches. It is here for user friendliness.

Attributes

- **unique_nodes_inds** (numpy.ndarray of int): The indices of the unique representation needed to create the unpacked one.
- shape_by_patch (numpy.ndarray of int): The shape of the separated nodes by patch.
- **nb_nodes** (int): The total number of unpacked nodes.
- **nb_unique_nodes** (int): The total number of unique nodes.
- **nb_patchs** (int): The number of patches.
- npa (int): The dimension of the parametric space of the B-splines.

MultiPatchBSplineConnectivity(unique_nodes_inds, shape_by_patch, nb_unique_nodes)

View Source

Parameters

- **unique_nodes_inds** (numpy.ndarray of int): The indices of the unique representation needed to create the unpacked one.
- shape_by_patch (numpy.ndarray of int): The shape of the separated nodes by patch.
- **nb_unique_nodes** (int): The total number of unique nodes.

```
unique_nodes_inds: numpy.ndarray
shape_by_patch: numpy.ndarray
nb_nodes: int
nb_unique_nodes: int
nb_patchs: int
npa: int
@classmethod
def from_nodes_couples(cls, nodes_couples, shape_by_patch):
```

View Source

Create the connectivity from a list of couples of unpacked nodes.

Parameters

- **nodes_couples** (numpy.ndarray of int): Couples of indices of unpacked nodes that are considered the same. Its shape should be (# of couples, 2)
- shape_by_patch (numpy.ndarray of int): The shape of the separated nodes by patch.

Returns

@classmethod

• MultiPatchBSplineConnectivity: Instance of MultiPatchBSplineConnectivity created.

```
def from_separated_ctrlPts(
  cls,
  separated_ctrlPts,
  eps=1e-10,
```

return_nodes_couples: bool = **False**

Create the connectivity from a list of control points given as a separated field by comparing every couple of points.

Parameters

):

- **separated_ctrlPts** (list of numpy.ndarray of float): Control points of every patch to be compared in the separated representation. Every array is of shape: (NPh , nb elem for dim 1, ..., nb elem for dim npa)
- eps (float, optional): Maximum distance between two points to be considered the same, by default 1e-10
- return_nodes_couples (bool, optional): If True , returns the nodes_couples created, by default False

Returns

• MultiPatchBSplineConnectivity: Instance of MultiPatchBSplineConnectivity created.

```
def unpack(self, unique_field):
```

View Source

View Source

Extract the unpacked representation from a unique representation.

Parameters

• unique_field (numpy.ndarray): The unique representation. Its shape should be : (field, shape, ..., self . nb_unique_nodes)

Returns

unpacked_field (numpy.ndarray): The unpacked representation. Its shape is: (field, shape, ..., self.nb_nodes)

```
def pack(self, unpacked_field, method='mean'):
```

View Source

Extract the unique representation from an unpacked representation.

Parameters

- unpacked_field (numpy.ndarray): The unpacked representation. Its shape should be : (field, shape, ..., self . nb_nodes)
- method (str): The method used to group values that could be different

Returns

unique_nodes (numpy.ndarray): The unique representation. Its shape is: (field, shape, ..., self.nb_unique_nodes)

```
def separate(self, unpacked_field):
```

View Source

Extract the separated representation from an unpacked representation.

Parameters

unpacked_field (numpy.ndarray): The unpacked representation. Its shape is: (field, shape, ..., self.nb_nodes)

Returns

• **separated_field** (list of numpy.ndarray): The separated representation. Every array is of shape: (field, shape, ..., nb elem for dim 1, ..., nb elem for dim npa)

def agglomerate(self, separated_field):

View Source

Extract the unpacked representation from a separated representation.

Parameters

• **separated_field** (list of numpy.ndarray): The separated representation. Every array is of shape: (field, shape, ..., nb elem for dim 1, ..., nb elem for dim npa)

Returns

unpacked_field (numpy.ndarray): The unpacked representation. Its shape is: (field, shape, ..., self.nb_nodes)

```
def unique_field_indices(self, field_shape, representation='separated'):
```

View Source

Get the unique, unpacked or separated representation of a field's unique indices.

Parameters

- **field_shape** (tuple of int): The shape of the field. For example, if it is a vector field, **field_shape** should be (3,). If it is a second order tensor field, it should be (3, 3).
- representation (str, optional): The user must choose between "unique", "unpacked", and "separated". It corresponds to the type of representation to get, by default "separated"

Returns

unique_field_indices (numpy.ndarray of int or list of numpy.ndarray of int): The unique, unpacked or separated representation of a field's unique indices. If unique, its shape is (field_shape , self . nb_unique_nodes). If unpacked, its shape is : (field_shape , self . nb_nodes). If separated, every array is of shape : (* field_shape , nb elem for dim 1, ..., nb elem for dim npa).

def get_duplicate_unpacked_nodes_mask(self):

• View Source

Returns a boolean mask indicating which nodes in the unpacked representation are duplicates.

Returns

duplicate_nodes_mask (numpy.ndarray): Boolean mask of shape (nb_nodes,) where True indicates a node is
duplicated across multiple patches and False indicates it appears only once.

def extract_exterior_borders(self, splines):

View Source

Extract exterior borders from B-spline patches.

Parameters

• splines (list[BSpline]): Array of B-spline patches to extract borders from.

Returns

- border_connectivity (MultiPatchBSplineConnectivity): Connectivity information for the border patches.
- border splines (list[BSpline]): Array of B-spline patches representing the borders.
- border_unique_to_self_unique_connectivity (numpy.ndarray of int): Array mapping border unique nodes to original unique nodes.

Raises

• AssertionError: If isoparametric space dimension is less than 2.

def extract_interior_borders(self, splines):

View Source

Extract interior borders from B-spline patches where nodes are shared between patches.

Parameters

• splines (list[BSpline]): Array of B-spline patches to extract borders from.

Returns

- border_connectivity (MultiPatchBSplineConnectivity): Connectivity information for the border patches.
- border_splines (list[BSpline]): Array of B-spline patches representing the borders.
- **border_unique_to_self_unique_connectivity** (numpy.ndarray of int): Array mapping border unique nodes to original unique nodes.

Raises

• AssertionError: If parametric space dimension is less than 2.

```
def subset(self, splines, patches_to_keep):
```

View Source

Create a subset of the multi-patch B-spline connectivity by keeping only selected patches.

Parameters

- splines (list[BSpline]): Array of B-spline patches to subset.
- patches_to_keep (numpy.array of int): Indices of patches to keep in the subset.

Returns

- **new_connectivity** (MultiPatchBSplineConnectivity): New connectivity object containing only the selected patches.
- new_splines (list[BSpline]): Array of B-spline patches for the selected patches.
- **new_unique_to_self_unique_connectivity** (numpy.ndarray of int): Array mapping new unique nodes to original unique nodes.

```
def make_control_poly_meshes(
```

```
self,
splines: Iterable[bsplyne.b_spline.BSpline],
separated_ctrl_pts: Iterable[numpy.ndarray[numpy.floating]],
n_eval_per_elem: Union[Iterable[int], int] = 10,
n_step: int = 1,
unique_fields: dict = {},
separated_fields: Optional[dict] = None,
XI_list: Optional[Iterable[tuple[numpy.ndarray[numpy.floating], ...]]] = None,
paraview_sizes: dict = {}
) -> list[meshio._mesh.Mesh]:
```

View Source

```
def make elem separator meshes(
self.
splines: Iterable[bsplyne.b_spline.BSpline],
separated_ctrl_pts: Iterable[numpy.ndarray[numpy.floating]],
n_eval_per_elem: Union[Iterable[int], int] = 10,
n_{step}: int = 1,
unique_fields: dict = {},
separated_fields: Optional[dict] = None,
XI_list: Optional[Iterable[tuple[numpy.ndarray[numpy.floating], ...]]] = None,
paraview_sizes: dict = {},
parallel: bool = True,
verbose: bool = True
) -> list[meshio._mesh.Mesh]:

    View Source

def make_elements_interior_meshes(
self,
splines: Iterable[bsplyne.b_spline.BSpline],
separated_ctrl_pts: Iterable[numpy.ndarray[numpy.floating]],
n_eval_per_elem: Union[Iterable[int], int] = 10,
n_{step}: int = 1,
unique fields: dict = {},
separated_fields: Optional[dict] = None,
XI_list: Optional[Iterable[tuple[numpy.ndarray[numpy.floating], ...]]] = None,
parallel: bool = True,
verbose: bool = True
) -> list[meshio._mesh.Mesh]:

    View Source

def make_all_meshes(
self,
splines: Iterable[bsplyne.b_spline.BSpline],
separated_ctrl_pts: Iterable[numpy.ndarray[numpy.floating]],
n_{step}: int = 1,
n_eval_per_elem: Union[int, Iterable[int]] = 10,
unique fields: dict = {},
separated_fields: Optional[list[dict]] = None,
XI_list: Optional[Iterable[tuple[numpy.ndarray[numpy.floating], ...]]] = None,
verbose: bool = True,
fields_on_interior_only: Union[bool, Literal['auto'], list[str]] = 'auto'
) -> tuple[list[meshio._mesh.Mesh], list[meshio._mesh.Mesh], list[meshio._mesh.Mesh]]:

    View Source
```

Generate all mesh representations (interior, element borders, and control points) for a multipatch B-spline geometry.

This method creates three types of meshes for visualization or analysis:

- The interior mesh representing the B-spline surface or volume.
- The element separator mesh showing the borders between elements.
- The control polygon mesh showing the control structure.

Parameters

- **splines** (Iterable[BSpline]): List of B-spline patches to process.
- **separated_ctrl_pts** (Iterable[np.ndarray[np.floating]]): Control points for each patch in separated representation.
- **n_step** (int, optional): Number of time steps to generate. By default, 1.
- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each

isoparametric dimension. If an int is provided, the same number is used for all dimensions. If an Iterable is provided, each value corresponds to a different dimension. By default, 10.

- unique_fields (dict, optional): Fields in unique representation to visualize. By default, {} . Keys are field names, values are arrays (not callables nor FE fields).
- separated_fields (Union[list[dict], None], optional): Fields to visualize at each time step. List of self.nb_patchs dictionaries (one per patch) of format: { "field_name": field_value } where field_value can be either:
 - A np.ndarray with shape (n_step, field_size, self.shape_by_patch[patch])
 - A np.ndarray with shape (n_step, field_size, *grid_shape)
 - 3. A function that computes field values (np.ndarray[np.floating]) at given points from the BSpline instance and XI. By default, None.
- XI_list (Union[None, Iterable[tuple[np.ndarray[np.floating], ...]]], optional): Parametric coordinates at which to evaluate the B-spline patches and fields. If not None, overrides the n_eval_per_elem parameter. If None, regular grids are generated according to n_eval_per_elem. By default, None.
- verbose (bool, optional): Whether to print progress information. By default, True.
- fiels_on_interior_only (Union[bool, Literal['auto'], list[str]], optionnal): Whether to include fields only on the interior mesh (True), on all meshes (False), or on specified field names. If set to 'auto', fields named 'u', 'U', 'displacement' or 'displ' are included on all meshes while others are only included on the interior mesh. By default, 'auto'.

Returns

- tuple[list[io.Mesh], list[io.Mesh], list[io.Mesh]]: Tuple containing three lists of io.Mesh objects:
 - o Interior meshes for each time step.
 - Element separator meshes for each time step.
 - o Control polygon meshes for each time step.

Raises

- NotImplementedError: If a callable is passed in unique_fields.
- ValueError: If a field in unique_fields does not have the correct shape.

Notes

- The isoparametric space refers to the parametric space of the B-splines.
- Fields can be visualized as scalars or vectors.
- Supports time-dependent visualization through n_step.
- Fields in unique_fields must be arrays; to use callables, use separated_fields.

Examples

```
>>> interior, borders, control = connectivity.make_all_meshes(splines, separated_ctrl_pts
)
```

def save paraview(self. splines: Iterable[bsplyne.b_spline.BSpline], separated_ctrl_pts: Iterable[numpy.ndarray[numpy.floating]], path: str, name: str, n_{step} : int = 1, n_eval_per_elem: Union[int, Iterable[int]] = 10, unique_fields: dict = {}, separated_fields: Optional[list[dict]] = None, XI_list: Optional[Iterable[tuple[numpy.ndarray[numpy.floating], ...]]] = None, groups: Optional[dict[str, dict[str, Union[str, int]]]] = None, make_pvd: bool = True, verbose: bool = True, fields_on_interior_only: Union[bool, Literal['auto'], list[str]] = 'auto'): View Source

Save multipatch B-spline visualization data as Paraview files.

This method generates three types of visualization files for a multipatch B-spline geometry:

- Interior mesh showing the B-spline surface/volume
- Element borders showing the mesh structure
- Control points mesh showing the control structure

All files are saved in VTU format, with an optional PVD file to group them for Paraview.

Parameters

- splines (Iterable[BSpline]): List of B-spline patches to save.
- **separated_ctrl_pts** (Iterable[np.ndarray[np.floating]]): Control points for each patch in separated representation.
- path (str): Directory path where the files will be saved.
- name (str): Base name for the output files.
- n_step (int, optional): Number of time steps to save. By default, 1.
- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. If an int is provided, the same number is used for all dimensions. If an Iterable is provided, each value corresponds to a different dimension. By default, 10.
- unique_fields (dict, optional): Fields in unique representation to save. By default, {} . Keys are field names, values are arrays (not callables nor FE fields).
- separated_fields (Union[list[dict], None], optional): Fields to visualize at each time step. List of self.nb_patchs dictionaries (one per patch) of format: { "field_name": field_value } where field_value can be either:

```
    A numpy array with shape (n_step, field_size, self.shape_by_patch[patch]) where:

            n_step: Number of time steps
            field_size: Size of the field at each point (1 for scalar, 3 for vector)
            self.shape_by_patch[patch]: Same shape as the patch's control points grid (excluding NPh)

    A numpy array with shape (n_step, field_size, *grid_shape) where:

            n_step: Number of time steps
            field_size: Size of the field at each point (1 for scalar, 3 for vector)
            *grid_shape: Shape of the evaluation grid (number of points along each isoparametric axis)

    A function that computes field values (np.ndarray[np.floating]) at given points from the BSpline instance and XI, the tuple of arrays containing evaluation points for each dimension (tuple[np.ndarray[np.floating], ...]). The result should be an array of shape (n_step, n_points, field_size) where:
```

```
    n_step: Number of time steps
    n_points: Number of evaluation points (n_xi × n_eta × ...)
```

field_size: Size of the field at each point (1 for scalar, 3 for vector)

By default, None.

- XI_list (Iterable[tuple[np.ndarray[np.floating], ...]], optional): Parametric coordinates at which to evaluate the B-spline patches and fields. If not None, overrides the n_eval_per_elem parameter. If None, regular grids are generated according to n_eval_per_elem.
- **groups** (Union[dict[str, dict[str, Union[str, int]]], None], optional): Nested dictionary specifying file groups for PVD organization. Format: { "group_name": { "ext": str, # File extension (e.g., "vtu") "npart": int, # Number of parts in the group "nstep": int # Number of timesteps } } If provided, existing groups are updated; if None, groups are created automatically. By default, None.
- make_pvd (bool, optional): Whether to create a PVD file grouping all VTU files. By default, True.
- verbose (bool, optional): Whether to print progress information. By default, True.
- fields_on_interior_only (Union[bool, Literal['auto'], list[str]], optionnal): Whether to include fields only on the interior mesh (True), on all meshes (False), or on specified field names. If set to 'auto', fields named 'u', 'U', 'displacement' or 'displ' are included on all meshes while others are only included on the interior mesh. By default, 'auto'.

Returns

• groups (dict[str, dict[str, Union[str, int]]]): Updated groups dictionary with information about saved files.

Raises

- NotImplementedError: If a callable is passed in unique_fields .
- ValueError: If the multiprocessing pool is not running and cannot be restarted.

Notes

- Creates three types of VTU files for each time step:
 - {name}_interior_{part}_{step}.vtu
 - {name}_elements_borders_{part}_{step}.vtu
 - {name}_control_points_{part}_{step}.vtu
- If make_pvd=True, creates a PVD file named {name}.pvd.
- Fields can be visualized as scalars or vectors in Paraview.
- The method supports time-dependent visualization through n_step.
- Fields in unique_fields must be arrays; to use callables, use separated_fields.

Examples

Save a multipatch B-spline visualization:

```
>>> connectivity.save_paraview(splines, separated_ctrl_pts, "./output", "multipatch"
)
```

Save with a custom separated field on a 2 patches multipatch:

```
>>> fields = [{"temperature": np.random.rand(1, 4, 4)}, {"temperature": np.random.rand(1, 7, 3)}]
>>> connectivity.save_paraview(splines, separated_ctrl_pts, "./output", "multipatch", separated_fie
)
```

```
CouplesBSplineBorder(
spline1_inds,
spline2_inds,
axes1,
axes2,
front_sides1,
front_sides2,
transpose_2_to_1,
flip_2_to_1,
NPa
)

    View Source

spline1_inds
spline2 inds
axes1
axes2
front_sides1
front_sides2
transpose_2_to_1
flip_2_to_1
NPa
nb_couples
@classmethod
def extract border pts(cls, field, axis, front side, field dim=1, offset=0):

    View Source

@classmethod
def extract_border_spline(cls, spline, axis, front_side):

    View Source

@classmethod
def transpose_and_flip(cls, field, transpose, flip, field_dim=1):

    View Source

@classmethod
def transpose_and_flip_knots(cls, knots, spans, transpose, flip):

    View Source

@classmethod
def transpose_and_flip_back_knots(cls, knots, spans, transpose, flip):

    View Source

@classmethod
def transpose_and_flip_spline(cls, spline, transpose, flip):

    View Source

@classmethod
def from_splines(cls, separated_ctrl_pts, splines):

    View Source

def append(self, other):

    View Source

def get_operator_allxi1_to_allxi2(self, spans1, spans2, couple_ind):

    View Source
```

bsplyne.parallel_utils

View Source

```
def parallel_blocks(
```

```
funcs: Union[Callable, Iterable[Callable]],
all_args: Optional[Iterable[tuple]] = None,
num_blocks: Optional[int] = None,
verbose: bool = True,
pbar_title: str = 'Processing blocks',
disable_parallel: bool = False
) -> list:
```

View Source

Execute a function in parallel over blocks of arguments, saving each block's results to disk and reloading them sequentially.

This function divides the input all_args into a specified number of blocks, applies func to each tuple of arguments in parallel using multiple processes, and collects the results into a single list. Intermediate results are stored as .npy files in a temporary directory and are loaded and concatenated after processing.

Parameters

- **funcs** (Union[Callable, Iterable[Callable]]): If multiple functions are passed, their number should match the number of arguments passed. Function to apply to each tuple of arguments in all_args.
- all_args (Union[Iterable[tuple], None], optional): Iterable of tuples, where each tuple contains the arguments for a single call to func . If the function takes no argument, set all_args to None . By default, None.
- **num_blocks** (Union[int, None], optional): Number of blocks to split all_args into for parallel processing. If None, defaults to half the number of available CPU cores. By default, None.
- **verbose** (bool, optional): If True, displays a progress bar for both block processing and result gathering. By default, True.
- pbar_title (str, optional): Title for the progress bar. By default, "Processing blocks".
- disable_parallel (bool, optional): If True, disables parallel processing and runs sequentially. By default, False.

Returns

• **list**: List containing the results from applying func to each tuple of arguments in all_args , in the original order.

Notes

- Each block is processed in a separate process and results are saved as .npy files in a temporary directory.
- The temporary directory and files are removed after results are gathered.
- If running in a Jupyter environment, progress bars are displayed in a single position for better visualization.

bsplyne.b_spline_basis

View Source



class BSplineBasis:

View Source

BSpline basis in 1D.

A class representing a one-dimensional B-spline basis with functionality for evaluation, manipulation and visualization of basis functions. Provides methods for basis function evaluation, derivatives computation, knot insertion, order elevation, and integration point generation.

Attributes

- **p** (int): Degree of the polynomials composing the basis.
- **knot** (np.ndarray[np.floating]): Knot vector defining the B-spline basis. Contains non-decreasing sequence of isoparametric coordinates.
- m (int): Last index of the knot vector (size 1).
- n (int): Last index of the basis functions. When evaluated, returns an array of size n + 1.
- span (tuple[float, float]): Interval of definition of the basis (knot[p], knot[m p]).

Notes

The basis functions are defined over the isoparametric space specified by the knot vector. Basis function evaluation and manipulation methods use efficient algorithms based on Cox-de Boor recursion formulas.

See Also

```
numpy.ndarray : Array type used for knot vector storage
scipy.sparse : Sparse matrix formats used for basis function evaluations
```

BSplineBasis(p: int, knot: Iterable[float])

View Source

Initialize a B-spline basis with specified degree and knot vector.

Parameters

- **p** (int): Degree of the B-spline polynomials.
- **knot** (Iterable[float]): Knot vector defining the B-spline basis. Must be a non-decreasing sequence of real numbers.

Returns

• **BSplineBasis**: The initialized **BSplineBasis** instance.

Notes

The knot vector must satisfy these conditions:

- Size must be at least p + 2
- Must be non-decreasing
- For non closed B-spline curves, first and last knots must have multiplicity p + 1

The basis functions are defined over the isoparametric space specified by the knot vector. The span of the basis is [knot[p], knot[m - p]], where m is the last index of the knot vector.

Examples

Create a quadratic B-spline basis with uniform knot vector:

```
>>> basis = BSplineBasis(2, [0., 0., 0., 1., 1.])
```

knot: numpy.ndarray[numpy.floating]

m: int

n: int

span: tuple[float, float]

def linspace(self, n_eval_per_elem: int = 10) -> numpy.ndarray[numpy.floating]:

View Source

Generate evenly spaced points over the basis span.

Creates a set of evaluation points by distributing them uniformly within each knot span (element) of the basis. Points are evenly spaced within elements but spacing may vary between different elements.

Parameters

• n_eval_per_elem (int, optional): Number of evaluation points per element. By default, 10.

Returns

• xi (np.ndarray[np.floating]): Array of evenly spaced points in isoparametric coordinates over the basis span.

Notes

The method:

- 1. Identifies unique knot spans (elements) in the isoparametric space
- 2. Distributes points evenly within each element
- 3. Combines points from all elements into a single array

Examples

```
>>> basis = BSplineBasis(2, [0., 0., 0., 1., 1., 1.])
>>> basis.linspace(5)
array([0., 0.2, 0.4, 0.6, 0.8, 1.])
```

def linspace for integration(

```
self,
```

n_eval_per_elem: int = 10,

bounding_box: Optional[tuple[float, float]] = None

) -> tuple[numpy.ndarray[numpy.floating], numpy.ndarray[numpy.floating]]:

View Source

Generate points and weights for numerical integration over knot spans in the isoparametric space. Points are evenly distributed within each element (knot span), though spacing may vary between different elements.

Parameters

- n_eval_per_elem (int, optional): Number of evaluation points per element. By default, 10.
- **bounding_box** (Union[tuple[float, float], None], optional): Lower and upper bounds for integration. If None, uses the span of the basis. By default, None.

Returns

- **xi** (np.ndarray[np.floating]): Array of integration points in isoparametric coordinates, evenly spaced within each element.
- dxi (np.ndarray[np.floating]): Array of corresponding integration weights, which may vary between elements

Notes

The method generates integration points by:

- 1. Identifying unique knot spans (elements) in the isoparametric space
- 2. Distributing points evenly within each element

3. Computing appropriate weights for each point based on the element size

When bounding_box is provided, integration is restricted to that interval, and elements are adjusted accordingly.

Examples

```
>>> basis = BSplineBasis(2, [0, 0, 0, 1, 1, 1])
>>> xi, dxi = basis.linspace_for_integration(5
)
```

Generate Gauss-Legendre quadrature points and weights for numerical integration over the B-spline basis.

Parameters

- n_eval_per_elem (Union[int, None], optional): Number of evaluation points per element. If None, takes the value self.p + 1. By default, None.
- **bounding_box** (Union[tuple[float, float], None], optional): Lower and upper bounds for integration. If None, uses the span of the basis. By default, None.

Returns

- xi (np.ndarray[np.floating]): Array of Gauss-Legendre quadrature points in isoparametric coordinates.
- dxi (np.ndarray[np.floating]): Array of corresponding integration weights.

Notes

The method generates integration points and weights by:

- 1. Identifying unique knot spans (elements) in the isoparametric space
- 2. Computing Gauss-Legendre points and weights for each element
- 3. Transforming points and weights to account for element size

When bounding_box is provided, integration is restricted to that interval.

Examples

```
>>> basis = BSplineBasis(2, [0, 0, 0, 1, 1, 1])
>>> xi, dxi = basis.gauss_legendre_for_integration(3
)
>>> xi  # Gauss-Legendre points
array([0.11270167, 0.5 , 0.88729833])
>>> dxi  # Integration weights
array([0.27777778, 0.444444444, 0.27777778])
```

def normalize_knots(self):

View Source

Normalize the knot vector to the interval [0, 1].

Maps the knot vector to the unit interval by applying an affine transformation that preserves the relative spacing between knots. Updates both the knot vector and span attributes.

Examples

```
>>> basis = BSplineBasis(2, [0., 0., 0., 2., 2., 2.])
>>> basis.normalize_knots()
>>> basis.knot
array([0., 0., 0., 1., 1., 1.])
>>> basis.span
(0, 1)
```

```
def N(
```

self.

XI: numpy.ndarray[numpy.floating],

```
k: int = 0
```

```
) -> scipy.sparse._coo.coo_matrix:
```

View Source

Compute the k-th derivative of the B-spline basis functions at specified points.

Parameters

- XI (np.ndarray[np.floating]): Points in the isoparametric space at which to evaluate the basis functions.
- k (int, optional): Order of the derivative to compute. By default, 0.

Returns

• **DN** (sps.coo_matrix): Sparse matrix containing the k-th derivative values. Each row corresponds to an evaluation point, each column to a basis function. Shape is (XI.size, n + 1).

Notes

Uses Cox-de Boor recursion formulas to compute basis function derivatives. Returns values in sparse matrix format for efficient storage and computation.

Examples

```
>>> basis = BSplineBasis(2, [0., 0., 0., 1., 1., 1.])
>>> basis.N([0., 0.5, 1.]).A # Evaluate basis functions
array([[1. , 0. , 0. ],
       [0.25, 0.5 , 0.25],
       [0. , 0. , 1. ]])
>>> basis.N([0., 0.5, 1.], k=1).A # Evaluate first derivatives
array([[-2., 2., 0.],
       [-1., 0., 1.],
       [ 0., -2., 2.]])
```

```
def plotN(self, k: int = 0, show: bool = True):
```

View Source

Plot the B-spline basis functions or their derivatives over the span.

Visualizes each basis function $N_i(\xi)$ or its k-th derivative over its support interval using matplotlib. The plot includes proper LaTeX labels and a legend if there are 10 or fewer basis functions.

Parameters

- k (int, optional): Order of derivative to plot. By default, 0 (plots the basis functions themselves).
- **show** (bool, optional): Whether to display the plot immediately. Can be useful to add more stuff to the plot. By default, True.

Notes

- Uses adaptive sampling with points only in regions where basis functions are non-zero
- Plots each basis function in a different color with LaTeX-formatted labels
- Legend is automatically hidden if there are more than 10 basis functions
- The x-axis represents the isoparametric coordinate ξ

Examples

```
>>> basis = BSplineBasis(2, [0., 0., 0., 1., 1., 1.])
>>> basis.plotN() # Plot basis functions
>>> basis.plotN(k=1) # Plot first derivatives
```

def knotInsertion(

self.

 $knots_to_add: numpy.ndarray[numpy.floating]$

```
) -> scipy.sparse._coo.coo_matrix:
```

View Source

Insert knots into the B-spline basis and return the transformation matrix.

Parameters

• knots_to_add (np.ndarray[np.floating]): Array of knots to insert into the knot vector.

Returns

• **D** (sps.coo_matrix): Transformation matrix such that new control points = D @ old control points.

Notes

Updates the basis by:

- Inserting new knots into the knot vector
- Incrementing m and n by the number of inserted knots
- Computing transformation matrix **D** for control points update

Examples

The knot vector is modified (as well as n and m):

```
>>> basis.knot
array([0. , 0. , 0. , 0.33, 0.67, 1. , 1. , 1. ])
```

def orderElevation(self, t: int) -> scipy.sparse._coo.coo_matrix:

View Source

Elevate the polynomial degree of the B-spline basis and return the transformation matrix.

Parameters

• t (int): Amount by which to increase the basis degree. New degree will be current degree plus t .

Returns

• **STD** (sps.coo_matrix): Transformation matrix for control points such that: new_control_points = STD @ old_control_points

Notes

The method:

- 1. Separates B-spline into Bézier segments via knot insertion
- 2. Elevates degree of each Bézier segment
- 3. Recombines segments into elevated B-spline via knot removal
- 4. Updates basis degree, knot vector and other attributes

Examples

Elevate quadratic basis to cubic:

The knot vector and the degree are modified (as well as n and m):

```
>>> basis.knot
array([0., 0., 0., 0., 1., 1., 1.])
>>> basis.p
```

bsplyne.b_spline

View Source



class BSpline: • View Source

BSpline class for representing and manipulating B-spline curves, surfaces and volumes.

A class providing functionality for evaluating, manipulating and visualizing B-splines of arbitrary dimension. Supports knot insertion, order elevation, and visualization through Paraview and Matplotlib.

Attributes

- NPa (int): Dimension of the isoparametric space.
- bases (np.ndarray[BSplineBasis]): Array containing BSplineBasis instances for each isoparametric dimension.

Notes

- Supports B-splines of arbitrary dimension (curves, surfaces, volumes, etc.)
- Provides methods for evaluation, derivatives, refinement and visualization
- Uses Cox-de Boor recursion formulas for efficient basis function evaluation
- Visualization available through Paraview (VTK) and Matplotlib

See Also

```
BSplineBasis: Class representing one-dimensional B-spline basis functions
numpy.ndarray: Array type used for control points and evaluations
scipy.sparse: Sparse matrix formats used for basis function evaluations

BSpline(
degrees: Iterable[int],
knots: Iterable[numpy.ndarray[numpy.floating]]
)

• View Source
```

Initialize a BSpline instance with specified degrees and knot vectors.

Creates a BSpline object by generating basis functions for each isoparametric dimension using the provided polynomial degrees and knot vectors.

Parameters

- **degrees** (Iterable[int]): Collection of polynomial degrees for each isoparametric dimension. The length determines the dimensionality of the parametric space (NPa). For example:
 - o [p] for a curve
 - o [p, q] for a surface
 - [p, q, r] for a volume
 - o ...
- **knots** (Iterable[np.ndarray[np.floating]]): Collection of knot vectors for each isoparametric dimension. Each knot vector must be a numpy array of floats . The number of knot vectors must match the number of degrees. For a degree p , the knot vector must have size m + 1 where m>=p .

Notes

- The number of control points in each dimension will be m p where m is the size of the knot vector minus 1 and p is the degree
- Each knot vector must be non-decreasing
- The multiplicity of each knot must not exceed p + 1

Examples

Create a 2D B-spline surface:

Create a 1D B-spline curve:

```
>>> degree = [3]
>>> knot = [np.array([0, 0, 0, 0, 1, 1, 1], dtype='float')]
>>> curve = BSpline(degree, knot)
```

NPa: int

bases: numpy.ndarray[bsplyne.b_spline_basis.BSplineBasis]

@classmethod
def from_bases(
 cls,
 bases: Iterable[bsplyne.b_spline_basis.BSplineBasis]
) -> BSpline:

View Source

Create a BSpline instance from an array of BSplineBasis objects. This is an alternative constructor that allows direct initialization from existing basis functions rather than creating new ones from degrees and knot vectors.

Parameters

• bases (Iterable[BSplineBasis]): An iterable (e.g. list, tuple, array) containing BSplineBasis instances. Each basis represents one parametric dimension of the resulting B-spline. The number of bases determines the dimensionality of the parametric space.

Returns

• **BSpline**: A new **BSpline** instance with the provided basis functions.

Notes

- The method initializes a new BSpline instance with empty degrees and knots
- The bases array is populated with the provided BSplineBasis objects
- The dimensionality (NPa) is determined by the number of basis functions

Examples

```
>>> basis1 = BSplineBasis(2, np.array([0, 0, 0, 1, 1, 1]))
>>> basis2 = BSplineBasis(2, np.array([0, 0, 0, 0.5, 1, 1, 1]))
>>> spline = BSpline.from_bases([basis1, basis2])
```

def getDegrees(self) -> numpy.ndarray[numpy.integer]:

View Source

Returns the polynomial degree of each basis function in the isoparametric space.

Returns

degrees (np.ndarray[np.integer]): Array containing the polynomial degrees of the B-spline basis functions.
 The array has length NPa (dimension of isoparametric space), where each element represents the degree of the corresponding isoparametric dimension.

Notes

- For a curve (1D), returns [degree_xi]
- For a surface (2D), returns [degree_xi, degree_eta]
- For a volume (3D), returns [degree_xi, degree_eta, degree_zeta]

• ...

Examples

def getKnots(self) -> list[numpy.ndarray[numpy.floating]]:

View Source

Returns the knot vector of each basis function in the isoparametric space.

This method collects all knot vectors from each BSplineBasis instance stored in the bases array. The knot vectors define the isoparametric space partitioning and the regularity properties of the B-spline.

Returns

knots (list[np.ndarray[np.floating]]): List containing the knot vectors of the B-spline basis functions. The list
has length NPa (dimension of isoparametric space), where each element is a numpy.ndarray containing the
knots for the corresponding isoparametric dimension.

Notes

- For a curve (1D), returns [knots_xi]
- For a surface (2D), returns [knots_xi, knots_eta]
- For a volume (3D), returns [knots_xi, knots_eta, knots_zeta]
- Each knot vector must be non-decreasing
- The multiplicity of interior knots determines the continuity at that point

Examples

def getNbFunc(self) -> int:

• View Source

Compute the total number of basis functions in the B-spline.

This method calculates the total number of basis functions by multiplying the number of basis functions in each isoparametric dimension (n + 1 for each dimension).

Returns

• int: Total number of basis functions in the B-spline. This is equal to the product of (n + 1) for each basis, where n is the last index of each basis function.

Notes

- For a curve (1D), returns (n + 1)
- For a surface (2D), returns $(n1 + 1) \times (n2 + 1)$
- For a volume (3D), returns $(n1 + 1) \times (n2 + 1) \times (n3 + 1)$
- The number of basis functions equals the number of control points needed

Examples

```
def getSpans(self) -> list[tuple[float, float]]:
```

View Source

Returns the span of each basis function in the isoparametric space.

This method collects the spans (intervals of definition) from each BSplineBasis instance stored in the bases array.

Returns

• **spans** (list[tuple[float, float]]): List containing the spans of the B-spline basis functions. The list has length NPa (dimension of isoparametric space), where each element is a tuple (a, b) containing the lower and upper bounds of the span for the corresponding isoparametric dimension.

Notes

- For a curve (1D), returns [(xi_min, xi_max)]
- For a surface (2D), returns [(xi_min, xi_max), (eta_min, eta_max)]
- For a volume (3D), returns [(xi_min, xi_max), (eta_min, eta_max), (zeta_min, zeta_max)]
- The span represents the interval where the B-spline is defined
- Each span is determined by the p -th and (m p) -th knots, where p is the degree and m is the last index of the knot vector

Examples

def linspace(

```
self,
n_eval_per_elem: Union[int, Iterable[int]] = 10
) -> tuple[numpy.ndarray[numpy.floating], ...]:
```

View Source

Generate sets of evaluation points over the span of each basis in the isoparametric space.

This method creates evenly spaced points for each isoparametric dimension by calling linspace on each BSplineBasis instance stored in the bases array.

Parameters

• n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. If an int is provided, the same number is used for all dimensions. If an Iterable is provided, each value corresponds to a different dimension. By default, 10.

Returns

• XI (tuple[np.ndarray[np.floating], ...]): Tuple containing arrays of evaluation points for each isoparametric dimension. The tuple has length NPa (dimension of isoparametric space).

Notes

- For a curve (1D), returns (xi points,)
- For a surface (2D), returns (xi points, eta points)
- For a volume (3D), returns (xi points, eta points, zeta points)
- The number of points returned for each dimension depends on the number of elements in that dimension times the value of n eval per elem

Examples

def linspace_for_integration(

```
self,
```

```
n_eval_per_elem: Union[int, Iterable[int]] = 10,
bounding_box: Optional[Iterable] = None
```

) -> tuple[tuple[numpy.ndarray[numpy.floating], ...], tuple[numpy.ndarray[numpy.floating], ...]]: • View Source

Generate sets of evaluation points and their integration weights over each basis span.

This method creates evenly spaced points and their corresponding integration weights for each isoparametric dimension by calling linspace_for_integration on each BSplineBasis instance stored in the bases array.

Parameters

- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. If an int is provided, the same number is used for all dimensions. If an Iterable is provided, each value corresponds to a different dimension. By default, 10.
- **bounding_box** (Union[Iterable[tuple[float, float]], None], optional): Lower and upper bounds for each isoparametric dimension. If None, uses the span of each basis. Format: [(xi_min, xi_max), (eta_min, eta_max), ...]. By default, None.

Returns

- XI (tuple[np.ndarray[np.floating], ...]): Tuple containing arrays of evaluation points for each isoparametric dimension. The tuple has length NPa (dimension of isoparametric space).
- **dXI** (tuple[np.ndarray[np.floating], ...]): Tuple containing arrays of integration weights for each isoparametric dimension. The tuple has length NPa (dimension of isoparametric space).

Notes

- For a curve (1D), returns ((xi points), (xi weights))
- For a surface (2D), returns ((xi points, eta points), (xi weights, eta weights))
- For a volume (3D), returns ((xi points, eta points, zeta points), (xi weights, eta weights, zeta weights))
- The points are centered in their integration intervals
- The weights represent the size of the integration intervals

Examples

def gauss_legendre_for_integration(

self,

n_eval_per_elem: Union[int, Iterable[int], NoneType] = None,

bounding_box: Optional[Iterable] = None

) -> tuple[tuple[numpy.ndarray[numpy.floating], ...], tuple[numpy.ndarray[numpy.floating], ...]]: • View Source

Generate sets of evaluation points and their Gauss-Legendre integration weights over each basis span.

This method creates Gauss-Legendre quadrature points and their corresponding integration weights for each isoparametric dimension by calling <code>gauss_legendre_for_integration</code> on each <code>BSplineBasis</code> instance stored in the <code>bases</code> array.

Parameters

- n_eval_per_elem (Union[int, Iterable[int], None], optional): Number of evaluation points per element for each isoparametric dimension. If an int is provided, the same number is used for all dimensions. If an Iterable is provided, each value corresponds to a different dimension. If None, uses (p + 2)//2 points per element where p is the degree of each basis. This number of points ensures an exact integration of a p -th degree polynomial. By default, None.
- **bounding_box** (Union[Iterable[tuple[float, float]], None], optional): Lower and upper bounds for each isoparametric dimension. If None, uses the span of each basis. Format: [(xi_min, xi_max), (eta_min, eta_max), ...]. By default, None.

Returns

- XI (tuple[np.ndarray[np.floating], ...]): Tuple containing arrays of Gauss-Legendre points for each isoparametric dimension. The tuple has length NPa (dimension of isoparametric space).
- **dXI** (tuple[np.ndarray[np.floating], ...]): Tuple containing arrays of Gauss-Legendre weights for each isoparametric dimension. The tuple has length NPa (dimension of isoparametric space).

Notes

- For a curve (1D), returns ((xi points), (xi weights))
- For a surface (2D), returns ((xi points, eta points), (xi weights, eta weights))
- For a volume (3D), returns ((xi points, eta points, zeta points), (xi weights, eta weights, zeta weights))
- The points and weights follow the Gauss-Legendre quadrature rule
- When n_eval_per_elem is None , uses (p + 2)//2 points per element for exact integration of polynomials up to degree p

Examples

Maps all knot vectors to the interval [0, 1] in each isoparametric dimension.

This method normalizes the knot vectors of each BSplineBasis instance stored in the bases array by applying an affine transformation that maps the span interval to [0, 1].

Notes

- The transformation preserves the relative spacing between knots
- The transformation preserves the multiplicity of knots
- The transformation is applied independently to each isoparametric dimension
- This operation modifies the knot vectors in place

Examples

def DN(

self,

XI: Union[numpy.ndarray[numpy.floatinq], tuple[numpy.ndarray[numpy.floatinq], ...]],

k: Union[int, Iterable[int]] = 0

) -> Union[scipy.sparse._base.spmatrix, numpy.ndarray[scipy.sparse._base.spmatrix]]:

Compute the k -th derivative of the B-spline basis at given points in the isoparametric space.

View Source

This method evaluates the basis functions or their derivatives at specified points, returning a matrix that can be used to evaluate the B-spline through a dot product with the control points.

Parameters

- XI (Union[np.ndarray[np.floating], tuple[np.ndarray[np.floating], ...]]): Points in the isoparametric space where to evaluate the basis functions. Two input formats are accepted:
 - 1. numpy.ndarray : Array of coordinates with shape (NPa , n_points). Each column represents one
 evaluation point [xi , eta , ...]. The resulting matrices will have shape (n_points, number of functions).
 - 2. tuple: Contains NPa arrays of coordinates (xi, eta, ...). The resulting matrices will have (n_xi × n_eta × ...) rows.
- k (Union[int, Iterable[int]], optional): Derivative orders to compute. Two formats are accepted:
 - 1. int: Same derivative order along all axes. Common values:
 - k=0: Evaluate basis functions (default)
 - k=1 : Compute first derivatives (gradient)
 - k=2 : Compute second derivatives (hessian)
 - 2. list[int]: Different derivative orders for each axis. Example: [1, 0] computes first derivative w.r.t xi, no derivative w.r.t eta. By default, 0.

Returns

- **DN** (Union[sps.spmatrix, np.ndarray[sps.spmatrix]]): Sparse matrix or array of sparse matrices containing the basis evaluations:
 - If k is a list or is 0: Returns a single sparse matrix containing the mixed derivative specified by the list.

• If k is an int > 0: Returns an array of sparse matrices with shape [NPa]* k. For example, if k=1, returns NPa matrices containing derivatives along each axis.

Notes

- For evaluating the B-spline with control points in NPh -D space: values = DN @ ctrl_pts.reshape((NPh, -1)).T
- When using tuple input format for XI , points are evaluated at all combinations of coordinates
- When using array input format for XI , each column represents one evaluation point
- The gradient (k=1) returns NPa matrices for derivatives along each axis
- Mixed derivatives can be computed using a list of derivative orders

Examples

Create a 2D quadratic B-spline:

Evaluate basis functions at specific points using array input:

Compute first derivatives using tuple input:

Compute mixed derivatives:

def knotInsertion(

self,

ctrl_pts: numpy.ndarray[numpy.floating],
knots_to_add: Iterable[Union[numpy.ndarray[numpy.float64], int]]
) -> numpy.ndarray[numpy.floating]:

View Source

Add knots to the B-spline while preserving its geometry.

This method performs knot insertion by adding new knots to each isoparametric dimension and computing the new control points to maintain the exact same geometry. The method modifies the <code>BSpline</code> object by updating its basis functions with the new knots.

Parameters

- ctrl_pts (np.ndarray[np.floating]): Control points defining the B-spline geometry. Shape: (NPh , n1, n2, ...) where:
 - NPh is the dimension of the physical space
 - o ni is the number of control points in the i-th isoparametric dimension
- **knots_to_add** (Iterable[Union[np.ndarray[np.floating], int]]): Refinement specification for each isoparametric dimension. For each dimension, two formats are accepted:
 - 1. numpy.ndarray : Array of knots to insert. These knots must lie within the span of the existing knot vector.
 - 2. int: Number of equally spaced knots to insert in each element.

Returns

• new_ctrl_pts (np.ndarray[np.floating]): New control points after knot insertion. Shape: (NPh , m1, m2, ...) where mi ≥ ni is the new number of control points in the i-th isoparametric dimension.

Notes

- Knot insertion preserves the geometry and parameterization of the B-spline
- The number of new control points depends on the number and multiplicity of inserted knots
- When using integer input, knots are inserted with uniform spacing in each element
- The method modifies the basis functions but maintains C^{p-m} continuity, where p is the degree and m is the multiplicity of the inserted knot

Examples

Create a 2D quadratic B-spline and insert knots:

Insert specific knots in first dimension only:

Insert two knots per element in both dimensions:

def orderElevation(

self,

ctrl_pts: numpy.ndarray[numpy.floating],
t: Iterable[int]

) -> numpy.ndarray[numpy.floating]:

View Source

Elevate the polynomial degree of the B-spline while preserving its geometry.

This method performs order elevation by increasing the polynomial degree of each isoparametric dimension and computing the new control points to maintain the exact same geometry. The method modifies the BSpline object by updating its basis functions with the new degrees.

Parameters

- **ctrl_pts** (np.ndarray[np.floating]): Control points defining the B-spline geometry. Shape: (NPh , n1, n2, ...) where:
 - NPh is the dimension of the physical space
 - o ni is the number of control points in the i-th isoparametric dimension
- t (Iterable[int]): Degree elevation for each isoparametric dimension. For each dimension i, the new degree will be p_i + t_i where p_i is the current degree.

Returns

• new_ctrl_pts (np.ndarray[np.floating]): New control points after order elevation. Shape: (NPh, m1, m2, ...) where mi ≥ ni is the new number of control points in the i-th isoparametric dimension.

Notes

- Order elevation preserves the geometry and parameterization of the B-spline
- The number of new control points depends on the current degree and number of elements
- The method modifies the BSpline object by updating its basis functions
- This operation is more computationally expensive than knot insertion

Examples

Create a 2D quadratic B-spline and elevate its order:

Elevate order by 1 in first dimension only:

```
>>> t = [1, 0] # Increase degree by 1 in first dimension
>>> new_ctrl_pts = spline.orderElevation(ctrl_pts, t)
>>> new_ctrl_pts.shape
(3, 6, 4) # Two new control points added in first dimension (one per element)
>>> spline.getDegrees() # The degrees are modified
array([3, 2])
```

def greville_abscissa(

self,

return_weights: bool = False

) -> Union[list[numpy.ndarray[numpy.floating]], tuple[list[numpy.ndarray[numpy.floating]], list[numpy.ndarray[

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Compute the Greville abscissa and optionally their weights for each isoparametric dimension.

The Greville abscissa can be interpreted as the "position" of the control points in the isoparametric space. They are often used as interpolation points for B-splines.

Parameters

• return_weights (bool, optional): If True, also returns the weights (span lengths) of each basis function. By default, False.

Returns

- **greville** (list[np.ndarray[np.floating]]): List containing the Greville abscissa for each isoparametric dimension. The list has length NPa, where each element is an array of size n + 1, n being the last index of the basis functions in that dimension.
- weights (list[np.ndarray[np.floating]], optional): Only returned if return_weights is True . List containing the weights for each isoparametric dimension. The list has length NPa , where each element is an array containing the span length of each basis function.

Notes

- For a curve (1D), returns [xi abscissa]
- For a surface (2D), returns [xi abscissa, eta abscissa]
- For a volume (3D), returns [xi abscissa, eta abscissa, zeta abscissa]
- The Greville abscissa are computed as averages of p consecutive knots
- The weights represent the size of the support of each basis function
- The number of abscissa in each dimension equals the number of control points

Examples

Compute Greville abscissa for a 2D B-spline:

Compute both abscissa and weights:

```
>>> greville, weights = spline.greville_abscissa(return_weights=True
)
>>> weights[0] # weights for xi direction
array([0.5, 1. , 1. , 0.5])
```


Create meshes containing all the data needed to plot the control polygon of the B-spline.

This method generates a list of io.Mesh objects representing the control mesh (polygonal connectivity) of the B-spline, suitable for visualization (e.g. in Paraview). It supports time-dependent fields and arbitrary dimension.

Parameters

- ctrl_pts (np.ndarray[np.floating]): Array of control points of the B-spline, with shape (NPh , number of elements for dim 1, ..., number of elements for dim NPa), where NPh is the physical space dimension and NPa is the dimension of the isoparametric space.
- n step (int, optional): Number of time steps to plot. By default, 1.
- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. By default, 10.
 - If an int is provided, the same number is used for all dimensions.
 - If an Iterable is provided, each value corresponds to a different dimension.
- **n_step** (int, optional): Number of time steps to plot. By default, 1.
- fields (dict, optional): Dictionary of fields to plot at each time step. Keys are field names. Values can be:
 - a function taking (BSpline spline, tuple of np.ndarray[np.floating] XI) and returning a
 np.ndarray[np.floating] of shape (n_step, number of combinations of XI, field size),
 - a np.ndarray[np.floating] defined on the control points, of shape (n_step, field size,
 * ctrl_pts.shape[1:]), which is then interpolated using the B-spline basis functions,
 - o a np.ndarray[np.floating] defined **on the evaluation grid**, of shape (n_step, field size, *grid shape), where grid shape matches the discretization provided by XI or n_eval_per_elem. In this case, the field is interpolated in physical space using scipy.interpolate.griddata.
- XI (tuple[np.ndarray[np.floating], ...], optional): Parametric coordinates at which to evaluate the B-spline and fields. If not None, overrides the n_eval_per_elem parameter. If None, a regular grid is generated according to n_eval_per_elem.
- paraview_sizes (dict, optionnal): The fields present in this dict are overrided by np.NaN s. The keys must be the fields names and the values must be the fields sizes for paraview. By default, {}.

Returns

• **list[io.Mesh]**: List of **io.Mesh** objects, one for each time step, containing the control mesh geometry and associated fields.

Notes

- The control mesh is constructed by connecting control points along each isoparametric direction.
- Fields can be provided either as functions evaluated at the Greville abscissae, or as arrays defined on the control points or on a regular parametric grid (in which case they are interpolated at the Greville abscissae).
- The first axis of the field array or function output corresponds to the time step, even if there is only one.
- The method is compatible with B-splines of arbitrary dimension.

Examples

```
def make_elem_separator_meshes(
```

```
self,
ctrl_pts: numpy.ndarray[numpy.floating],
n_eval_per_elem: Union[int, Iterable[int]] = 10,
n_step: int = 1,
fields: dict = {},
XI: Optional[tuple[numpy.ndarray[numpy.floating], ...]] = None,
paraview_sizes: dict = {}
) -> list[meshio._mesh.Mesh]:
```

Create meshes representing the boundaries of every element in the B-spline for visualization.

This method generates a list of io.Mesh objects containing the geometry and optional fields needed to plot the limits (borders) of all elements from the isoparametric space of the B-spline. Supports time-dependent fields and arbitrary dimension.

View Source

Parameters

- ctrl_pts (np.ndarray[np.floating]): Array of control points of the B-spline, with shape (NPh, number of elements for dim 1, ..., number of elements for dim NPa), where NPh is the physical space dimension and NPa is the dimension of the isoparametric space.
- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. By default, 10.
 - If an int is provided, the same number is used for all dimensions.
 - If an Iterable is provided, each value corresponds to a different dimension.
- n_step (int, optional): Number of time steps to plot. By default, 1.
- fields (dict, optional): Dictionary of fields to plot at each time step. Keys are field names. Values can be:
 - o a function taking (BSpline spline, tuple of np.ndarray[np.floating] XI) and returning a np.ndarray[np.floating] of shape (n_step, number of combinations of XI, field size),
 - a np.ndarray[np.floating] defined on the control points, of shape (n_step, field size,
 * ctrl_pts.shape[1:]), which is then interpolated using the B-spline basis functions,
 - o a np.ndarray[np.floating] defined **on the evaluation grid**, of shape (n_step, field size, *grid shape), where grid shape matches the discretization provided by XI or n_eval_per_elem. In this case, the field is interpolated in physical space using scipy.interpolate.griddata.
- XI (tuple[np.ndarray[np.floating], ...], optional): Parametric coordinates at which to evaluate the B-spline and fields. If not None, overrides the n_eval_per_elem parameter. If None, a regular grid is generated according to n_eval_per_elem.
- paraview_sizes (dict, optionnal): The fields present in this dict are overrided by np.NaN s. The keys must be the fields names and the values must be the fields sizes for paraview. By default, {}.

Returns

• **list[io.Mesh]**: List of io.Mesh objects, one for each time step, containing the element boundary geometry and associated fields.

Notes

- The element boundary mesh is constructed by connecting points along the unique knot values in each isoparametric direction, outlining the limits of each element.
- Fields can be provided either as callable functions, as arrays defined on the control points, or as arrays

already defined on a regular evaluation grid.

- When fields are defined on a grid, they are interpolated in the physical space using scipy.interpolate.griddata with linear interpolation.
- The first axis of the field array or function output corresponds to the time step, even if there is only one.
- The method supports B-splines of arbitrary dimension.

Examples

def make_elements_interior_meshes(

Create meshes representing the interior of each element in the B-spline.

This method generates a list of io.Mesh objects containing the geometry and optional fields for the interior of all elements, suitable for visualization (e.g., in ParaView). Supports time-dependent fields and arbitrary dimension.

Parameters

- ctrl_pts (np.ndarray[np.floating]): Array of control points of the B-spline, with shape (NPh, number of points for dim 1, ..., number of points for dim NPa), where NPh is the physical space dimension and NPa is the dimension of the isoparametric space.
- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. By default, 10.
 - If an int is provided, the same number is used for all dimensions.
 - If an Iterable is provided, each value corresponds to a different dimension.
- n step (int, optional): Number of time steps to plot. By default, 1.
- fields (dict, optional): Dictionary of fields to plot at each time step. Keys are field names. Values can be:
 - a function taking (BSpline spline, tuple of np.ndarray[np.floating] XI) and returning a np.ndarray[np.floating] of shape (n_step, number of combinations of XI, field size),
 - a np.ndarray[np.floating] defined on the control points, of shape (n_step, field size,
 * ctrl_pts.shape[1:]), in which case it is interpolated using the B-spline basis functions,
 - o a np.ndarray[np.floating] defined directly on the evaluation grid, of shape (n_step, field size, *grid shape), where grid shape is the shape of the discretization XI (i.e., number of points along each parametric axis). By default, {} (no fields).
- XI (tuple[np.ndarray[np.floating], ...], optional): Parametric coordinates at which to evaluate the B-spline and fields. If not None, overrides the n_eval_per_elem parameter. If None, a regular grid is generated according to n_eval_per_elem.

Returns

• **list[io.Mesh]**: List of io.Mesh objects, one for each time step, containing the element interior geometry and associated fields.

- The interior mesh is constructed by evaluating the B-spline at a regular grid of points in the isoparametric space, with connectivity corresponding to lines (1D), guads (2D), or hexahedra (3D).
- Fields can be provided either as arrays (on control points or on the discretization grid) or as functions.
- Arrays given on control points are automatically interpolated using the B-spline basis functions.
- Arrays already given on the evaluation grid are used directly without interpolation.
- The first axis of the field array or function output must correspond to the time step, even if there is only one.
- The method is compatible with B-splines of arbitrary dimension.

Examples

```
>>> degrees = [2, 2]
>>> knots = [np.array([0, 0, 0.5, 1, 1, 1], dtype='float'),
             np.array([0, 0, 0, 1, 1, 1], dtype='float')]
>>> spline = BSpline(degrees, knots)
>>> ctrl_pts = np.random.rand(3, 4, 3) # 3D control points for a 2D surface
>>> # Field given on control points (needs interpolation)
>>> field_on_ctrl_pts = np.random.rand(1, 1, 4, 3)
>>> # Field given directly on the evaluation grid (no interpolation)
>>> field_on_grid = np.random.rand(1, 1, 10, 10)
>>> meshes = spline.make_elements_interior_meshes(
        ctrl_pts,
       fields={'temperature': field_on_ctrl_pts, 'pressure': field_on_grid
. . .
}
       XI= # TODO
. . .
...)
>>> mesh = meshes[0]
```

def saveParaview(

Save B-spline visualization data as Paraview files.

This method creates three types of visualization files:

- Interior mesh showing the B-spline surface/volume
- Element borders showing the mesh structure
- Control points mesh showing the control structure

All files are saved in VTU format with an optional PVD file to group them.

Parameters

- **ctrl_pts** (np.ndarray[np.floating]): Control points defining the B-spline geometry. Shape: (NPh , n1, n2, ...) where:
 - NPh is the dimension of the physical space
 - o ni is the number of control points in the i-th isoparametric dimension
- path (str): Directory path where the PV files will be saved
- name (str): Base name for the output files
- **n_step** (int, optional): Number of time steps to save. By default, 1.

- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for each isoparametric dimension. By default, 10.
 - If an int is provided, the same number is used for all dimensions.
 - If an Iterable is provided, each value corresponds to a different dimension.
- **fields** (Union[dict, None], optional): Fields to visualize at each time step. Dictionary format: { "field_name": field_value } where field_value can be either:
 - 1. A numpy array with shape (n_step, field_size, *ctrl_pts.shape[1:]) where:
 - n_step: Number of time steps
 - field_size : Size of the field at each point (1 for scalar, 3 for vector)
 - o *ctrl_pts.shape[1:]:Same shape as control points (excluding NPh)
 - 2. A numpy array with shape (n_step, field_size, *grid_shape) where:
 - n_step: Number of time steps
 - field_size : Size of the field at each point (1 for scalar, 3 for vector)
 - *grid_shape : Shape of the evaluation grid (number of points along each isoparametric axis)
 - 3. A function that computes field values (np.ndarray[np.floating]) at given points from the BSpline instance and XI, the tuple of arrays containing evaluation points for each dimension (tuple[np.ndarray[np.floating], ...]). The result should be an array of shape (n_step, n_points, field_size) where:
 - n_step: Number of time steps
 - ∘ n_points : Number of evaluation points (n_xi × n_eta × ...)
 - field_size : Size of the field at each point (1 for scalar, 3 for vector)

By default, None.

- XI (tuple[np.ndarray[np.floating], ...], optional): Parametric coordinates at which to evaluate the B-spline and fields. If not None, overrides the n_eval_per_elem parameter. If None, a regular grid is generated according to n_eval_per_elem.
- **groups** (Union[dict[str, dict[str, Union[str, int]]], None], optional): Nested dictionary specifying file groups for PVD organization. Format: { "group_name": { "ext": str, # File extension (e.g., "vtu") "npart": int, # Number of parts in the group "nstep": int # Number of timesteps } } The method automatically creates/updates three groups:
 - o "interior": For the B-spline surface/volume mesh
 - o "elements_borders": For the element boundary mesh
 - o "control_points": For the control point mesh

If provided, existing groups are updated; if None, these groups are created. By default, None.

- make_pvd (bool, optional): Whether to create a PVD file grouping all VTU files. By default, True.
- verbose (bool, optional): Whether to print progress information. By default, True.
- fields_on_interior_only (Union[bool, Literal['auto'], list[str]], optionnal): Whether to include fields only on the interior mesh (True), on all meshes (False), or on specified field names. If set to 'auto', fields named 'u', 'U', 'displacement' or 'displ' are included on all meshes while others are only included on the interior mesh. By default, 'auto'.

Returns

• groups (dict[str, dict[str, Union[str, int]]): Updated groups dictionary with information about saved files.

Notes

- Creates three types of VTU files for each time step:
 - {name}_interior_{part}_{step}.vtu
 - {name}_elements_borders_{part}_{step}.vtu
 - o {name}_control_points_{part}_{step}.vtu
- If make_pvd=True, creates a PVD file named {name}.pvd
- Fields can be visualized as scalars or vectors in Paraview
- The method supports time-dependent visualization through n_step

Examples

Save a 2D B-spline visualization:

Save with a custom field:

```
>>> def displacement(spline, XI):
... # Compute displacement field
... return np.random.rand(1, np.prod([x.size for x in XI]), 3)
>>> fields = {"displacement": displacement}
>>> spline.saveParaview(ctrl_pts, "./output", "bspline", fields=fields
)
```

```
def getGeomdl(self, ctrl_pts):
```

• View Source

```
def plotMPL(
    self,
    ctrl_pts: numpy.ndarray[numpy.floating],
    n_eval_per_elem: Union[int, Iterable[int]] = 10,
    ax: Optional[matplotlib.axes._axes.Axes] = None,
    ctrl_color: str = '#1b9e77',
    interior_color: str = '#7570b3',
    elem_color: str = '#666666',
    border_color: str = '#d95f02',
    language: Union[Literal['english'], Literal['français']] = 'english'
):
```

View Source

Plot the B-spline using Matplotlib.

Creates a visualization of the B-spline geometry showing the control mesh, B-spline surface/curve, element borders, and patch borders. Supports plotting 1D curves and 2D surfaces in 2D space, and 2D surfaces and 3D volumes in 3D space.

Parameters

- **ctrl_pts** (np.ndarray[np.floating]): Control points defining the B-spline geometry. Shape: (NPh, n1, n2, ...) where:
 - NPh is the dimension of the physical space (2 or 3)
 - o ni is the number of control points in the i-th isoparametric dimension
- n_eval_per_elem (Union[int, Iterable[int]], optional): Number of evaluation points per element for visualizing the B-spline. Can be specified as:
 - Single integer: Same number for all dimensions
 - Iterable of integers: Different numbers for each dimension By default, 10.
- ax (Union[mpl.axes.Axes, None], optional): Matplotlib axes for plotting. If None, creates a new figure and axes. For 3D visualizations, must be a 3D axes if provided (created with projection='3d'). Default is None (creates new axes).
- ctrl_color (str, optional): Color for the control mesh visualization:
 - Applied to control points (markers)
 - Applied to control mesh lines Default is '#1b9e77' (green).
- interior_color (str, optional): Color for the B-spline geometry:
 - o For curves: Line color
 - o For surfaces: Face color (with transparency)

- o For volumes: Face color of boundary surfaces (with transparency) Default is '#7570b3' (purple).
- elem_color (str, optional): Color for element boundary visualization:
 - o Shows internal mesh structure
 - o Helps visualize knot locations Default is '#666666' (gray).
- border_color (str, optional): Color for patch boundary visualization:
 - Outlines the entire B-spline patch
 - Helps distinguish patch edges Default is '#d95f02' (orange).
- language (str, optional): Language for the plot labels. Can be 'english' or 'français'. Default is 'english'.

Notes

Visualization components:

- Control mesh: Shows control points and their connections
- B-spline: Shows the actual curve/surface/volume
- Element borders: Shows the boundaries between elements
- Patch borders: Shows the outer boundaries of the B-spline

Supported configurations:

- 1D B-spline in 2D space (curve)
- 2D B-spline in 2D space (surface)
- 2D B-spline in 3D space (surface)
- 3D B-spline in 3D space (volume)

For 3D visualization:

- Surfaces are shown with transparency
- Volume visualization shows the faces with transparency
- View angle is automatically set for surfaces based on surface normal

Examples

Plot a 2D curve in 2D space:

```
>>> degrees = [2]
>>> knots = [np.array([0, 0, 0, 1, 1, 1], dtype='float')]
>>> spline = BSpline(degrees, knots)
>>> ctrl_pts = np.random.rand(2, 3) # 2D control points
>>> spline.plotMPL(ctrl_pts)
```

Plot a 2D surface in 3D space:

Plot on existing axes with custom colors:

```
>>> fig = plt.figure()
>>> ax = fig.add_subplot(projection='3d')
>>> spline.plotMPL(ctrl_pts, ax=ax, ctrl_color='red', interior_color='blue'
)
```

bsplyne.save_utils

View Source



def writePVD(fileName: str, groups: dict[str, dict]):

View Source

Writes a Paraview Data (PVD) file that references multiple VTK files.

Creates an XML-based PVD file that collects and organizes multiple VTK files into groups, allowing visualization of multi-part, time-series data in Paraview.

Parameters

- fileName (str): Base name for the mesh files (without numbers and extension)
- **groups** (dict[str, dict]): Nested dictionary specifying file groups with format: {"group_name": {"ext": "file_extension", "npart": num_parts, "nstep": num_timesteps}}

Notes

VTK files must follow naming pattern: {fileName}_{group}_{part}_{timestep}.{ext} Example: for fileName="mesh", group="fluid", part=1, timestep=5, ext="vtu": mesh_fluid_1_5.vtu

Returns

None

def merge_meshes(meshes: Iterable[meshio._mesh.Mesh]) -> meshio._mesh.Mesh:

View Source

Merges multiple meshio. Mesh objects into a single mesh.

Parameters

• meshes (Iterable[io.Mesh]): An iterable of meshio.Mesh objects to merge.

Returns

• **io.Mesh**: A single meshio.Mesh object containing the merged meshes with combined vertices, cells and point data.

def merge_saves(

```
path: str,
name: str,
nb_patchs: int,
nb_steps: int,
group_names: list[str]
) -> None:
```

• View Source

Merge multiple mesh files and save the merged results.

This function reads multiple mesh files for each group and time step, merges them into a single mesh, and writes the merged mesh to a new file. It also generates a PVD file to describe the collection of merged meshes.

Parameters

- path (str): The directory path where the mesh files are located.
- name (str): The base name of the mesh files.
- **nb_patchs** (int): The number of patches to merge for each group and time step.
- nb_steps (int): The number of time steps for which meshes are available.
- group_names (list[str]): A list of group names to process.

Returns

None