



**bsplyne** is a Python library for working with N-dimensional B-splines. It implements the Cox-de Boor algorithm for basis evaluation, order elevation, knot insertion, and provides a connectivity class for multi-patch structures. Additionally, it includes visualization tools with export capabilities to Paraview.

**Note:** This library is not yet available on PyPI. To install, please clone the repository and install it manually.

## Installation

Since **bsplyne** is not yet on PyPI, you can install it locally as follows:

```
git clone https://github.com/Dorian210/bsplyne
cd bsplyne
pip install -e .
```

## Dependencies

Make sure you have the following dependencies installed:

- `numpy`
- `numba`
- `scipy`
- `matplotlib`
- `meshio`
- `tqdm`
- `pathos`

## Main Modules

- **BSplineBasis**  
Implements B-spline basis function evaluation using the Cox-de Boor recursion formula.
- **BSpline**  
Provides methods for creating and manipulating N-dimensional B-splines, including order elevation and knot

insertion.

- **MultiPatchBSplineConnectivity**  
Manages the connectivity between multiple N-dimensional B-spline patches.
- **CouplesBSplineBorder** (less documented)  
Handles coupling between B-spline borders.

## Examples

Several example scripts demonstrating the usage of **bsplyne** can be found in the [examples/](#) directory. These scripts cover:

- Basis evaluation on a curved line
- Plotting with Matplotlib
- Order elevation
- Knot insertion
- Surface examples
- Exporting to Paraview

## Documentation

The full API documentation is available in the [docs/](#) directory of the project or via the [online documentation portal](#).

## Contributions

At the moment, I am not actively reviewing contributions. However, if you encounter issues or have suggestions, feel free to open an issue.

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### class BSpline:

- [View Source](#)

B-Spline from a [NPa](#) -D parametric space into a NPh-D physical space. NPh is not an attribute of this class.

#### Attributes

- **NPa** (int): Parametric space dimension.
- **bases** (numpy.array of BSplineBasis): [numpy . array](#) containing a [BSplineBasis](#) instance for each of the [NPa](#) axis of the parametric space.

### BSpline(degrees, knots)

- [View Source](#)

#### Parameters

- **degrees** (numpy.array of int): Contains the degrees of the B-spline in each parametric dimension.
- **knots** (list of numpy.array of float): Contains the knot vectors of the B-spline for each parametric dimension.

#### Returns

- **BSpline** (BSpline instance): Contains the [BSpline](#) object created.

#### Examples

Creation of a 2D shape as a [BSpline](#) instance :

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]
>>> BSpline(degrees, knots)
```

### NPa

### bases

@classmethod

**def from\_bases(cls, bases):**

- [View Source](#)

Create a [BSpline](#) instance from an array of [BSplineBasis](#) .

#### Parameters

- **bases** (numpy.ndarray of BSplineBasis): The array of [BSplineBasis](#) instances.

#### Returns

- **BSpline**: Contains the [BSpline](#) object created.

### def getDegrees(self):

- [View Source](#)

Returns the degree of each basis in the parametric space.

#### Parameters

- **None**

#### Returns

- **degrees** (numpy.array of int): Contains the degrees of the B-spline.

#### Examples

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]

>>> spline = BSpline(degrees, knots)
>>> spline.getDegrees()
array([2, 2])
```

**def getKnots(self):**

• [View Source](#)

Returns the knot vector of each basis in the parametric space.

Parameters

- **None**

Returns

- **knots** (list of numpy.array of float): Contains the knot vectors of the B-spline.

Examples

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]

>>> spline = BSpline(degrees, knots)
>>> spline.getKnots()
[array([0. , 0. , 0. , 0.5, 1. , 1. , 1. ]),
 array([0. , 0. , 0. , 0.5, 1. , 1. , 1. ])]
```

**def getNbFunc(self):**

• [View Source](#)

Compute the number of basis functions of the spline.

Returns

- **int**: Number of basis functions.

**def getSpans(self):**

• [View Source](#)

Return the span of each basis in the parametric space.

Parameters

- **None**

Returns

- **spans** (list of tuple(float, float)): Contains the span of the B-spline.

**def linspace(self, n\_eval\_per\_elem=10):**

• [View Source](#)

Generate [NPa](#) sets of xi values over the span of each basis.

Parameters

- **n\_eval\_per\_elem** (numpy.array of int or int, optional): Number of values per element over each parametric axis, by default 10

Returns

- **XI** (tuple of numpy.array of float): Set of xi values over each span.

**def linspace\_for\_integration(self, n\_eval\_per\_elem=10, bounding\_box=None):**

• [View Source](#)

Generate `NPa` sets of xi values over the span of the basis, centered on intervals of returned lengths.

#### Parameters

- **n\_eval\_per\_elem** (numpy.array of int or int, optional): Number of values per element over each parametric axis, by default 10
- **bounding\_box** (numpy.array of float , optional): Lower and upper bounds on each axis, by default `[[xi0, xin], [eta0, etan], ...]`

#### Returns

- **XI** (tuple of numpy.array of float): Set of xi values over each span.
- **dXI** (tuple of numpy.array of float): Set of integration weight of each point in **XI** .

```
def gauss_legendre_for_integration(self, n_eval_per_elem=None, bounding_box=None):
```

• [View Source](#)

Generate a set of xi values with their corresponding weight according to the Gauss Legendre integration method over a given bounding box.

#### Parameters

- **n\_eval\_per\_elem** (numpy.array of int, optional): Number of values per element over each parametric axis, by default `self.getDegrees() + 1`
- **bounding\_box** (numpy.array of float, optional): Lower and upper bounds, by default `self . span`

#### Returns

- **XI** (tuple of numpy.array of float): Set of xi values over each span.
- **dXI** (tuple of numpy.array of float): Set of integration weight of each point in **XI** .

```
def normalize_knots(self):
```

• [View Source](#)

Maps the knots vectors to `[0, 1]`.

```
def DN(self, XI, k=0):
```

• [View Source](#)

Compute the `k` -th derivative of the B-spline basis at the points in the parametric space given as input such that a dot product with the reshaped and transposed control points evaluates the B-spline.

#### Parameters

- **XI** (numpy.array of float or tuple of numpy.array of float): If `numpy . array of float` , contains the `NPa` -uplets of parametric coordinates as `[[xi_0, ...], [eta_a, ...], ...]`. Else, if `tuple of numpy . array of float` , contains the `NPa` parametric coordinates as `[[xi_0, ...], [eta_0, ...], ...]`.
- **k** (list of int or int, optional): If `numpy . array of int` , or if `k` is 0, compute the `k` -th derivative of the B-spline basis evaluated on each axis of the parametric space. If `int` , compute the `k` -th derivative along every axis. For example, if `k` is 1, compute the gradient, if `k` is 2, compute the hessian, and so on. , by default 0

#### Returns

- **DN** (scipy.sparse.csr\_matrix of float or numpy.array of scipy.sparse.csr\_matrix of float): Contains the basis of the B-spline.

#### Examples

Evaluation of a 2D BSpline basis on these **XI** values : `[[0, 0.5], [1, 0]]`

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]
>>> spline = BSpline(degrees, knots)
>>> XI = np.array([[0, 0.5], [1, 0]], dtype='float')
>>> spline.DN(XI, [0, 0]).A
array([[0., 0., 0., 1., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.],
       [0., 0., 0., 0., 0.5, 0., 0., 0., 0.5, 0., 0., 0., 0., 0., 0.]])
```

Evaluation of the 2D BSpline basis's derivative along the first axis :

```
>>> XI = (np.array([0, 0.5], dtype='float'),
          np.array([1], dtype='float'))
>>> spline.DN(XI, [1, 0]).A
array([[ 0., -0., -0., -4., 0., 0., 0., 4., 0., 0., 0., 0., 0., 0., 0.],
       [ 0., 0., 0., 0., -2., 0., 0., 2., 0., 0., 0., 0., 0., 0., 0.]])
```

```
def knotInsertion(
    self,
    ctrlPts,
    knots_to_add: Iterable[Union[numpy.ndarray[Any, numpy.dtype[numpy.float64]], int]]
):
```

• [View Source](#)

Add the knots passed in parameter to the knot vector and modify the attributes so that the evaluation of the spline stays the same.

Parameters

- **ctrlPts** (numpy.array of float): Contains the control points of the B-spline as [X, Y, Z, ...]. Its shape : (NPh, nb elem for dim 1, ..., nb elem for dim [NPa](#) )
- **knots\_to\_add** (Iterable[Union[npt.NDArray[np.float64], int]]): Refinement on each axis : If [NDArray](#) , contains the knots to add on said axis. It must not contain knots outside of the old knot vector's interval. If [int](#) , correspond to the number of knots to add in each B-spline element.

Returns

- **ctrlPts** (numpy.array of float): Contains the control points of the B-spline as [X, Y, Z, ...]. Its shape : (NPh, nb elem for dim 1, ..., nb elem for dim [NPa](#) )

Examples

Knot insertion on a 2D BSpline in a 3D space :

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]

>>> ctrlPts = np.random.rand(3, 4, 4)
>>> spline = BSpline(degrees, knots)
>>> knots_to_add = [np.array([0.5, 0.75], dtype='float'),
                    np.array([], dtype='float')]
>>> ctrlPts = pline.knotInsertion(ctrlPts, knots_to_add)
```

```
def orderElevation(self, ctrlPts, t):
```

• [View Source](#)

Performs the order elevation algorithm on every B-spline basis and apply the changes to the control points of the B-spline.

Parameters

- **ctrlPts** (numpy.array of float): Contains the control points of the B-spline as [X, Y, Z, ...]. Its shape : (NPh, nb

elem for dim 1, ..., nb elem for dim `NPa` )

- **t** (numpy.array of int): New degree of each B-spline basis will be its current degree plus the value of `t` corresponding.

Returns

- **ctrlPts** (numpy.array of float): Contains the control points of the B-spline as [X, Y, Z, ...]. Its shape : (NPh, nb elem for dim 1, ..., nb elem for dim `NPa` )

Examples

Order elevation on a 2D BSpline in a 3D space :

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]

>>> ctrlPts = np.random.rand(3, 4, 4)
>>> spline = BSpline(degrees, knots)
>>> ctrlPts = spline.knotInsertion(ctrlPts, [1, 0])
```

**def greville\_abscissa(self, return\_weights=False):**

• [View Source](#)

Compute the Greville abscissa.

Parameters

- **return\_weights** (bool, optional): If `True` , return the weight, the length of the span of the basis function corresponding to each abscissa, by default `False`

Returns

- **greville** (list of np.array of float): Greville abscissa on each parametric axis.
- **weights** (list of np.array of float): Span of each basis function on each parametric axis.

```
def saveParaview(
    self,
    ctrlPts,
    path,
    name,
    n_step=1,
    n_eval_per_elem=10,
    fields=None,
    groups=None,
    make_pvd=True,
    verbose=True,
    fiels_on_interior_only=True
):
```

• [View Source](#)

Saves a plot as a set of .vtu files with a .pvd file.

Parameters

- **ctrlPts** (numpy.array of float): Contains the control points of the B-spline as [X, Y, Z, ...]. Its shape : (NPh, nb elem for dim 1, ..., nb elem for dim `NPa` )
- **path** (string): Path of the directory in which all the files to show in Paraview will be dumped.
- **name** (string): Prefix of the files created.
- **n\_step** (int): Number of time steps to plot.
- **n\_eval\_per\_elem** (numpy.array of int or int, default 10): Contains the number of evaluation of the B-spline in each direction of the parametric space for each element.
- **fields** (dict of function or of numpy.array of float, default None): Fields to plot at each time step. The name of

the field will be the dict key. If the value given is a `function`, it must take the spline and a `tuple` of parametric points that could be given to `self.DN` for example. It must return its value for each time step and on each combination of parametric points. `function ( BSpline spline, tuple ( numpy . array of float ) XI) -> numpy . array of float` of shape `( n_step , nb combinations of XI, size for paraview)` If the value given is a `numpy . array of float`, the shape must be `( n_step , size for paraview, * ctrlPts . shape [1:])`

- **groups** (dict of dict, default None): `dict` (out) of `dict` (in) as :
  - (out) :
    - "interior" : (in) type of `dict` ,
    - "elements\_borders" : (in) type of `dict` ,
    - "control\_points" : (in) type of `dict` .
    - other keys from the input that are not checked
  - (in) :
    - "ext" : name of the extension of the group,
    - "npart" : number of parts to plot together,
    - "nstep" : number of time steps.
- **make\_pvd** (bool, default True): If True, create a PVD file for all the data in `groups` .
- **verbose** (bool, default True): If True, print the advancement state to the standard output.
- **fields\_on\_interior\_only** (bool, default True): Whether to save the fields on the control mesh and elements border too.

## Returns

- **groups** (dict of dict): `dict` (out) of `dict` (in) as :
  - (out) :
    - "interior" : (in) type of `dict` ,
    - "elements\_borders" : (in) type of `dict` ,
    - "control\_points" : (in) type of `dict` .
    - other keys from the input that are not checked
  - (in) :
    - "ext" : name of the extension of the group,
    - "npart" : number of parts to plot together,
    - "nstep" : number of time steps.

## Examples

Save a 2D BSpline in a 3D space in the file `file.pvd` at the location `/path/to/file` :

```
>>> degrees = np.array([2, 2], dtype='int')
>>> knots = [np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float'),
              np.array([0, 0, 0, 0.5, 1, 1, 1], dtype='float')]

>>> ctrlPts = np.random.rand(3, 4, 4)
>>> spline = BSpline(degrees, knots)
>>> spline.saveParaview(ctrlPts, "/path/to/file", "file")
```

**def** getGeomdl(`self`, ctrl\_pts):

• [View Source](#)

**def** plotPV(`self`, ctrl\_pts):

• [View Source](#)



```
def plotMPL(  
    self,  
    ctrl_pts,  
    n_eval_per_elem=10,  
    ax=None,  
    ctrl_color='#1b9e77',  
    interior_color='#7570b3',  
    elem_color='#666666',  
    border_color='#d95f02'  
):
```

• [View Source](#)

# bsplyne.b\_spline\_basis

- [View Source](#)



**class BSplineBasis:**

- [View Source](#)

BSpline basis in 1D.

## Attributes

- **p** (int): Degree of the polynomials composing the basis.
- **knot** (numpy.array of float): Knot vector of the BSpline.
- **m** (int): Last index of the knot vector.
- **n** (int): Last index of the basis : when evaluated, returns an array of size **n** + 1.
- **span** (tuple of 2 float): Interval of definition of the basis.

**BSplineBasis(p, knot)**

- [View Source](#)

Create a **BSplineBasis** object that can compute its basis, and the derivatives of these functions.

## Parameters

- **p** (int): Degree of the BSpline.
- **knot** (numpy.array of float): Knot vector of the BSpline.

## Returns

- **BSplineBasis** (BSplineBasis instance): Contains the **BSplineBasis** object created.

## Examples

Creation of a **BSplineBasis** instance of degree 2 and knot vector [0, 0, 0, 1, 1, 1] :

```
>>> BSplineBasis(2, np.array([0, 0, 0, 1, 1, 1], dtype='float'))
```

**p**

**knot**

**m**

**n**

**span**

**def linspace(self, n\_eval\_per\_elem=10):**

- [View Source](#)

Generate a set of xi values over the span of the basis.

## Parameters

- **n\_eval\_per\_elem** (int, optional): Number of values per element, by default 10

## Returns

- **numpy.array of float**: Set of xi values over the span.

**def linspace\_for\_integration(self, n\_eval\_per\_elem=10, bounding\_box=None):**

- [View Source](#)

Generate a set of xi values over the span of the basis, centered on intervals of returned lengths.

## Parameters

- **n\_eval\_per\_elem** (int, optional): Number of values per element, by default 10

- **bounding\_box** (numpy.array of float, optional): Lower and upper bounds, by default `self . span`

Returns

- **xi** (numpy.array of float): Set of xi values over the span.
- **dxi** (numpy.array of float): Integration weight of each point.

```
def gauss_legendre_for_integration(self, n_eval_per_elem=None, bounding_box=None):
```

• [View Source](#)

Generate a set of xi values with their corresponding weight according to the Gauss Legendre integration method over a given bounding box.

Parameters

- **n\_eval\_per\_elem** (int, optional): Number of values per element, by default `self.p + 1`
- **bounding\_box** (numpy.array of float, optional): Lower and upper bounds, by default `self . span`

Returns

- **xi** (numpy.array of float): Set of xi values over the span.
- **dxi** (numpy.array of float): Integration weight of each point.

```
def normalize_knots(self):
```

• [View Source](#)

Maps the knots vector to [0, 1].

```
def N(self, XI, k=0):
```

• [View Source](#)

Compute the `k`-th derivative of the BSpline basis functions for a set of values in the parametric space.

Parameters

- **XI** (numpy.array of float): Values in the parametric space at which the BSpline is evaluated.
- **k** (int, optional): `k`-th derivative of the BSpline evaluated. The default is 0.

Returns

- **DN** (scipy.sparse.coo\_matrix of float): Sparse matrix containing the values of the `k`-th derivative of the BSpline basis functions in the rows for each value of `XI` in the columns.

Examples

Evaluation of the BSpline basis on these `XI` values : [0, 0.5, 1]

```
>>> basis = BSplineBasis(2, np.array([0, 0, 0, 1, 1, 1], dtype='float'))
>>> basis.N(np.array([0, 0.5, 1], dtype='float')).A
array([[1. , 0. , 0. ],
       [0.25, 0.5 , 0.25],
       [0. , 0. , 1. ]])
```

Evaluation of the 1st derivative of the BSpline basis on these `XI` values : [0, 0.5, 1]

```
>>> basis = BSplineBasis(2, np.array([0, 0, 0, 1, 1, 1], dtype='float'))
>>> basis.N(np.array([0, 0.5, 1], dtype='float'), k=1).A
array([[ -2.,  2.,  0.],
       [ -1.,  0.,  1.],
       [ 0., -2.,  2.]])
```

```
def plotN(self, k=0, show=True):
```

• [View Source](#)

Plots the basis functions over the span.

Parameters

- **k** (int, optional): **k** -th derivative of the BSpline plotted. The default is 0.
- **show** (bool, optional): Should the plot be displayed ? The default is True.

Returns

- **None.**

**def knotInsertion(self, knots\_to\_add):**

• [View Source](#)

Performs the knot inserion process on the `BSplineBasis` instance and returns the **D** matrix.

Parameters

- **knots\_to\_add** (numpy.array of float): Array of knots to append to the knot vector.

Returns

- **D** (scipy.sparse.coo\_matrix of float): The matrix **D** such that :  $\text{newCtrlPtsCoordinate} = \mathbf{D} @ \text{ancientCtrlPtsCoordinate}$ .

Examples

Insert the knots [0.5, 0.5] to the `BSplineBasis` instance and return the operator to apply on the control points.

```
>>> basis = BSplineBasis(2, np.array([0, 0, 0, 1, 1, 1], dtype='float'))
>>> basis.knotInsertion(np.array([0.5, 0.5], dtype='float')).A
array([[1. , 0. , 0. ],
       [0.5, 0.5, 0. ],
       [0.25, 0.5, 0.25],
       [0. , 0.5, 0.5 ],
       [0. , 0. , 1. ]])
```

The knot vector is modified (as well as n and m) :

```
>>> basis.knot
array([0. , 0. , 0. , 0.5, 0.5, 1. , 1. , 1. ])
```

**def orderElevation(self, t):**

• [View Source](#)

Performs the order elevation algorithm on the basis and return a linear transformation to apply on the control points.

Parameters

- **t** (int): New degree of the B-spline basis will be its current degree plus **t** .

Returns

- **STD** (scipy.sparse.coo\_matrix of float): The matrix **STD** such that :  $\text{newCtrlPtsCoordinate} = \mathbf{STD} @ \text{ancientCtrlPtsCoordinate}$ .

Examples

Elevate the orderof the `BSplineBasis` instance by 1 and return the operator to apply on the control points.

```
>>> basis = BSplineBasis(2, np.array([0, 0, 0, 1, 1, 1], dtype='float'))
>>> basis.orderElevation(1).A
array([[1. , 0. , 0. , 0. ],
       [0.33333333, 0.66666667, 0. , 0. ],
       [0. , 0.66666667, 0.33333333],
       [0. , 0. , 1. , 0. ]])
```

The knot vector and the degree are modified (as well as n and m) :

```
>>> basis.knot  
array([0., 0., 0., 0., 1., 1., 1., 1.]
```

```
>>> basis.p  
3
```



- [View Source](#)

```
@nb.njit(cache=True)
def find(parent, x):
```

- [View Source](#)

```
@nb.njit(cache=True)
def union(parent, rank, x, y):
```

- [View Source](#)

```
@nb.njit(cache=True)
def get_unique_nodes_inds(nodes_couples, nb_nodes):
```

- [View Source](#)

```
class MultiPatchBSplineConnectivity:
```

- [View Source](#)

Contains all the methods to link multiple B-spline patches. It uses 3 representations of the data :

- a unique representation, possibly common with other meshes, containing only unique nodes indices,
- a unpacked representation containing duplicated nodes indices,
- a separated representation containing duplicated nodes indices, separated between patches. It is here for user friendliness.

## Attributes

- **unique\_nodes\_inds** (numpy.ndarray of int): The indices of the unique representation needed to create the unpacked one.
- **shape\_by\_patch** (numpy.ndarray of int): The shape of the separated nodes by patch.
- **nb\_nodes** (int): The total number of unpacked nodes.
- **nb\_unique\_nodes** (int): The total number of unique nodes.
- **nb\_patches** (int): The number of patches.
- **npa** (int): The dimension of the parametric space of the B-splines.

```
MultiPatchBSplineConnectivity(unique_nodes_inds, shape_by_patch, nb_unique_nodes)
```

- [View Source](#)

## Parameters

- **unique\_nodes\_inds** (numpy.ndarray of int): The indices of the unique representation needed to create the unpacked one.
- **shape\_by\_patch** (numpy.ndarray of int): The shape of the separated nodes by patch.
- **nb\_unique\_nodes** (int): The total number of unique nodes.

**unique\_nodes\_inds**: numpy.ndarray

**shape\_by\_patch**: numpy.ndarray

**nb\_nodes**: int

**nb\_unique\_nodes**: int

**nb\_patches**: int

**npa**: int

```
@classmethod
def from_nodes_couples(cls, nodes_couples, shape_by_patch):
```

- [View Source](#)

Create the connectivity from a list of couples of unpacked nodes.

## Parameters

- **nodes\_couples** (numpy.ndarray of int): Couples of indices of unpacked nodes that are considered the same. Its shape should be (# of couples, 2)
- **shape\_by\_patch** (numpy.ndarray of int): The shape of the separated nodes by patch.

## Returns

- **MultiPatchBSplineConnectivity**: Instance of [MultiPatchBSplineConnectivity](#) created.

@classmethod

```
def from_separated_ctrlPts(
    cls,
    separated_ctrlPts,
    eps=1e-10,
    return_nodes_couples: bool = False
):
```

• [View Source](#)

Create the connectivity from a list of control points given as a separated field by comparing every couple of points.

## Parameters

- **separated\_ctrlPts** (list of numpy.ndarray of float): Control points of every patch to be compared in the separated representation. Every array is of shape : ( *NPh* , nb elem for dim 1, ..., nb elem for dim *npa* )
- **eps** (float, optional): Maximum distance between two points to be considered the same, by default 1e-10
- **return\_nodes\_couples** (bool, optional): If *True* , returns the *nodes\_couples* created, by default False

## Returns

- **MultiPatchBSplineConnectivity**: Instance of [MultiPatchBSplineConnectivity](#) created.

```
def unpack(self, unique_field):
```

• [View Source](#)

Extract the unpacked representation from a unique representation.

## Parameters

- **unique\_field** (numpy.ndarray): The unique representation. Its shape should be : (field, shape, ..., *self* . *nb\_unique\_nodes* )

## Returns

- **unpacked\_field** (numpy.ndarray): The unpacked representation. Its shape is : (field, shape, ..., *self* . *nb\_nodes* )

```
def pack(self, unpacked_field, method='mean'):
```

• [View Source](#)

Extract the unique representation from an unpacked representation.

## Parameters

- **unpacked\_field** (numpy.ndarray): The unpacked representation. Its shape should be : (field, shape, ..., *self* . *nb\_nodes* )
- **method** (str): The method used to group values that could be different

## Returns

- **unique\_nodes** (numpy.ndarray): The unique representation. Its shape is : (field, shape, ..., *self* . *nb\_unique\_nodes* )

```
def separate(self, unpacked_field):
```

• [View Source](#)

Extract the separated representation from an unpacked representation.

## Parameters

- **unpacked\_field** (numpy.ndarray): The unpacked representation. Its shape is : (field, shape, ..., `self.nb_nodes` )

## Returns

- **separated\_field** (list of numpy.ndarray): The separated representation. Every array is of shape : (field, shape, ..., nb elem for dim 1, ..., nb elem for dim `npa` )

**def agglomerate**(`self`, separated\_field):

• [View Source](#)

Extract the unpacked representation from a separated representation.

## Parameters

- **separated\_field** (list of numpy.ndarray): The separated representation. Every array is of shape : (field, shape, ..., nb elem for dim 1, ..., nb elem for dim `npa` )

## Returns

- **unpacked\_field** (numpy.ndarray): The unpacked representation. Its shape is : (field, shape, ..., `self.nb_nodes` )

**def unique\_field\_indices**(`self`, field\_shape, representation='separated'):

• [View Source](#)

Get the unique, unpacked or separated representation of a field's unique indices.

## Parameters

- **field\_shape** (tuple of int): The shape of the field. For example, if it is a vector field, `field_shape` should be (3,). If it is a second order tensor field, it should be (3, 3).
- **representation** (str, optional): The user must choose between "unique" , "unpacked" , and "separated" . It corresponds to the type of representation to get, by default "separated"

## Returns

- **unique\_field\_indices** (numpy.ndarray of int or list of numpy.ndarray of int): The unique, unpacked or separated representation of a field's unique indices. If unique, its shape is ( `field_shape` , `self.nb_unique_nodes` ). If unpacked, its shape is : ( `field_shape` , `self.nb_nodes` ). If separated, every array is of shape : (\* `field_shape` , nb elem for dim 1, ..., nb elem for dim `npa` ).

**def get\_duplicate\_unpacked\_nodes\_mask**(`self`):

• [View Source](#)

Returns a boolean mask indicating which nodes in the unpacked representation are duplicates.

## Returns

- **duplicate\_nodes\_mask** (numpy.ndarray): Boolean mask of shape (nb\_nodes,) where True indicates a node is duplicated across multiple patches and False indicates it appears only once.

**def extract\_exterior\_borders**(`self`, splines):

• [View Source](#)

Extract exterior borders from B-spline patches.

## Parameters

- **splines** (list[BSpline]): Array of B-spline patches to extract borders from.

## Returns

- **border\_connectivity** (MultiPatchBSplineConnectivity): Connectivity information for the border patches.
- **border\_splines** (list[BSpline]): Array of B-spline patches representing the borders.
- **border\_unique\_to\_self\_unique\_connectivity** (numpy.ndarray of int): Array mapping border unique nodes to original unique nodes.



Raises

- **AssertionError**: If isoparametric space dimension is less than 2.

```
def extract_interior_borders(self, splines):
```

• [View Source](#)

Extract interior borders from B-spline patches where nodes are shared between patches.

Parameters

- **splines** (list[BSpline]): Array of B-spline patches to extract borders from.

Returns

- **border\_connectivity** (MultiPatchBSplineConnectivity): Connectivity information for the border patches.
- **border\_splines** (list[BSpline]): Array of B-spline patches representing the borders.
- **border\_unique\_to\_self\_unique\_connectivity** (numpy.ndarray of int): Array mapping border unique nodes to original unique nodes.

Raises

- **AssertionError**: If parametric space dimension is less than 2.

```
def subset(self, splines, patches_to_keep):
```

• [View Source](#)

Create a subset of the multi-patch B-spline connectivity by keeping only selected patches.

Parameters

- **splines** (list[BSpline]): Array of B-spline patches to subset.
- **patches\_to\_keep** (numpy.array of int): Indices of patches to keep in the subset.

Returns

- **new\_connectivity** (MultiPatchBSplineConnectivity): New connectivity object containing only the selected patches.
- **new\_splines** (list[BSpline]): Array of B-spline patches for the selected patches.
- **new\_unique\_to\_self\_unique\_connectivity** (numpy.ndarray of int): Array mapping new unique nodes to original unique nodes.

```
def save_block(
    self,
    splines,
    block,
    separated_ctrl_pts,
    path,
    name,
    n_step,
    n_eval_per_elem,
    separated_fields,
    fiels_on_interior_only
):
```

• [View Source](#)

Process a block of patches, saving the meshes in their corresponding file. Each block has its own progress bar.

```
def save_paraview(
    self,
    splines,
    separated_ctrl_pts,
    path,
    name,
    n_step=1,
    n_eval_per_elem=10,
    unique_fields={},
    separated_fields=None,
    verbose=True,
    fields_on_interior_only=True
):
```

• [View Source](#)

Save the multipatch B-spline data to Paraview format using parallel processing.

#### Parameters

- **splines** (list[B-spline]): Array of B-spline patches to save
- **separated\_ctrl\_pts** (list[numpy.ndarray]): Control points for each patch in separated representation
- **path** (str): Directory path where files will be saved
- **name** (str): Base name for the saved files
- **n\_step** (int, optional): Number of time steps, by default 1
- **n\_eval\_per\_elem** (int or list[int], optional): Number of evaluation points per element, by default 10
- **unique\_fields** (dict, optional): Fields in unique representation to save, by default {}
- **separated\_fields** (list[dict], optional): Fields in separated representation to save, by default None
- **verbose** (bool, optional): Whether to show progress bars, by default True
- **fields\_on\_interior\_only** (bool, optional): Whether to save fields on interior only, by default True

#### Raises

- **NotImplementedError**: If a callable is passed in unique\_fields
- **ValueError**: If pool is not running and cannot be restarted

**class CouplesBSplineBorder:**

• [View Source](#)

```
CouplesBSplineBorder(
    spline1_inds,
    spline2_inds,
    axes1,
    axes2,
    front_sides1,
    front_sides2,
    transpose_2_to_1,
    flip_2_to_1,
    NPa
)
```

• [View Source](#)

**spline1\_inds**

**spline2\_inds**

**axes1**

**axes2**

**front\_sides1**

**front\_sides2**

**transpose\_2\_to\_1**

**flip\_2\_to\_1**

**NPa**

**nb\_couples**

@classmethod

**def extract\_border\_pts**(cls, field, axis, front\_side, field\_dim=1, offset=0):

• [View Source](#)

@classmethod

**def extract\_border\_spline**(cls, spline, axis, front\_side):

• [View Source](#)

@classmethod

**def transpose\_and\_flip**(cls, field, transpose, flip, field\_dim=1):

• [View Source](#)

@classmethod

**def transpose\_and\_flip\_knots**(cls, knots, spans, transpose, flip):

• [View Source](#)

@classmethod

**def transpose\_and\_flip\_back\_knots**(cls, knots, spans, transpose, flip):

• [View Source](#)

@classmethod

**def transpose\_and\_flip\_spline**(cls, spline, transpose, flip):

• [View Source](#)

@classmethod

**def from\_splines**(cls, separated\_ctrl\_pts, splines):

• [View Source](#)

**def append**(self, other):

• [View Source](#)

**def get\_operator\_allxi1\_to\_allxi2**(self, spans1, spans2, couple\_ind):

• [View Source](#)

**def get\_connectivity**(self, shape\_by\_patch):

• [View Source](#)

**def get\_borders\_couples**(self, separated\_field, offset=0):

• [View Source](#)

**def get\_borders\_couples\_splines**(self, splines):

• [View Source](#)

**def compute\_border\_couple\_DN**(self, couple\_ind: int, splines: list, XI1\_border: list, k1: list):

• [View Source](#)



- [View Source](#)

**p** = 2

**knot** = array([0. , 0. , 0. , 0.25, 0.5 , 0.75, 1. , 1. , 1. ])

**C** = array([1.00002282, 1.00002282, 0.84721156, 0.56754107, 0.19634954, 0. ])

**base\_quarter\_circle** = [show](#)

**def new\_quarter\_circle**(center, normal, radius):

- [View Source](#)

**base\_circle** = [show](#)

**def new\_circle**(center, normal, radius):

- [View Source](#)

**base\_disk** = [show](#)

**def new\_disk**(center, normal, radius):

- [View Source](#)

**base\_degenerated\_disk** = [show](#)

**def new\_degenerated\_disk**(center, normal, radius):

- [View Source](#)

**base\_quarter\_pipe** = [show](#)

**def new\_quarter\_pipe**(center\_front, orientation, radius, length):

- [View Source](#)

**base\_pipe** = [show](#)

**def new\_pipe**(center\_front, orientation, radius, length):

- [View Source](#)

**base\_quarter\_cylinder** = [show](#)

**def new\_quarter\_cylinder**(center\_front, orientation, radius, length):

- [View Source](#)

**base\_cylinder** = [show](#)

**def new\_cylinder**(center\_front, orientation, radius, length):

- [View Source](#)

**base\_degenerated\_cylinder** = [show](#)

**def new\_degenerated\_cylinder**(center\_front, orientation, radius, length):

• [View Source](#)

**p\_closed** = 2

**knot\_closed** = [show](#)

**a** = 0.998323859441081

**b** = -0.4135192822211451

**C\_closed** = [show](#)

**base\_closed\_circle** = [show](#)

**def new\_closed\_circle**(center, normal, radius):

• [View Source](#)

**base\_closed\_disk** = [show](#)

**def new\_closed\_disk**(center, normal, radius):

• [View Source](#)

**base\_closed\_pipe** = [show](#)

**def new\_closed\_pipe**(center\_front, orientation, radius, length):

• [View Source](#)

**base\_closed\_cylinder** = [show](#)

**def new\_closed\_cylinder**(center\_front, orientation, radius, length):

• [View Source](#)

**def new\_quarter\_strut**(center\_front, orientation, radius, length):

• [View Source](#)

**def new\_cube**(center, orientation, side\_length):

• [View Source](#)



- [View Source](#)

```
@nb.njit(cache=True)
def wide_product_max_nnz(a_indptr: numpy.ndarray, b_indptr: numpy.ndarray, height: int) -> int:
```

- [View Source](#)

Compute the maximum number of nonzeros in the result.

#### Parameters

- **a\_indptr** (np.ndarray): CSR pointer array for matrix A.
- **b\_indptr** (np.ndarray): CSR pointer array for matrix B.
- **height** (int): Number of rows (must be the same for both A and B).

#### Returns

- **max\_nnz** (int): Total number of nonzero elements in the resulting matrix.

```
@nb.njit(cache=True)
def wide_product_row(
    a_data: numpy.ndarray,
    a_indices: numpy.ndarray,
    b_data: numpy.ndarray,
    b_indices: numpy.ndarray,
    b_width: int,
    out_data: numpy.ndarray,
    out_indices: numpy.ndarray
) -> int:
```

- [View Source](#)

Compute the wide product for one row.

For each nonzero in the row of A and each nonzero in the row of B, it computes:  $\text{out\_index} = \text{a\_indices}[i] * \text{b\_width} + \text{b\_indices}[j]$   $\text{out\_value} = \text{a\_data}[i] * \text{b\_data}[j]$

#### Parameters

- **a\_data** (np.ndarray): Nonzero values for the row in A.
- **a\_indices** (np.ndarray): Column indices for the row in A.
- **b\_data** (np.ndarray): Nonzero values for the row in B.
- **b\_indices** (np.ndarray): Column indices for the row in B.
- **b\_width** (int): Number of columns in B.
- **out\_data** (np.ndarray): Preallocated output array for the row's data.
- **out\_indices** (np.ndarray): Preallocated output array for the row's indices.

#### Returns

- **off** (int): Number of nonzero entries computed for this row.

```
@nb.njit(cache=True)
def wide_product_numba(
    height: int,
    a_data: numpy.ndarray,
    a_indices: numpy.ndarray,
    a_indptr: numpy.ndarray,
    a_width: int,
    b_data: numpy.ndarray,
    b_indices: numpy.ndarray,
    b_indptr: numpy.ndarray,
    b_width: int
):
```

• [View Source](#)

Compute the row-wise wide (Khatri-Rao) product for two CSR matrices.

For each row  $i$ , the result $[i, :] = \text{kron}(A[i, :], B[i, :])$ , i.e. the Kronecker product of the  $i$ -th rows of  $A$  and  $B$ .

#### Parameters

- **height** (int): Number of rows in  $A$  and  $B$ .
- **a\_data** (np.ndarray): Data array for matrix  $A$  (CSR format).
- **a\_indices** (np.ndarray): Indices array for matrix  $A$ .
- **a\_indptr** (np.ndarray): Index pointer array for matrix  $A$ .
- **a\_width** (int): Number of columns in  $A$ .
- **b\_data** (np.ndarray): Data array for matrix  $B$  (CSR format).
- **b\_indices** (np.ndarray): Indices array for matrix  $B$ .
- **b\_indptr** (np.ndarray): Index pointer array for matrix  $B$ .
- **b\_width** (int): Number of columns in  $B$ .

#### Returns

- **out\_data** (np.ndarray): Data array for the resulting CSR matrix.
- **out\_indices** (np.ndarray): Indices array for the resulting CSR matrix.
- **out\_indptr** (np.ndarray): Index pointer array for the resulting CSR matrix.
- **total\_nnz** (int): Total number of nonzero entries computed.

```
def my_wide_product(
    A: scipy.sparse._base.spmatrix,
    B: scipy.sparse._base.spmatrix
) -> scipy.sparse._csr.csr_matrix:
```

• [View Source](#)

Compute a "1D" Kronecker product row by row.

For each row  $i$ , the result  $C[i, :] = \text{kron}(A[i, :], B[i, :])$ . Matrices  $A$  and  $B$  must have the same number of rows.

#### Parameters

- **A** (scipy.sparse.spmatrix): Input sparse matrix  $A$  in CSR format.
- **B** (scipy.sparse.spmatrix): Input sparse matrix  $B$  in CSR format.

#### Returns

- **C** (scipy.sparse.csr\_matrix): Resulting sparse matrix in CSR format with shape  $(A.\text{shape}[0], A.\text{shape}[1]*B.\text{shape}[1])$ .