

# Lecture Notes on

# **Unit 01 Differential Equations**

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## **1 DEFINITIONS AND TERMINOLOGY, IVP, AND SLOPE FIELDS**

- 1.1 (1.1) - Definitions and Terminology**
- 1.2 (1.2) - Initial Value Problems**
- 1.3 (2.1) - Solution Curves Without A Formula**

## 2 SEPARABLE EQUATIONS

2.1 (2.2) - (General Overview) Separable Equations

2.2 Graphical Interpretations

2.3 Initial Value Problems (continued)

### **3 LINEAR EQUATIONS**

**3.1 (2.3) - (General Overview) Linear Equations**

**3.2 Integrating Factor Method**

**3.3 Interpret and Understand the Structure and Behavior of Solutions and Their Domain**

## 4 EXACT EQUATIONS

- 4.1 (2.4) - (General Overview) Exact Equations
- 4.2 Classifying and Solving Potential Functions
- 4.3 Solving Equations by Integration and Applying Initial Conditions

## 5 SOLUTIONS BY SUBSTITUTION

**5.1 (2.5) - (General Overview) Solutions By Substitutions**

**5.2 Homogeneous Equations**

**5.3 Bernoulli Equations**

**5.4 Other substitutions and methods**

## 6 LINEAR MODELS

- 6.1 (3.1) - (General Overview) Modeling with 1st Order Differential Equations**
- 6.2 Exponential Growth and Decay**
- 6.3 Newton's Law Of Cooling**
- 6.4 Mixing Problems**
- 6.5 Proportional Change Models**