UCF "Practice" Local Contest — August 19-23, 2024

First Last Sorting

filename: firstlast
Difficulty Level: Medium-Hard
Time Limit: 2 seconds

Arup has just created a data structure that makes the two following list transformations in constant O(1) time:

- a. Take any element in the list and move it to the front.
- b. Take any element in the list and move it to the back.

You've realized that sorting speed can be improved using these transformations. For example, consider the input list:

8, 3, 6, 7, 4, 1, 5, 2

We can do the following sequence of transformations to sort this list:

| 8, | 3, | 7, | 4, | 1, | 5, | 2, | 6 | (move 6 to end) |
|----|----|----|----|----|----|----|---|-------------------|
| 8, | 3, | 4, | 1, | 5, | 2, | 6, | 7 | (move 7 to end) |
| 2, | 8, | 3, | 4, | 1, | 5, | 6, | 7 | (move 2 to front) |
| 1, | 2, | 8, | 3, | 4, | 5, | 6, | 7 | (move 1 to front) |
| 1. | 2 | 3. | 4 | 5. | 6. | 7. | 8 | (move 8 to end) |

You are now curious. Given an input array of distinct values, what is the fewest number of these first/last operations necessary to sort the array?

The Problem:

Given an initial permutation of the integers 1, 2, ..., n, determine the fewest number of first/last operations necessary to get the list of values sorted in increasing order.

The Input:

The first line of input will contain a single positive integer, n ($n \le 10^5$), representing the number of values to be sorted. The next n lines contain one integer each. All of these integers will be distinct values in between 1 and n (inclusive), representing the original order of the data to sort for the input case.

The Output:

On a line by itself, output the fewest number of first/last operations necessary to sort the input list.

| 8 3 6 7 4 1 5 | 5 |
|---------------------------------|---|
| 5 1 2 5 3 4 | 1 |