

# Module-02, Basic Mathematics and Statistics

## Mathematics (Linear Algebra)

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December 24, 2023



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# Linear Algebra

For data Science and AI, the basic and fundamental concept is need to known about data representations. The Linear algebra play a key role in emerging field like data science, machine learning and deep learning. So we now start it basic concepts.

## Definition

Algebra is the branch of mathematics, which deal with variables like,  $x$ ,  $y$  and  $z$ . if the variable have power is "one" are called linear. So these studies is called linear algebra.

- Linear algebra, consist of vectors and Matrix.
- Basic operation on matrix like, multiplication and matrix decomposition.



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# System of Linear Equations

The number of linear equations more the one, it makes a system of linear equations. Starting very basic,

- Let us consider general notation for two equations

$$a_1x + b_1y = c_1 \quad (1)$$

$$a_2x + b_2y = c_2 \quad (2)$$

- Let example for two equations

$$2x + 3y = 1 \quad (3)$$

$$3x + 2y = 3 \quad (4)$$

- Solution to above system

The solutions for above system of equations is  $(x, y)$ ,  $(12/5, -3/5)$



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# Matrix Algebra

As, we known that the matrix have rows and columns vectors, how to we get matrix from above discussion.

- General matrix and vector notations

$$Ax = c \quad (5)$$

- Where,  
     $A$  is matrix  
     $x$  variables.  
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# Matrix Algebra

As, we known matrix's has rows and columns, two or more rows or columns make matrix. single row called row vector similar single column called column vector.

- How to convert general system of equations to matrix form

$$\begin{bmatrix} a_1 & b_1 \\ a_2 & b_2 \end{bmatrix}, \begin{bmatrix} x \\ y \end{bmatrix}, \begin{bmatrix} c_1 \\ c_2 \end{bmatrix}$$

- Now equation(5) become try to such a way,

$$Ax = y$$

where,

x,y are independent, dependent variables.

- $$\begin{bmatrix} a_1 & b_1 \\ a_2 & b_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \end{bmatrix}$$



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# Working with Matrix Algebra

- How to find  $x$ .
- We need to shift the matrix to right side.

$$x = A^{-1}c \quad (6)$$

- How to find  $A^{-1}$   
As we know,

$$A^{-1} = \frac{adj(A)}{det(A)} \quad (7)$$



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Great Job  
Thank you

