

some properties of superfluid helium of relevance to dark matter detection

George Seidel, Brown University

Outline

historical introduction

properties of helium deduced from

alphas and electrons stopped in liquid

atomic scattering in gas

interaction of quasiparticles with surfaces

calorimetry and conclusions

historical introduction

Cabrera, Krauss and Wilczek 1985

HERON 1987- 1999 (Lanou, Maris, Seidel)

Helium Roton Observation of Neutrinos

detect pp solar neutrinos with 40 keV threshold

10 ton He fiducial volume at 50 mK

record evaporated He atoms produced by rotons

and UV scintillation using coded aperture

array of calorimeter/wafers

calorimeters film free -- thermal gain

demonstrated technical feasibility

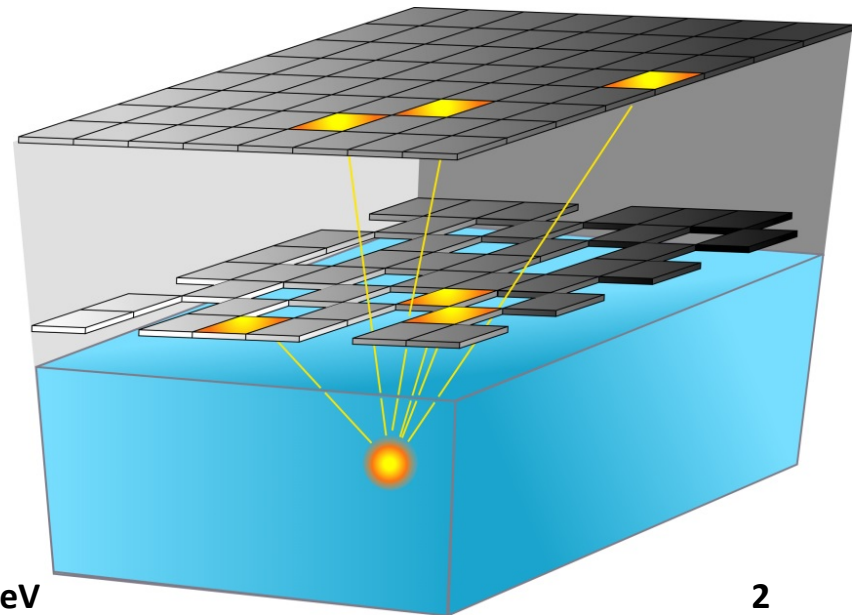
did not proceed to large scale detector

age of principals

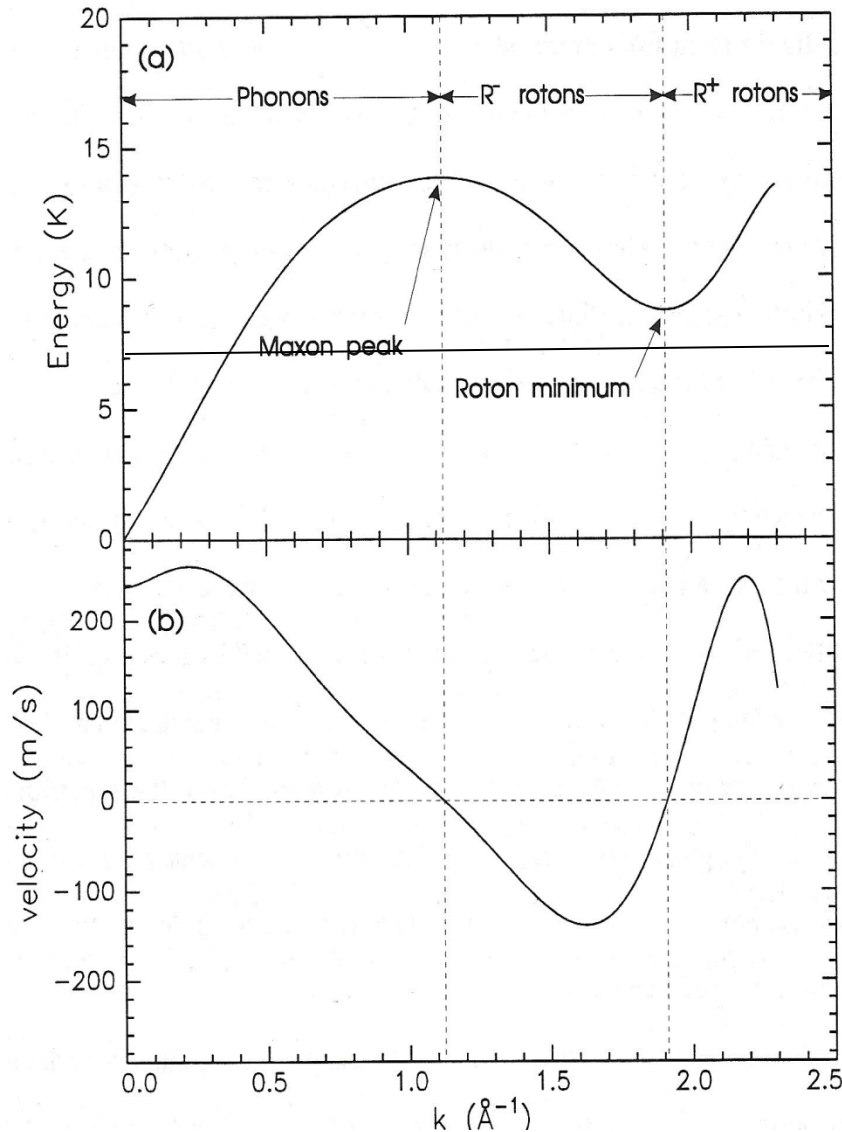
physics no longer current

Huang et al, Astroparticle Physics 30,1 (2008).

*HERON as a dark matter detector?
in "Dark Matter, Quantum Measurement"
ed Tran Thanh Van, Editions Frontieres,
Gif-sur-Yvette (1996)*

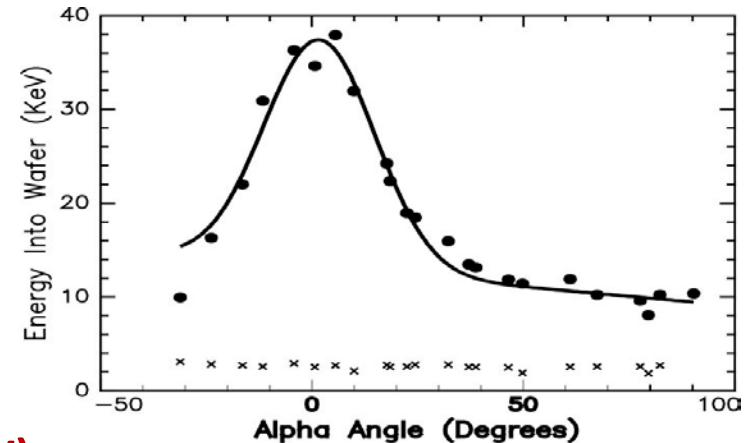
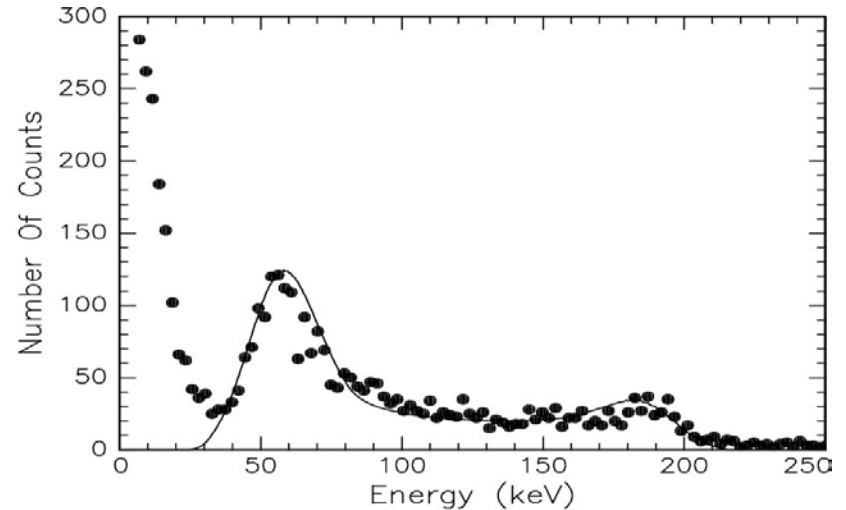
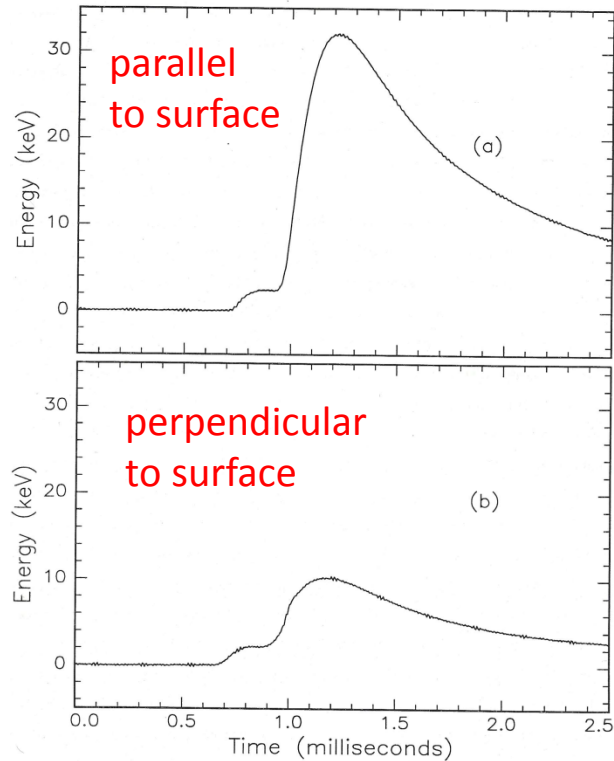


some properties of superfluid helium



- gas/liquid energy difference **7.16 K (.618 meV)**
- vapor density: $1.5 \times 10^{21} T^{1.5} e^{-7.16/T} \text{ \#/cm}^3$
at 100 mK $n \approx 4 \times 10^{-12} \text{ /cm}^3$
- roton energy minimum **8.65 K**
- roton/roton scattering $\sim 10^{-14} \text{ cm}^2$
- roton/ ^3He scattering $\sim 10^{-15} \text{ cm}^2$
- ^3He has bound state on surface of $\sim 2 \text{ K}$
- electron forms bubble **19 Å radius**
hydrodynamic mass $\sim 250 m_{\text{He}}$
- positive ion forms “snowball”
mass $\sim 40 m_{\text{He}}$
- metastable triplet excimer forms
bubble **7 Å radius**

alpha signal with calorimeter



collimated α source

roton emission anisotropic

400 Å radius column heated to ~ 2 K

propagate into cold liquid from last scatter

UV energy less than expected (W value 43 eV)

quenching from Penning processes



Bandler, etal, Phys Rev Lett 74, 3169 (1995).

electron signal

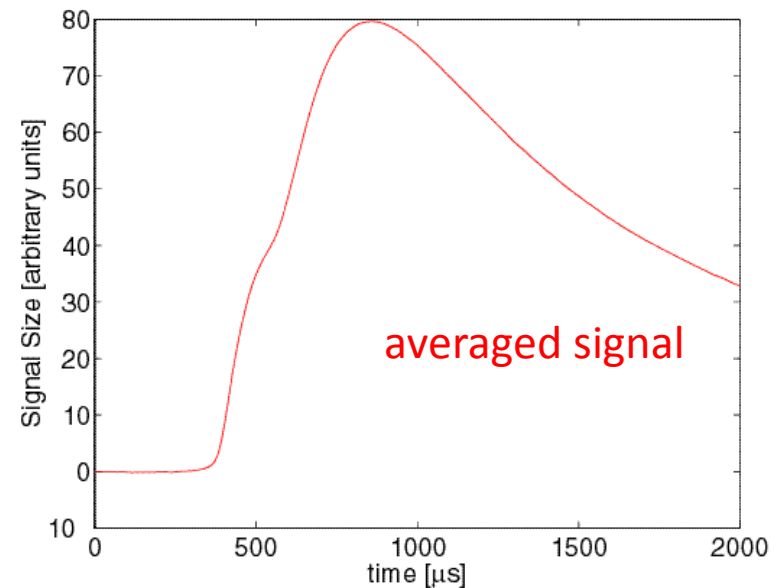
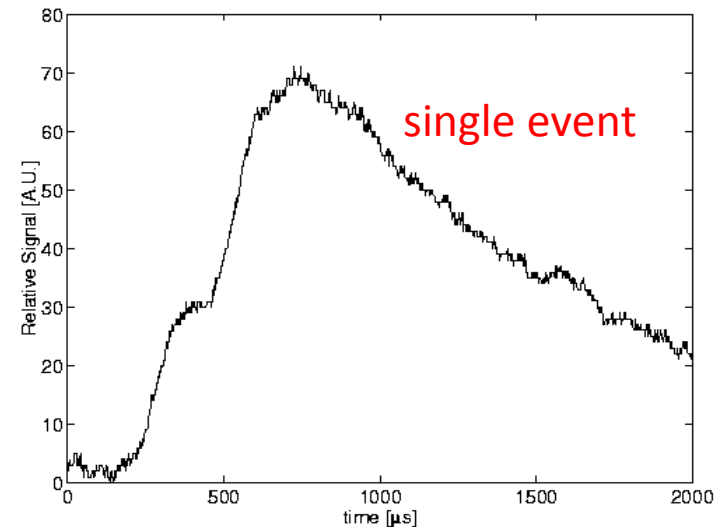
^{113}Sn source, monochromatic 364 keV

scintillation signal greater than predicted
assuming singlet to triplet ratio of 1 to 3

experimentally
ratio of singlet to triplets close to 1 to 1

geminate recombination

Adams, et al , J Low Temp Phys 113, 1121 (1998).
Adams, thesis, Brown University (2000).



energy partition

deposition

detection

ionization

ultraviolet

excitation

triplets

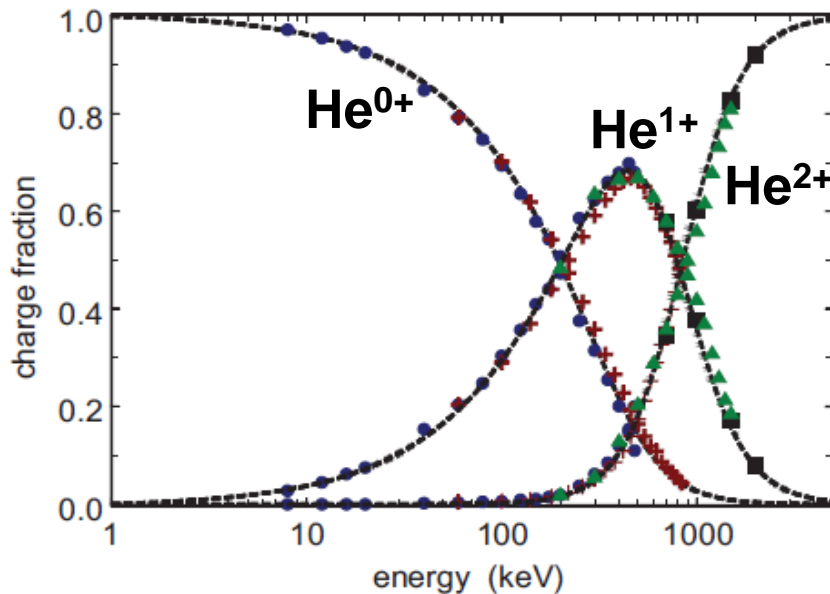
infrared

elastic

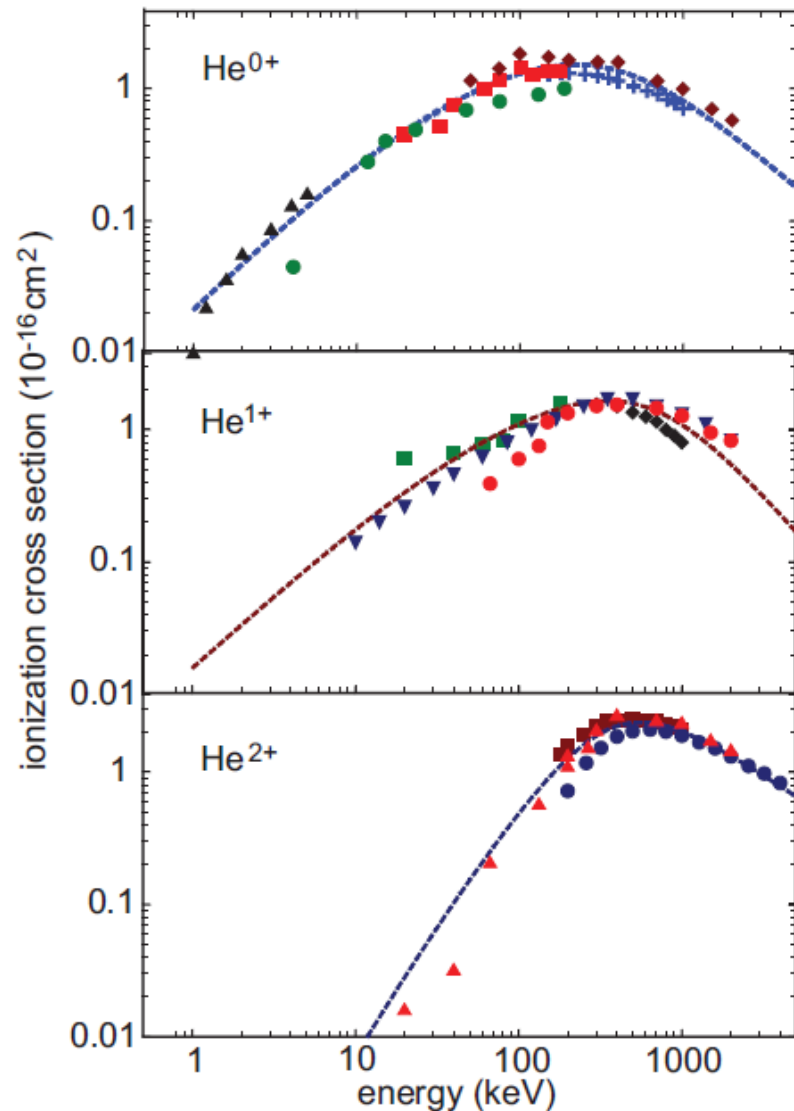
quasiparticles

atomic He/He scattering data

charge state of He atom/ion
cross sections for ionizations and
excitations
other processes
elastic scattering



Ito & Seidel, Phys Rev C 88, 025805 (2013).

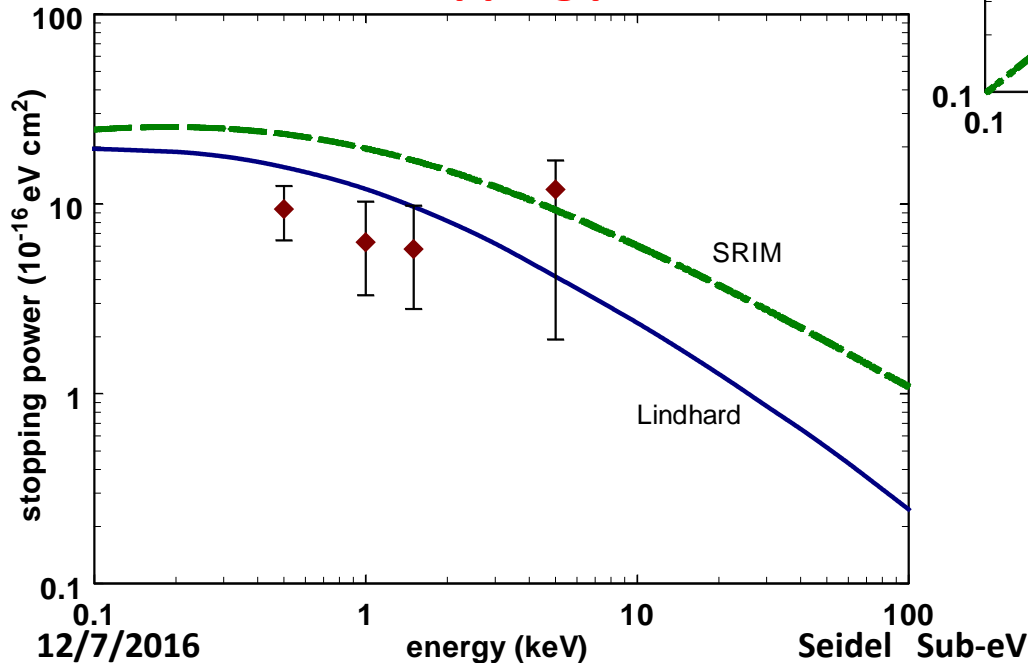


stopping power

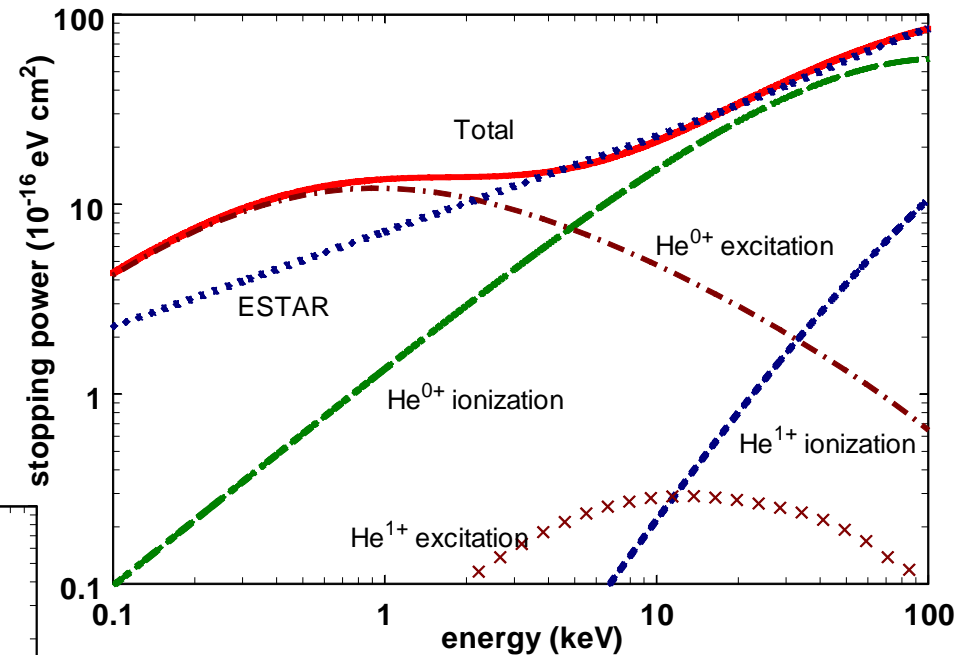
use stopping power as check
to determine if estimates
are consistent

$$SP = \sum_i \sum_j F_i \sigma_{i,j} \varepsilon_{i,j}$$

nuclear stopping power



electronic stopping power



Seidel, to be published.

energy partition

deposition

detection

ionization

ultraviolet

excitation

triplets

elastic

infrared

quasiparticles

for ionization

dimer formation

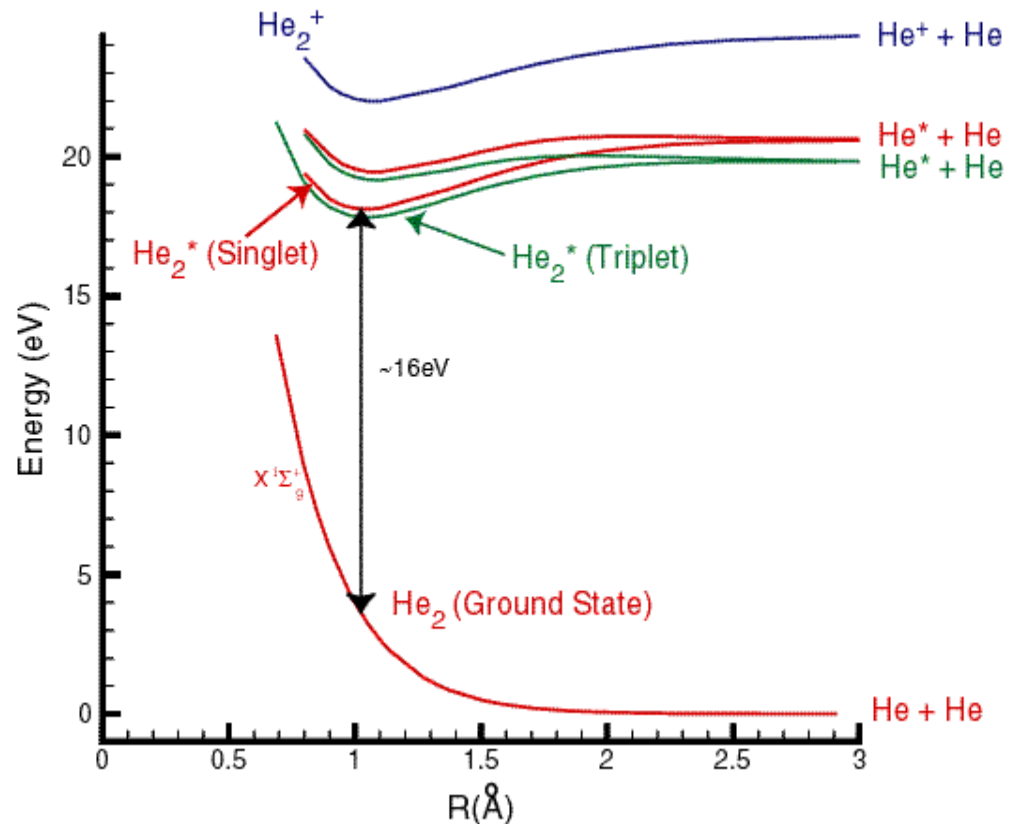
ground state dissociation

secondary electrons

radiative transitions in IR

metastable triplets

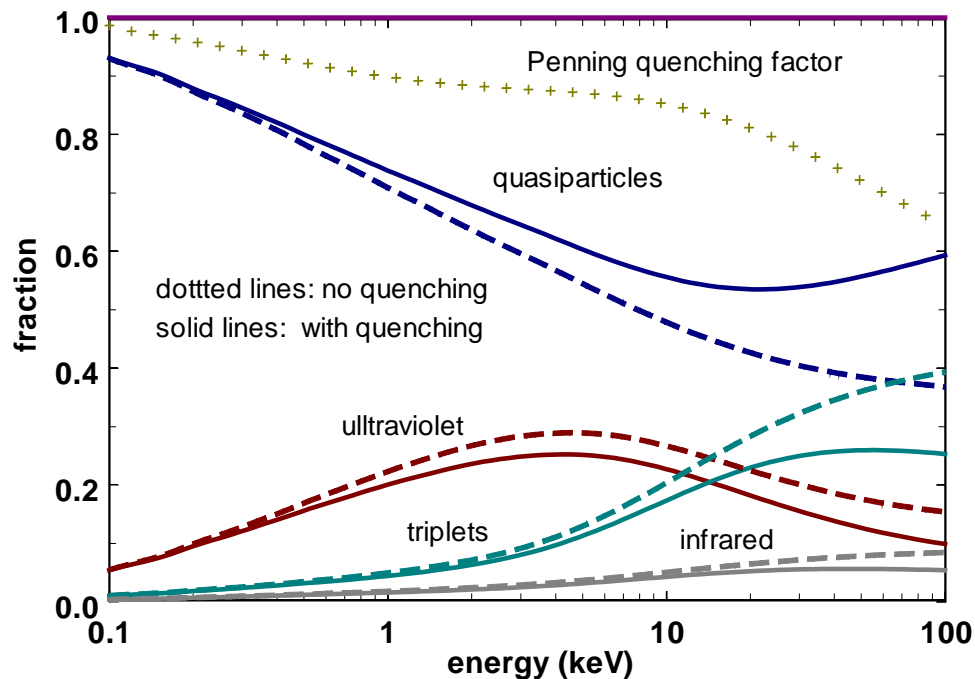
non radiative quenching (Penning)



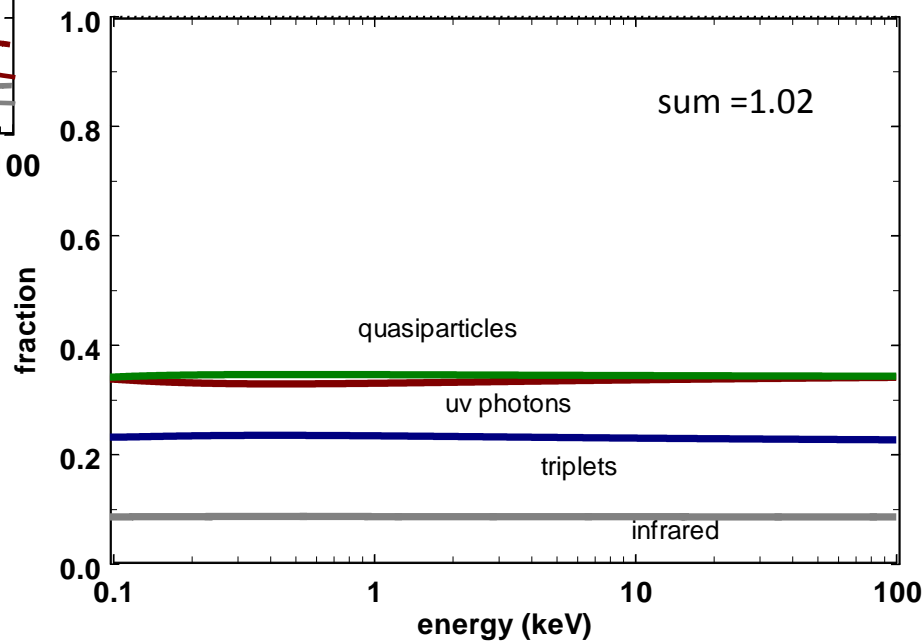
energy partition

nuclear recoil

fraction of energy



electron recoil



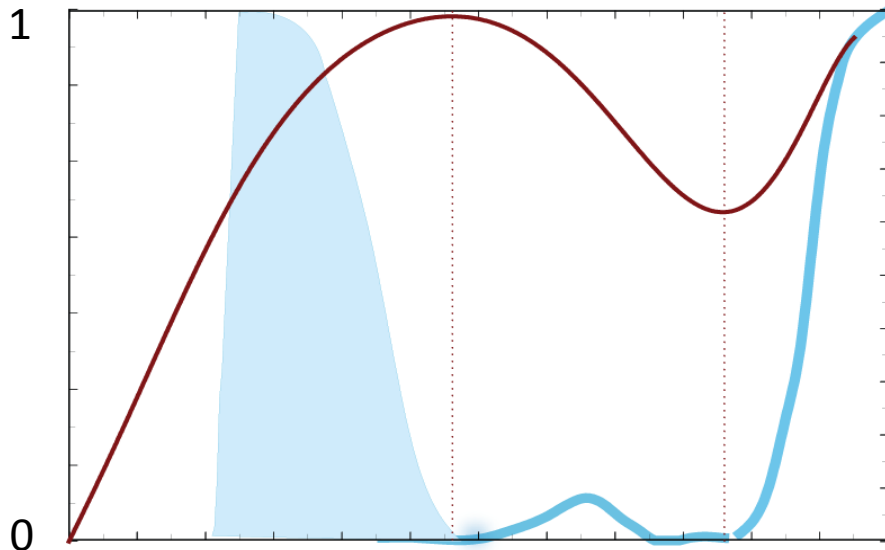
for electrons have at least one ionization or excitation down to 20eV
energy loss in elastic scattering event is very small

evaporation

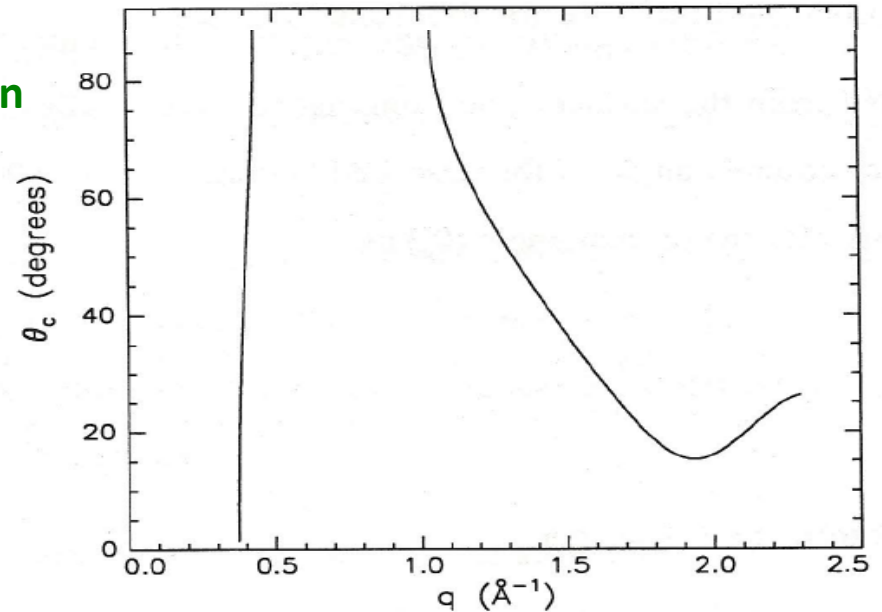
kinematic conditions

$p_{||}$ conserved; $\varepsilon_r = \Phi + p^2/2m_4$
for $\theta > \theta_{\text{critical}}$, have total internal reflection
 $\theta_{\text{critical}} \approx 25^\circ$ for excitations of importance
surface waves (ripplons) not significant

evaporation probability



critical angle



probability high for R^+ rotons away from minimum but critical angle is small

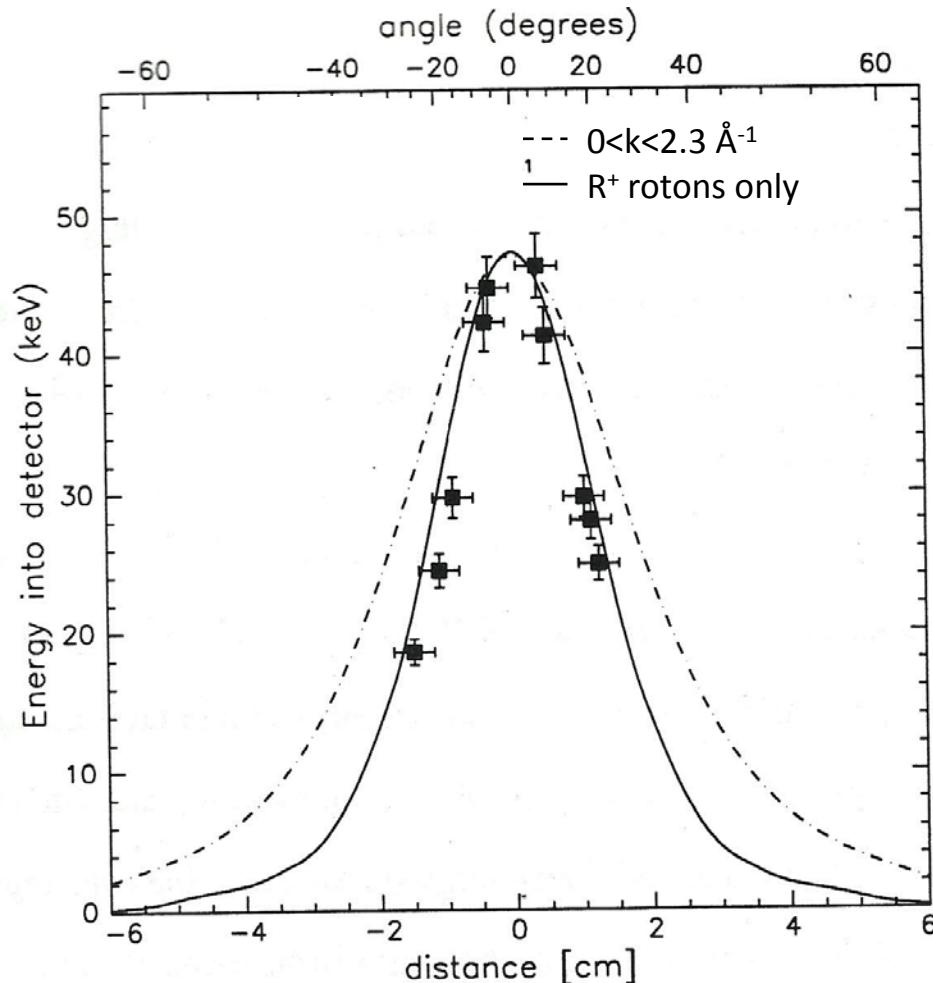
probability low for R^- rotons

probability for phonons depends on angle of incidence

far fewer phonons generated than R^+ rotons

evaporation

angular dependence



measurement of evaporation signal as function of position of source

measurements fit by R^+ rotons only
no need to invoke phonons

25° cone contains 4.8% of solid angle

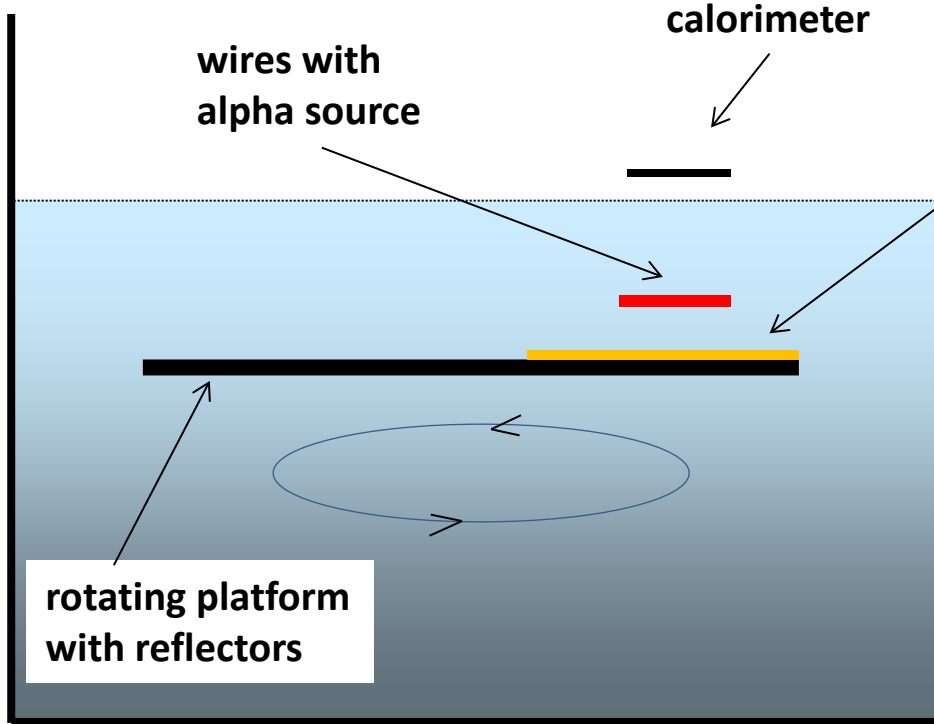
heater results identical

R^+ rotons only excitations of consequence

Enss, etal, Physica B 194, 515(1994).

very rough estimate
50% probability of evaporation

roton reflection from solid surface



reflector
NaF, silicon
brass, sapphire

in separate experiment reflection
determined to be diffuse

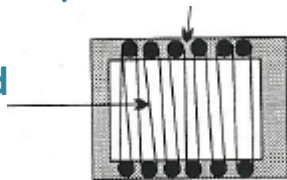
30% reflection as rotons

rotons do not contribute to heat
transfer

Andreev reflection
 R^+ roton reflected
as R^- roton

overhead view of α source evaporated
on underside of 5 and 10 μm wires

wires wrapped around
pins in holder
 $\sim 1000 \mu\text{m}$ spacing



Bandler, thesis, Brown University (1996).

calorimeters

detection of single UV photons and triplet excimers by calorimeters immersed in liquid helium below 100 mK should be possible (certainly true for metallic magnetic calorimeters)

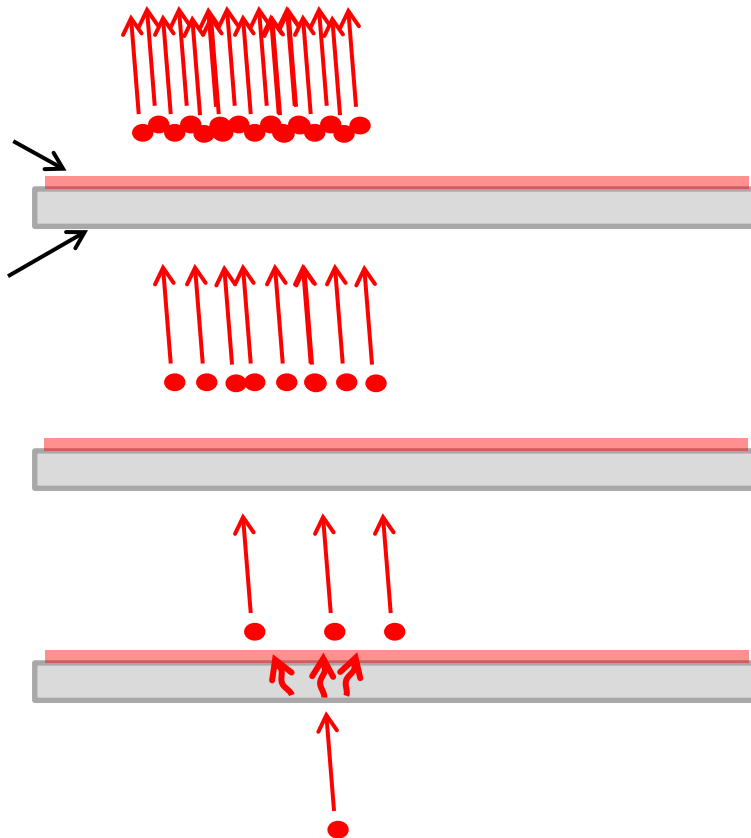
roton detection requires the use of evaporation

development of very low-energy threshold, large-area calorimeters is the principal need for a successful helium-based dark matter detector (alternatively, smaller area with multiplexing)

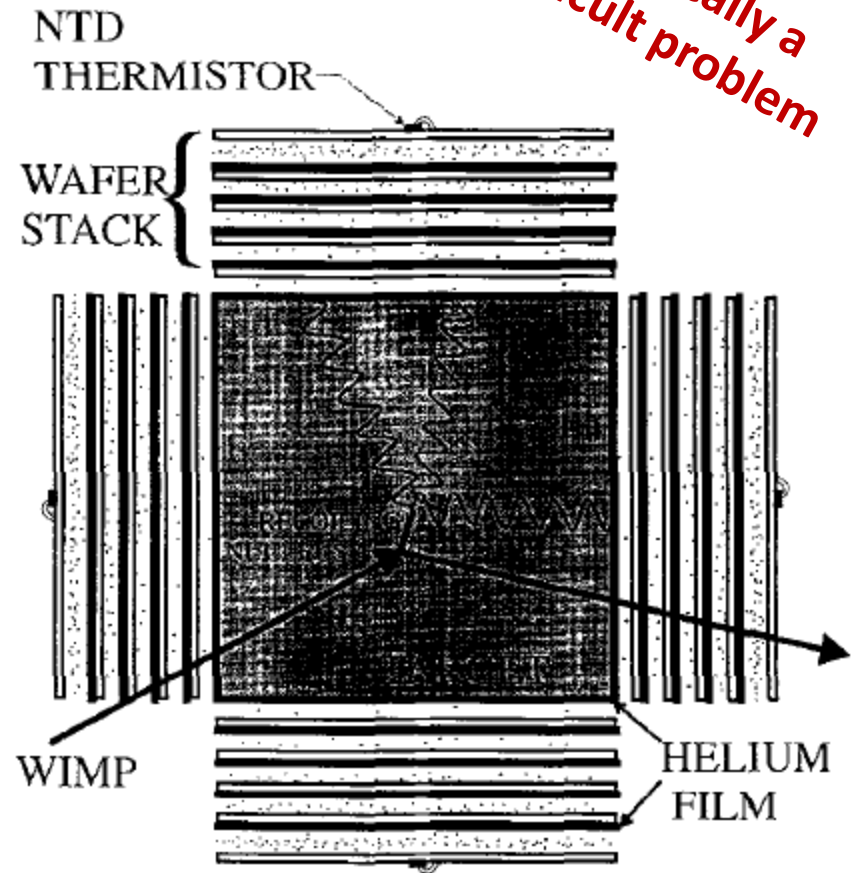
the energy threshold of calorimeters will determine the limit of low dark mass detection

thermal amplification

strong binding substrate on one
side weak binding on the other



bare silicon on one side
He film on other – gain of .2



More, etal, NIM A 370, 147 (1996).
Phys. Rev. B 54, 535 (1996).

other considerations

single electron sensitivity

can move electron to free surface,
extract it from liquid with assistance of vortex ring,
accelerate it in vacuum,
detect it calorimetrically

Sethumadhavan, etal, NIM A 520,142 (2004).

difficulty:

separating electron from positive ion
electron diffuses only $\sim 400 \text{ \AA}$ before forming bubble
high field required to separate charges

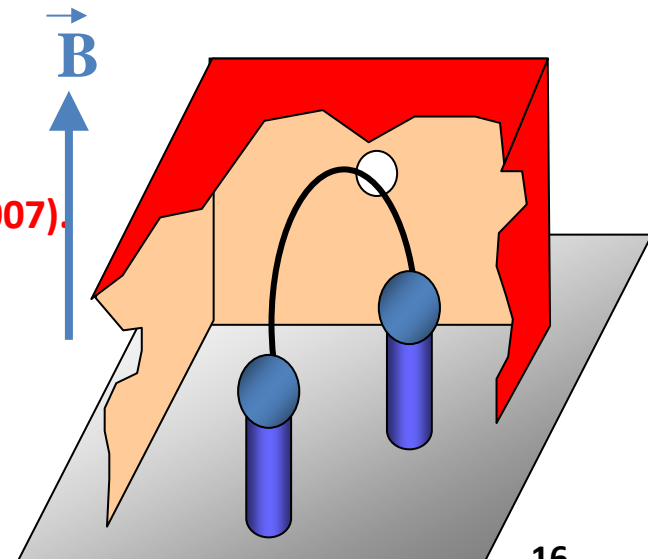
Seidel, etal, Phys. Rev. C 89, 025808 (2014).

quasiparticle detection using a nanomechanical device

example of superfluid ^3He ; vibrating wire,
1 keV threshold

Winkelmann etal, NIM A 574, 264 (2007).

nothing apparent at present that
surpasses calorimetry



comments and conclusions

- better quantitative measurements of properties of helium would be helpful in designing a dark matter detector
- discrimination between nuclear and electron scattering is, in principle, possible with recoil energies down to 20 eV
- quasiparticle detection via evaporation is limited to R^+ rotons
- event location can be determined from evaporation pattern on calorimeter array
- use of quasiparticles reflected from container surfaces may be possible but is problematic
- low eV dark matter detection needs the development of low threshold energy calorimetric detection using large area wafers

back up

charges in liquid helium

electron forms a bubble in liquid helium
energy ~ 1 eV below conduction band
bubble formation not fully understood

$$E = \frac{h^2}{8mR^2} + 4\pi R^2 \sigma + \frac{4\pi}{3} R^3 P$$

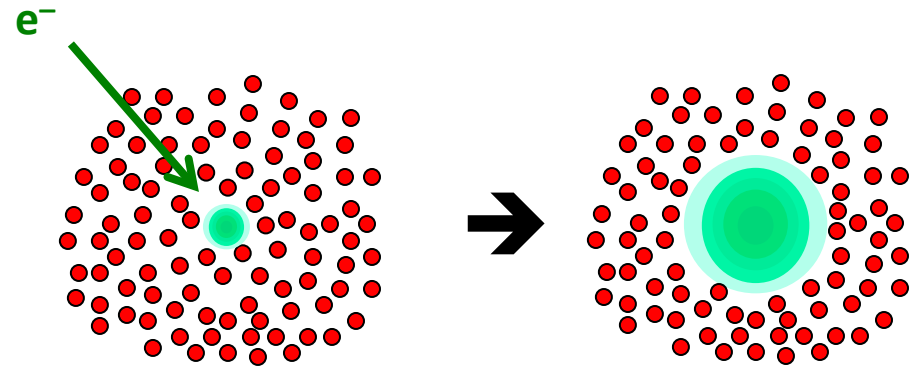
for $P = 0$

$$R = \left(\frac{h^2}{32\pi m \sigma} \right)^{1/4}$$

1s ground state, $R = 19 \text{ \AA}$ displaces ~ 590 He atoms
hydrodynamic mass $\sim 250 m_{\text{He}}$

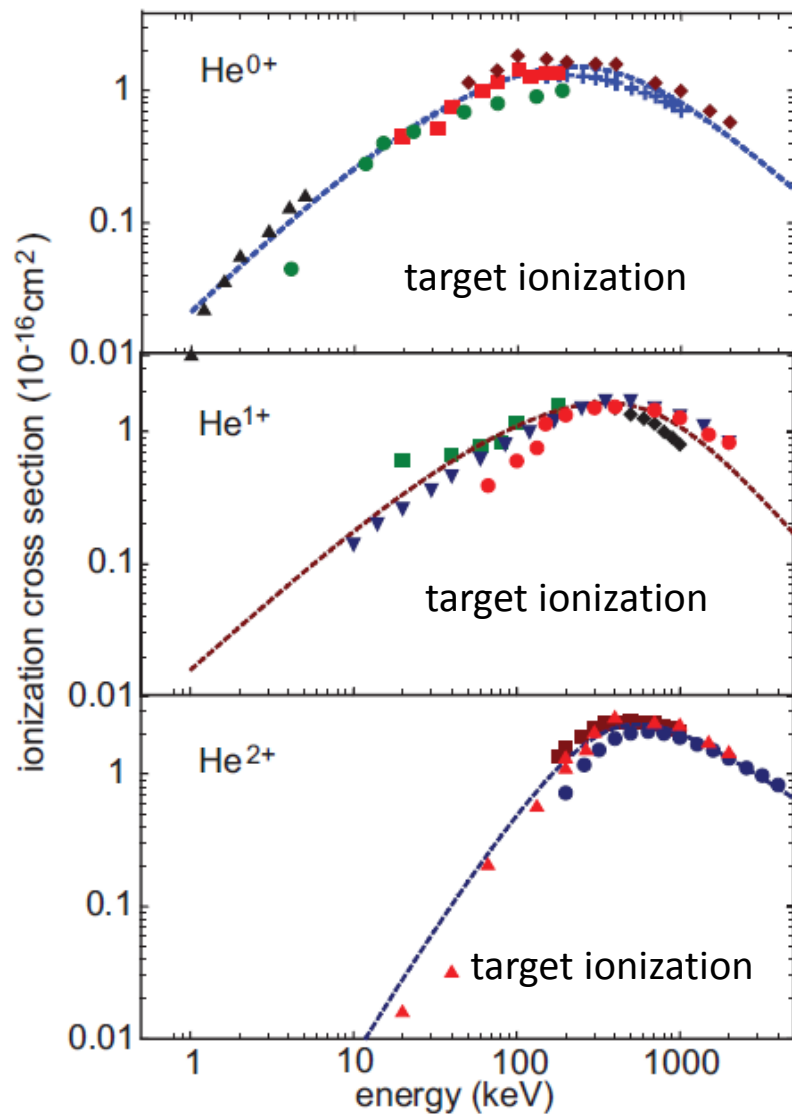
a positive ion is not He_2^+ ;
forms a snowball because of electrostriction

$$R \approx 7 \text{ \AA} \quad m_{\text{snowball}} \approx 40 m_{\text{He}}$$

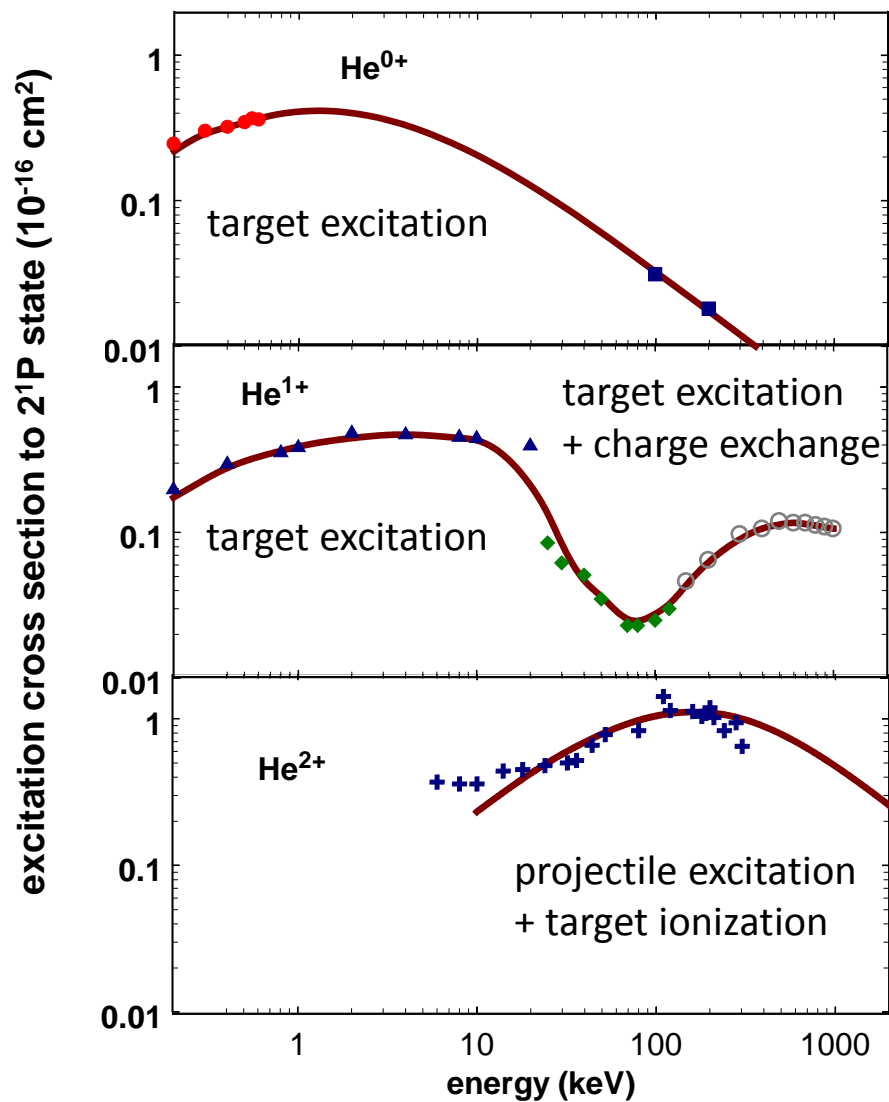


$\text{He}_2^*(a^3\Sigma)$ dimer
forms a bubble,
 $R \approx 7 \text{ \AA}$

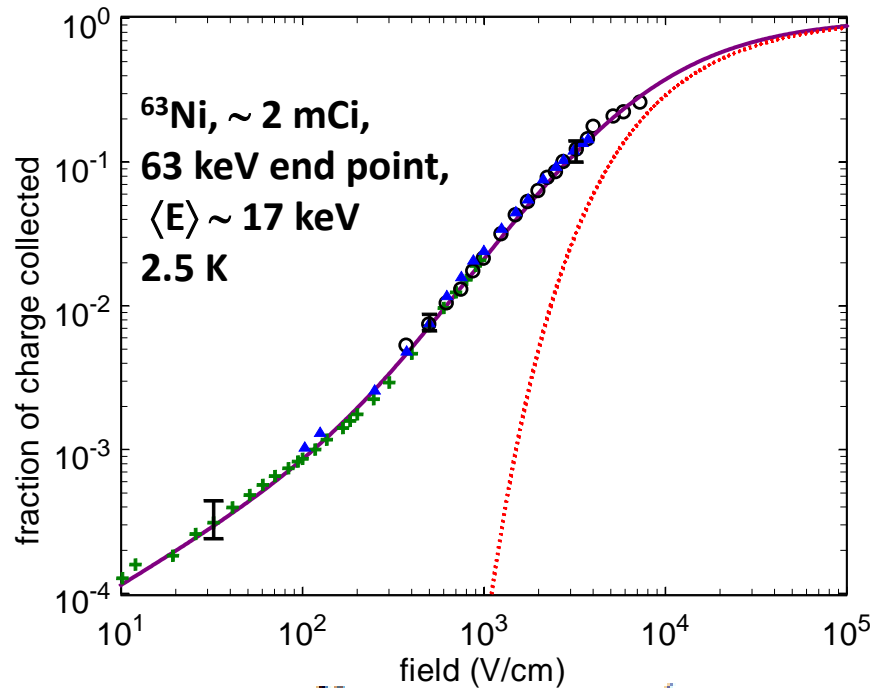
ionization cross section



excitation cross section



current vs field



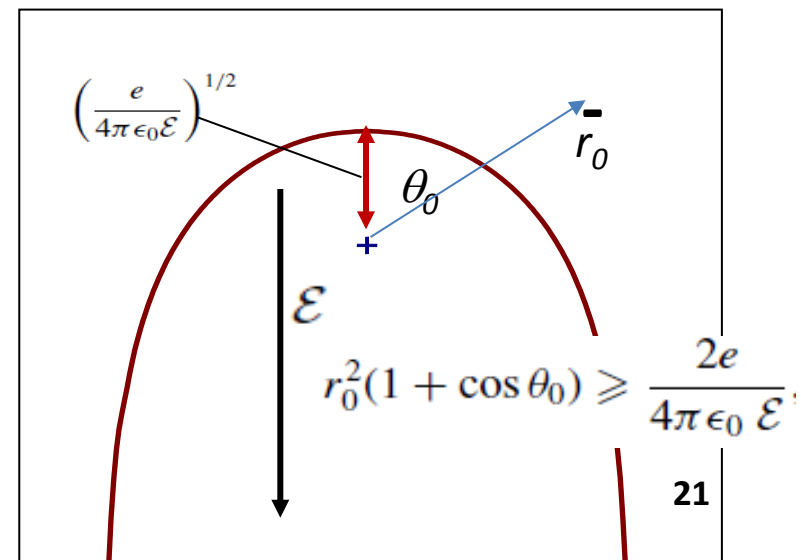
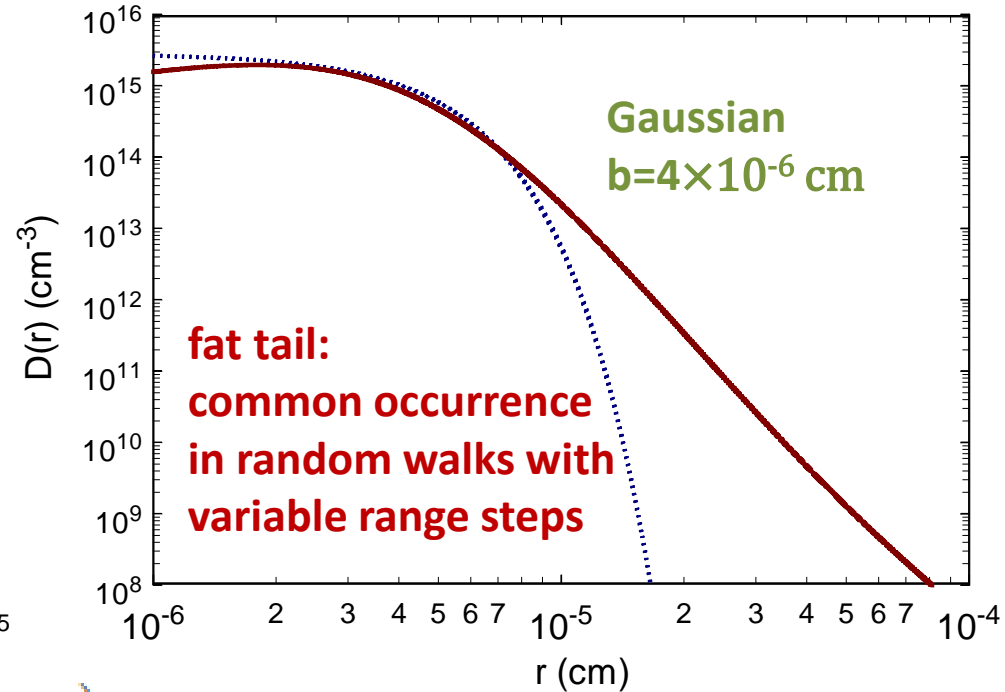
$$i(\mathcal{E}) = 4\pi \int_{(e/4\pi\epsilon_0\mathcal{E})^{1/2}}^{\infty} D(r)r^2 dr \left(1 - \frac{e}{4\pi\epsilon_0\mathcal{E}r^2} \right)$$

$$D(r) = \frac{4\pi^{1/2}\epsilon_0^{3/2}\mathcal{E}^{5/2}}{e^{3/2}} \frac{d}{d\mathcal{E}} \left(i + \mathcal{E} \frac{di}{d\mathcal{E}} \right)$$

where $r = (e/4\pi\epsilon_0\mathcal{E})^{1/2}$

Seidel, et al, Phys. Rev. C 89, 025808 (2014)

density vs distance



elastic scattering of electrons

based on random walk and known cross section for elastic scattering of low energy electrons
expect secondary electrons have Gaussian distribution with half width of $\sim 2000 \text{ \AA}$ rather than 400 \AA as measured

physics of how an electron forms a bubble is not well understood

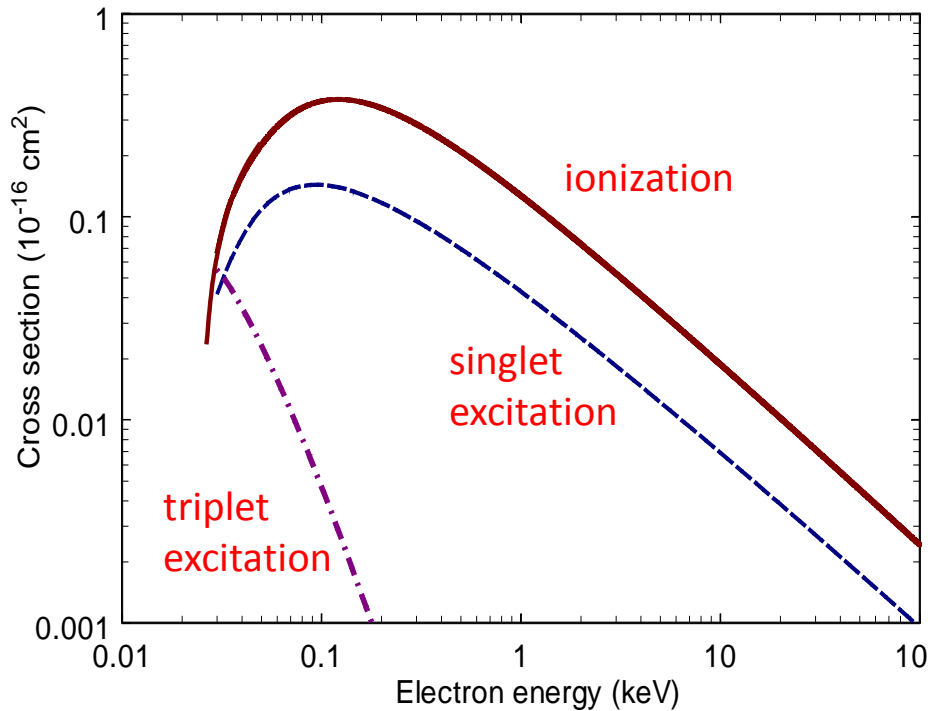
very different electron distribution than for Ar or Xe

determine particle density along track
compute **quenching** from Penning process
assume density is uniform in
cylinder, neglect diffusion

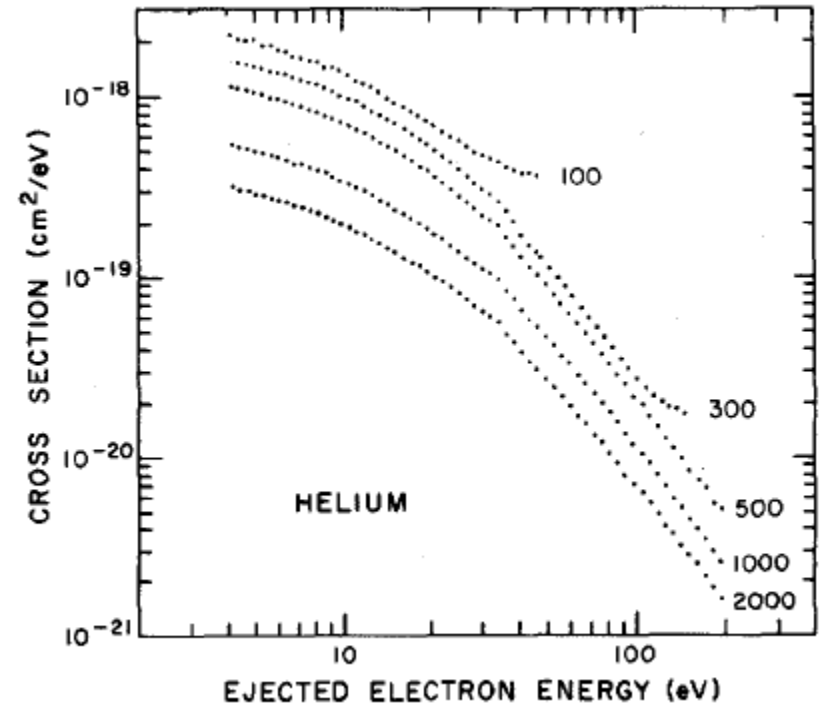
$$\frac{dn}{dt} = -\gamma n^2 - \frac{r n}{\tau}$$

$$\xi = n_0$$

cross sections for electron scattering on helium



energy distribution electron recoils



Ralchenko, etal, At. Data & Nucl. Data Tables 94, 603 (2008).

C. B. Opal, etal, At. Data 4, 209 (1972).

film suppression

burner

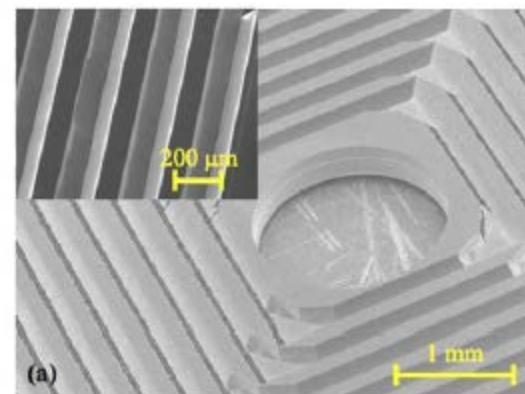
25 mK
300 mK
700 mK

to heat
exchanger
at 300 mK

to mixing
chamber

film
thickness 200 Å
velocity 50 cm/s
heat to evaporate
0.38 mW/cm

knife edge
suppressor



sharp on an atomic scale;
removal of last monolayer
more difficult