Duvall Pinkney WEEK 4 homework: classification Evaluate k-nearest-neighbor method with different k values on the dataset used in Week 03 notebook (Source: https://raw.githubusercontent.com/empathy87/The-Elements-of-Statistical-Learning-Python-Notebooks/master/data/mixture.txt (https://raw.githubusercontent.com/empathy87/The-Elements-of-Statistical-Learning-Python-Notebooks/master/data/mixture.txt)

- 1. Load the data as a Pandas data frame.
- 2. Split the data into 80% training data and 20% test data.
- 3. Build three k-nearest-neighbor model with k = 1, 5, 25, respectively.
- 4. Train the models on the training set, and obtain the model predictions on the test set.
- 5. Calculate the test accuracy score for each model. Which k value give the best accuracy score?

In [51]:

import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
%matplotlib inline

```
In [54]: url = "https://pjreddie.com/media/files/mnist_train.csv"
    train_data = pd.read_csv(url, header=None, sep=',')
    train_data
```

Out[54]:

	0	1	2	3	4	5	6	7	8	9	 775	776	777	778	779	780	781	782	783	784
0	5	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
2	4	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
3	1	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
4	9	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
59995	8	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
59996	3	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
59997	5	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
59998	6	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
59999	8	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0

60000 rows × 785 columns

```
In [55]: url2 = "https://pjreddie.com/media/files/mnist_test.csv"
    test_data = pd.read_csv(url2, header=None, sep=',')
    test_data
```

Out[55]:

	0	1	2	3	4	5	6	7	8	9	 775	776	777	778	779	780	781	782	783	784
0	7	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
1	2	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
2	1	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
4	4	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
9995	2	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
9996	3	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
9997	4	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
9998	5	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0
9999	6	0	0	0	0	0	0	0	0	0	 0	0	0	0	0	0	0	0	0	0

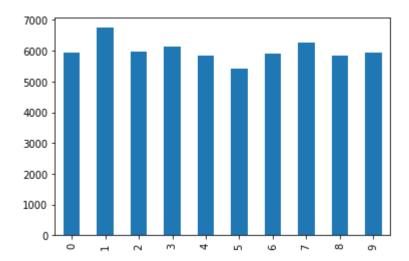
10000 rows × 785 columns

```
In [56]: print("Shape:",test_data.shape)
         print("Columns names", test_data.columns)
         print("Data types: ", test_data.dtypes)
         Shape: (10000, 785)
         Columns names Int64Index([ 0, 1, 2,
                                                  3,
                                                      4, 5, 6, 7, 8, 9,
                    775, 776, 777, 778, 779, 780, 781, 782, 783, 784],
                   dtype='int64', length=785)
         Data types: 0
                            int64
               int64
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         4
                . . .
         780
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         782
               int64
         783
                int64
         784
                int64
         Length: 785, dtype: object
```

```
In [42]: print("Shape:",train data.shape)
         print("Columns names", train data.columns)
         print("Data types: ", train data.dtypes)
         Shape: (59999, 785)
         Columns names Index(['5', '0', '0.1', '0.2', '0.3', '0.4', '0.5', '0.6', '0.7', '0.8',
                 '0.608', '0.609', '0.610', '0.611', '0.612', '0.613', '0.614', '0.615',
                 '0.616', '0.617'],
               dtype='object', length=785)
         Data types: 5
                                int64
         0
                   int64
         0.1
                   int64
         0.2
                  int64
         0.3
                   int64
                   . . .
         0.613
                   int64
         0.614
                  int64
         0.615
                  int64
         0.616
                  int64
         0.617
                  int64
         Length: 785, dtype: object
In [57]: data = train_data.rename({0: 'label'}, axis=1)
         data['label'].value counts().sort index()
Out[57]: 0
              5923
         1
              6742
         2
              5958
              6131
          3
         4
              5842
         5
              5421
         6
              5918
         7
              6265
         8
              5851
              5949
         Name: label, dtype: int64
```

```
In [59]: data['label'].value_counts().sort_index().plot.bar()
```

Out[59]: <matplotlib.axes._subplots.AxesSubplot at 0x1bfa8742a88>



```
In [23]: testing_data = split_train_test(test_data, 0.2)
len(testing_data)
```

Out[23]: 2

```
In [24]: training_data = split_train_test(train_data, 0.8)
len(training_data)
```

Out[24]: 2

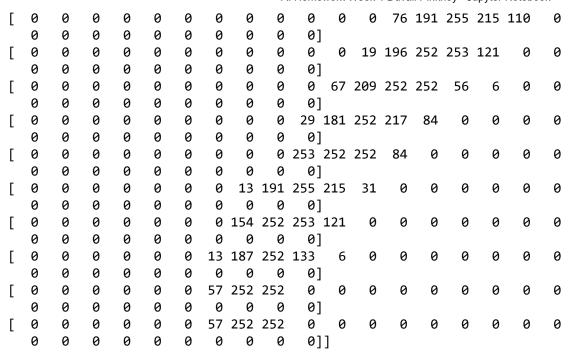
```
In [62]: # Visualize data as images
    ind = 123 # Going to show the image on this row
    input_features = [x for x in data.columns if x != "label"]
    # print(input_features)
    data_example = data.loc[ind, input_features] # Use .loc[] expression to extract data from a data frame.
    print(data_example.shape)

(784,)

In [63]: # Convert the data example to a numpy array
    data_example_array = data_example.values
    print(data_example_array.shape)

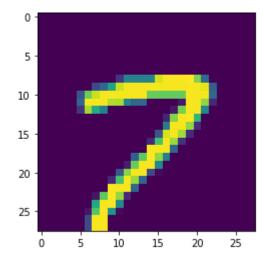
(784,)
```

```
# Transform the array to a 28*28 2D array
In [64]:
          data example array transformed = data example array.reshape([28, 28])
          print(data example array transformed.shape)
          print(data example array transformed)
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```



In [65]: plt.imshow(data_example_array_transformed)

Out[65]: <matplotlib.image.AxesImage at 0x1bfa8bc8b08>



```
In [66]: # Write a function to automate the process
def get_image(data, ind):
    # Use data.loc to extract the 784 pixel values

input_features2 = [column for column in data.columns if column != 'label']
    data_example = data.loc[ind, input_features2]

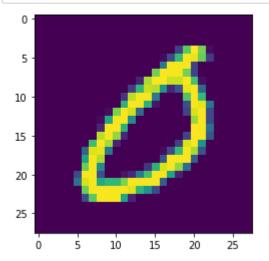
# Convert the List to a numpy array
    data_example_numpyArray = data_example.values

# Change the shape to [28, 28]
    data_example_numpyArray_transformed = data_example_numpyArray.reshape([28,28]))

# Use imshow() to display the image.
    plt.imshow(data_example_numpyArray_transformed)

# return data_example_array_transformed
```



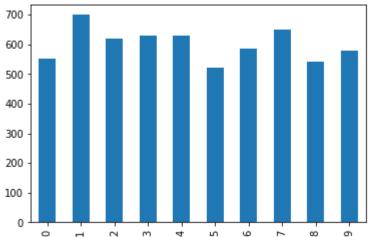


```
In [39]:
         # How to evaluate the kNN model?
         # Visualize the decision region.
         # 1. create a 100 * 100 grid of points to cover the entire plane.
         plot data = pd.DataFrame()
         x1_coordinates = np.linspace(-3, 4, 100) # sample 100 points per row
         x2 coordinates = np.linspace(-2, 3, 100) # sample 100 rows (total: 100 * 100 = 10,000 points)
         for x1 in x1 coordinates:
             for x2 in x2 coordinates:
                 plot_data = plot_data.append({'x1': x1,
                                         'x2': x2},
                                        ignore index=True)
         plot_data
         # 2. use the kNN model to make a prediction on each of the 10,000 points.
         plot data['prediction'] = model 3nn.predict(plot data)
         plot data.head()
```

Out[39]:

	x1	x2
0	-3.0	-2.000000
1	-3.0	-1.949495
2	-3.0	-1.898990
3	-3.0	-1.848485
4	-3.0	-1 797980

```
In [68]: # Create a smaller training set to reduce training time
         sample size = 6000
         samples = np.random.choice(data.index, sample size, replace=False)
         mnist train small = data.loc[samples]
         print(mnist train small.shape)
          (6000, 785)
In [69]: KNeighborsClassifier(algorithm='auto', leaf_size=30, metric='minkowski',
                              metric_params=None, n_jobs=None, n_neighbors=3, p=2,
                              weights='uniform')
Out[69]: KNeighborsClassifier(algorithm='auto', leaf_size=30, metric='minkowski',
                              metric_params=None, n_jobs=None, n_neighbors=3, p=2,
                              weights='uniform')
In [49]: input features = [ x for x in plot data.columns if x != "label"]
In [70]: # Verify mnist train small still contains enough training examples for each label
         mnist train small['label'].value counts().sort index().plot.bar()
Out[70]: <matplotlib.axes. subplots.AxesSubplot at 0x1bfd2036788>
           700
```



```
In [71]: #K nearest neighbor model
         #Build three k-nearest-neighbor model with k = 1, 5, 25
         from sklearn.neighbors import KNeighborsClassifier
         knn = KNeighborsClassifier(n neighbors=1)
         knn.fit(mnist train small[input features], mnist train small['label'])
Out[71]: KNeighborsClassifier(algorithm='auto', leaf size=30, metric='minkowski',
                              metric params=None, n jobs=None, n neighbors=1, p=2,
                              weights='uniform')
In [72]: from sklearn.neighbors import KNeighborsClassifier
         knn = KNeighborsClassifier(n neighbors=5)
         knn.fit(mnist train small[input features], mnist train small['label'])
Out[72]: KNeighborsClassifier(algorithm='auto', leaf_size=30, metric='minkowski',
                              metric params=None, n jobs=None, n neighbors=5, p=2,
                              weights='uniform')
In [73]: from sklearn.neighbors import KNeighborsClassifier
         knn = KNeighborsClassifier(n neighbors=25)
         knn.fit(mnist_train_small[input_features], mnist_train_small['label'])
Out[73]: KNeighborsClassifier(algorithm='auto', leaf size=30, metric='minkowski',
                              metric params=None, n jobs=None, n neighbors=25, p=2,
                              weights='uniform')
 In [ ]:
```

```
In [86]: # Build a linear SVM classifier
         from sklearn.svm import LinearSVC
         model svm = LinearSVC()
         model svm.fit(mnist train small[input_features], mnist_train_small['label'])
         C:\Users\thees\Anaconda3\lib\site-packages\sklearn\svm\base.py:929: ConvergenceWarning: Liblinear failed to co
         nverge, increase the number of iterations.
           "the number of iterations.", ConvergenceWarning)
Out[86]: LinearSVC(C=1.0, class weight=None, dual=True, fit intercept=True,
                   intercept scaling=1, loss='squared hinge', max iter=1000,
                   multi class='ovr', penalty='12', random state=None, tol=0.0001,
                   verbose=0)
In [87]: # Use the model to make predictions on the test images
         test data['prediction svm'] = model svm.predict(test data[input features])
In [88]: # Calculate accuracy score
         accuracy score(test data['label'], test data['prediction svm'])
         NameError
                                                    Traceback (most recent call last)
         <ipython-input-88-03c111e3d8d0> in <module>
               1 # Calculate accuracy score
         ----> 3 accuracy score(test data['label'], test data['prediction svm'])
         NameError: name 'accuracy score' is not defined
```

In [77]: test_data.head()

Out[77]:

	0	1	2	3	4	5	6	7	8	9	•••	775	776	777	778	779	780	781	782	783	784
0	7	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0
1	2	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0
2	1	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0
4	4	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0

5 rows × 785 columns

```
In [85]: # Extract rows that are mis-classified
         filter1 = (test data['label'] != test data['prediction'])
         test data[filter1][['label', 'prediction']]
                                                    Traceback (most recent call last)
         KeyError
         ~\Anaconda3\lib\site-packages\pandas\core\indexes\base.py in get loc(self, key, method, tolerance)
            2896
                              try:
         -> 2897
                                  return self. engine.get loc(key)
            2898
                              except KeyError:
         pandas/ libs/index.pyx in pandas. libs.index.IndexEngine.get loc()
         pandas/ libs/index.pyx in pandas. libs.index.IndexEngine.get loc()
         pandas/ libs/hashtable class helper.pxi in pandas. libs.hashtable.PyObjectHashTable.get item()
         pandas/ libs/hashtable class helper.pxi in pandas. libs.hashtable.PyObjectHashTable.get item()
         KeyError: 'label'
         During handling of the above exception, another exception occurred:
         KeyError
                                                    Traceback (most recent call last)
         <ipython-input-85-167524130096> in <module>
               1 # Extract rows that are mis-classified
               2
         ----> 3 filter1 = (test data['label'] != test data['prediction'])
               4 test data[filter1][['label', 'prediction']]
         ~\Anaconda3\lib\site-packages\pandas\core\frame.py in __getitem__(self, key)
            2993
                              if self.columns.nlevels > 1:
            2994
                                  return self. getitem multilevel(key)
         -> 2995
                              indexer = self.columns.get loc(key)
            2996
                              if is integer(indexer):
            2997
                                  indexer = [indexer]
         ~\Anaconda3\lib\site-packages\pandas\core\indexes\base.py in get loc(self, key, method, tolerance)
            2897
                                  return self._engine.get_loc(key)
            2898
                              except KeyError:
         -> 2899
                                  return self. engine.get loc(self. maybe cast indexer(key))
```

```
indexer = self.get_indexer([key], method=method, tolerance=tolerance)
if indexer.ndim > 1 or indexer.size > 1:

pandas/_libs/index.pyx in pandas._libs.index.IndexEngine.get_loc()

pandas/_libs/index.pyx in pandas._libs.index.IndexEngine.get_loc()

pandas/_libs/hashtable_class_helper.pxi in pandas._libs.hashtable.PyObjectHashTable.get_item()

pandas/_libs/hashtable_class_helper.pxi in pandas._libs.hashtable.PyObjectHashTable.get_item()

KeyError: 'label'
```

```
In [79]: # Show one image that is incorrectly classified
         # Create a copy of test data without the prediction and prediction svm column
         test data2 = test data.drop(['prediction', 'prediction sym'], axis=1)
         ind = 9922
         get image(test data2, ind)
         KeyError
                                                    Traceback (most recent call last)
         <ipython-input-79-5adc46439460> in <module>
               3 # Create a copy of test data without the prediction and prediction svm column
         ----> 4 test data2 = test data.drop(['prediction', 'prediction sym'], axis=1)
                5
               6 \text{ ind} = 9922
         ~\Anaconda3\lib\site-packages\pandas\core\frame.py in drop(self, labels, axis, index, columns, level, inpla
         ce, errors)
            4115
                              level=level.
                              inplace=inplace,
             4116
         -> 4117
                              errors=errors,
            4118
                          )
            4119
         ~\Anaconda3\lib\site-packages\pandas\core\generic.py in drop(self, labels, axis, index, columns, level, inp
         lace, errors)
             3912
                          for axis, labels in axes.items():
             3913
                              if labels is not None:
                                  obj = obj. drop axis(labels, axis, level=level, errors=errors)
         -> 3914
             3915
             3916
                          if inplace:
         ~\Anaconda3\lib\site-packages\pandas\core\generic.py in drop axis(self, labels, axis, level, errors)
             3944
                                  new axis = axis.drop(labels, level=level, errors=errors)
             3945
                              else:
         -> 3946
                                  new axis = axis.drop(labels, errors=errors)
             3947
                              result = self.reindex(**{axis name: new axis})
             3948
         ~\Anaconda3\lib\site-packages\pandas\core\indexes\base.py in drop(self, labels, errors)
             5338
                          if mask.any():
```

```
if errors != "ignore":
raise KeyError("{} not found in axis".format(labels[mask]))
indexer = indexer[~mask]
return self.delete(indexer)

KeyError: "['prediction' 'prediction_svm'] not found in axis"
```

```
In [76]: # Show the label and the prediction of this image
         print("Label:", test data.loc[ind, 'label'])
         print("Prediction by kNN:", test data.loc[ind, 'prediction'])
         KeyError
                                                    Traceback (most recent call last)
         ~\Anaconda3\lib\site-packages\pandas\core\indexes\base.py in get loc(self, key, method, tolerance)
            2896
         -> 2897
                                  return self. engine.get loc(key)
            2898
                              except KeyError:
         pandas/ libs/index.pyx in pandas._libs.index.IndexEngine.get_loc()
         pandas/ libs/index.pyx in pandas. libs.index.IndexEngine.get loc()
         pandas/ libs/index class helper.pxi in pandas. libs.index.Int64Engine. check type()
         KeyError: 'label'
         During handling of the above exception, another exception occurred:
         KeyError
                                                    Traceback (most recent call last)
         <ipython-input-76-5fe95549b521> in <module>
               1 # Show the label and the prediction of this image
         ----> 2 print("Label:", test data.loc[ind, 'label'])
               3 print("Prediction by kNN:", test data.loc[ind, 'prediction'])
         ~\Anaconda3\lib\site-packages\pandas\core\indexing.py in getitem (self, key)
            1416
                                  except (KeyError, IndexError, AttributeError):
            1417
                                      pass
                              return self._getitem_tuple(key)
         -> 1418
            1419
                         else:
            1420
                             # we by definition only have the 0th axis
         ~\Anaconda3\lib\site-packages\pandas\core\indexing.py in getitem tuple(self, tup)
             803
                     def _getitem_tuple(self, tup):
             804
                         try:
         --> 805
                              return self. getitem lowerdim(tup)
                         except IndexingError:
             806
             807
                              pass
         ~\Anaconda3\lib\site-packages\pandas\core\indexing.py in getitem lowerdim(self, tup)
```

```
959
                            return section
    960
                        # This is an elided recursive call to iloc/loc/etc'
                        return getattr(section, self.name)[new key]
--> 961
    962
                raise IndexingError("not applicable")
    963
~\Anaconda3\lib\site-packages\pandas\core\indexing.py in getitem (self, key)
   1422
   1423
                    maybe callable = com.apply if callable(key, self.obj)
-> 1424
                    return self. getitem axis(maybe callable, axis=axis)
   1425
   1426
            def is scalar access(self, key: Tuple):
~\Anaconda3\lib\site-packages\pandas\core\indexing.py in _getitem_axis(self, key, axis)
                # fall thru to straight lookup
   1848
                self. validate_key(key, axis)
   1849
-> 1850
                return self. get label(key, axis=axis)
   1851
   1852
~\Anaconda3\lib\site-packages\pandas\core\indexing.py in get label(self, label, axis)
    154
                    # but will fail when the index is not present
    155
                    # see GH5667
                    return self.obj. xs(label, axis=axis)
--> 156
                elif isinstance(label, tuple) and isinstance(label[axis], slice):
    157
                    raise IndexingError("no slices here, handle elsewhere")
    158
~\Anaconda3\lib\site-packages\pandas\core\generic.py in xs(self, key, axis, level, drop level)
                    loc, new index = self.index.get loc level(key, drop level=drop level)
   3735
   3736
                else:
-> 3737
                    loc = self.index.get loc(key)
   3738
   3739
                    if isinstance(loc, np.ndarray):
~\Anaconda3\lib\site-packages\pandas\core\indexes\base.py in get loc(self, key, method, tolerance)
                        return self._engine.get_loc(key)
   2897
   2898
                    except KeyError:
-> 2899
                        return self. engine.get loc(self. maybe cast indexer(key))
   2900
                indexer = self.get indexer([key], method=method, tolerance=tolerance)
                if indexer.ndim > 1 or indexer.size > 1:
   2901
pandas/ libs/index.pyx in pandas. libs.index.IndexEngine.get loc()
```

```
pandas/_libs/index.pyx in pandas._libs.index.IndexEngine.get_loc()

pandas/_libs/index_class_helper.pxi in pandas._libs.index.Int64Engine._check_type()

KeyError: 'label'
In []:
```