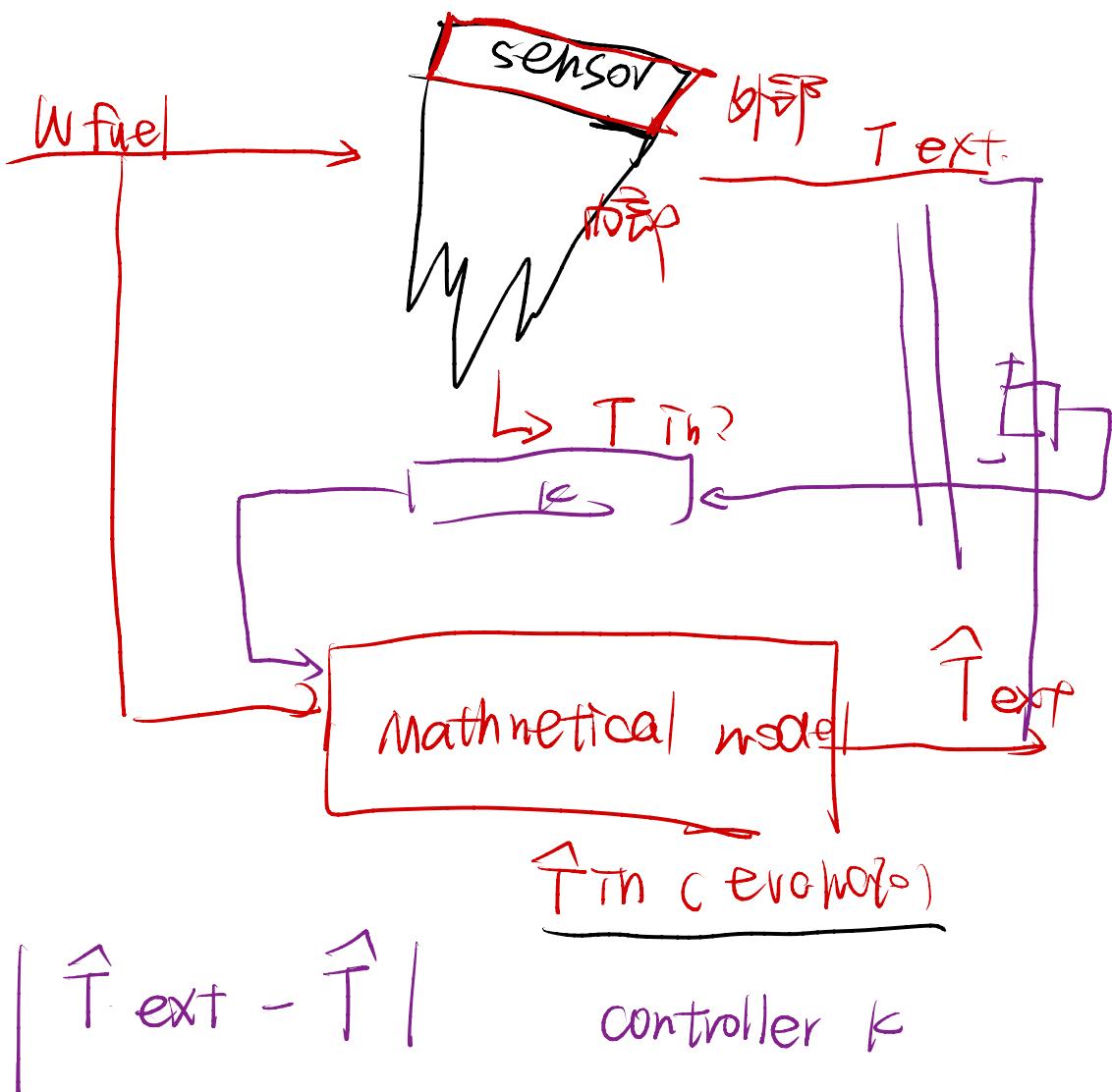


Kalman filter



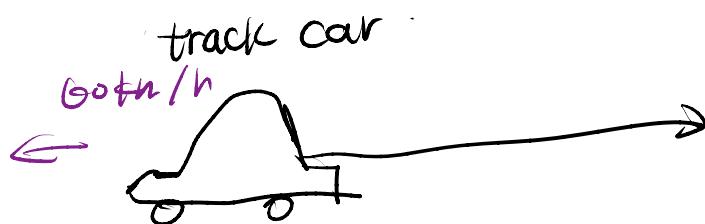
什何什

Example



Detailed part

$\dot{x} \rightarrow \text{speed}$



$$\dot{x}_{t+1} = 1 \cdot x_t + \delta t \cdot \dot{x}_t$$

$$\dot{x}_{t+1} = 0 \cdot x_t + 1 \cdot \dot{x}_t$$

$$\begin{bmatrix} x_{t+1} \\ \dot{x}_{t+1} \end{bmatrix} = \begin{bmatrix} 1 & \delta t \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x_t \\ \dot{x}_t \end{bmatrix}$$

Predict $x_1 \in (0, 8, 1)$

$$\bar{x}_1 < 60$$

yellow blue

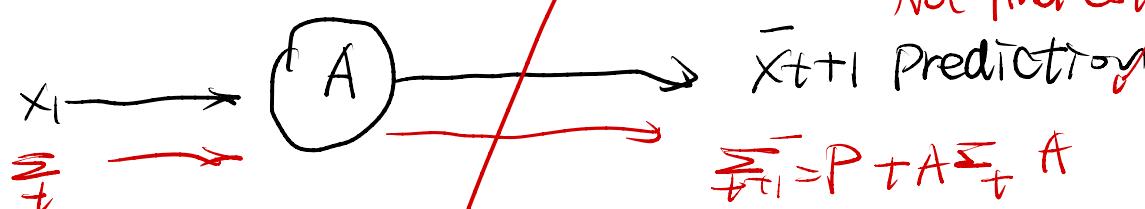
$$x_{t+1} = Ax_t + u \quad u \sim N(0, P)$$

$u \sim N(0, P)$ 随机误差

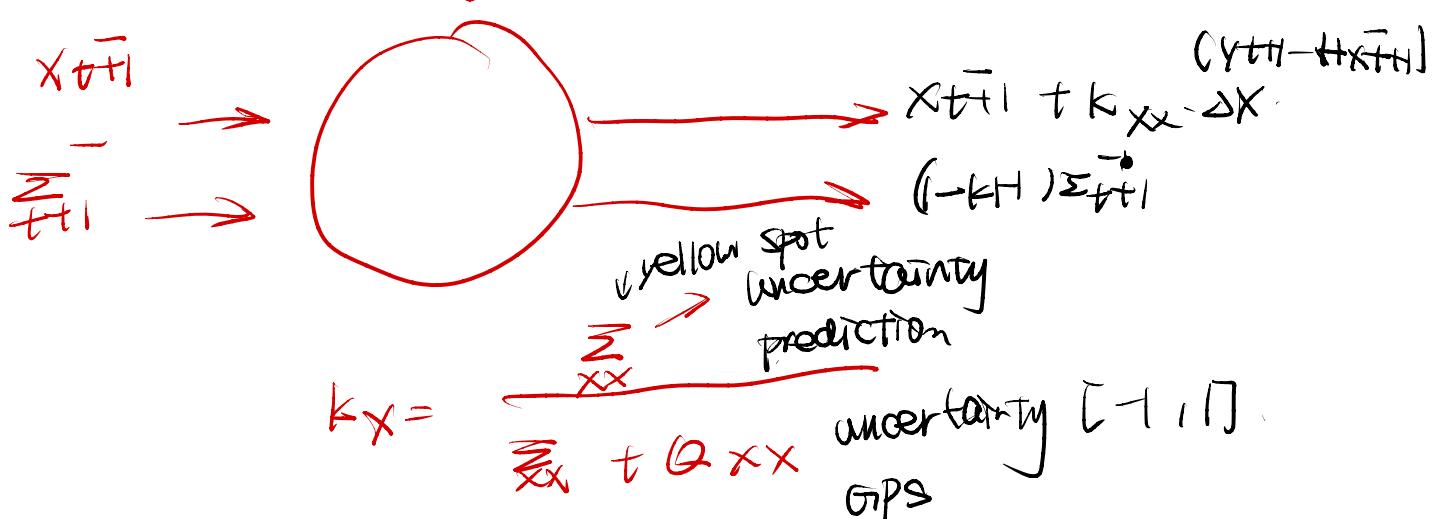
$$y_t = Hx_t + v \quad v \sim N(0, Q)$$

$$H \in \mathbb{R}^{1 \times 3}$$

Prediction step



update step



$$\dot{\bar{x}}_{t+1}^+ = \dot{\bar{x}}_{t+1}^- + k_x \Delta x$$

$$k_x = \frac{\sum \bar{x}_i \cdot \dot{\bar{x}}_i}{\sum \bar{x}_i^2 + Q_{xx}}$$

Independent \Rightarrow useless

① measurement situation function

<u>estimate of current</u>	Predicted of current	k_{xx} ↓ Factor	Predicted of current
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$$\hat{x}_k = \hat{x}_{k-1} + k_k (z_k - H_k \hat{x}_k) \xrightarrow{\text{真实 measurement}}$$

② predict state

$$\hat{x}_k = F_k \hat{x}_{k-1} + B_k u_k$$

↓ 状态演化
 ↓ control by u_k
 ↓ 系统噪声

③ covariance prediction

Initial one	$\text{cov}(x_i, \bar{x}_j) = \frac{1}{m-1} \sum_{k=1}^m (x_{ik} - \bar{x}_i)(x_{jk} - \bar{x}_j)$
$P_k = F_k P_{k-1} F_k^T + Q_k$ <small>状态噪声</small>	<small>测量噪声</small>

④ k_x

$$k_k = P_k H_k^T (H_k P_k H_k^T + R_k)^{-1}$$

state estimation uncertainty = $\frac{P_k H_k^T}{H_k P_k H_k^T + R_k} \rightarrow$ measurement uncertainty

5. state update

$$P_k = (I - K_k H_k) P_k$$

Extended Kalman Filter (EKF)

Quite same non-linear

1. Prediction step:

state

$$\hat{x}_k = f(x_{k-1}, u_k) + \hat{e}_k$$

covariance:

$$P_k = F_k P_{k-1} F_k^T + Q_k$$

2. Measurement update

M P

$$z_k = h(\hat{x}_k)$$

Kalman Gain

$$K_k = P_k H_k^T (H_k P_k H_k^T + R_k)^{-1}$$

State Update

$$\hat{x}_k = \hat{x}_k + K_k (z_k - h(\hat{x}_k))$$

Covariance Update

$$P_k = (I - K_k H_k) P_k$$