Writing Bayesian Hierarchical Models

ESS 575 Models for Ecological Data

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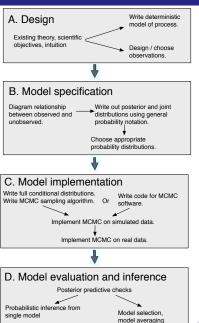
What is this course about?



All modeling problems have idiosyncrasies

- Sampling error in the predictors or responses
- Calibration error for predictors or responses
- Prior knowledge of parameters
- Missing data
- Multiple scales of data (group level effects)
- Prediction and forecasting
- Spatial or temporal dependence
- Derived quantities

The Bayesian method



Cross cutting theme

Things to watch for today

- Sampling error in x's
- Calibration error in y's
- Treatment effects
- Derived quantities
- Group level effects

All of these will appear in the exercises you do next week.

Things to watch for today

Partitioning uncertainty

- Process variance
- Sampling variance
- Calibration variance (aka observation variance)

Steps in writing Bayesian models

- 1. Write your deterministic model.
- 2. Draw Bayesian network (DAG) describing relationships between observed and unobserved quantities.
- 3. Use the Bayesian network to write proportionality between posterior and joint distributions using bracket notation [|].
 - 3.1 Posterior distribution: [unobserved quantities | data]
 - 3.2 Joint distribution
 - 3.2.1 All nodes in Bayesian network at the heads of arrows (children) must be on the left hand side of a conditioning symbol |.
 - 3.2.2 All nodes in Bayesian network at the tails of arrows (parents) must be on the right hand side of a conditioning symbol |.
 - 3.2.3 All nodes at the end of an arrow with no arrow coming into them must be expressed unconditionally, i.e., they must have numeric arguments.
- 4. Assign specific PDF or PMF to each of the brackets.
- 5. Choose numeric values for parameters of prior distributions