

***pandas* for Analytics Practitioners, with Applications in Optimization**

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Question

- You're working to apply optimization to a new problem
- Do you spend more time
 - Dealing with the data
 - Reading it in, organizing it for optimization, etc.
 - Writing your model
 - Tuning the optimizer's performance

What is Python?

- From Wikipedia:
 - **Python** is a widely used high-level, general-purpose, interpreted, dynamic programming language. Its design philosophy emphasizes code readability, and its syntax allows programmers to express concepts in fewer lines of code than would be possible in languages such as C++ or Java. The language provides constructs intended to enable clear programs on both a small and large scale. ^[27]
 - Python supports multiple programming paradigms, including object-oriented, imperative and functional programming or procedural styles. It features a dynamic type system and automatic memory management and has a large and comprehensive standard library.

What is pandas?

- From pandas.pydata.org:
 - *pandas* is an open source, BSD-licensed library providing high-performance, easy-to-use data structures and data analysis tools for the [Python](#) programming language.
- Library Highlights
 - A fast and efficient **DataFrame** object for data manipulation with integrated indexing;
 - Tools for **reading and writing data** between in-memory data structures and different formats: CSV and text files, Microsoft Excel, SQL databases, and the fast HDF5 format;
 - Intelligent **data alignment** and integrated handling of **missing data**: gain automatic label-based alignment in computations and easily manipulate messy data into an orderly form;
 - Flexible **reshaping** and pivoting of data sets;
 - Intelligent label-based **slicing**, **fancy indexing**, and **subsetting** of large data sets;
 - Columns can be inserted and deleted from data structures for **size mutability**;
 - Aggregating or transforming data with a powerful **group by** engine allowing split-apply-combine operations on data sets;
 - High performance **merging and joining** of data sets;
- Note: Examples in this presentation require pandas v0.20 or later

Outline

- Tidy Data
- pandas Fundamentals
- Reading Data
- Creating New Columns
- Analyzing data
- Reshaping Data
- Merging/joining
- GroupBy
- Optimization

Tidy Data – Defined for Statistics

- "Tidy data is a standard way of mapping the meaning of a dataset to its structure. A dataset is messy or tidy depending on how rows, columns and tables are matched up with observations, variables and types. In tidy data:
 1. Each variable forms a column.
 2. Each observation forms a row.
 3. Each type of observational unit forms a table."
- Hadley Wickham, "Tidy Data", Journal of Statistical Software, Volume 59(10), August 2014.
<https://www.jstatsoft.org/article/view/v059i10/v59i10.pdf>

Tidy and Untidy Data in Optimization (1)

- Untidy data from AMPL
(steelT.*):

```
set PROD;      # products
param T > 0;    # number of weeks
param revenue {PROD,1..T} >= 0;
param market {PROD,1..T} >= 0;

param T := 4;
set PROD := bands coils;
param revenue:  1      2      3      4 :=
    bands    25     26     27     27
    coils    30     35     37     39 ;
param market:  1      2      3      4 :=
    bands   6000   6000   4000   6500
    coils   4000   2500   3500   4200 ;
```

- Tidy form:

		market	revenue
PROD	T		
bands	1	6000	25
coils	1	4000	30
bands	2	6000	26
coils	2	2500	35
bands	3	4000	27
coils	3	3500	37
bands	4	6500	27
coils	4	4200	39

Tidy and Untidy Data in Optimization (2)

• Untidy data from OPL (knapsack.*)

```
int NbItems = ...;
int NbResources = ...;
range Items = 1..NbItems;
range Resources = 1..NbResources;
int Use[Resources][Items] = ...;

NbResources = 7;
NbItems = 12;
Use = [
    [ 19, 1, 10, 1, 1, 14, 152, 11, 1, 1, 1, 1 ],
    [ 0, 4, 53, 0, 0, 80, 0, 4, 5, 0, 0, 0 ],
    [ 4, 660, 3, 0, 30, 0, 3, 0, 4, 90, 0, 0 ],
    [ 7, 0, 18, 6, 770, 330, 7, 0, 0, 6, 0, 0 ],
    [ 0, 20, 0, 4, 52, 3, 0, 0, 0, 5, 4, 0 ],
    [ 0, 0, 40, 70, 4, 63, 0, 0, 60, 0, 4, 0 ],
    [ 0, 32, 0, 0, 0, 5, 0, 3, 0, 660, 0, 9 ]];
```

• Tidy Form:

		Use
Resources	Items	
R1	I1	19
	I10	1
	I11	1
	I12	1
	I2	1
	I3	10
	I4	1
...	I5	1
	I6	14
	I7	152

	I3	40
	I4	70
	I5	4
R6	I6	63
	I9	60
R7	I10	660
	I12	9
	I2	32
	I6	5
	I8	3

Tidy Data – Defined for Optimization

- Wickham Definition for Statistics:

"Tidy data is a standard way of mapping the meaning of a dataset to its structure. A dataset is messy or tidy depending on how rows, columns and tables are matched up with **observations**, **variables** and types. In tidy data:

1. Each **variable** forms a column.
2. Each **observation** forms a row.
3. Each type of **observational unit** forms a table."

- Lustig Definition for Optimization:

Tidy data is a standard way of mapping the meaning of a dataset to its structure. A dataset is messy or tidy depending on how rows, columns and tables are matched up with **records**, **parameters** and types. In tidy data:

1. Each **parameter** forms a column.
2. Each **record** forms a row.
3. Each type of **data unit sharing an index** forms a table.
4. **A MultiIndex of each record implicitly defines multiple sets**

Example of a Table in Tidy Data

		market	revenue
PROD	T		
bands	1	6000	25
coils	1	4000	30
bands	2	6000	26
coils	2	2500	35
bands	3	4000	27
coils	3	3500	37
bands	4	6500	27
coils	4	4200	39

Parameters

1. Each **parameter** forms a column.
2. Each **record** forms a row.
3. Each type of **data unit sharing an index** forms a table.
4. A **MultIndex** of each record implicitly defines multiple sets

MultIndex

('bands', 1)
('coils', 1)
('bands', 2)
('coils', 2)
('bands', 3)
('coils', 3)
('bands', 4)
('coils', 4)

PROD = ['bands', 'coils']

T = [1, 2, 3, 4]

Tidy Data Read Into Pandas

- `tidysteel.csv`

```
PROD,T,market,revenue  
bands,1,6000,25  
coils,1,4000,30  
bands,2,6000,26  
coils,2,2500,35  
bands,3,4000,27  
coils,3,3500,37  
bands,4,6500,27  
coils,4,4200,39
```



`01.tidysteel.ipynb`

pandas Fundamentals



pandas Series

- Essentially a vector of values (or objects)
- Indexed sequentially (default) and possibly by a specified set of labels

- Examples

- Create a simple series, which will get indexed sequentially

- ```
s1 = pd.Series([3,1,4,1,5,9,2,6])
```

- Get a specific element: `s1[5]`

- Create a series indexed by letters in the alphabet.

- ```
s2 = pd.Series([0.1*i for i in range(10)],  
               index=list(string.ascii_uppercase)[:10])
```

- Get a specific element: `s2['F']`

- Create a series of random numbers, indexed by a MultiIndex.

- ```
s3 = pd.Series(np.random.randn(6),
 index=pd.MultiIndex
 .from_product([['A','B'],
 [4,5,6]]))
```

- Get a specific element: `s3['B',5]`



02.Series.ipynb

# Indexing for Series

- A simple index can be built from any list
  - This is called indexing by label
  - Duplicate labels are allowed, but be careful!
- You can pick slices of the index
- Examples
  - Get a mid-sequence of elements  
`s1[2:4]`
  - Get elements from one point to the end  
`s2['G':]`
  - Get elements up to a specific point  
`s2[:'C']`
  - Use integer index to get values from label indexed Series  
`s2[5:8]`
  - Get specified subset of rows  
`s2[['B', 'E', 'G']]`

# Avoiding Ambiguity with integer Index

- If the index is integer, and not sequential, then referring to specific elements can be ambiguous
  - Use `.loc` or `.iloc` instead
    - `.loc` uses the labels for indexing
    - `.iloc` uses the positional index (row number)

- Example

```
s4 = pd.Series([10*i for i in range(10)],
 index=[10-i for i in range(10)])
```

- What is `s4[8]` ???
  - pandas will return 20

`s4.loc[8]` is 20

`s4.iloc[8]` is 80

|    |    |
|----|----|
| 10 | 0  |
| 9  | 10 |
| 8  | 20 |
| 7  | 30 |
| 6  | 40 |
| 5  | 50 |
| 4  | 60 |
| 3  | 70 |
| 2  | 80 |
| 1  | 90 |

# Multindex

- An index with dimension, consisting of levels
- Think of it as a set of tuples
- Three equivalent ways of creating a MultiIndex

```
mi1 = pd.MultiIndex
 .from_product([['a','b','c'], [1,2]])

mi2 = pd.MultiIndex
 .from_tuples([('a', 1), ('a', 2), ('b', 1),
 ('b', 2), ('c', 1), ('c', 2)])

mi3 = pd.MultiIndex
 .from_arrays([['a','a','b','b','c','c'],
 [1,2,1,2,1,2]])
```



03.Multindex.ipynb

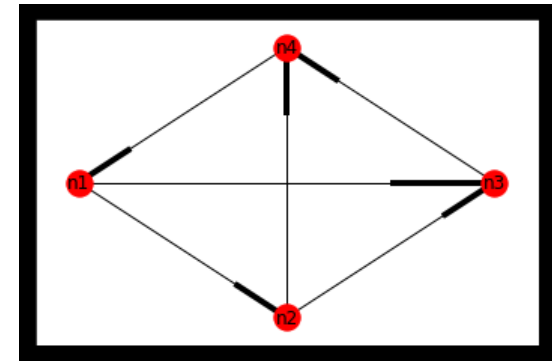


# Slices with MultiIndex

| Code                                                              | Result                                                                                                                                                                                                                                                          | Description |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
|-------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|---|---|---|---------------------------------------|---|--------------------------------------|---|---|---|---|---|---|---|---|------------------------------------------------------|
| <code>s1 = pd.Series(<br/>    range(6),<br/>    index=mi1)</code> | <table><tr><td rowspan="2">a</td><td>1</td><td>0</td></tr><tr><td>2</td><td>1</td></tr><tr><td rowspan="2">b</td><td>1</td><td>2</td></tr><tr><td>2</td><td>3</td></tr><tr><td rowspan="2">c</td><td>1</td><td>4</td></tr><tr><td>2</td><td>5</td></tr></table> | a           | 1 | 0 | 2 | 1                                     | b | 1                                    | 2 | 2 | 3 | c | 1 | 4 | 2 | 5 | Create the series, using the MultiIndex as the index |
| a                                                                 | 1                                                                                                                                                                                                                                                               |             | 0 |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
|                                                                   | 2                                                                                                                                                                                                                                                               | 1           |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| b                                                                 | 1                                                                                                                                                                                                                                                               | 2           |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
|                                                                   | 2                                                                                                                                                                                                                                                               | 3           |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| c                                                                 | 1                                                                                                                                                                                                                                                               | 4           |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
|                                                                   | 2                                                                                                                                                                                                                                                               | 5           |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| <code>s1['a']</code>                                              | <table><tr><td>1</td><td>0</td></tr><tr><td>2</td><td>1</td></tr></table>                                                                                                                                                                                       | 1           | 0 | 2 | 1 | Get all rows where first label is 'a' |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| 1                                                                 | 0                                                                                                                                                                                                                                                               |             |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| 2                                                                 | 1                                                                                                                                                                                                                                                               |             |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| <code>s1[:,2]</code>                                              | <table><tr><td>a</td><td>1</td></tr><tr><td>b</td><td>3</td></tr><tr><td>c</td><td>5</td></tr></table>                                                                                                                                                          | a           | 1 | b | 3 | c                                     | 5 | Get all rows where second label is 2 |   |   |   |   |   |   |   |   |                                                      |
| a                                                                 | 1                                                                                                                                                                                                                                                               |             |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| b                                                                 | 3                                                                                                                                                                                                                                                               |             |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |
| c                                                                 | 5                                                                                                                                                                                                                                                               |             |   |   |   |                                       |   |                                      |   |   |   |   |   |   |   |   |                                                      |

# Network Application

```
mi4 = pd.MultiIndex.from_tuples(
 [('n1','n2'),('n1','n3'),
 ('n2','n4'),('n3','n4'),
 ('n2','n3'),('n4','n1')],
 names=['from','to'])
```



| Code                                                    | Result                                                                                                                                                                                                                                                                 | Description |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
|---------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------|----|----|----|----------------------|----|----|---|----|----|---|----|----|---|----|----|---|----------------------------------------------------|
| <pre>s4 = pd.Series(     range(6),     index=mi4)</pre> | <table><tr><td rowspan="2">n1</td><td>n2</td><td>0</td></tr><tr><td>n3</td><td>1</td></tr><tr><td>n2</td><td>n4</td><td>2</td></tr><tr><td>n3</td><td>n4</td><td>3</td></tr><tr><td>n2</td><td>n3</td><td>4</td></tr><tr><td>n4</td><td>n1</td><td>5</td></tr></table> | n1          | n2 | 0  | n3 | 1                    | n2 | n4 | 2 | n3 | n4 | 3 | n2 | n3 | 4 | n4 | n1 | 5 | Create a series indexed by the arc (from,to) pairs |
| n1                                                      | n2                                                                                                                                                                                                                                                                     |             | 0  |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
|                                                         | n3                                                                                                                                                                                                                                                                     | 1           |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n2                                                      | n4                                                                                                                                                                                                                                                                     | 2           |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n3                                                      | n4                                                                                                                                                                                                                                                                     | 3           |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n2                                                      | n3                                                                                                                                                                                                                                                                     | 4           |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n4                                                      | n1                                                                                                                                                                                                                                                                     | 5           |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| <pre>s4['n1']</pre>                                     | <table><tr><td>n2</td><td>0</td></tr><tr><td>n3</td><td>1</td></tr></table>                                                                                                                                                                                            | n2          | 0  | n3 | 1  | Get all arcs from n1 |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n2                                                      | 0                                                                                                                                                                                                                                                                      |             |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n3                                                      | 1                                                                                                                                                                                                                                                                      |             |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| <pre>s4['n2']</pre>                                     | <table><tr><td>n4</td><td>2</td></tr><tr><td>n3</td><td>4</td></tr></table>                                                                                                                                                                                            | n4          | 2  | n3 | 4  | Get all arcs from n2 |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n4                                                      | 2                                                                                                                                                                                                                                                                      |             |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n3                                                      | 4                                                                                                                                                                                                                                                                      |             |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| <pre>s4[:, 'n3']</pre>                                  | <table><tr><td>n1</td><td>1</td></tr><tr><td>n2</td><td>4</td></tr></table>                                                                                                                                                                                            | n1          | 1  | n2 | 4  | Get all arcs into n3 |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n1                                                      | 1                                                                                                                                                                                                                                                                      |             |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |
| n2                                                      | 4                                                                                                                                                                                                                                                                      |             |    |    |    |                      |    |    |   |    |    |   |    |    |   |    |    |   |                                                    |

# DataFrame

- A pandas DataFrame is a table. Each column is a Series, and each Series is sharing the same Index/MultiIndex

| Specify Each Column (Series)                                                                                                                                                                                                                                                                                                                                                                                                                               | Specify Each Row (Record)                                                                                                             |       |       |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------|-------|-------|------|------|----|--|--|----|----|---|---|----|-----|----|----|----|-----|----|----|----|-----|----|----|----|-----|----|----|----|-----|----|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|------|-------|------|----|--|--|----|----|---|---|----|----|-----|----|----|----|-----|----|----|----|-----|----|----|----|-----|----|----|----|-----|
| <pre>df1 = pd.DataFrame(<br/>{ 'cost': [10*i for i in range(6)],<br/>  'bound': [100*i for i in range(6)]<br/>},<br/>  index=mi4)</pre>                                                                                                                                                                                                                                                                                                                    | <pre>df2 = pd.DataFrame.from_records(<br/>  [(10*i, 100*i) for i in range(6)],<br/>  columns=['cost','bound'],<br/>  index=mi4)</pre> |       |       |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| <table><tr><th></th><th></th><th>bound</th><th>cost</th></tr><tr><th>from</th><th>to</th><td></td><td></td></tr><tr><td rowspan="2">n1</td><td>n2</td><td>0</td><td>0</td></tr><tr><td>n3</td><td>100</td><td>10</td></tr><tr><td>n2</td><td>n4</td><td>200</td><td>20</td></tr><tr><td>n3</td><td>n4</td><td>300</td><td>30</td></tr><tr><td>n2</td><td>n3</td><td>400</td><td>40</td></tr><tr><td>n4</td><td>n1</td><td>500</td><td>50</td></tr></table> |                                                                                                                                       |       | bound | cost | from | to |  |  | n1 | n2 | 0 | 0 | n3 | 100 | 10 | n2 | n4 | 200 | 20 | n3 | n4 | 300 | 30 | n2 | n3 | 400 | 40 | n4 | n1 | 500 | 50 | <table><tr><th></th><th></th><th>cost</th><th>bound</th></tr><tr><th>from</th><th>to</th><td></td><td></td></tr><tr><td rowspan="2">n1</td><td>n2</td><td>0</td><td>0</td></tr><tr><td>n3</td><td>10</td><td>100</td></tr><tr><td>n2</td><td>n4</td><td>20</td><td>200</td></tr><tr><td>n3</td><td>n4</td><td>30</td><td>300</td></tr><tr><td>n2</td><td>n3</td><td>40</td><td>400</td></tr><tr><td>n4</td><td>n1</td><td>50</td><td>500</td></tr></table> |  |  | cost | bound | from | to |  |  | n1 | n2 | 0 | 0 | n3 | 10 | 100 | n2 | n4 | 20 | 200 | n3 | n4 | 30 | 300 | n2 | n3 | 40 | 400 | n4 | n1 | 50 | 500 |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                                                                                                                                       | bound | cost  |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| from                                                                                                                                                                                                                                                                                                                                                                                                                                                       | to                                                                                                                                    |       |       |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n1                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n2                                                                                                                                    | 0     | 0     |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                            | n3                                                                                                                                    | 100   | 10    |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n2                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n4                                                                                                                                    | 200   | 20    |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n3                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n4                                                                                                                                    | 300   | 30    |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n2                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n3                                                                                                                                    | 400   | 40    |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n4                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n1                                                                                                                                    | 500   | 50    |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                                                                                                                                       | cost  | bound |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| from                                                                                                                                                                                                                                                                                                                                                                                                                                                       | to                                                                                                                                    |       |       |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n1                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n2                                                                                                                                    | 0     | 0     |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                            | n3                                                                                                                                    | 10    | 100   |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n2                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n4                                                                                                                                    | 20    | 200   |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n3                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n4                                                                                                                                    | 30    | 300   |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n2                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n3                                                                                                                                    | 40    | 400   |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |
| n4                                                                                                                                                                                                                                                                                                                                                                                                                                                         | n1                                                                                                                                    | 50    | 500   |      |      |    |  |  |    |    |   |   |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |                                                                                                                                                                                                                                                                                                                                                                                                                                                            |  |  |      |       |      |    |  |  |    |    |   |   |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |    |    |    |     |

Q: Anything interesting about these 2 results?

# Indexing for DataFrames

- You can get an individual column in one of two ways

`df1.cost`

`df1['cost']`

- Because of the second method, getting a subset of the rows is trickier



04.DataFrame.ipynb

# Indexing Options and Errors

| Doesn't work                  | Error reported                                                  | Works                                      |
|-------------------------------|-----------------------------------------------------------------|--------------------------------------------|
| <code>df1['n1']</code>        | <code>KeyError: 'n1'</code>                                     | <code>df1.loc['n1']</code>                 |
| <code>df1['n1',:]</code>      | <code>TypeError: unhashable type: 'slice'</code>                | <code>df1.loc['n1',:]</code>               |
| <code>df1.loc[:, 'n3']</code> | <code>KeyError: 'the label [n3] is not in the [columns]'</code> | <code>df1.loc[('n1', 'n3'), 'cost']</code> |

- Solution for general slicing

`idx=pd.IndexSlice`

|                                            |                                                                                                                       |                                    |
|--------------------------------------------|-----------------------------------------------------------------------------------------------------------------------|------------------------------------|
| <code>df1.loc[idx[:, 'n3'], 'cost']</code> | <code>KeyError: 'MultiIndex Slicing requires the index to be fully lexsorted tuple len (2), lexsort depth (0)'</code> | <code>df1.loc[idx['n1', :]]</code> |
|--------------------------------------------|-----------------------------------------------------------------------------------------------------------------------|------------------------------------|

- Sort the index

`dfs = df1.sort_index()` # Make new DataFrame

`df1.sort_index(inplace=True)` # Same DataFrame

|                                    |                                                                 |                                            |
|------------------------------------|-----------------------------------------------------------------|--------------------------------------------|
| <code>dfs.loc[idx[:, 'n3']]</code> | <code>KeyError: 'the label [n3] is not in the [columns]'</code> | <code>dfs.loc[idx[:, 'n3'], 'cost']</code> |
|------------------------------------|-----------------------------------------------------------------|--------------------------------------------|

# DataFrame Indexing Recommendations

- Get one column

```
df1.cost
```

- Get more than one column

```
df1[['cost', 'bound']]
```

- To get a slice of rows, use `IndexSlice` and sort the index.

```
idx = pd.IndexSlice
```

```
df1.sort_index(inplace=True)
```

- Use `.loc` and specify the columns

```
df1.loc[idx[:, 'n3'], 'cost']
```

```
df1.loc[idx[:, 'n3'], :]
```

- Or pick a column (it becomes a Series) and avoid `.loc`

```
df1.cost['n1', :]
```

```
df1.cost[:, 'n3']
```

# Reading Data into DataFrames



# CSV and Excel Files

- pandas `read_csv()` and `read_excel()` functions have lots of options
- Default for CSV: `df = pd.read_csv('myfile.csv')`
  - Assume a comma separator
  - Assume there is a header row defining column names
  - Creates a sequential index for the DataFrame
  - Uses all columns and all rows
- Default for Excel: `df = pd.read_excel('myfile.xlsx')`
  - Read the first sheet in the workbook
  - Assume the first row contains names of columns
  - Creates a sequential index for the DataFrame
  - Uses all columns and rows that have values
    - Be careful with a sheet that has extraneous data!
- Various parameters allow you to override the default behaviors



# Read CSV Data Into Pandas

- **tidysteel.csv**

PROD,T,market,revenue

bands,1,6000,25

coils,1,4000,30

bands,2,6000,26

coils,2,2500,35

bands,3,4000,27

coils,3,3500,37

bands,4,6500,27

coils,4,4200,39



01.tidysteel.ipynb

```
mrdf = pd.read_csv('01.tidysteel.csv',
 index_col=[0,1])
```

|       |   | market | revenue |
|-------|---|--------|---------|
| PROD  | T |        |         |
| bands | 1 | 6000   | 25      |
| coils | 1 | 4000   | 30      |
| bands | 2 | 6000   | 26      |
| coils | 2 | 2500   | 35      |
| bands | 3 | 4000   | 27      |
| coils | 3 | 3500   | 37      |
| bands | 4 | 6500   | 27      |
| coils | 4 | 4200   | 39      |

# Read Database Data into pandas

- Consider a MySQL table called "gas" in a schema called "pandas"

| name    | demand | price | octane | lead |
|---------|--------|-------|--------|------|
| Super   | 3000.0 | 70.0  | 10.0   | 1.0  |
| Regular | 2000.0 | 60.0  | 8.0    | 2.0  |
| Diesel  | 1000.0 | 50.0  | 6.0    | 1.0  |

- Use python package **sqlalchemy** to get connection to database (database specific)

```
import sqlalchemy as sqla
engine = sqla.create_engine(
 'mysql+pymysql://irv:password@localhost:3306')
conn=engine.connect()
```

# Multiple ways to read the table

- Read all columns, no index created

```
df1 = pd.read_sql_table("gas", con=conn, schema="pandas")
```

- Read all columns, specify column for index

```
df2 = pd.read_sql_table("gas", con=conn, schema="pandas",
 index_col="name")
```

- Look up metadata to get primary key information

```
pkeys = (sqla.Table('gas', sqla.MetaData(), autoload=True,
 autoload_with=engine, schema='pandas')
 .primary_key.columns.keys()) # Get the primary keys
df3 = pd.read_sql_table("gas", con=conn, schema="pandas",
 index_col=pkeys)
```

- You can also do classic SQL queries

```
df4 = pd.read_sql("SELECT name, demand, price from pandas.gas",
 conn, index_col="name")
```



05.Database.ipynb

# Read HTML table data

- Pandas can read data from HTML tables
- May need to figure out where the table is within the HTML page.

- Using example from Gurobi:

<http://www.gurobi.com/resources/examples/food-manufacture-II>

```
df = pd.read_html("http://www.gurobi.com/resources/examples/food-manufacture-II")[1]
```

- Note that a list is returned. Have to get the right table.



06.html.ipynb

## Problem Description

A manufacturer needs to refine several raw oils and blend them together to produce a given food product that can be sold. The raw oils needed can be divided into two categories:

| Category            | Oil   |
|---------------------|-------|
| Vegetable oils:     | VEG 1 |
|                     | VEG 2 |
| Non-vegetable oils: | OIL 1 |
|                     | OIL 2 |
|                     | OIL 3 |

The manufacturer can choose to buy raw oils for the current month and/or buy them on the futures market for delivery in a subsequent month. Prices for immediate deliver and in the futures market are given below in \$/ton:

| Month    | VEG 1 | VEG 2 | OIL 1 | OIL 2 | OIL 3 |
|----------|-------|-------|-------|-------|-------|
| January  | 110   | 120   | 130   | 110   | 115   |
| February | 130   | 130   | 110   | 90    | 115   |
| March    | 110   | 140   | 130   | 100   | 95    |
| April    | 120   | 110   | 120   | 120   | 125   |
| May      | 100   | 120   | 150   | 110   | 105   |
| June     | 90    | 100   | 140   | 80    | 135   |

# More on I/O supported by pandas

## Reading Functions

`read_csv`

`read_excel`

`read_hdf`

`read_sql`

`read_json`

`read_html`

`read_stata`

`read_sas`

`read_clipboard`

`read_pickle`

## Writing Functions

`to_csv`

`to_excel`

`to_hdf`

`to_sql`

`to_json`

`to_html`

`to_stata`

`to_clipboard`

`to_pickle`

# Manipulating Data



# Creating Indexes

- All the reading functions allow you to specify which columns make up the Index/MultiIndex
- But you can also set the index if there is not one  
`df1 = df.set_index(['Month'])`
- You can also reset the index to be numerical  
`df2 = df1.reset_index()`
- If you want to change the index from one column to another, reset and then set:  
`df3 = df1.reset_index().set_index(['VEG 1'])`



06.html.ipynb

# Read the Data, then get the index sets!

- Get the complete index set as a list

```
list(mrdf.index)
```

- Look at the unique values corresponding to the index name 'PROD'

```
set(mrdf.index.get_level_values('PROD'))
```

- Look at the unique values corresponding to the index name 'T'

```
set(mrdf.index.get_level_values('T'))
```



01.tidysteel.ipynb



# Creating New Columns

- Given a DataFrame, you can create new columns that are arithmetic combinations of other columns
  - The computations are done treating Series as vectors

- Example:

```
df = df.assign(totmin = 60*df.hours + df.minutes)
```

- Alternative:

```
df['totmin'] = 60*df.hours + df.minutes
```

|   | hours | minutes |
|---|-------|---------|
| 0 | 5     | 14      |
| 1 | 2     | 4       |
| 2 | 5     | 7       |
| 3 | 9     | 51      |
| 4 | 9     | 1       |
| 5 | 5     | 14      |
| 6 | 5     | 51      |
| 7 | 3     | 1       |



07.assign.ipynb

|   | hours | minutes | totmin |
|---|-------|---------|--------|
| 0 | 5     | 14      | 314    |
| 1 | 2     | 4       | 124    |
| 2 | 5     | 7       | 307    |
| 3 | 9     | 51      | 591    |
| 4 | 9     | 1       | 541    |
| 5 | 5     | 14      | 314    |
| 6 | 5     | 51      | 351    |
| 7 | 3     | 1       | 181    |

# Example Using Date Data

- 33850 records of Begin/End Dates "dates.csv"

Begin, End

20150407, 20150411

20150404, 20150411

20150409, 20150413

20150409, 20150417

20150409, 20150411

20150403, 20150411

20150403, 20150409

20150403, 20150408

20150403, 20150403

# Multiple Transformations with .assign

```
ddf = didf.assign(delta = didf.End-didf.Begin,
 BegYear = didf.Begin//10000,
 EndYear = didf.End//10000)
```



07.assign.ipynb

```
ddf = (
 ddf.assign(BegMonth = (ddf.Begin-ddf.BegYear*10000)//100,
 EndMonth = (ddf.End-ddf.EndYear*10000)//100,
 BegDay = ddf.Begin % 100,
 EndDay = ddf.End % 100)
 [['Begin', 'BegYear', 'BegMonth', 'BegDay', 'End',
 'EndYear', 'EndMonth', 'EndDay', 'delta']]
)
```

- Note use of multiple assignments, and chaining to reorder the columns

|   | Begin    | BegYear | BegMonth | BegDay | End      | EndYear | EndMonth | EndDay | delta |
|---|----------|---------|----------|--------|----------|---------|----------|--------|-------|
| 0 | 20150407 | 2015    | 4        | 7      | 20150411 | 2015    | 4        | 11     | 4     |
| 1 | 20150404 | 2015    | 4        | 4      | 20150411 | 2015    | 4        | 11     | 7     |

# pandas has built-in Date/Time handling

```
dtidf = didf.assign(
 BegTime = pd.to_datetime(didf.Begin, format='%Y%m%d'),
 EndTime = pd.to_datetime(didf.End, format='%Y%m%d')
)
```



07.assign.ipynb

```
dtidf = (dtidf.assign(BegYear = dtidf.BegTime.dt.year,
 BegMonth = dtidf.BegTime.dt.month,
 BegDay = dtidf.BegTime.dt.day,
 EndYear = dtidf.EndTime.dt.year,
 EndMonth = dtidf.EndTime.dt.month,
 EndDay = dtidf.EndTime.dt.day,
 delta = dtidf.EndTime - dtidf.BegTime)
 [['Begin', 'BegTime', 'BegYear', 'BegMonth', 'BegDay',
 'End', 'EndTime', 'EndYear', 'EndMonth', 'EndDay', 'delta']])
```

|   | Begin    | BegTime    | BegYear | BegMonth | BegDay | End      | EndTime    | EndYear | EndMonth | EndDay | delta  |
|---|----------|------------|---------|----------|--------|----------|------------|---------|----------|--------|--------|
| 0 | 20150407 | 2015-04-07 | 2015    | 4        | 7      | 20150411 | 2015-04-11 | 2015    | 4        | 11     | 4 days |
| 1 | 20150404 | 2015-04-04 | 2015    | 4        | 4      | 20150411 | 2015-04-11 | 2015    | 4        | 11     | 7 days |

dtidf.dtypes

|          |                |          |                 |
|----------|----------------|----------|-----------------|
| Begin    | int64          | End      | int64           |
| BegTime  | datetime64[ns] | EndTime  | datetime64[ns]  |
| BegYear  | int64          | EndYear  | int64           |
| BegMonth | int64          | EndMonth | int64           |
| BegDay   | int64          | EndDay   | int64           |
|          |                | delta    | timedelta64[ns] |

# Understanding Data

- After you read in a table, there are useful features to look at parts of the data

| Method                       | Result                                            |
|------------------------------|---------------------------------------------------|
| <code>df.head(n)</code>      | First n (default 5) rows of DataFrame             |
| <code>df.tail(n)</code>      | Last n (default 5) rows of DataFrame              |
| <code>df.describe()</code>   | Descriptive statistics of each column             |
| <code>len(df)</code>         | Number of rows in DataFrame                       |
| <code>df.sum()</code>        | Sum of each column                                |
| <code>df.min()</code>        | Minimum value of each column                      |
| <code>df.max()</code>        | Maximum value of each column                      |
| <code>df.hist(bins=n)</code> | Histogram of each column with n bins (default 10) |

# You can filter and sort data

- Filtering

```
df[df.normal < -25]
df[(df.uniform - df.normal > 7) & (df.normal > 0)]
```

- Sorting

```
df.sort_values(by='normal', inplace=True)
```

- Note how the index is preserved when sorting!

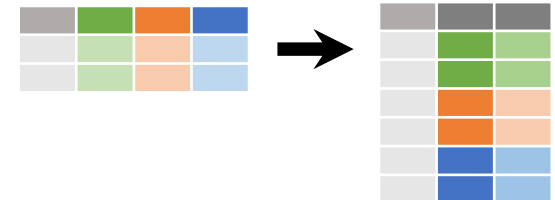


08.Analyze.ipynb

# Other Data Transformations

- Melting Helps Make Tidy Data!

```
pd.melt(df, id_vars='rowindex',
 value_name='valname')
```



- Pivoting Does the Reverse

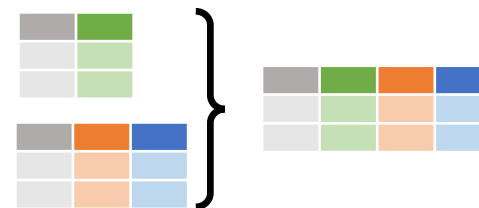
```
df.pivot(index='index',
 columns='var',
 values='val')
```



- You can concatenate rows or columns

```
pd.concat([df1, df2])
```

```
pd.concat([df1, df2], axis=1)
```



09.Transform.ipynb

# Merging/Joining

- pandas Supports Database-style Joins and Merges
  - Essential for combining different tables across indices

| adf |    | bdf |    |
|-----|----|-----|----|
| x1  | x2 | x1  | x3 |
| A   | 1  | A   | T  |
| B   | 2  | B   | F  |
| C   | 3  | D   | T  |



| x1 | x2 | x3  |
|----|----|-----|
| A  | 1  | T   |
| B  | 2  | F   |
| C  | 3  | NaN |

```
pd.merge(adf, bdf,
 how='left', on='x1')
```

Join matching rows from bdf to adf.

| x1 | x2  | x3 |
|----|-----|----|
| A  | 1.0 | T  |
| B  | 2.0 | F  |
| D  | NaN | T  |

```
pd.merge(adf, bdf,
 how='right', on='x1')
```

Join matching rows from adf to bdf.

| x1 | x2 | x3 |
|----|----|----|
| A  | 1  | T  |
| B  | 2  | F  |

```
pd.merge(adf, bdf,
 how='inner', on='x1')
```

Join data. Retain only rows in both sets.

| x1 | x2  | x3  |
|----|-----|-----|
| A  | 1   | T   |
| B  | 2   | F   |
| C  | 3   | NaN |
| D  | NaN | T   |

```
pd.merge(adf, bdf,
 how='outer', on='x1')
```

Join data. Retain all values, all rows.



# Merging/Joining Example

| <i>personhoursperday</i> |     | hours |
|--------------------------|-----|-------|
| id                       | day |       |
| ADK0000000000ICFPT       | Mo  | 0     |
| BEL0000000001JDGQU       | Mo  | 8     |
| CFM0000000002KEHRV       | Mo  | 0     |
| DGN0000000003LFISW       | Mo  | 0     |
| EHO0000000004MGJTX       | Mo  | 0     |

| <i>prefs table</i>  |                     | pref |
|---------------------|---------------------|------|
| person_id           | site_id             |      |
| MPW00000000272UORBF | ADK00000000364ICFPT | 64   |
| ORY00000000196WQTDH | ADK00000000364ICFPT | 32   |
| QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   |
| TWD00000000123BVYIM | ADK00000000364ICFPT | 57   |
| ADK0000000000ICFPT  | ADK00000000390ICFPT | 35   |

| <i>sitehoursperday</i> |     | hours |
|------------------------|-----|-------|
| id                     | day |       |
| ADK00000000364ICFPT    | Mo  | 8.0   |
|                        | Tu  | 8.0   |
|                        | We  | 8.0   |
|                        | Th  | 8.0   |
|                        | Fr  | 4.0   |

|    | person_id           | site_id             | pref | day | daily_hours |
|----|---------------------|---------------------|------|-----|-------------|
| 0  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Mo  | 8.0         |
| 1  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Tu  | 8.0         |
| 2  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | We  | 8.0         |
| 3  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Th  | 4.0         |
| 4  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Fr  | 4.0         |
| 9  | ORY00000000196WQTDH | ADK00000000364ICFPT | 32   | We  | 4.0         |
| 10 | ORY00000000196WQTDH | ADK00000000364ICFPT | 32   | Th  | 4.0         |
| 11 | ORY00000000196WQTDH | ADK00000000364ICFPT | 32   | Fr  | 4.0         |
| 14 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | Mo  | 6.0         |
| 15 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | Tu  | 6.0         |
| 16 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | We  | 6.0         |
| 17 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | Th  | 6.0         |
| 21 | TWD00000000123BVYIM | ADK00000000364ICFPT | 57   | Mo  | 6.0         |
| 22 | TWD00000000123BVYIM | ADK00000000364ICFPT | 57   | Tu  | 6.0         |

# pandas Merging/Joining Example

| <i>peoplehoursperday</i> |     | hours |
|--------------------------|-----|-------|
| id                       | day |       |
| ADK0000000000ICFPT       | Mo  | 0     |
| BEL0000000001JDGQU       | Mo  | 8     |
| CFM0000000002KEHRV       | Mo  | 0     |
| DGN0000000003LFISW       | Mo  | 0     |
| EHO0000000004MGJTX       | Mo  | 0     |

| <i>prefs table</i>  |                     | pref |
|---------------------|---------------------|------|
| person_id           | site_id             |      |
| MPW00000000272UORBF | ADK00000000364ICFPT | 64   |
| ORY00000000196WQTDH | ADK00000000364ICFPT | 32   |
| QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   |
| TWD00000000123BVYIM | ADK00000000364ICFPT | 57   |
| ADK00000000000ICFPT | ADK00000000390ICFPT | 35   |

| <i>sitehoursperday</i> |     | hours |
|------------------------|-----|-------|
| id                     | day |       |
| ADK00000000364ICFPT    | Mo  | 8.0   |
|                        | Tu  | 8.0   |
|                        | We  | 8.0   |
|                        | Th  | 8.0   |
|                        | Fr  | 4.0   |

```

prefswithdaily = (
 pd.merge(prefs.reset_index(),
 peoplehoursperday.reset_index(),
 left_on='person_id', right_on='id', how='left')
 .drop('id',axis=1)
 .rename(columns={'hours' : 'person_hours'})
 .merge(sitehoursperday.reset_index(),
 left_on=['site_id','day'],
 right_on=['id','day'], how='inner')
 .drop('id',axis=1)
 .rename(columns={'hours' : 'site_hours'})
)

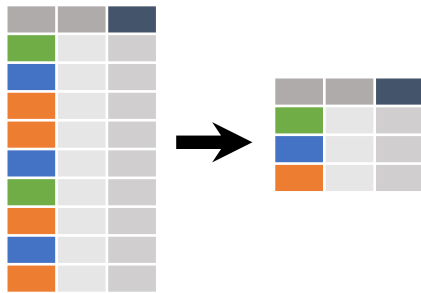
```



10.Merging.ipynb

# groupby – A Powerful pandas Operator

- When working with data, we often need to apply a mathematical operator (sum, min, max, etc.) across a column, grouped by other sets of columns



`df.groupby(by="col")`

Return a GroupBy object, grouped by values in column named "col".

`df.groupby(level="ind")`

Return a GroupBy object, grouped by values in index level named "ind".

| Function            | Description           | Function                   | Description                  |
|---------------------|-----------------------|----------------------------|------------------------------|
| <code>size()</code> | Size of each group    | <code>sum()</code>         | Sum values of each group     |
| <code>min()</code>  | Minimum of each group | <code>max()</code>         | Maximum of each group        |
| <code>mean()</code> | Mean of each group    | <code>agg(function)</code> | Apply function to each group |

# groupby Examples

| <i>peoplehoursperday</i> |     | hours |
|--------------------------|-----|-------|
| id                       | day |       |
| ADK0000000000ICFPT       | Mo  | 0     |
| BEL0000000001JDGQU       | Mo  | 8     |
| CFM0000000002KEHRV       | Mo  | 0     |
| DGN0000000003LFISW       | Mo  | 0     |
| EHO0000000004MGJTX       | Mo  | 0     |

```
peoplehoursperday
.groupby(level='id').sum()
```

|                     | hours |
|---------------------|-------|
| id                  |       |
| ADK0000000000ICFPT  | 6     |
| ADK00000000026ICFPT | 8     |
| ADK00000000052ICFPT | 16    |
| ADK00000000078ICFPT | 16    |
| ADK00000000104ICFPT | 25    |

```
peoplehoursperday
.groupby(level='day').sum()
```

|     | hours |
|-----|-------|
| day |       |
| Fr  | 1110  |
| Mo  | 1518  |
| Sa  | 133   |
| Su  | 88    |
| Th  | 1696  |
| Tu  | 1818  |
| We  | 1757  |



11.GroupBy.ipynb

# pandas for Optimization

# Comparing AMPL to pandas

- Model File

```
set PROD;
param T > 0;

param rate {PROD} > 0;
param avail {1..T} >= 0;
```

- Data File

```
param T := 4;
set PROD := bands coils;

param avail := 1 40 2 40 3 32 4 40 ;

param rate := bands 200 coils 140 ;
```



12.datacompare.ipynb

- avail.csv

```
Period,avail
1,40
2,40
3,32
4,40
```

- rate.csv

```
PROD,rate
bands,200
coils,140
```

- Code

```
avail = pd.read_csv('avail.csv',
 index_col=0)
rate = pd.read_csv('rate.csv',
 index_col=0)
T = max(avail.index.get_level_values(0))
PROD = set(rate.index.get_level_values(0))
```

- Note how the sets are inferred from the data

# AMPL and pandas Data Representation

## ● AMPL ".dat" file

```

param T := 4;
set PROD := bands coils;

param avail := 1 40 2 40 3 32 4 40 ;

param rate := bands 200 coils 140 ;
param inv0 := bands 10 coils 0 ;

param prodcost := bands 10 coils 11 ;
param invcost := bands 2.5 coils 3 ;

param revenue: 1 2 3 4 :=
 bands 25 26 27 27
 coils 30 35 37 39 ;

param market: 1 2 3 4 :=
 bands 6000 6000 4000 6500
 coils 4000 2500 3500 4200 ;

```

## ● Excel for pandas

|    | A              | B            | C           | D               | E              |
|----|----------------|--------------|-------------|-----------------|----------------|
| 1  | <b>Product</b> | <b>rate</b>  | <b>inv0</b> | <b>prodcost</b> | <b>invcost</b> |
| 2  | bands          | 220          | 10          | 10              | 2.5            |
| 3  | coils          | 154          | 0           | 11              | 3              |
| 4  |                |              |             |                 |                |
| 5  |                |              |             |                 |                |
| 6  |                |              |             |                 |                |
| 7  | <b>Revenue</b> | <b>1</b>     | <b>2</b>    | <b>3</b>        | <b>4</b>       |
| 8  | <b>bands</b>   | 25           | 26          | 27              | 27             |
| 9  | <b>coils</b>   | 30           | 35          | 37              | 39             |
| 10 |                |              |             |                 |                |
| 11 | <b>Market</b>  | <b>1</b>     | <b>2</b>    | <b>3</b>        | <b>4</b>       |
| 12 | <b>bands</b>   | 6000         | 6000        | 4000            | 6500           |
| 13 | <b>coils</b>   | 4000         | 2500        | 3500            | 4200           |
| 14 |                |              |             |                 |                |
| 15 |                |              |             |                 |                |
| 16 |                |              |             |                 |                |
| 17 | <b>Time</b>    | <b>avail</b> |             |                 |                |
| 18 | <b>1</b>       | 40           |             |                 |                |
| 19 | <b>2</b>       | 40           |             |                 |                |
| 20 | <b>3</b>       | 32           |             |                 |                |
| 21 | <b>4</b>       | 40           |             |                 |                |

# AMPL and pandas data declarations

- AMPL declarations
- python code with pandas

```
set PROD;
param T > 0;

param rate {PROD} > 0;
param inv0 {PROD} >= 0;
param avail {1..T} >= 0;
param market {PROD,1..T} >= 0;

param prodcost {PROD} >= 0;
param invcost {PROD} >= 0;
param revenue {PROD,1..T} >= 0;
```

```
productDF = pd.read_excel("steelT.xlsx", index_col=0,
 skip_footer=18)
revenue = pd.read_excel("steelT.xlsx", index_col=0,
 skiprows=6, skip_footer=12)
market = pd.read_excel("steelT.xlsx", index_col=0,
 skiprows=10, skip_footer=8)
avail = pd.read_excel("steelT.xlsx", index_col=0,
 skiprows=16, parse_cols=1)
rmDF = pd.concat(
 [(pd.melt(market.reset_index(),
 id_vars=['Product'],
 value_name='market',
 var_name='T')
 .set_index(['Product', 'T'])
 .astype('float64')),
 (pd.melt(revenue.reset_index(),
 id_vars=['Product'],
 value_name='revenue',
 var_name='T')
 .set_index(['Product', 'T'])
 .astype('float64'))
], axis=1)
```



# Decision Variable Declaration

- AMPL

```
var Make {PROD,1..T} >= 0;
var Inv {PROD,0..T} >= 0;
var Sell {p in PROD, t in 1..T} >= 0, <= market[p,t];
```

- pandas

```
from docplex.mp.model import Model
model = Model(name='steelT')
```

```
dvars = pd.DataFrame(
 {'Make' : model.continuous_var_list(rmDF.index, name='Make'),
 'Inv' : model.continuous_var_list(rmDF.index, name='Inv'),
 'Sell' : model.continuous_var_list(rmDF.index,
 ub=list(rmDF.market.values),
 name='Sell')},
 index=rmDF.index)
```

- Note that we chose to not create variables for Inv[p,0]



13.steelT.ipynb

# Decision Variables DataFrame

|              |          | Inv              | Make              | Sell              |
|--------------|----------|------------------|-------------------|-------------------|
| Product      | T        |                  |                   |                   |
| <b>bands</b> | <b>1</b> | Inv_('bands', 1) | Make_('bands', 1) | Sell_('bands', 1) |
| <b>coils</b> | <b>1</b> | Inv_('coils', 1) | Make_('coils', 1) | Sell_('coils', 1) |
| <b>bands</b> | <b>2</b> | Inv_('bands', 2) | Make_('bands', 2) | Sell_('bands', 2) |
| <b>coils</b> | <b>2</b> | Inv_('coils', 2) | Make_('coils', 2) | Sell_('coils', 2) |
| <b>bands</b> | <b>3</b> | Inv_('bands', 3) | Make_('bands', 3) | Sell_('bands', 3) |
| <b>coils</b> | <b>3</b> | Inv_('coils', 3) | Make_('coils', 3) | Sell_('coils', 3) |
| <b>bands</b> | <b>4</b> | Inv_('bands', 4) | Make_('bands', 4) | Sell_('bands', 4) |
| <b>coils</b> | <b>4</b> | Inv_('coils', 4) | Make_('coils', 4) | Sell_('coils', 4) |

# Easiest to Merge Data and Variables

```
mainDF = (
 dvars.merge(rmDF, left_index=True, right_index=True, how='inner')
 .reset_index()
 .merge(productDF.reset_index(),
 left_on='Product', right_on='Product', how='left')
 .set_index(['Product', 'T'])
)
```

|                |          | Inv              | Make              | Sell              | market | revenue | rate | inv0 | prodcost | invcost |
|----------------|----------|------------------|-------------------|-------------------|--------|---------|------|------|----------|---------|
| <b>Product</b> | <b>T</b> |                  |                   |                   |        |         |      |      |          |         |
| <b>bands</b>   | <b>1</b> | Inv_('bands', 1) | Make_('bands', 1) | Sell_('bands', 1) | 6000.0 | 25.0    | 220  | 10   | 10       | 2.5     |
| <b>coils</b>   | <b>1</b> | Inv_('coils', 1) | Make_('coils', 1) | Sell_('coils', 1) | 4000.0 | 30.0    | 154  | 0    | 11       | 3.0     |
| <b>bands</b>   | <b>2</b> | Inv_('bands', 2) | Make_('bands', 2) | Sell_('bands', 2) | 6000.0 | 26.0    | 220  | 10   | 10       | 2.5     |
| <b>coils</b>   | <b>2</b> | Inv_('coils', 2) | Make_('coils', 2) | Sell_('coils', 2) | 2500.0 | 35.0    | 154  | 0    | 11       | 3.0     |
| <b>bands</b>   | <b>3</b> | Inv_('bands', 3) | Make_('bands', 3) | Sell_('bands', 3) | 4000.0 | 27.0    | 220  | 10   | 10       | 2.5     |
| <b>coils</b>   | <b>3</b> | Inv_('coils', 3) | Make_('coils', 3) | Sell_('coils', 3) | 3500.0 | 37.0    | 154  | 0    | 11       | 3.0     |
| <b>bands</b>   | <b>4</b> | Inv_('bands', 4) | Make_('bands', 4) | Sell_('bands', 4) | 6500.0 | 27.0    | 220  | 10   | 10       | 2.5     |
| <b>coils</b>   | <b>4</b> | Inv_('coils', 4) | Make_('coils', 4) | Sell_('coils', 4) | 4200.0 | 39.0    | 154  | 0    | 11       | 3.0     |

# Objective Function

- AMPL

maximize Total\_Profit:

```
sum {p in PROD, t in 1..T} (revenue[p,t]*Sell[p,t] -
 prodcost[p]*Make[p,t] - invcost[p]*Inv[p,t]);
```

- python

```
model.maximize(model.sum(
 mainDF.revenue*mainDF.Sell
 -mainDF.prodcost*mainDF.Make
 -mainDF.invcost*mainDF.Inv))
```

# Time constraints

- AMPL

subject to Time {t in 1..T}:

sum {p in PROD} (1/rate[p]) \* Make[p,t] <= avail[t];

- python

```
model.add_constraints(
 [(tsum <= avail, "Time_"+str(t))
 for (t, tsum, avail) in
 (pd.DataFrame((mainDF.Make/mainDF.rate)
 .groupby(level='T')
 .agg(model.sum),
 columns=['tsum'])
 .merge(avail, left_index=True, right_index=True)
 .itertuples())
])
```

# Initial Inventory/Balance constraint

- AMPL

subject to Init\_Inv {p in PROD}:  $\text{Inv}[p,0] = \text{inv0}[p];$

- python

```
idx = pd.IndexSlice
```

```
mainDF.sort_index(inplace=True)
```

```
model.add_constraints(
 [(Make + inv0 == Sell + Inv,
 'Balance_'+Product+'_'+str(t))
 for ((Product, t), Make, inv0, Sell, Inv) in
 mainDF.loc[idx[:,1],
 ['Make','inv0','Sell','Inv']]
 .itertuples()
])
```

# Balance Constraints

- AMPL

subject to Balance {p in PROD, t in 1..T}:  
    Make[p,t] + Inv[p,t-1] = Sell[p,t] + Inv[p,t];

- python

```
model.add_constraints(
 [(Make + mainDF.Inv.loc[Product, t-1] == Sell + Inv,
 'Balance_'+Product+'_'+str(t))
 for ((Product, t), Make, Sell, Inv) in
 mainDF.loc[idx[:,2:], ['Make','Sell','Inv']]
 .itertuples()
]
)
```

# Solve and Obtain the Solution

```
model.solve()
soln = pd.DataFrame({'Make' : [x.solution_value for x in mainDF.Make],
 'Sell' : [x.solution_value for x in mainDF.Sell],
 'Inv' : [x.solution_value for x in mainDF.Inv]},
 index = mainDF.index)
```

|                |          | Inv   | Make   | Sell   |
|----------------|----------|-------|--------|--------|
| <b>Product</b> | <b>T</b> |       |        |        |
| <b>bands</b>   | <b>1</b> | 0.0   | 5990.0 | 6000.0 |
|                | <b>2</b> | 0.0   | 6000.0 | 6000.0 |
|                | <b>3</b> | 0.0   | 2040.0 | 2040.0 |
|                | <b>4</b> | 0.0   | 2800.0 | 2800.0 |
| <b>coils</b>   | <b>1</b> | 540.0 | 1967.0 | 1427.0 |
|                | <b>2</b> | 0.0   | 1960.0 | 2500.0 |
|                | <b>3</b> | 0.0   | 3500.0 | 3500.0 |
|                | <b>4</b> | 0.0   | 4200.0 | 4200.0 |



# A More Complex Example



# Our Example Problem

- Assign hours of work of people to sites per day of week
- Each person can work
  - At most a specified number of hours per day
  - At most a specified number of hours per week
  - At most a specified number of days per week
- Each site needs a set of people assigned for a number of hours per day
- When a person is assigned to a site
  - They must be assigned for at least an hour, in half-hour increments
  - They must be assigned for at least 2 days in the week
- There is a preference score for each person/site pair that is eligible to be assigned
  - Maximize the preferences
- There are not enough people available to cover all the site requirements, so maximize the coverage as best as possible

# Data: Sites.csv

id,num\_hours

TWD0000000357BVYIM,12.0

UXE0000000358CWZJN,179.0

VYF0000000359DXAKO,171.0

WZG0000000360EYBLP,11.0

XAH0000000361FZCMQ,10.0

...

# Data: People.csv

```
id,total_hrs_per_week,days_per_week
ADK00000000000ICFPT,6,3
BEL00000000001JDGQU,12,3
CFM00000000002KEHRV,10,7
DGN00000000003LFISW,28,6
EH00000000004MGJTX,14,1
FIP00000000005NHKUY,25,3
GJQ00000000006OILVZ,20,4
...
```

# Data: peoplehoursperday.csv

id,day,hours

GJQ00000002660ILVZ,Fr,2

UXE0000000150CWZJN,We,4

FIP0000000161NHKUY,Su,0

ILS0000000138QKNXB,We,0

SVC0000000278AUXHL,Tu,7

JMT0000000139RLOYC,Tu,4

PSZ0000000223XRUEI,We,8

...

# Data: sitehoursperday.csv

id,day,hours

ADK0000000364ICFPT,Mo,8.0

ADK0000000364ICFPT,Tu,8.0

ADK0000000364ICFPT,We,8.0

ADK0000000364ICFPT,Th,8.0

ADK0000000364ICFPT,Fr,4.0

ADK0000000390ICFPT,Mo,8.0

ADK0000000390ICFPT,Tu,8.0

ADK0000000390ICFPT,We,8.0

ADK0000000416ICFPT,Tu,2.5

ADK0000000416ICFPT,We,2.5

ADK0000000442ICFPT,Mo,7.0

...

# Data: prefs.csv

person\_id,site\_id,pref

MPW0000000272UORBF,ADK0000000364ICFPT,64

ORY0000000196WQTDH,ADK0000000364ICFPT,32

QTA0000000146YSVFJ,ADK0000000364ICFPT,97

TWD0000000123BVYIM,ADK0000000364ICFPT,57

ADK0000000000ICFPT,ADK0000000390ICFPT,35

ADK0000000026ICFPT,ADK0000000390ICFPT,95

ADK0000000052ICFPT,ADK0000000390ICFPT,97

ADK0000000130ICFPT,ADK0000000390ICFPT,49

ADK0000000156ICFPT,ADK0000000390ICFPT,45

ADK0000000234ICFPT,ADK0000000390ICFPT,83

ADK0000000260ICFPT,ADK0000000390ICFPT,40

...

# OPL Declarations to Read In Data

```
setof(string) sites = ...;
float num_hours_per_site[sites] = ...;
```

```
tuple tPeopleData {
 float total_hrs_per_week;
 float days_per_week;
}
setof(string) people = ...;
tPeopleData peopleData[people] = ...;
```

```
tuple tIdDayIndex {
 string id;
 string day;
};
setof(tIdDayIndex) siteHoursPerDayIndex = ...;
float hours_per_site_day[siteHoursPerDayIndex] = ...;
```

```
setof(tIdDayIndex) peopleHoursPerDayIndex = ...;
float hours_per_people_day[peopleHoursPerDayIndex] = ...;
```

```
tuple tPeopleSiteIndex {
 string person_id;
 string site_id;
};
setof(tPeopleSiteIndex) prefIndex= ...;
float pref[prefIndex] = ...;
```

**Each declaration includes declaring an index set and an array of data indexed on that set**



# OPL Data File to Read in Data

```
SheetConnection siteSheet("sites.csv");
SheetConnection peopleSheet("people.csv");
SheetConnection siteHoursPerDaySheet("sitehoursperday.csv");
SheetConnection peopleHoursPerDaySheet("peoplehoursperday.csv");
SheetConnection prefSheet("prefs.csv");
```

```
sites from SheetRead(siteSheet, "A2:A549");
num_hours_per_site from SheetRead(siteSheet, "B2:B549");

people from SheetRead(peopleSheet, "A2:A358");
peopleData from SheetRead(peopleSheet, "B2:C358");

siteHoursPerDayIndex from SheetRead(siteHoursPerDaySheet, "A2:B1705");
hours_per_site_day from SheetRead(siteHoursPerDaySheet, "C2:C1705");

peopleHoursPerDayIndex from SheetRead(peopleHoursPerDaySheet, "A2:B2500");
hours_per_people_day from SheetRead(peopleHoursPerDaySheet, "C2:C2500");

prefIndex from SheetRead(prefSheet, "A2:B33301");
pref from SheetRead(prefSheet, "C2:C33301");
```



**Read statements needed for each index set, and for each data array.  
Precise locations in Excel worksheet are required.**

# Python (pandas) to read in data

```
import pandas as pd
```

```
sites = pd.read_csv("sites.csv", index_col=0)
```

```
people = pd.read_csv("people.csv", index_col=0)
```

```
peoplehoursperday = pd.read_csv("peoplehoursperday.csv", index_col=[0,1])
```

```
sitehoursperday = pd.read_csv("sitehoursperday.csv", index_col=[0,1])
```

```
prefs = pd.read_csv("prefs.csv", index_col=[0,1])
```

# Do people and peoplehoursperday correspond?

O  
P  
L

```
setof(string) peopleInPeopleHoursPerDay =
 { p | <p, d> in peopleHoursPerDayIndex };
assert (card(people) == card(peopleInPeopleHoursPerDay));
assert forall (p in people) (p in peopleInPeopleHoursPerDay);
execute {
 writeln("PeopleHoursPerDay and People refer to same people.
 Assertion succeeded.");
 writeln("Number of people = ", Op1.card(people));
};
```

p  
a  
n  
d  
a  
s

```
uniquePeople =
 set(people.index.get_level_values('id'))

print ("PeopleHoursPerDay and People refer to same people? ",
 set(peoplehoursperday.index.get_level_values('id'))
 == uniquePeople)

print ("Number of people ", len(people))
```

# Check that the people in the prefs table are in the people table

O  
P  
L

```
setof(string) peopleInPrefs = { p | <p,s> in prefIndex };

setof(string) peopleToPeoplePrefs = people diff peopleInPrefs;
assert (card(peopleToPeoplePrefs) == card(people) - card(peopleInPrefs));

execute {
 writeln("People in prefs and People refer to same people? ",
 (Opl.card(people) == Opl.card(peopleInPrefs)) &&
 (Opl.card(peopleToPeoplePrefs) == 0));

 writeln("Number of people in prefs = ", Opl.card(peopleInPrefs));
 writeln("People in prefs are in people table? ",
 Opl.card(peopleToPeoplePrefs) == Opl.card(people) - Opl.card(peopleInPrefs));
}
```

p  
a  
n  
d  
a  
s

```
peopleInPrefs = set(prefs.index.get_level_values('person_id'))

print ("People in Prefs and People refer to same people? ",
 (len(uniquePeople) == len(peopleInPrefs)) and
 (uniquePeople == peopleInPrefs))

print ("Number of people in prefs = ", len(peopleInPrefs))

print ("People in prefs are in people table? ",
 peopleInPrefs.issubset(uniquePeople))
```

# Output

PeopleHoursPerDay and People refer to same people? True  
Number of people 357

People in Prefs and People refer to same people? False  
Number of people in prefs = 338

People in prefs are in people table? True

**So we can conclude that there are people who have no sites they can be assigned to**

**There are additional data checks (omitted for brevity)**

# Merging/Joining

| <i>peoplehoursperday</i> |     | hours |
|--------------------------|-----|-------|
| id                       | day |       |
| ADK0000000000ICFPT       | Mo  | 0     |
| BEL0000000001JDGQU       | Mo  | 8     |
| CFM0000000002KEHRV       | Mo  | 0     |
| DGN0000000003LFISW       | Mo  | 0     |
| EHO0000000004MGJTX       | Mo  | 0     |

| <i>prefs table</i>  |                     | pref |
|---------------------|---------------------|------|
| person_id           | site_id             |      |
| MPW00000000272UORBF | ADK00000000364ICFPT | 64   |
| ORY00000000196WQTDH | ADK00000000364ICFPT | 32   |
| QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   |
| TWD00000000123BVYIM | ADK00000000364ICFPT | 57   |
| ADK0000000000ICFPT  | ADK00000000390ICFPT | 35   |

| <i>sitehoursperday</i> |     | hours |
|------------------------|-----|-------|
| id                     | day |       |
| ADK00000000364ICFPT    | Mo  | 8.0   |
|                        | Tu  | 8.0   |
|                        | We  | 8.0   |
|                        | Th  | 8.0   |
|                        | Fr  | 4.0   |

|    | person_id           | site_id             | pref | day | daily_hours |
|----|---------------------|---------------------|------|-----|-------------|
| 0  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Mo  | 8.0         |
| 1  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Tu  | 8.0         |
| 2  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | We  | 8.0         |
| 3  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Th  | 4.0         |
| 4  | MPW00000000272UORBF | ADK00000000364ICFPT | 64   | Fr  | 4.0         |
| 9  | ORY00000000196WQTDH | ADK00000000364ICFPT | 32   | We  | 4.0         |
| 10 | ORY00000000196WQTDH | ADK00000000364ICFPT | 32   | Th  | 4.0         |
| 11 | ORY00000000196WQTDH | ADK00000000364ICFPT | 32   | Fr  | 4.0         |
| 14 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | Mo  | 6.0         |
| 15 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | Tu  | 6.0         |
| 16 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | We  | 6.0         |
| 17 | QTA00000000146YSVFJ | ADK00000000364ICFPT | 97   | Th  | 6.0         |
| 21 | TWD00000000123BVYIM | ADK00000000364ICFPT | 57   | Mo  | 6.0         |
| 22 | TWD00000000123BVYIM | ADK00000000364ICFPT | 57   | Tu  | 6.0         |

# Merging: OPL vs. pandas

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```
setof(tIdDayIndex) prefPeopleHoursByDayIndexAll =
 { <p,d> | p in peopleInPrefs, <p,d> in peopleHoursPerDayIndex };
setof(tIdDayIndex) prefSitesHoursByDayIndexAll =
 { <s,d> | s in sitesInPrefs, <s,d> in siteHoursPerDayIndex };

tuple tPersonSiteDay {
 string person_id;
 string site_id;
 string day;
};
setof(tPersonSiteDay) prefsPersonSiteDayIndexAll =
 { <p,s,d> | <p,s> in prefIndex,
 <p,d> in prefPeopleHoursByDayIndexAll,
 <s,d> in prefSitesHoursByDayIndexAll };

float hoursPerPersonSiteDayAll[<p,s,d> in prefsPersonSiteDayIndexAll] =
 min1(hours_per_people_day[<p,d>], hours_per_site_day[<s,d>]);

setof(tPersonSiteDay) prefsPersonSiteDayIndex =
 { <p,s,d> | <p,s,d> in prefsPersonSiteDayIndexAll : hoursPerPersonSiteDayAll[<p,s,d>] > 0};
```

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```
prefswithdaily = (
 pd.merge(prefs.reset_index(), peoplehoursperday.reset_index(),
 left_on='person_id', right_on='id', how='left')
 .drop('id',axis=1)
 .rename(columns={'hours' : 'person_hours'})
 .merge(sitehoursperday.reset_index(), left_on=['site_id','day'], right_on=['id','day'], how='inner')
 .drop('id',axis=1)
 .rename(columns={'hours' : 'site_hours'})
)
prefswithdaily['daily_hours'] = prefswithdaily[['person_hours','site_hours']].min(axis=1)
prefswithdaily = prefswithdaily.drop(['person_hours','site_hours'],axis=1)
[prefswithdaily.daily_hours > 0]
```

# Determining Eligible pairs, people, sites

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```
setof(tPersonSiteDay) allVarsIndex = prefsPersonSiteDayIndex;

setof(tPeopleSiteIndex) eligiblePairs = { <p,s> | <p,s,d> in allVarsIndex };

setof(string) eligiblePeople = { p | <p,s> in eligiblePairs };

setof(string) eligibleSites = { s | <p,s> in eligiblePairs };
```

p  
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s

```
allvars = prefswithdaily.set_index(['person_id', 'site_id', 'day'])

eligiblePairs = set((p,s) for (p,s,d) in allvars.index)

eligiblePeople = set(p for p,s in eligiblePairs)

eligibleSites = set(s for p,s in eligiblePairs)
```



# Decision Variables

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```
int blocksPerPersonSiteDay[<p,s,d> in prefsPersonSiteDayIndex] =
 ftoi(round(2.0*hoursPerPersonSiteDayAll[<p,s,d>]));

dvar int+ h[<p,s,d> in allVarsIndex] in 0..blocksPerPersonSiteDay[<p,s,d>];
dvar int+ pairday[<p,s,d> in allVarsIndex] in 0..1;
dvar int+ z[eligiblePairs] in 0..1;
dvar float+ shortage[eligibleSites];
dvar float+ excess[eligibleSites];
```

p  
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```
from gurobipy import *
m=Model("sched")

allvars['h'] = m.addVars(allvars.index, ub=2*allvars.daily_hours.values,
 vtype=GRB.INTEGER, name="h").values()
allvars['pairday'] = m.addVars(allvars.index, vtype=GRB.BINARY,
 name='pairday').values()

zvars = pd.DataFrame({'z' : m.addVars(eligiblePairs,
 vtype=GRB.BINARY, name="z").values()},
 index=pd.MultiIndex.from_tuples(eligiblePairs,
 names=['person_id', 'site_id']))

siteSlackVars = pd.DataFrame(
 { 'shortage' : m.addVars(eligibleSites,
 vtype=GRB.CONTINUOUS, name='shortage').values(),
 'excess' : m.addVars(eligibleSites,
 vtype=GRB.CONTINUOUS, name='excess').values() },
 index=pd.Index(eligibleSites, name='site_id'))
```

# Objective Function (Hierarchical)

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```
minimize 1.0*totalShortage + 0.0*totalExcess + 0.0*totalPrefs;

totalShortage == sum(s in eligibleSites) shortage[s];
totalExcess == sum(s in eligibleSites) excess[s];
totalPrefs == sum(p in eligiblePairs) pref[p]*z[p];

/* Script */
thisOplModel.generate();
cplex.solve();
thisOplModel.postProcess();
var objVal = cplex.getObjValue();

cplex.setObjCoef(thisOplModel.totalShortage, 0);
cplex.setObjCoef(thisOplModel.totalExcess, 1);
thisOplModel.shortageBound.UB = objVal + 0.25;
cplex.solve();
objVal = cplex.getObjValue();
thisOplModel.excessBound.UB = objVal + 0.25;
cplex.setObjCoef(thisOplModel.totalExcess, 0);
cplex.setObjCoef(thisOplModel.totalPrefs, -1); // To maximize
cplex.solve();
```

p  
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```
m.setObjective(quicksum(siteSlackVars.shortage), sense=GRB.MINIMIZE)
m.optimize()
m.addConstr(quicksum(siteSlackVars.shortage) <= m.ObjVal+0.25, name='shortageBound')
m.setObjective(quicksum(siteSlackVars.excess))
m.optimize()
m.addConstr(quicksum(siteSlackVars.excess) <= m.ObjVal+0.25, name='excessBound')

conDF = zvars.merge(prefs, left_index=True, right_index=True, how='left')
m.setObjective(quicksum(conDF.pref*conDF.z), sense=GRB.MAXIMIZE)
m.optimize()
```

# Constraint: Limit Hours Per Person Per Day (1)

$$\sum_{(p,s,d)} h[p, s, d] \leq 2 * people\_hours\_per\_day[p, d] , \forall (p, d)$$

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```
forall (<p,d> in prefPeopleHoursByDayIndex) {
 PersonHoursPerDay [<p,d>]:
 sum(<p,s,d> in allVarsIndex) h [<p,s,d>] <= 2*hours_per_people_day [<p,d>];
}
```

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```
phpdict = { k : v['hours']
 for k,v in peoplehoursperday.to_dict(orient='index').items() }

m.addConstrs((h.sum(person_id,'*',day) <= 2*phpdict[person_id,day]
 for (person_id, day) in
 set((person_id,day) for (person_id,site_id,day) in h.keys()))),
 name='PersonHoursPerDay')
```

0.54 secs

P  
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2

```
gb = allvars.h.groupby(level=['person_id', 'day'])
m.addConstrs((quicksum(gb.get_group(group_name))
 <= 2*peoplehoursperday.loc[group_name]
 for group_name in gb.groups.keys()),
 name='PersonHoursPerDay2')
```

1.28 secs

# Constraint: Limit Hours Per Person Per Day (2)

$$\sum_{(p,s,d)} h[p, s, d] \leq 2 * person\_hours\_per\_day[p, d] , \forall (p, d)$$

O  
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s  
3

```
forall (<p,d> in prefPeopleHoursByDayIndex) {
 PersonHoursPerDay[<p,d>]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] <= 2*hours_per_people_day[<p,d>];
}
```

```
gb = allvars.h.groupby(level=['person_id', 'day'])
m.addConstrs((quicksum(gb.get_group(group_name))
 <= 2*peoplehoursperday.loc[group_name]
 for group_name in gb.groups.keys()),
 name='PersonHoursPerDay2')
```

1.28 secs

```
phpdict = { k : v['hours']
 for k,v in peoplehoursperday.to_dict(orient='index').items() }

gb = allvars.h.groupby(level=['person_id', 'day'])
m.addConstrs((quicksum(gb.get_group(group_name)) <= 2*phpdict[group_name]
 for group_name in gb.groups.keys()),
 name='PersonHoursPerDay3')
```

0.82 secs

# Constraint: Limit Hours Per Person Per Day (3)

$$\sum_{(p,s,d)} h[p, s, d] \leq 2 * person\_hours\_per\_day[p, d] , \forall (p, d)$$

O  
P  
L

```
forall (<p,d> in prefPeopleHoursByDayIndex) {
 PersonHoursPerDay[<p,d>]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] <= 2*hours_per_people_day[<p,d>];
}
```

P  
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s  
3

```
phpdict = { k : v['hours']
 for k,v in peoplehoursperday.to_dict(orient='index').items() }

gb = allvars.h.groupby(level=['person_id', 'day'])
m.addConstrs((quicksum(gb.get_group(group_name)) <= 2*phpdict[group_name]
 for group_name in gb.groups.keys()),
 name='PersonHoursPerDay3')
```

**0.82 secs**

P  
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4

```
phpdict = { k : v['hours']
 for k,v in peoplehoursperday.to_dict(orient='index').items() }

gb = allvars.h.groupby(level=['person_id', 'day']).aggregate(quicksum)
gbdict = gb.to_dict()

m.addConstrs((gbdict[group_name] <= 2*phpdict[group_name]
 for group_name in gbdict.keys()),
 name='PersonHoursPerDay4')
```

**0.37 secs**

# Constraint: Limit Hours Per Person Per Day (4)

$$\sum_{(p,s,d)} h[p,s,d] \leq 2 * person\_hours\_per\_day[p,d] , \forall (p,d)$$

O  
P  
L

```
forall (<p,d> in prefPeopleHoursByDayIndex) {
 PersonHoursPerDay[<p,d>]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] <= 2*hours_per_people_day[<p,d>];
}
```

P  
a  
n  
d  
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s  
4

```
phpdict = { k : v['hours']
 for k,v in peoplehoursperday.to_dict(orient='index').items() }

gb = allvars.h.groupby(level=['person_id', 'day']).aggregate(quicksum)
gbdict = gb.to_dict()

m.addConstrs((gbdict[group_name] <= 2*phpdict[group_name]
 for group_name in gbdict.keys()),
 name='PersonHoursPerDay4')
```

0.37 secs

P  
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n  
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s  
5

```
conDF = pd.DataFrame(
 allvars.h.groupby(level=['person_id', 'day']).aggregate(quicksum)
 .rename('thesum'))
conDF.index.names = ['id', 'day'] # Renaming needed so that merge will work correctly
conDF = conDF.merge(peoplehoursperday, left_index=True, right_index=True, how='left')
for it in conDF.itertuples():
 m.addConstr(it.thesum <= 2*it.hours,
 name='PersonHoursPerDay5'+it.Index[0]+'_'+it.Index[1]+'')
```

0.28 secs

# Utility: Naming Constraints

- Gurobi 7.0 API for addConstrs() implicitly names constraints when you have a generator to define names, but if generator is “too big”, it fails
- So define a naming function:

```
import collections
def lpnamer(prefix, tup):
 if isinstance(tup, str):
 result = prefix + '[' + tup + ']'
 elif not isinstance(tup, collections.Iterable):
 result = prefix + '[' + str(tup) + ']'
 else:
 tup2 = [val for val in tup]
 tmp = '[' + ','.join(tup2) + ']'
 result = prefix + tmp
 return result
```

# Constraint: Limit Hours Per Person Per Day (5)

$$\sum_{(p,s,d)} h[p, s, d] \leq 2 * person\_hours\_per\_day[p, d] , \forall (p, d)$$

O  
P  
L

```
forall (<p,d> in prefPeopleHoursByDayIndex) {
 PersonHoursPerDay[<p,d>]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] <= 2*hours_per_people_day[<p,d>];
}
```

P  
a  
n  
d  
a  
s  
5

```
conDF = pd.DataFrame(
 allvars.h.groupby(level=['person_id', 'day']).aggregate(quicksum)
 .rename('thesum'))
conDF.index.names = ['id', 'day'] # Renaming needed so that merge will work correctly
conDF = conDF.merge(peoplehoursperday, left_index=True, right_index=True, how='left')
for it in conDF.itertuples():
 m.addConstr(it.thesum <= 2*it.hours,
 name='PersonHoursPerDay5'+it.Index[0]+'_'+it.Index[1]+'')
```

P  
a  
n  
d  
a  
s  
6

```
conDF = pd.DataFrame(
 allvars.h.groupby(level=['person_id', 'day']).aggregate(quicksum)
 .rename('thesum'))
conDF.index.names = ['id', 'day'] # Renaming needed so that merge will work correctly
conDF = conDF.merge(peoplehoursperday, left_index=True, right_index=True, how='left')
for it in conDF.itertuples():
 m.addConstr(it.thesum <= 2*it.hours,
 name=lpname('PersonHoursPerDay6', it.Index))
```



# Constraint: Limit Hours Per Site Per Day

O  
P  
L

```
forall (<s,d> in prefSitesHoursByDayIndex) {
 SiteHoursPerDay[<s,d>]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] <= 2*hours_per_site_day[<s,d>];
}
```

P  
a  
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s

```
conDF = pd.DataFrame(allvars.h.groupby(level=['site_id', 'day'])
 .aggregate(quicksum)
 .rename('thesum'))

conDF.index.names = ['id', 'day']

conDF = conDF.merge(sitehoursperday, left_index=True, right_index=True, how='left')

for it in conDF.itertuples():
 m.addConstr(it.thesum <= 2*it.hours, name=lpnamer('SiteHoursPerDay',it.Index))
```

**Use same merge technique as shown previously**

# Constraint: Limit Hours Per Week

O  
P  
L

```
forall (p in eligiblePeople) {
 TotalHoursPerWeek[p]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] <= 2*peopleData[p].total_hrs_per_week;
}
```

P  
a  
n  
d  
a  
s

```
conDF = pd.DataFrame(allvars.h.groupby(level='person_id')
 .aggregate(quicksum).rename('thesum'))

conDF.index.names = ['id']

conDF = conDF.merge(people, left_index=True, right_index=True, how='left')

for it in conDF.itertuples():
 m.addConstr(it.thesum <= 2*it.total_hrs_per_week,
 name=lpnamer('TotalHoursPerWeek',it.Index))
```

**Use same merge technique as shown previously**

# Constraint: Must be assigned for at least an hour

O  
P  
L

```
forall (<p,s,d> in allVarsIndex) {
PairDayUp[<p,s,d>]:
 h[<p,s,d>] <= blocksPerPersonSiteDay[<p,s,d>]*pairday[<p,s,d>];
PairDayLow[<p,s,d>]:
 2*pairday[<p,s,d>] <= h[<p,s,d>];
}
```

| person_id          | site_id            | day | pref | daily_hours | h                                                                   | pairday                                                               |
|--------------------|--------------------|-----|------|-------------|---------------------------------------------------------------------|-----------------------------------------------------------------------|
| MPW0000000272UORBF | ADK0000000364ICFPT | Mo  | 64   | 8.0         | <gurobi.Var<br>h[MPW0000000272UORBF,<br>ADK0000000364ICFPT,Mo]<br>> | <gurobi.Var<br>pairday[MPW0000000272UORBF,<br>ADK0000000364ICFPT,Mo]> |
|                    |                    | Tu  | 64   | 8.0         | <gurobi.Var<br>h[MPW0000000272UORBF,<br>ADK0000000364ICFPT,Tu]>     | <gurobi.Var<br>pairday[MPW0000000272UORBF,<br>ADK0000000364ICFPT,Tu]> |

P  
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```
for it in allvars.itertuples() :
 m.addConstr(it.h <= 2*it.daily_hours*it.pairday,
 name=lpnamer("PairDayUp",it.Index))
 m.addConstr(2*it.pairday <= it.h,
 name=lpnamer("PairDayLow",it.Index)) # One hour minimum
```

# Constraint: Limit on Total Days Per Week

O  
P  
L

```
forall (p in eligiblePeople) {
 TotalDaysPerWeek[p]:
 sum(<p,s,d> in allVarsIndex) pairday[<p,s,d>] <= peopleData[p].days_per_week;
}
```

P  
a  
n  
d  
a  
s

```
conDF = pd.DataFrame(allvars.pairday.groupby(level='person_id')
 .aggregate(quicksum).rename('thesum'))

conDF.index.names = ['id']

conDF = conDF.merge(people, left_index=True, right_index=True, how='left')

for it in conDF.itertuples():
 m.addConstr(it.thesum <= it.days_per_week,
 name=lpnamer('TotalDaysPerWeek[' + it.Index))
```

**Use same merge technique as shown previously**

## Constraint: If assigned to a site, must be for at least 2 days

O  
P  
L

```
forall (<p,s> in eligiblePairs) {
 ZVarUp[<p,s>]:
 2*z[<p,s>] <= sum(<p,s,d> in allVarsIndex) pairday[<p,s,d>];
 ZVarLow[<p,s>]:
 sum(<p,s,d> in allVarsIndex) pairday[<p,s,d>] <=
 card({<p,s,d> | <p,s,d> in allVarsIndex})*z[<p,s>];
}
```

Use same merge technique as shown previously.  
Compute the sum as an object

P  
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s

```
agggb = allvars.pairday.groupby(level=['person_id','site_id'])
 .agg(quicksum).rename('sumpairday')

aggzmerge = pd.merge(pd.DataFrame(agggb), pd.DataFrame(zvars),
 left_index=True, right_index=True, how='inner')

for it in aggzmerge.itertuples():
 m.addConstr(2*it.z <= it.sumpairday, name=lpnamer('ZVarUp',it.Index))
 m.addConstr(it.sumpairday <= it.sumpairday.size()*it.z,
 name=lpnamer('ZVarLow',it.Index))
```

# Constraint: Track Hours Assigned to Site

O  
P  
L

```
forall (s in eligibleSites) {
 SiteHours[s]:
 sum(<p,s,d> in allVarsIndex) h[<p,s,d>] + shortage[s] - excess[s]
 == 2*num_hours_per_site[s];
}
```

siteSlackVars

| site_id            | excess                                  | shortage                                  |
|--------------------|-----------------------------------------|-------------------------------------------|
| ADK0000000364ICFPT | <gurobi.Var excess[ADK0000000364ICFPT]> | <gurobi.Var shortage[ADK0000000364ICFPT]> |
| ADK0000000390ICFPT | <gurobi.Var excess[ADK0000000390ICFPT]> | <gurobi.Var shortage[ADK0000000390ICFPT]> |
| ADK0000000416ICFPT | <gurobi.Var excess[ADK0000000416ICFPT]> | <gurobi.Var shortage[ADK0000000416ICFPT]> |
| ADK0000000442ICFPT | <gurobi.Var excess[ADK0000000442ICFPT]> | <gurobi.Var shortage[ADK0000000442ICFPT]> |
| ADK0000000468ICFPT | <gurobi.Var excess[ADK0000000468ICFPT]> | <gurobi.Var shortage[ADK0000000468ICFPT]> |

sites

| id                 | num_hours |
|--------------------|-----------|
| TWD0000000357BVYIM | 12.0      |
| UXE0000000358CWZJN | 179.0     |
| VYF0000000359DXAKO | 171.0     |
| WZG0000000360EYBLP | 11.0      |
| XAH0000000361FZCMQ | 10.0      |

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s

```
shortageSums = pd.DataFrame(allvars.h.groupby(level='site_id')
 .agg(quicksum).rename('thesum'))

shortageSums.index.names = ['id']

conDF = (siteSlackVars
 .merge(shortageSums, left_index=True, right_index=True, how='left')
 .merge(sites, left_index=True, right_index=True, how='left')
)

for it in conDF.itertuples():
 m.addConstr(it.thesum + it.shortage - it.excess == 2*it.num_hours,
 name=lpnamer('SiteHours',it.Index))
```

# Solving

```
m.setParam(GRB.Param.TimeLimit, 300)
m.setParam(GRB.Param.CutPasses, 1)
m.optimize()
```

```
m.addConstr(quicksum(siteSlackVars.shortage) <= m.ObjVal+0.25, name='shortageBound')
m.setObjective(quicksum(siteSlackVars.excess))
```

```
resetParams()
m.setParam(GRB.Param.TimeLimit, 180)
m.setParam(GRB.Param.Presolve, 0)
m.setParam(GRB.Param.Cuts, 0)
m.optimize()
```

```
m.addConstr(quicksum(siteSlackVars.excess) <= m.ObjVal+0.25, name='excessBound')
conDF = zvars.merge(prefs, left_index=True, right_index=True, how='left')
m.setObjective(quicksum(conDF.pref*conDF.z), sense=GRB.MAXIMIZE)
```

```
resetParams()
m.setParam(GRB.Param.MIPGap, 0.01) # Set gap to 1%
m.setParam(GRB.Param.Cuts, 0)
m.setParam(GRB.Param.SubMIPNodes, 1500)
m.setParam(GRB.Param.TimeLimit, 180)
m.optimize()
```

# Solution

```
hvals = pd.Series([h.x for h in allvars.h], index=allvars.index)
pairings = hvals[hvals>0]
```

|                    |                    |     | hours |
|--------------------|--------------------|-----|-------|
| person_id          | site_id            | day |       |
| ORY0000000196WQTDH | ADK0000000364ICFPT | Th  | 4.0   |
|                    |                    | Fr  | 4.0   |
| QTA0000000146YSVFJ | ADK0000000364ICFPT | Mo  | 2.0   |
|                    |                    | Tu  | 12.0  |
|                    |                    | We  | 12.0  |
| TWD0000000123BVYIM | ADK0000000364ICFPT | Mo  | 12.0  |
|                    |                    | Th  | 12.0  |
| ADK0000000130ICFPT | ADK0000000390ICFPT | Mo  | 16.0  |
|                    |                    | Tu  | 2.0   |
| BEL0000000235JDGQU | ADK0000000390ICFPT | Tu  | 14.0  |



# Conclusion

- pandas and Python provide a powerful combination for working with data used to build optimization models
  - There are other powerful features in pandas for analyzing and organizing data
    - Reshaping, Grouping, Functions on data, plotting
- Using pandas, you can write efficient code for building optimization models
- Think Different!
  - Data FIRST
  - Model SECOND