## ECE/CS 559 Neural Networks, Fall 2017 - Homework #7 Due: 11/10/2017, the end of class.

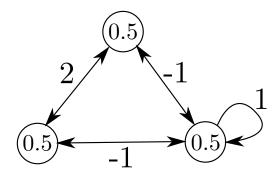
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All the notes in the beginning of Homework #1 apply. As usual, please include the computer codes in your report.

- 1. **(40pts)** Let  $\phi(x) = 1$  if  $x \ge 0$ , and  $\phi(x) = -1$  if x < 0. Consider some  $\mathbf{x}_1, \dots, \mathbf{x}_n \in \{-1, +1\}^m$ . In associative memory, we have designed the synaptic weight matrix as  $\mathbf{W} = \sum_{i=1}^n \mathbf{x}_i \mathbf{x}_i^T$ . Suppose that there exists  $\mathbf{z} \in \mathbb{R}^m$  that satisfies the following properties:
  - $\mathbf{z} = \phi(\mathbf{W}\mathbf{z})$ .
  - For any  $i \in \{1, ..., n\}$ , we have  $\mathbf{z} \neq \mathbf{x}_i$  and  $\mathbf{z} \neq -\mathbf{x}_i$ .

In class, we have called  $\mathbf{z}$  a spurious memory pattern. We never gave an example of  $\mathbf{x}_1, \dots, \mathbf{x}_n$  that results in the existence of a spurious pattern. Find such an example and show your work. You may use computer search.

2. **(60pts)** Consider the Hopfield network below. The activation function is, as usual,  $\phi(x) = 1$  if  $x \ge 0$ , and  $\phi(x) = -1$  if x < 0.



Draw the state transition diagrams (with energy levels) for both synchronous and asynchronous update rules. Indicate the urstate(s) and the steady state(s) of the network. An urstate is a state with no predecessors (i.e., if S is an urstate, then no other state, including S itself, should be able to transition to S).