

Review notes

Expert Systems

$$A \Rightarrow C$$

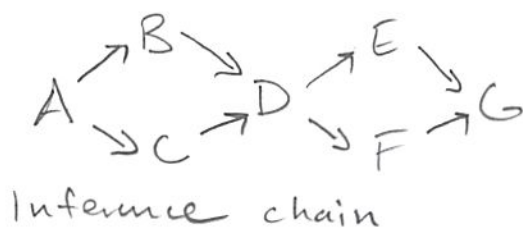
$$A \Rightarrow B$$

$$B \cup C \Rightarrow D$$

$$D \Rightarrow E$$

$$D \Rightarrow F$$

$$E \cup F \Rightarrow G$$



① Given A, carry out forward chaining.

Pass 1: $A \Rightarrow C$

$A \Rightarrow B$

no other rules can be fired.

2: $B \cup C \Rightarrow D$

3: $D \Rightarrow E$

$D \Rightarrow F$

4: $E \cup F \Rightarrow G$

$\Rightarrow A, B, C, D, E, F, G$ known

② Given B, w/ E as the goal, carry out backward chaining.

goal E: $D \Rightarrow E$, D new subgoal

D: $B \cup C \Rightarrow D$, assume C comes first just for example
C new subgoal

C: $A \Rightarrow C$, A new subgoal

A: fails

B: Fact.

③ Following ②, is F known during inference?

Backward: No

Forward: Yes

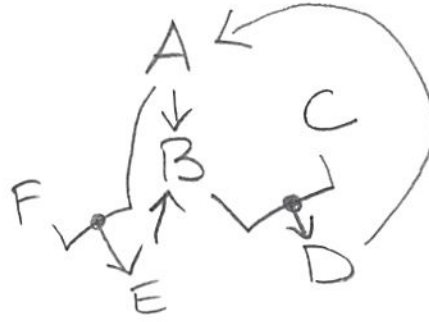
$$A \Rightarrow B$$

$$B \cap C \Rightarrow D$$

$$D \Rightarrow A$$

$$A \cap F \Rightarrow E$$

$$E \Rightarrow B$$



① B & C are fact. Carry out Forward Chaining.

Pass 1: $B \cap C \Rightarrow \underline{D}$

2: $D \Rightarrow \underline{A}$

3: $A \Rightarrow B$, already known

\Rightarrow Fact: A, B, C, D

② B & C are fact Carry out Backward chaining.
What is E?

E: $A \cap F \Rightarrow E$, A new subgoal

A: $D \Rightarrow A$, D new subgoal

D: $B \cap C \Rightarrow D$, B new subgoal

B: Fact

C: Fact, Thus, A true

F: fail

Bayes Rule

	C		$\neg C$	
	B	$\neg B$	B	$\neg B$
A	.05	.2	.15	.05
$\neg A$.1	.05	.3	.1

Hypothesis: C \Rightarrow rank: $p(C|E)$ vs. $p(\neg C|E)$

Let E be: $\neg A, \neg B$

$$\begin{aligned}
 p(C|\neg A, \neg B) &= p(\neg A, \neg B|C) p(C) / \text{data} \rightarrow \text{ignore} \\
 &= \underbrace{p(\neg A|C) p(\neg B|C)}_{\text{assump. of ind.}} p(C)
 \end{aligned}$$

$$\begin{aligned}
 P(C) &= \sum_{(A,B)} P(A,B,C) = P(A,B,C) + P(A,\neg B,C) + P(\neg A,B,C) + P(\neg A,\neg B,C) \\
 &= 0.05 + 0.2 + 0.1 + 0.05 \\
 &= 0.4
 \end{aligned}$$

$$\begin{aligned}
 P(\neg A|C) &= P(\neg A \cap C) / P(C) \\
 &= \left(\sum_B P(\neg A, B, C) \right) / P(C) \\
 &= (P(\neg A, B, C) + P(\neg A, \neg B, C)) / P(C) \\
 &= (0.1 + 0.05) / 0.4 \\
 &= 0.375
 \end{aligned}$$

$$\begin{aligned}
 P(\neg B|C) &= P(\neg B \cap C) / P(C) \\
 &= \left(\sum_A P(A, \neg B, C) \right) / P(C) \\
 &= (P(A, \neg B, C) + P(\neg A, \neg B, C)) / P(C) \\
 &= (0.2 + 0.05) / 0.4 \\
 &= 0.25 / 0.4 \\
 &= 0.625
 \end{aligned}$$

$$\begin{aligned}
 P(C|\neg A, \neg B) &= (0.375)(0.625)(0.4) / \text{data} \\
 &= 0.09375 / \text{data}
 \end{aligned}$$

Now repeat for $P(C|\neg A, \neg B)$

$$\begin{aligned}
 P(\neg C|\neg A, \neg B) &= P(\neg A, \neg B|\neg C) P(\neg C) / \text{data} \\
 &= P(\neg A|\neg C) P(\neg B|\neg C) P(\neg C) / \text{data}
 \end{aligned}$$

$$P(\neg C) = 0.15 + 0.05 + 0.3 + 0.1 = 0.6$$


$$\begin{aligned}
 P(\neg A|\neg C) &= P(\neg A, \neg C) / P(\neg C) \\
 &= (P(\neg A, B, \neg C) + P(\neg A, \neg B, \neg C)) / P(\neg C) \\
 &= (0.3 + 0.1) / 0.6 \\
 &= 0.667
 \end{aligned}$$

$$\begin{aligned}
 P(\neg B|\neg C) &= P(\neg B, \neg C) / P(\neg C) \\
 &= (P(A, \neg B, \neg C) + P(\neg A, \neg B, \neg C)) / P(\neg C) \\
 &= (0.05 + 0.1) / 0.6 = 0.25
 \end{aligned}$$

$$P(\neg C | \neg A, \neg B) = (0.667)(0.25)(0.6) / \text{data} \quad 4$$

$$= 0.10005 / \text{data}$$

$$\frac{P(\neg C | \neg A, \neg B)}{\text{data}} > \frac{P(C | \neg A, \neg B)}{\text{data}}$$


 same term
 dont bother
 a comparison

save time,
 calc. for

$$\frac{0.10005}{\text{data}} \rightarrow 0.09375 ?$$

$\neg C$