μ/π separation using

Convolutional Neural Networks

for the MicroBooNE Charged Current Inclusive Cross Section Measurement

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DISSERTATION

Submitted in partial fulfillment of the requirements for the degree Doctor of Philosophy in Physics

- * - DRAFT December 16, 2017 - * -

December, 2017 Syracuse University Syracuse, New York

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Abstract

The purpose of this thesis was to use Convolutional Neural Networks (CNN) to separate $\mu's$ and $\pi's$ for use in increasing the acceptance rate of $\mu's$ below the implemented 75cm track length cut in the Charged Current Inclusive (CC-Inclusive) event selection for the CC-Inclusive Cross-Section Measurement. In doing this, we increase acceptance rate for CC-Inclusive events below a specific momentum range.



Dedication

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I dedicate this dissertation to the two important women in my life; My wife and my mom. Both have been there cheering me on giving me strength and love as I worked towards the hardest accomplishment I've ever done.

Jessica Nicole Esquivel



Acknowledgements

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Of the many people who deserve thanks, some are particularly prominent, such as my supervisor...

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"If the don't give you a seat at the table, bring a folding chair."

— Shirley Chisholm

bring a folding chair."
— Shirley Chisholm

²⁷⁷ Chapter 1

₇₈ Introduction

This thesis will be a description of work done to further increase efficiency and purity 279 of the charged current inclusive cross section measurement using the MicroBooNE 280 detector. It will also describe the MicroBooNE detector, what neutrinos are, the charged 281 current inclusive cross section measuremnt and it's importance as well as convolutional 282 neural networks and how they can be used in μ/π separation. Chapter 2 will talk 283 about the background of neutrinos and the people and detectors that discovered 284 neutrinos as well as an in depth history of neutrino oscillation and the discovery that 285 neutrinos have mass. Chapter 3 will discuss the MicroBooNE experiement, specifically, 286 how Liquid Argon Time Projection Chambers work, the Light Collection System and 287 the Electronic and Readout Trigger systems. Chapter ?? will describe the Booster 288 Neutrino Beam sationed at Fermi National Accelerator Lab. Chapter 4 will discuss the 289 work that was done to detect the first neutrinos seen in the MicroBooNE detector and the software reconstruction efforts required to create an automated neutrino ID filter 291 that was used to find the first neutrinos and then was later expanded on to create the 292 charged current inclusive filter that will be discussed in chapter 5 Chapter 6 will give a 293 brief description of what Convolutional Neural Networks are and how it will be used 294 for μ/π separation in this selection. Chapter 7 will discuss the hardware frameworks 295 and training methods used to train multiple Convolutional Neural Networks for use 296 in the charged current inclusive cross section measurement. Chapters 8, 9 and 10 will 297 discuss the results of using Convolutional Neural Networks on monte-carlo and data to sift out charged current inclusive neutrino events.

Chapter 2

^₃ Neutrinos

2.1 What are Neutrinos

Neutrinos are one of the fundamental particles which make up the universe. They are also one of the least understood. Neutrinos are not affected by the electromagnetic forces because they do not have electric charge. Neutrinos are affected by a "weak" sub-atomic force of much shorter range than electromagnetism, and are therefore able to pass through great distances in matter without being affected by it. Until the late 90's, neutrinos were thought to have no mass. Due to their mass, neutrinos are also affected by gravity. Neutrinos are created by radioactive decay or nuclear reactions such as the ones that happen in the sun, in nuclear reactors or when cosmic rays hit atoms. There are three types of neutrinos, ν_e , ν_μ and ν_τ which correspond to their charged lepton pairs.

As previously stated, neutrinos are very weakly interacting; in fact, neutrinos can pass unscathed through a wall of lead several hundred light-years thick. Because neutrinos interact so rarely, studying neutrinos requires a massive detector and a powerful neutrino source. With that being said, we can only infer their existence when they interact in a detector. In a collision, distinct charged particles are produced with each type of neutrino. An electron neutrino will create an electron, a muon neutrino will create a muon, and a tau neutrino will create a tau. The track the particle leaves in the detector is how one figures out what type of neutrino interaction was "seen". Liquid Argon Time Projection Chambers are the newest type of detectors being used to study neutrinos due to their excellent imaging and particle identification capabilities.

2.2 History of Neutrinos

The neutrino was first postulated by Wolfgang Pauli in 1931 to explain how beta 324 decay could resolve the conservation of energy, momentum and angular momentum problem. Pauli suggested that this missing energy might be carried off, unseen, by a 326 neutral particle (he called neutron) which was escaping detection. James Chadwick 327 discovered a much heavier nuclear particle in 1932 that he also named neutron, leaving 328 two particles with the same name. Enrico Fermi was the first person to coin the 329 term neutrino (which means little neutral one in latin) in 1933 to fix this confusion. Fermi's paper, which was published in 1934, unified Pauli's neutrino with Paul Dirac's 331 positron and Werner Heisenberg's neutron-proton model and his theory accurately 332 explained many experimentally observed results. Wang Ganchang first proposed the use of beta capture to experimentally detect neutrinos and in 1959 Clyde Cowan and 334 Frederick Reines published their work stating that they had detected the neutrino. 335 The experiment called for antineutrinos created in a nuclear reactor by beta decay that 336 reacted with protons producing neutrons and positrons: $\nu_e + p^+ \rightarrow n^0 + e^+$. Once 337 this happens, the positron finds an electron and they annihilate each other and the resulting gamma rays are detectable. The neutron is detected by neutron capture and 339 the releasing of another gamma ray. In 1962 Leon M. Lenderman, Melvin Schwartz and Jack Steinberger were the first to detect interactions of the muon neutrino. The first detection of the tau neutrino was announced in the summer of 2000 by the 342 DONUT collaboration at Fermilab. In the late 1960s, many experiments found that the number of electron neutrinos arriving from the sun was around 1/3 to 1/2 the number 344 predicted by the Standard Solar Model. This became known as the solar neutrino 345 problem and remained unresolved for around thirty years. This problem was resolved by the discovery of neutrino oscillation and mass. [1]

2.3 Neutrino Oscillations

Neutrino oscillation was first predicted by Bruno Pontecorvo. It describes the phenomenon of a neutrino created with a specific lepton flavor (electron, muon or tau) that is later measured to have a different flavor. Neutrino oscillation is important theoretically and experimentally due to the fact that this observation implies that the neutrino has a non-zero mass, which is not part of the original Standard Model of particle physics. [2]

2.3.1 Solar Oscillations and the Solar Neutrino Problem

The solar neutrino flux derived from Bahcall's Standard Solar Model is shown in figure 2.1. Nuclear fusion and decay processes produce an abundant amount of neutrinos. The standard solar model predicts that these reactions produce several groups of neutrinos, each with differing fluxes and energy spectra. The figure also shows the ranges of detection of existing solar neutrino experiments in different shades of blue to illustrate that they sample different portions of the solar neutrino energy spectrum. Three of these experiments, plus a new one, are discussed below.

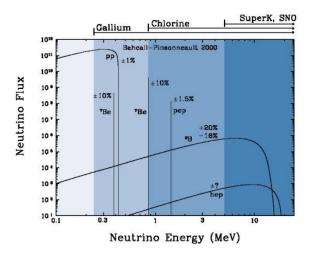


Figure 2.1: The Standard Solar Model

Since neutrinos rarely interact with matter, they pass through the sun and the earth undetected. About 65-billion neutrinos from the sun stream through every square centimeter on the Earth every second, yet we are oblivious to their passage in our every-day lives. [3]

The first experiment to detect the effects of neutrino oscillation was the Ray Davis's Homestake Experiment. The detector was stationed in the Homestake Gold Mine in Lead, South Dakota. It was 1,478 meters underground and was 380 m^3 . The detector was filled with perchloroethylene. Perchloroethylene was chosen because of it's high concentrations of chlorine. When an ν_e interaced with chlorine-37 atom, the atom would transform to argon-37 which was then extracted and counted. The neutrino capture reaction is shown in equation 2.1. Davis observed a deficit of about 1/3 the flux of solar neutrinos that was predicted by Bahcall's Standard Solar Model.

The unexplained difference between the measured solar neutrino flux and model predictions lead to the Solar Neutrino Problem. [4]

$$\nu_e + {}^{37}Cl \rightarrow {}^{37}Ar + e^-$$
 (2.1)

While it is now known that the Homestake Experiment detected neutrinos, some physicist were weary of the results. Conclusive evidence of the Solar Neutrino Problem was provided by the Kamiokande-II experiment, a water Cherenkov detector with a low enough energy threshold to detect neutrinos through neutrino-electron elastic scattering. In the elastic scattering interaction the electrons coming out of the point of reaction strongly point in the direction that the neutrino was traveling, away from the sun. While the neutrinos observed in Kamiokande-II were clearly from the sun, there was still a discrepancy between Kamiokande-II and Homestake; The Kamiokande-II experiment measured about 1/2 the predicted flux, rather than the 1/3 that the Homestake Experiment saw.

The solution to the solar neutrino problem was finally experimentally determined by the Sudbury Neutrino Observatory(SNO). The Ray Davis's Homestake Experiment was only sensitive to electron neutrinos, and the Kamiokande-II Experiment was dominated by the electron neutrino signal. The SNO experiment had the capability to see all three neutrino flavors. Because of this, it was possible to measure the electron neutrinos and total neutrino flux. The experiment demonstrated that the deficit was due to the MSW effect, the conversion of electron neutrinos from their pure flavor state into the second neutrino mass eigenstate as they passed through a resonance due to the changing density of the sun. The resonance is energy dependent, and is visible near 2MeV. The water cherenkov detectors only detect neutrinos above about 5MeV, while the radiochemical experiments were sensitive to lower energy (0.8MeV for chlorine, 0.2MeV for gallium), and this turned out to be the source of the difference in the observed neutrino rates at the two types of experiments. Figure 2.2 shows Homestake, Kamiokande-II and SNO experiments.

MSW Effect

The Mikheyev-Smirnov-WOlfenshein effect is a process which acts to modify neutrino oscillations in matter. The presence of electrons in matter changes the energy

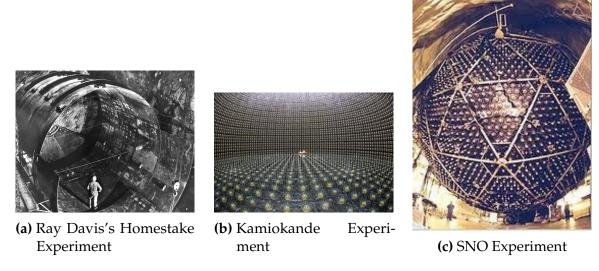


Figure 2.2: Solar Neutrino Experiments

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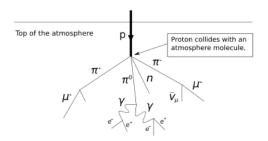
levels of the mass eigenstates of neutrinos due to charged current coherent forward scattering of the electron neutrinos. This coherent forward scattering is similar to the electromagnetic process with respect to the refractive index of light in a medium. Because of this MSW Effect, neutrinos in vacuum have a different effective mass than neutrinos in matter and because neutrino oscillations depend on the squared mass difference of the neutrinos, the neutrino oscillations are different in matter than in vacuum. This effect is important at the sun where electron neutrinos are produced. The neutrinos of high energy leaving the sun are in a vacuum propagation eigenstate v_2 that has a very small overlap with the electron neutrino $v_e = v_1 cos(\theta) + v_2 sin(\theta)$ seen by the charged current reactions in Kamiokande-II and SNO. The discrepancy of the deficit between SNO, Kamiokande-II and Homestake is due to the energy of the solar neutrinos. The MSW effect "turns on" at about 2MeV and at lower energies, this MSW effect is negligible. [5]

2.3.2 Atmospheric Oscillations and the Atmospheric Neutrino Anomaly

Atmospheric neutrinos are neutrinos that stem from the decay hadrons coming from primary cosmic rays. The dominant part of the decay chain is shown in equations 2.2 and 2.3

$$\pi^+ \to \mu^+ \nu_u \mu^+ \to e^+ \nu_e \overline{\nu_u} \tag{2.2}$$

 $\pi^- \to \mu^- \overline{\nu_u} \mu^- \to e^- \overline{\nu_e} \nu_u \tag{2.3}$



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Figure 2.3: Cosmic Ray Shower

Figure 2.3 shows the cosmic ray shower. In general, these neutrinos have energies from 1GeV to 100s of GeV and the ratio of v_{μ} s to v_{e} s equals to 2 (see equation 2.4)

$$R = \frac{(\nu_{\mu} + \overline{\nu_{\mu}})}{(\nu_{e} + \overline{\nu_{e}})} \tag{2.4}$$

There have been two types of detectors used to study atmospheric neutrinos: Water Cherenkov detectors and tracking calorimeters. Super-Kamiokande is the detector we will focus on. These atmospheric detector experiments measure the ratio of ν_{μ} to ν_{e} . They also measure the zenith angle distribution of the neutrinos. These experiments report a double ratio (shown in equation 2.5). This double ratio is the ratio measured in the detector to the ratio thats expected which is 2. If the double ratio equals to 1, the data agrees with the prediction. Various measurements from multiple experiments are shown in figure 2.4. Except for Frejus, all R measurements are less than 1. This discrepancy between the predicted R and the measured R became known as the Atmospheric Neutrino Anomaly.

$$R = \frac{(N_{\mu}/N_{e})_{DATA}}{(N_{\mu}/N_{e})_{SIM}}$$
 (2.5)

Kamiokande-II has the the capability of measuring the direction of the incoming neutrinos. The expectation of atmospheric neutrino detection is that the flux be

Experiment	Type of experiment	R
Super-Kamiokande	Water Cerenkov	0.675 ± 0.085
Soudan2	Iron Tracking Calorimeter	0.69 ± 0.13
IMB	Water Cerenkov	0.54 ± 0.12
Kamiokande	Water Cerenkov	0.60 ± 0.07
Frejus	Iron Tracking Calorimeter	1.0 ± 0.15

Figure 2.4: Measurments of the double ratio for various atmospheric neutrino experiments

isotropic due to the fact that atmospheric neutrinos can reach the detector from all 437 directions. Kamiokande-II noticed that muon-like data did not agree well with this 438 expectation. At low energies approximately half of the ν_{μ} are missing over the full range of zenith angles. At high energies the number of v_u coming down from above 440 the detector seems to agree with expectation, but half of the same v_{μ} coming up from 441 below the detector are missing. This anomaly can be easily explained by neutrino 442 flavor oscillations. Due to the fact that the neutrino travels less distance coming 443 straight down into the detector (about 15km) than coming up from the bottom of the detector(13000km) changes the probability of oscillation. The probability of oscillation 445 for the muon neutrinos coming down into the detector is roughly zero, whereas 446 for neutrinos coming up, the oscillation probability is $sin^2(2\theta)$. Both the solar and atmospheric neutrino problems can be explained by neutrino oscillation so its fitting 448 to derive this phenomenon mathematically. In the next two sections, two flavor and three flavor neutrino oscillation derivations will be explained. 450

51 2.3.3 Two Flavor Neutrino Oscillation Formulation

The flavor eigenstates can oscillate between eachother because they are composed of an add-mixture of mass eigenstates(ν_1, ν_2). Figure 2.5 shows the mass and flavor eigenstates rotated by an angle θ which is the mixing angle.

In matrix form the wavefunctions are:

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$$\begin{pmatrix} \nu_{\mu} \\ \nu_{e} \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} * \begin{pmatrix} \nu_{1} \\ \nu_{2} \end{pmatrix} \tag{2.6}$$

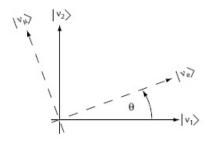


Figure 2.5: The flavor eigenstates are rotated by an angle θ with respect to the mass eigenstates

Applying the time evolution operator to ν_{μ} :

$$|\nu_{\mu}(t)> = -\sin\theta |\nu_{1}> e^{-i\frac{E_{1}t}{\hbar}} + \cos\theta |\nu_{2}> e^{-i\frac{E_{2}t}{\hbar}}$$
 (2.7)

where $E_1 = \sqrt{p^2c^2 + m_1^2c^4}$ and $E_2 = \sqrt{p^2c^2 + m_2^2c^4}$ and $p_1 = p_2$. For the time being, let us assume $\hbar = c = 1$. With this assumption: $E_1 = \sqrt{p^2 + m_1^2}$ and $E_2 = \sqrt{p^2 + m_2^2}$. The next modifications is to assume neutrinos are relativistic:

$$\gamma = \frac{E}{m_o^2 c^2} = \frac{\sqrt{p^2 c^2 + m_o^2 c^4}}{m_o c^2} \gg 1 \tag{2.8}$$

because of this,

$$p \gg m_o \tag{2.9}$$

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$$E = \sqrt{p^2 + m_o^2} = p\sqrt{1 + m_o^2/p^2} \simeq p + \frac{1}{2}\frac{m_o^2}{p}$$
 (2.10)

where the binomial expansion is used. Now E_1 and E_2 can be written as:

$$E_1 \simeq p + \frac{1}{2} \frac{m_1^2}{p}$$
 and $E_2 \simeq p + \frac{1}{2} \frac{m_2^2}{p}$ (2.11)

Now applying all these assumptions back into equation 2.7 gives us:

$$|\nu_{u}(t)\rangle = -\sin\theta |\nu_{1}\rangle e^{-i\left(p + \frac{1}{2}\frac{m_{1}^{2}}{p}\right)t} + \cos\theta |\nu_{2}\rangle e^{-i\left(p + \frac{1}{2}\frac{m_{2}^{2}}{p}\right)t}$$
(2.12)

$$|\nu_{\mu}(t)\rangle = e^{-i\left(p + \frac{1}{2}\frac{m_{1}^{2} - m_{2}^{2}}{p}\right)t}\left(-\sin\theta|\nu_{1}\rangle + \cos\theta|\nu_{2}\rangle\right)$$
 (2.13)

Substituting $\Delta m^2 = m_1^2 - m^2 2$ and $t = \frac{x}{c} = x$ and $e^{-iz} = e^{-i\left(p + \frac{1}{2}\frac{m_1^2}{p}\right)t}$ gives us:

$$|\nu_{\mu}(t)\rangle = e^{-iz} \left(-\sin\theta |\nu_1\rangle + \cos\theta |\nu_2\rangle e^{+ix\left(\frac{1}{2}\frac{\Delta m^2}{p}\right)} \right) \tag{2.14}$$

Finding the Probability for a $u_{\mu}
ightarrow
u_{e}$:

$$P(\nu_{\mu} \to \nu_{e}) = |\langle \nu_{e} | \nu_{\mu}(t) \rangle|^{2}$$
 (2.15)

Remembering that $< v_i | v_j > = \delta_{ij}$

$$<\nu_{e}|\nu_{\mu}(t)>=e^{-iz}\left(-sin\theta cos\theta+sin\theta cos\theta e^{\frac{i\Delta m^{2}x}{p}}\right)$$
 (2.16)

Taking the absolute value squared gives us:

$$P(\nu_{\mu} \to \nu_{e}) = |\langle \nu_{e} | \nu_{\mu}(t) \rangle|^{2} = e^{+iz} e^{-iz} \sin^{2}\theta \cos^{2}\theta \left(-1 + e^{\frac{i\Delta m^{2}x}{p}} \right) \left(-1 + e^{\frac{i\Delta m^{2}x}{p}} \right)$$
(2.17)

Since the neutrino is relativistic we can set $p = E_{\nu}$ and change x = L. Also recognizing the trigonometric relation $(1 - cos2\theta)/2 = sin^2\theta$ the above equation becomes:

$$P(\nu_{\mu} \rightarrow \nu_{e}) = \sin^{2}2\theta \sin^{2}\left(\frac{\Delta m^{2}L}{4E_{\nu}}\right) \tag{2.18}$$

All that's left to do now is re-introduce \hbar and c doing this we get:

$$P_{\nu_{\mu} \to \nu_{e}}(L, E) = \sin^{2}2\theta \sin^{2}\left(1.27\Delta m^{2} \frac{L}{E_{\nu}}\right)$$
(2.19)

This equations has three important variables.

• The angle θ : This angle, as mentioned before, is called the mixing angle. It defines the difference between the flavor and the mass eigenstates. When $\theta = 0$ the mass and flavor eigenstates are identical and now oscillations occur.

- The mass squared difference, Δm^2 : Again $\Delta m^2 = m_1^2 m_2^2$. The reason this is an important variable is because it implies that for neutrinos to oscillate, neutrinos must have mass. Furthermore, the mass squared difference also tells us that the neutrino mass eigenstates must be different.
- L/E: This is the variable that is of most interest to experimental physicists due to the fact that it is the variable that we set. L is the distance between the source and detector and E is the energy of the neutrino. For a given Δm^2 , the probability of oscillation changes with respect to L/E.

2.3.4 Three Flavor Neutrino Oscillation Formulation

Seeing the quantum mechanics involved in deriving the probability of a two flavor neutrino oscillation, it is now possible to formulate the three flavor neutrino oscillation. The three flavor neutrino oscillation formulation begins similarly to the two flavor, but there is the Pontecorvo-Maki-Nakagawa-Sakata matrix (PMNS) instead of the 2X2 matrix in the previous section. The PMNS matrix is show below:

$$\begin{pmatrix}
c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\
-s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\
s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13}
\end{pmatrix} * \begin{pmatrix}
e^{i\alpha_{1}/2} & 0 & 0 \\
0 & e^{i\alpha_{2}/2} & 0 \\
0 & 0 & 1
\end{pmatrix}$$
(2.20)

where $c_{ij} = cos\theta_{ij}$ and $s_{ij} = sin\theta_{ij}$

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Following the same steps as before we get:

$$P_{\alpha \to \beta} = \delta_{\alpha\beta} - 4\Sigma Re(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) sin^2 \left(\frac{\Delta m_{ij}^2 L}{4E}\right) 2\Sigma Im(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) sin \left(\frac{\Delta m_{ij}^2 L}{2E}\right)$$
(2.21)

The main things to notice here are δ_{ij} which is the CP violating term and has not been measured yet, and θ_{13} which has just been measured. CP violation is a violation

Neutrinos 13

of the postulated CP-symmetry. CP-symmetry states that the laws of physics should be the same if a particle were to be exchanged with its antiparticle and then if the left hand side of a decay were switched with the right hand side.

97 2.3.5 Reactor Oscillation

Many experiments have searched for oscillation of electron anti-neutrinos produced at nuclear reactors. Such oscillations give the value of the parameter θ_{13} . The KamLAND experiment, started in 2002, has made a high precision observation of reactor neutrino oscillation. Neutrinos produced in nuclear reactors have energies similar to solar neutrinos, a few MeV. The baselines of these experiments have ranged from tens of meters to over 100 km. On 8 March 2012, the Daya Bay team announced a 5.2σ discovery that $\theta_{13} \neq 0$.

505 Chapter 3

™ The MicroBooNE Experiment

The purpose of this chapter is to discuss and understand the details of the MicroBooNE detector. A thorough understanding of MicroBooNE and the technology behind liquid argon time projection chambers is important for understanding results as well as understanding how images were made for use in deep learning efforts that will be outlined in later chapters.

512 3.1 Liquid argon time projection chambers

Liquid Argon Time Projection Chambers (LArTPCs) are an exciting detector technol-513 ogy that provide excellent imaging and particle identification, and are now being 514 used to study neutrinos. The Time Projection Chamber (TPC) was first invented by 515 Nygren in 1974 [?] and the proposal for a LArTPC for neutrino physics was made 516 by Rubbia [?] in 1977 with the ICARUS collaboration implementing this concept [?]. 517 A LArTPC is a three-dimensional imaging detector that uses planes of wires at the 518 edge of an active volume to read out an interaction. When a neutrino interacts with an 519 argon atom, the charged particles that are produced ionize the LAr as they travel away 520 from the interaction. By placing a uniform electric field throughout the LAr volume, the ionization is made to drift towards a set of anode planes, which consist of wires 522 spaced very closely together collecting the ionized charge, which is subsequently read 523 out by electronics connected to the anode wires. The collected ionization creates a 524 spatial image of what happened in the detector on each anode plane. The position 525 resolution of the interaction along the beam direction (perpendicular to drift direction) relies on the wire pitch, while the resolution in drift direction is dependent on the

timing resolution of the electronics used and the longitudinal diffusion in the volume. 528 The drift time of the ionization relative to the time of the original signal allows the 529 signal to be projected back along the drift coordinate, hence the name LArTPC. Having 530 very small distances between each wire within an anode plane allows for very fine 531 granularity and detail to be captured, and having multiple wire planes at different angles provides independent two-dimensional views that can be combined into a 533 three dimensional picture of the interaction. Once the charge signal is created on the 534 anode planes, software analysis packages identify particles in the detector by using 535 deposited energy on the wires along their track length. The 30 year development of the 536 ICARUS detector has led to LArTPCs being used as cosmic ray [?], solar neutrino [?] 537 and accelerator neutrino [?] detectors. The ArgoNeuT experiment at Fermilab was 538 the first United States based liquid argon neutrino program that has since produced 539 short-baseline $\nu - Ar$ cross-section measurements in the NUMI beamline [?]. The MicroBooNE experiment is the second experiment in the US based LArTPC neutrino 541 program and will be discussed thoroughly in the next sections. The next phases of the liquid argon neutrino program are under way and are the Fermilab Short Base-543 line Neutrino (SBN) program [?] and the Deep Underground Neutrino Experiment 544 (DUNE) [6]. The SBN program will include three LArTPC detectors, including the MicroBooNE detector, on the Booster Neutrino Beam (BNB) to do multiple-baseline 546 oscillation measurements. The detector closest to the beam will be the 40 ton Short 547 Baseline Neutrino Detector (SBND) [?] at 150 m and the detector furthest is the 600 ton ICARUS T600 [?] detector positioned at 600 m. The DUNE collaboration will deliver 549 a 30 GeV neutrino beam 1300 km from Fermilab to a 34 kiloton LArTPC detector at Homestake, SD. DUNE will study the leptonic CP phase, δ_{cp} , as well as measure 551 neutrino and antineutrino oscillations.

3.2 The MicroBooNE Time Projection Chamber

MicroBooNE (Micro Booster Neutrino Experiment) is a 89 ton active volume (180 ton total mass) LArTPC which is then inserted into a cylindrical crysotat on axis of the Booster Neutrino Beam (BNB) stationed at Fermilab in Batavia, Illinois. Understanding LArTPC technology and detector physics is necessary to build a LArTPC the size of DUNE, and MicroBooNE has made many advances in developing this technology [7] [8].

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MicroBooNE's Time Projection Chamber (TPC) is 10.3 m long (beamline direction), 2.3 m high and 2.5 m wide (which corresponds to the drift distance). The TPC is shown in figure ??. MicroBooNE is the largest LArTPC currently running in the world [9]. This LArTPC has 3 wire planes: 1 plane that collects the ionization in the wires and is 0° to the virtical with 3456 wires spaced 3 mm apart, and 2 planes where the ionization drifts passed and induces a signal at $\pm 60^{\circ}$ to the vertical each with 2400 wires also spaced 3 mm apart. Each plane has a spacing also of 3 mm from eachother. The first two planes are the induction planes and the last is the collection. The 270 V/cm electric field of the TPC is created using 64 stainless steel tubes shaped into rectangules around the TPC and held in place by G10 to form a field cage. The cathode is charged at a high voltage of -70 kV and this voltage is stepped down across the field cage tubes using a voltage divider chain with an equivalent resitance of 240 $M\Omega$ between the tubes. The field cage tubes are separated by 4 cm from center to center. The electron drift distance is 2.5 m in the x direction with a drift time of 2.3 ms. Maintaining high charge yield is done by continuously recirculating and purifying the argon. The purity is monitored using MicroBooNE's light collection system. Another use of the light collection system is initial timing and drift coordinate of the interaction.

MicroBooNE's light collection system is a crucial part for 3D reconstruction of all particle interactions in the LArTPC. The initial interaction time, t_0 , and initial drift coordinate, x_0 , are not known from the TPC alone. For beam events, the accelerator clock is used to determine t_0 of the interaction and the x_0 can be inferred using drift time. Non-beam events, however, do not have this capability, which is why scintillation light from an interaction is used. The $\nu-Ar$ interaction produces scintillation light which is collected by photomultiplier tubes (PMTs) which allows the exact time, t_0 of the neutrino interaction to be determined. The scintillation light created propogates within nanoseconds to the light collection system compared to the milliseconds it takes the ionized electrons from the interaction to reach the anode wire planes. Therefore we can precisely know where along the drift direction the particle interaction first took place. The scintillation light is also localized, so combining the PMT information with the wire plane information allows for cosmic background rejection happening outside the beam timing window.

The light collection system is made up of 32 Hammamatsu R5912-02mod cryogenic PMTs with a diameter of 8-inches. The PMTs are located behind the 3 wire anode planes and provides 0.85% photocathode coverage. Each PMT has an acrylic plate mounted in front of it that is coated with a wave-length shifting material called TPB.

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The acrylic plates take in the scintillation light, at 128 nm, and re-emits it visible wavelengths visible to the PMTs, with a peak at 425 nm.

Both the light collection system and the TPC create analog signal that is read out and digitized by the electronics system. The process requires amplification and shaping of the signal which then is goes to the data aquisition (DAQ) software for writing of the digitized data to disk. The anode plane wires are connected to detector specific circuit boards (ASICS) that are submerged and operate inside the liquid argon volume. These ASICS send amplified signal to 11 feed-throughs where further amplification of the signal happens outside the cryostat. The signal is received by custom LArTPC readout modules distributed over nine readout crates which do the digitization. The TPC wires are digitized at 16 MHz then downsampled to 2 MHz. The TPC system reads out 4 frames of wire signal data per event, 1 frame before a trigger and 2 frames after the triggered frame. The four frames allows for identification of a neutrino interaction as well as cosmic background rejection. The process of digitization is similar for the light collection system. Each PMT signal undergoes a shaping with a 60 ns peaking time for digitization of multiple samples. The digitization occurs at 64 MHz but are not read out continuously during the TPC readout time. Only shaped PMT signal samples above a small threshold are read out and saved. Both the TPC and PMT readouts are initiated via triggers on a separate trigger board located in a warm electronics crate. The timing trigger is created by a timing signal from the BNB accelerator which is shaped and sent to the trigger board. The PMT trigger is generated when the PMT signal multiplicity is greater than 1 and the summed PMT pulse-height is more than 2 photo-electrons summed up over all PMT channels. When the trigger board gets both a timing trigger and a PMT trigger in coincidence, at BNB trigger is then generated by the board. This signal is then passed to all readout crates intiating the readout of data. The data is then sent to the DAQ software which then saves the data to disk into one event memory.

3.3 MicroBooNE's Physics Goals

3.3.1 The low-energy excess

The primary goal of the MicroBooNE experiment is to study and investigate the lowenergy excess seen in MiniBooNE. MicroBooNE has the capability of confirming or

denying this excess as electrons or photons due to the detector being in the same beam, 626 having a similar baseline, and lastly the detector being able to clearly distinguish 627 between electrons and photons. LArTPCs use the topology of events as well as energy 628 loss near the vertex to differentiate petween single e^- tracks and photon-induced 629 induced pair production $\gamma \to e^+e^-$, which wasn't possible in MiniBooNE, a Cherenkiv detector. This technique has been shown in the ArogoNeuT detector [?] and a side by 631 side comparison of both event types in a LArTPC can be seen in figure ??. An excess in electrons would point towards new oscillation physics beyond the standard model, 633 while photons would be within the standard model. MicroBooNE will ovserve a 4-5 σ 634 signal.

3.3.2 Cross sections

MicroBooNE's neutrino cross-section program will be the first $\nu-Ar$ cross-section in the 1 GeV energy range and one of only a few cross-section measurements of $\nu-Ar$ in the world. MicroBooNE is also the first liquid argon detector to collect the highest statistics sample of neutrino interactions. Investigating final-state-interactions in the 1 GeV energy range provides information about short range nuclear correlations that affect the interpretations of neutrino oscillation experiment data.

3.3.3 Astroparticle physics

99% of energy leaving a supernova leaves in the form of neutrinos which can be seen by detectors on earth's surface. MicroBooNE will have a dedicated supernova data stream and a connection to the SuperNova Early Warning System [?] so when a nearby supernova explosion occurs, continuous data will be written for several hours that can be later analyzed for supernova neutrino events. This information coupled with information from other experiments can be used to better understand supernovae.add infograph of supernova here

551 3.3.4 Liquid argon detector development

The last physics goal for the MicroBooNE collaboration is to provide important information regarding LArTPC technology. Being the first in large scare LArTPCs in the US,

MicroBooNE will be albe to provide improvements to High Voltage (HV) distribution,
Noise Characterization [?], and Michel Electron Reconstruction [8].

556 3.4 The Booster Neutrino Beam

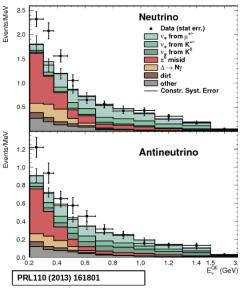
The MicroBooNE detector is stationed at Fermi National Accelerator Laboratory (FNAL) where it receives neutrinos from both the Booster Neutrino Beam (BNB) and Neutrinos from the Main Injector (NuMI) beams. MicroBooNE is on-axis for the BNB and off-axis by 135 mrad for NuMI. For the purpose of this analysis, only data from the BNB was used. This section will discuss how neutrinos are created using the BNB. How these neutrinos are produced as well as their flux through the MicroBooNE detector is necessary for any analysis because of the systematic uncertainties the beam introduces to a measurement.

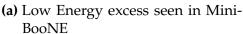
55 3.4.1 Creating the Booster Neutrino Beam

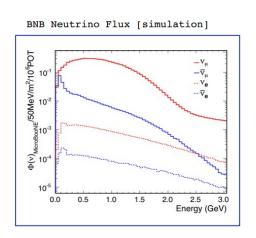
The BNB is a very pure ν_{μ} beam, with only 0.6% contamination from $\nu_{e}s$. The energy 666 also peaks around 700 MeV which is desired based on the probability of oscillation 667 equation which depends on the the value of L/E, where L is the distance of the 668 detector from the neutrino beam and E is the energy of the neutrino beam. L/E was 669 chosen to increase the probability of seeing neutrino oscillations in the MiniBooNE 670 Low Energy Excess (LEE) range based on the probability of oscillation equation, which is $P_{\nu_{\mu} \to \nu_{e}}(L, E) = \sin^{2} 2\theta \sin^{2} \left(1.27\Delta m^{2} \frac{L}{E_{\nu}}\right)$. The BNB collides 8.9 GeV/c momentum 672 protons from the FNAL booster synchrotron into a beryllium target which produces a 673 high flux of neutrinos. The protons originate from H^2 gas molecules that are turned 674 into H^- ions by a Cockroft-Walton generator shown in figure ??. The H^- initially are 675 accelerated to 1MeV kinetic energy and are then passed to a linear accelerator using alternating electromagnetic fields to increase their energy to 400MeV. The ions are 677 stripped of electrons by passing them through a carbon foil. The protons are bunched 678 into beam spills which contain $4*10^{12}$ protons in a 1.6 µs time window per spill. It's at this point that the protons are directed towards the beryllium target. The amount 680 of protons directed towards the target (POT) is measured by two toroids upstream of 681 the target with an error of 2%. Beam intensity, timing, width, position, and direction 682 are monitored by beam position monitors, multi-wire chamber and resistive monitors. 683

The beryllium target is 71.1 cm long, 1.7 proton interaction lengths, and is 0.51 cm in radius. The target is located inside a larger focusing electromagnet called the horn. THe horn is an aluminum alloy pulsed toroidal electromagnet. The pulsed current peaks at 170 kA with a time-width of 143 µs which coincides with the protons arriving on the target. The current flows from the inner conductor to the outer conductor with a maximum magnetic field of 1.5 Tesla. The magnetic field focuses the charged secondary particles produced by the p-Be interactions. The direction of current can be switched to changed to polarity of the secondary particles being focused creating a beam of either primarily neutrinos, with positively charged secondary particles, or antineutrinos.

Further down the beamline is a concrete collimator which absorbs particles not necessary to the neutrino flux. The collimator is 214 cm long and 30 cm in radius. After the collimator comes a 45 meter long, 1 meter raduis, air-filled cylindrical decay region which then ends in a beam-stop made of steam and concrete. The beam-stop contains an array of gas proportional counters to detect muons. add beam diagram here







(b) Energy spectrum of the Booster Neutrino Beam at Fermi National Laboratories

Figure 3.1: 3.1b Flux of BNB at FNAL.

3.5 Event Reconstruction

Chapter 4

Neutrino Identification: Finding MicroBooNE's first Neutrinos

The goal of the Neutrino Identification analysis was to positively identify BNB neutrino interactions in the MicroBooNE detector collected during the first days of running. 705 Neutrino event candidates were identified in part by using a cut on detected flash of 706 scintillation light during the 1.6 µs beam-spill length of the BNB as well as identifying reconstructed object from the TPC that are neutrino like. After this selection, 2D 708 and 3D event displays were used for verification of the selection performance. This 709 selection was targeted to reduce the ratio of neutrino events to cosmic-only events from 710 the initial 1 neutrino to 675 cosmics to a ratio of 1 to 0.5 or better which is equivalent to 711 a background reduction by a factor of 1000 or more. These selected events were used for MicroBooNE's public displays of neutrino interactions. A clearly visible neutrino 713 interaction with an identifiable vertex and at least 2 tracks originating from the vertex 714 was what the analysis focused on. This analysis wasn't optimized for high purity 715 or efficiency, but rather for very distinguishable neutrino interactions that could be identified by the public.

718 4.1 Flash Finding

Flash finding is the first step used in finding neutrino interactions. This section will detail how optical information is reconstructed as well as analysis scripts and event filters were used.

22 4.1.1 Flash Reconstruction

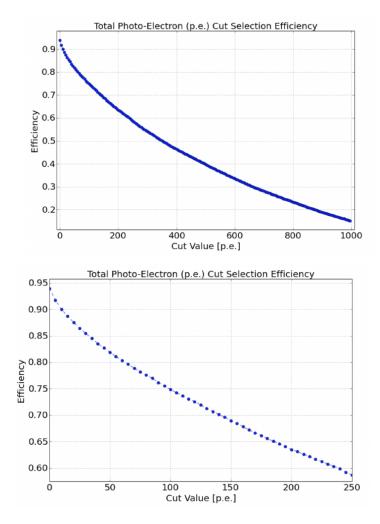
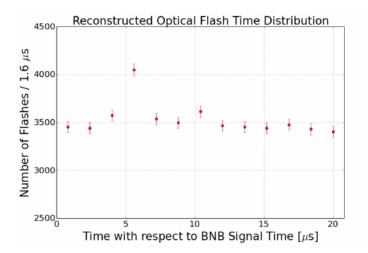


Figure 4.1: Efficiency for selecting beam events as a function of minimum total PE cut for all PE cuts as well as zoomed into interesting region.

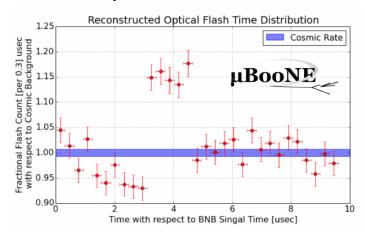
A flash is described as a collection of light seen at the same time within the detector. They are then reconstructed by identifying signal from the PMTs above a specific photoelectron (PE) threshold. These signals are called optical hits. Optical hits from all the PMTs are then accumulated into 1 μ s bins of time. If a specific bin is above a set PE threshold, then the optical hits that overlap in time are the labeled as the hits from the flash. All flash reconstructed properties like average time and x/y positions are then found via the flash labeled optical hits. The total size of the flash is found by summing up the total number of photoelectrons from all PMTs. Neutrino interactions and cosmic muons will have a larger flash size compared to noise and other low-energy backgrounds, therefore a total PE cut is used to reject these backgrounds. A total PE

cut of 50 PE was deemed sufficient for this analysis. Figure 4.1 show the total PE versus the selection efficency of selecting neutrino beam events.

735 4.1.2 Beam Timing



(a) Predicted distribution of flash times with respect to trigger time for 1 day of data taking at nominal rate and intensity



- **(b)** Measured distribution of flash times with a 50 PE threshold cut, with respect to trigger time. Shown as a ratio to the expected cosmic rate from off-beam data. A clear excess from neutrinos is visible between 3-5 µs after the trigger time.
- It is necessary to get the specific time from flashes if one uses flashes to filter out neutrino interactions coincident with the neutrino beam spill period and background. Before a filter can be applied, an understanding of the timing of the trigger and PMT

readout with respect to the arrival of neutrinos from the BNB. To do this, a 1.6 μs window near the expected beamtime was created and verified by finding that the number of flashes was significantly above the cosmic-ray background flashes. Beam data during the first week of running, October 16th 2016 through October 22nd 2016 and were used for a timing measurement. The total POT uses corresponds to roughly 24 hours of data taking at nominal intensity (4*X*10¹²*ppp*) and a 5 Hz repetition rate. Figure 4.2a shows size of the expected neutrino signal in time using Monte Carlo predictions and figure 4.2b shows the neutrino signal in data. The intensity in data is lower, however there can still be seen a significan excess above data.

4.1.3 Event Rates

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Applying a 50 PE threshold cut inside a 1.6 μs window reduces the cosmic-ray passing rate to 0.8%. With a 5 Hz beam rate, this corresponds to 135 cosmics passing per hour. The neutrino passing rate for this filter is about 22 events per hour. To further increase the neutrino to cosmic ratio, TPC topology cuts were implemented and will be discussed in the following section.

4.2 TPC Topology Selection

In order to further reduce the background of cosmic events, two independent selection streams using TPC wire data reconstruction was implemented. The first using 2D reconstructed clusters, and the second using 3D resonctructed tracks. Both streams look for neutrino interactions in the active TPC volume which are identifiable by two or more tracks originating from the same vertex.

Both 2D and 3D channels were optimized using monte carlo simulation which used a 128 kV cathode voltage. Passing rates were calculated using a 0.008 efficiency factor for cosmic events passing to simulate the flash finding described in section 4.1. This efficiency factor was an overestimation and was just used to get a general feel of what signal and background rates we would actually see in data.

765 4.2.1 Cosmic Tagging

The first step in TPC selection was based on the geometry of cosmic tracks in an event.
The cosmic ray muon geometry tagger runs on 3D tracks and assigns a score to each
reconstructed track on the likeliness of the track originating from a cosmic. The cosmic
scores are detailed below:

- 1: The track is tagged as entering or entering the TPC
- 0.95: The track is a delta ray associated with a tagged track
 - 0.5: The track is either entering or exiting, but not both
 - 0.4: The track is entering or exiting through the Z boundary
 - 0: The track isn't tagged

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Clusters are assigned either a 0 or 1, 1 being a cosmic. In simulation, 90% of cosmics are tagged as cosmics. These tracks are no longer considered when looking for a neutrino topology. Requiring that the tracks be contained in turn affects the neutrino efficiency by 20%. The algorithm checks that each track is contained within a boundary region of 10 cm from all sides of the TPC. This boundary region was optimized via handscanning of experimental data.

As can be expected, cosmic tagging is more efficient in the 3D channel (tracks) than the 2D channel (clusters) because the reconstructed tracks can use the full 3D position information of the entering and exiting points while the 2D channel mainly use the reconstructed x position of the cluster which is associated to timing.

Cosmic tagging uses timing information to reject tracks and clusters that are outside of drift window. The drift window for 128 kV is 1.6 μ s while for 70 kv, the actual voltage MicroBooNE is running at, is 2.3 μ s. Due to this variation between simulation and data, we expect to see 2.3/1.6 = 1.44 times more cosmic induced tracks or clusters in the drift window.

90 4.2.2 2D Cluster Selection

This selection was spearheaded by myself and Katherine Woodruff. After looking at experimental cosmics data, 2D clustering performs well, while 3D track reconstruction is affected by more variations in simulation, for example noise filters. This was the

motivation for having a selction only on 2D clusters in the collection (Y) plane. As stated previously, the goal of this analysis was to find identifiable neutrino interactions for use in public event displays, in future analyses, the 3D track reconstruction has been modified to further increase the tracking efficiency and has more information that just the clusters. For this analysis, however, 2D cluster information was sufficient enough for neutrino selection.

Primary Cuts

The first cuts were used to select which clusters to consider. First the clusters must have at least ten hits on the collection plane and have a cosmic tagging score < 0.4.
Only events that have at least two clusters that satisfy these primary cuts continue on.

After the initial cosmic tagging is applied, the following cuts are used to furture separate identifiable neutrinos for background cosmics.

The next cut was to remove long, vertical clusters. This was applied after seeing that most cosmic induced clusters passing were long with high angles, while neutrino induced clusters were mainly forward going. We required a good cluster to either have a projected start angle less than 30 degrees from the z axis or be less than 200 wires long. The length cut was added to make sure we don't cut any short high angle clusters that can correspond with a proton, or other highly ionizing particle associated with a long muon cluster. The 200 wire cut roughly equates to 0.6 m in the z direction, with a 3 mm wire pitch. Also, the projected angle is defined by $\tan \alpha = \Delta T/\Delta W$ where T is the time ticks and W is the wires.

The last cut requires the clusters to be either 30 time ticks or 30 wires. This cut was applied to reduce small delta rays associated with a cosmic without removing proton clusters associated with a long muon cluster, which saves ideal neutrino events that have both a long minimum ionizing muon like cluster and a short highly ionizing proton like cluster.

820 Secondary Cuts

The secondary cuts look to match long, low-angle clusters with short, high-charge clusters. Only clusters that have passed previous cuts are used. First clusters with length greater than 100 wires are chosen, which is approximately 0.3 m in the z

Cluster set	No Cuts	Primary Cuts	Secondary Cuts
Neutrinos only	570	303	32
Cosmics only (no flash)	308,016	291,879	602
Cosmics only (w/ flash)	2464	2335	5
Neutrinos/Cosmics	0.23	0.13	6.4

Table 4.1: Passing rates for 2D cluster cuts for neutrino on MC set and a cosmic only MC set. First column shows event rates with no cuts applied to both sets. Columns two and three show event rates after primary and secondary cuts are applied. Line three shows the second line scaled with the flash finding factor of 0.008. All events are normalized to per day assuming we are running at 5 Hz.

direction. Then we search for any cluster that is within approximately 3 cm (10 wires and 30 time ticks) away from the low-z end of the long cluster. This cluster must also be shorter than the first. In our reconstruction, the start and end point of a cluster can be swapped so both ends of the short cluster are compared to the long cluster.

Now that there is a vertex match, cuts based on charge and projected opening angle are implemented. We require the short cluster to have a higher start charge than the long cluster or the long cluster be longer than 500 wires. Start charge is defined as the charge on the first wire in ADC counts. The projected opening angle must also be between 11 and 90 degrees. This last cut is intended to remove clusters that are entirely overlapping or are part of the same long track. The resulting neutrino/cosmic event rate per day is shown in table 4.1. Figures 4.3 and 4.4 shows the percentages of clusters that pass each primary and secondary cuts.

4.2.3 3D Tracks and vertices Selection

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The neutrino selection for the 3D channel was based on a reconstructed vertex and two tracks. All vertices and tracks were looped over that had a cosmic tag score < 0.4 and the distances below were calculated:

- d: distance between the start points of the two tracks.
- d_1 : distance between vertex and start of track 1.
 - d_2 : distance between vertex and start of track 2.

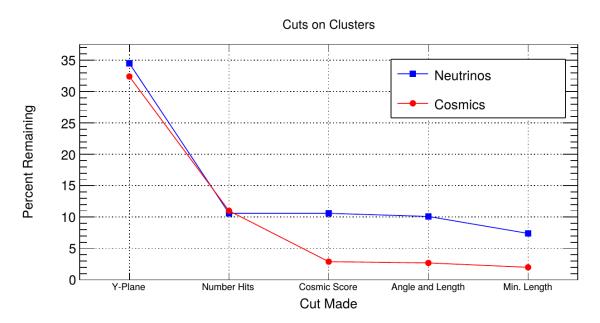


Figure 4.3: Percent of good clusters remaining for neutrinos and cosmics after the primary cuts were applied. This is relative to total number of initial clusters.

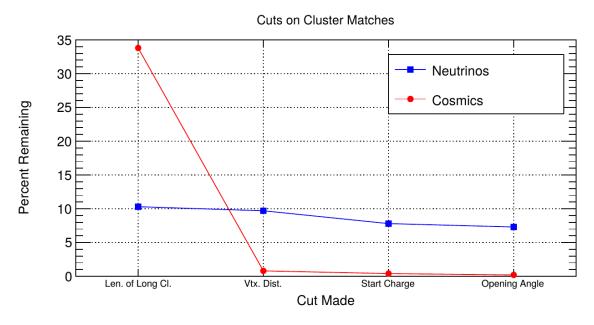


Figure 4.4: Percent matched cluster pairs remaining for neutrinos and cosmics after secondary cuts applied. This is relative to the number of events that contain clusters which pass the primary cuts.

The maximum distance of all three is then selected as the important characteristic per trio. The best trio is the one that has the smallest maximum distance. The $min(max_d)$ for all trios in an event were plotted for BNB neutrino events and for cosmics to find the best cut value for each tracking algorithm. The distribution of $min(max_{d,i})$ is smaller for neutrinos than for cosmics. The cut values for different tracking and clustering algorithms are shown below. These cut values were chosen to minimize the cosmic background to 20%.

- trackkalmanhit with cccluster $min(max_{d,i}) < 3$ cm.
- trackkalmanhit with pandoraNu $min(max_{d,i}) < 4.5$ cm.
 - pandoraNu with cccluster $min(max_{d,i}) < 5$ cm.

4.2.4 TPC Updates

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After doing a visual hand-scanning of the first beam data processed with the filters detailed above, the events passing had a larger contamination of background than expected. This was mainly in part due to the reconstruction performing better on simulation than on data. Due to this, additional cuts on both streams needed to be implemented in order to increase signal/background ratio. These cuts were added on top of the filters described above and further reduce the event count.

860 2D Filter Updates

The main background observed in the 2D filter were Michel events, where the muon and electron formed two connected clusters. These events were rejected by comparing the start and end charge deposition of the long cluster (i.e muon particle). The start charge deposition must be less than the end charge deposition. This cut is implemented because muons have a higher ionizaiton loss at the end.

866 3D Filter Updates

It was seen that cosmic tracks can often originate or end at the same point, therefore faking a signal. Cosmic tracks, however, are mostly vertical. By requiring the angle of the longer track have a cosine greater than 0.85 with respect to the z-axis as well

as requiring the longer track to have a length greater than 10 cm, we can reduce this background.

4.3 Conclusion

After processing these filters in parallel, it was shown that the 3D filter had a higher purity than the 2D filter because of the higher cosmic rejection being used due to 3D reconstruction. The 2D filter is blind to track entering/exiting from the top or bottom of the TPC. Although the 3D filter had a higher purity, the 2D filter was still able to find identifiable events in data that were used as public event displays. A sample of event displays are shown in figures ?? and ??.

... Chapter 5

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CC-Inclusive Cross Section Selection Filter

One of the cross-section measurements MicroBooNE can make is an inclusive chargedcurrent cross-section measurement (referred to as CC-inclusive). CC-inclusive events consist of a neutrino exchanging a W^{\pm} boson with an argon atom, producing a charged lepton and any number of other final state particles. In MicroBooNE's case, a CC-inclusive event will mostly have a defining muon track coming out of the vertex due to our neutrinos being predominately ν_u s. A cross-section measurement is the energy dependent probability of $\nu-Ar$ interaction in the detector. Cross-sections however are independent of the intensity or focus of the particle beam so they can be compared among different experiments. A background for a CC-inclusive crosssection measurement are the neutral-current events that contain a pion. It is possible to have a neutral current interaction with a $\pi + p$ event signature that looks like a charged current $\mu + p$ event. Reconstruction tools implemented to date don't efficiently separate muons from pions. A common way to separate these two particles species is to implement a track length cut. On average, muons tend to have longer track lengths in LArTPCs so by requiring that the hypothesized lepton be above a threshold track length, it is possible to increase signal to background.

MicroBooNE requires fully automated event reconstruction and selection algorithms for use in the many physics measurements being worked on to date due to the large data rate MicroBooNE receives. Being able to automatically pluck out the neutrino interaction among a sea of cosmics proved to be challenging but was accomplished. MicroBooNE has developed two complementary and preliminary selection algorithms to select charged-current $v_u - Ar$ interactions. Both are fully automated

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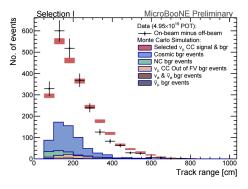
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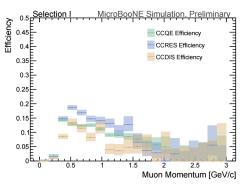
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and cut based. The results below focus on the first selection and the "In-Progress" plots presented on the poster associated with this proceeding will focus on further improving this algorithm using Convolutional Neural Network (CNN) implementations. The full details can be found in MicroBooNE public note [?] and for more information of CNN implementation on MicroBooNE data refer to [?]. Selection I is based on cuts developed in a MC performance study described in [?]. It identifies the muon from a neutrino interaction without biasing towards track multiplicity. To combat cosmic and neutral current background, the analysis is strongly biased towards forward-going long tracks which are contained. This limits phase space and reduces acceptance.

The efficiency and purity are used as performance values of selection I. Efficiency is described as the number of selected true ν_{μ} CC events divided by the number of expected true v_{μ} CC events. The purity is described as the number of selected true ν_{μ} CC events divided by the sum of itself and all the backgrounds. The efficiency of selection I is 12% and the purity is 39.7%. The poster related to this proceedings will focus on the last cut which requires the longest track to be longer than 75 cm. This cut has a passing rate of 30% w.r.t the previous cut and is implemented in part to separate charged-current events from neutral-current events that mimic our signal. Implementing a CNN for $\mu - \pi$ separation picks out differences in these two particles that are track range independent therefore eliminating the need for the 75 cm track length cut and increase efficiency and passing rate at low muon momentum. Figure 5.1a shows the track distribution of selection I and the lack of data below the 75 cm track length cut. Figure 5.1b shows the efficiency of selection I as a function of muon momentum. The selection begins with a cut that requires an optical flash greater than 50 photo electrons (PE) in the 1.6 μ s beam window. Next, two or more 3D reconstructed tracks must be within 5 cm from a 3D reconstructed vertex. The most forward going track vertex-track association is then selected for further cuts. The vertex from the chosen association must be in the fiducial volume, and the longest track from this association must be matched to a flash 80 cm in z. Lastly the longest track must be contained and longer than 75 cm.

5.1 The importance of μ/π separation





- **(a)** Track range distribution of selection I
- **(b)** Selection efficiency as a function of the true muon momentum

Figure 5.1: 5.1a Track range distribution for selection I. The track range is defined as the 3D distance between the start and end of the muon candidate track. No data is shown below 75 cm due to the track length cut described previously. **5.1b** Efficiency of the selected events by process quasi-elastic (QE), resonant (RES), and deep-inelastic (DIS). Statistical uncertainty is shown in the bands and the distributions are a function of true muon momentum. The rise of the efficiency between 0 GeV and 0.5 GeV is due to the minimum track length cut and the decreasing efficiency for higher momentum tracks is caused by the containment requirement.

SA Chapter 6

Background on Convolutional Neural Networks

Convolutional neural networks (CNNs) have been one of the most influential innovations in the field of computer vision. Neural networks became popular in 2012 when Alex Krizhevsky used them to win that year's ImageNet competition [?] by dropping the error from 26% to 15%. Since then, many companies are using deep learning including Facebook's tagging algorithms, Google for their photo search and Amazon for product recommendations. For the purpose of this thesis CNNs were used for image classification, specifically, images of varying particles created using LArTPC data.

6.1 Image Classification

Image classification is the process of inputting an image into the CNN an receiving a 946 probability of classes that best describes what is happening in the image. As humans, 947 image classification is something that is learned at a very young age and is easy to do without much effort. This is also apparent when hand-scanning LArTPC images. 949 After learning what a neutrino event looks like in MicroBooNE, it is relatively easy to recognize simple neutrino events from cosmic ray background as well as highly 951 ionizing particles like protons from minimum ionizing particles like muons. The very 952 detailed images LArTPC detectors output are prime candidates for input images into a CNN. CNNs mimic a human's ability to classify objects by creating an architecture 954 that can learn differences between all the images it's given as well as figure out the

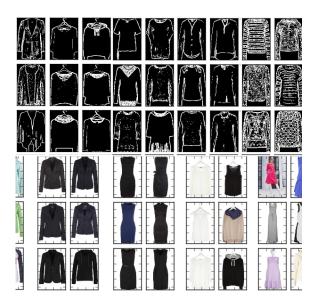


Figure 6.1: Applying a feature mask over a set of fashion items to extract necessary information for auto-encoding. Unnecessary information for example color or brand emblems are not saved. This feature map is an edge detection mask that leaves only shape information which helps to distinguish between different types of clothes.

unique features that make up each object. CNNs are modeled after the visual cortex. Hubel and Wiesel [?] found that there are small regions of neuronal cells in the brain that respond to specific regions of the visual field. They saw that some neurons fired when exposed to vertical edges while others fired when shown horizontal or diagonal edges. They also saw that these neurons were organized in columns. The idea of specific neurons inside of the brain firing to specific characteristics is the basis behind CNNs.

When used for image recognition, convolutional neural networks consist of multiple layers of feature maps that extract different information on small portions of the input image. How many layers and feature maps is tunable to increase the matching process. The output of these collections are then tiled so that they overlap to gain a better representation of the original image and allow for translation. To truly understand CNNs, a breakdown of what convolution means with regards to imaging is necessary. Convolution of an image is using a map of some sort to extract features from the input image by matrix multiplication. The map is multiplied to a small image patch and this is then saved. This is done until the whole image is processed and what is left is a feature map that has the important features extracted. An example of convolution for the process of object identification is shown in figure 6.1. In this figure you can see how an edge detection feature map is used to save only necessary

information for recognizing different types of clothes. You can also see by having multiple feature maps you can get more detail or less detail from an image which can then simplify or complicate the object recognition task. Being able to distinguish between a shirt or a leg garment is as much information you want, having a feature map that extracts outline edge or shape information would be all that you need. But if instead you wanted to distinguish between a formal cocktail dress or a summer dress, more information would need to be saved equating to many more feature maps for one image. Rather than trying to come up with a scheme of feature maps to run over the image by hand, CNNs do this automatically. CNNs take input parameters, for example number of layers, number of units per layers, number of connections per unit, and uses these to create the feature maps. The layers build upon each-other, for example if we were creating a CNN for facial recognition the convolutional layers will start learning feature combinations off of the previous layers. The simple edges, gradients, and corners of the first layers become things like eyes, noses, and hairs in later layers. This process is visualized in figure 6.2

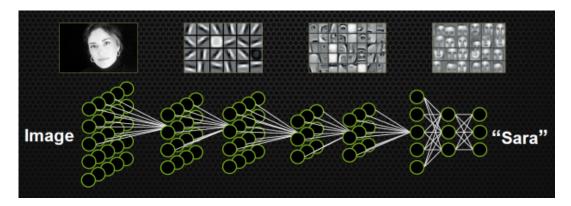


Figure 6.2: Pictorial Representation of Convolutional Neural Networks as well as a visual representation on CNN's complexity of layer feature extraction

6.2 AlexNet

91 6.3 GoogleNet

Chapter 7

Training Convolutional Neural Networks on particles WORKING

55 TITLE

Three Convolutional Neural Networks CNNs were trained throughout this analysis. There are differences to each CNN and will be described fully in the next sections but 997 the main difference are the amount of particle images used for training and validation. 998 CNN1075 used 1,075 muons and 10,75 pions for training and the same amout of each 999 particle for validation. CNN10000 used 10,000 muons and 10,000 pions split in half 1000 for testing and training. Lastly CNN100000 had muons, pions, protons, electrons, and gammas in it's training and validation set. Each particle had 20,000 images and 1002 training and validation was split 90% training, 10% validation. This chapter will also 1003 describe the different hardware frameworks used for training beginning on a CPU and ending on a GPU cluster. 1005

5 7.1 Hardware Frameworks used for Training

₀₇ 7.1.1 Syracuse CPU Machine setup

7.1.2 Syracuse University GPU Cluster Setup

5.2 Convolutional Neural Network Training

1010 7.2.1 Image Making Scheme

1011 Images used for Traing/Validation of Convolutional Neural Networks

add image making for CNN1075 The μ/π image dataset used to train and validate 1012 the CNN10000 was created using single generated isotropic muons and pions from 1013 0-2 GeV energ range. 10,000 muons and 10,000 pions were used for training and 1014 testing split 50%. The images were created based on wire number and time tick in the 1015 collection plane. Uboonecode v06_23_00 was used instead of v05_08_00 which was 1016 used previously. The wire signal was the raw ADC value after noise filtering. Each collection plane grayscale image was 3456x1280x1 where 5 time ticks were pooled into 1018 1 bin which is different than the previous dataset and was implemented due to the fact 1019 that the time ticks of an event went from 9400 to 6400 with the change of uboonecode 1020 version. The grayscale color standard is 8bit therefore the ADC value of wire and time 1021 tick was also downsampled due to the 12bit ADC value MicroBooNE has. To do this, 1022 the highest ADC pixel in the image was found and then this was divided by the rest 1023 placing all pixel values between 0-1. From there, all pixel values are then multiplied 1024 by 255. All images were made using a LArSoft module. Once the images were created, 1025 using and image manipulation framework called OpenCV images were read into a 1026 numpy array and cropped to the region of interest by only keeping rows and columns 1027 where all ADC values are higher than 0 and then resized it to 224x224 using OpenCV's 1028 resize function. This downsampling of ADC values creates a problem of information 1029 loss for example, a proton which is highly ionizing will have the same brightness as a 1030 minimum ionizing muon by virtue of how the images are created. Issues that arose 1031 in CNN1075 that were fixed in CNN10000 include zero-padding images in X and Y 1032 that are smaller than 224X224 to eliminate over-zooming effect and fixing a bug that 1033 shifted pixels separated by a dead-wire region. 1034

Images were also made from events that passed the cc-inclusive selection 1 filter 1035 right before the 75 cm track length cut and were classified using the CNN10000. The 1036 dataset used to create these images is the same one used in [?], prodgenie_bnb_nu_cosmic_uboone_mc 1037 These images were created using information from the track candidate that passed 1038 the filter. Only wire number and time ticks associated to the track candidate were 1039 drawn on the image to mimic a single particle generated image. These images were 1040 then classified using CNN10000. Two approaches were taken in making these images. 1041 The first was using the image normalization above where the maximum pixel in each 1042 image is used as a normalization constant to get all pixels between 0-1 then multiply 1043 all pixels by 255. As described above, this is the incorrect way to normalize; it should 1044 be normalized by dataset not by event, which is the second way the images were 1045 created. The results of CNN10000 performance are shown in section 7.2. 1046

1047 7.2.2 Training CNN1075

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The work shown in these next sections are based on the previous work done described in [?]. That CNN (now referred to as CNN1075) was trained using single generated isotropic muons and pions from 0-2 GeV energy range. 1,075 muons and pions were used to train the network and 1,075 μ/π were used as a validation set. The accuracy is how well CNN1075 is doing by epoch and was 74.5%. The loss is gradient descent or minimization of the error of the weights and biases used in each neuron of each layer of CNN1075 and was 58% with a trend sloping downwards on the loss curve as well as a trend sloping upward in the accuracy curve. Due to the depth of the neural network framework, it was necessary to train with a larger dataset and for more epochs, however, the downward slope of the loss curve is an indication that once trained for longer with a higher training sample, neural networks can be used for μ/π separation. Updates in the image making and downsampling algorithm were made to fix issues that arose in CNN1075.

7.2.3 Training CNN10000

The hyperparameters used for CNN10000 are shown. The batch size for the training and testing as well as the test iter were chosen to encompass the whole training/testing image set when doing accuracy/loss calculations. To do this, multiplying the test

iter by the test batch size give you the amount of images used when calculating accuracy/loss curves. For reference, the accuracy and loss are defined as well.

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• train_batch_size: 100
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       • test_batch_size: 100
       • test_iter: 100
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       • test_interval: 100
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       • base_lr: 0.001
       • lr_policy: "step"
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       • gamma: 0.1
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       • stepsize: 1000
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       • display: 100
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       • max_iter: 10000
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       • momentum: 0.99
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       • weight_decay: 0.0005
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• snapshot: 100

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- Accuracy: How often the CNN predicts the truth over total number of images
- Loss: Error between truth and prediction. Minimize loss by gradient descent to update weights and biases of CNN

The same architecure that was used to train CNN1075 was employed on CNN10000, Imagenet. Caffe [?] was the software package used for both CNNs. The differences include batch size and test_iter and momentum to account for the larger dataset. Both CNNs were trained on a CPU machine, Syracuse01. Further training will be done on a GPU cluster stationed at Syracuse University. Figure 7.1 shows the loss and accuracy of CNN10000. There is around a 10% increase in accuracy from CNN1075 to CNN10000, 85%, and around a 20% decrease in loss, 36%.

Figure 7.2 show a breakdown of μ/π separation for CNN10000. It also shows the network is not being overtrained due to the Accuracy of both the training and testing datasets being within .01% of eachother. The CNN is doing a very good job of

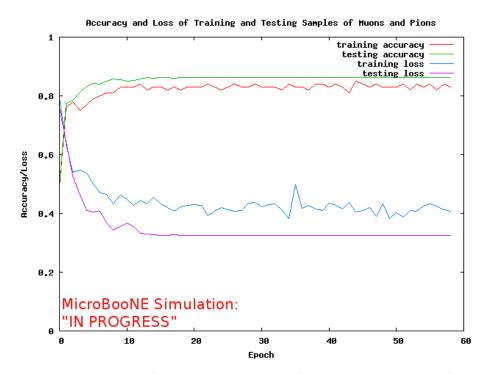
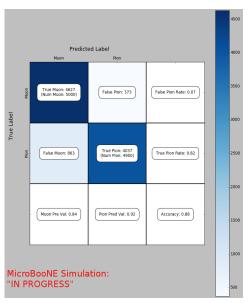
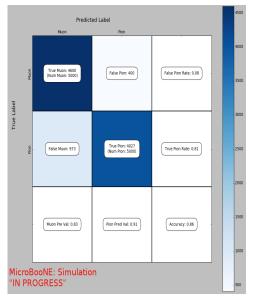


Figure 7.1: Accuracy vs. Loss of ImageNet 2-output μ/π sample consisting of 10000 images each.

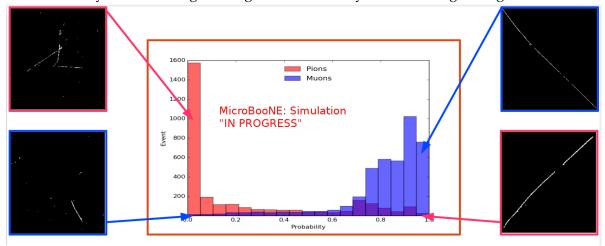
classifying true muons as muons, and our loss increase from CNN1075 is due to the increase in accurately classifing pions as pions.

7.2.4 Training CNN100000





- **(a)** Confusion Matrix showing Accuracy of CNN using training data
- **(b)** Confusion Matrix showing Accuracy of CNN using testing data



(c) Probability plot of muons and pions from testing set. Images surrounding histogram are a random event from lowest bin and highest bin for each particle.

Figure 7.2: Description of confusion matrix variables: False pion rate = $false\pi/total\pi$ True pion rate = $true\pi/total\pi$ Accuracy = $(true\pi rate + true\mu rate)/2$ Pion prediction value = $true\pi/(true\pi + false\pi)$ Muon prediction value = $true\mu/(true\mu + false\mu)$ 7.2c The probability plot includes muons and pions that are classified as primary particles.

Chapter 8

Results of Convolutional Neural Networks on particles WORKING

OPP TITLE

8.1 Classification using CNN10000

8.1.1 Classification of MC data using Selection I Original CC-Inclusive Filter

The next step that was taken was to use CNN10000 to classify track candidate images 1103 that were identified by the selection I original cc-inclusive filter described in [?]. 1104 Passing rates for each cut in cc-inclusive filter are show in figure 8.1. For the incorrect image making normalization dataset, out of 188,880 events, 7438 passed the cut right 1106 before 75 cm track length cut which is 3.9% of total data. Discrepancies in passing rates 1107 are due to grid submission issues, however, this dataset is used to check if changes 1108 in image making normalization affects μ/π separation probability due to CNN10000 1109 being trained with incorrectly image making normalized data. For the second dataset with correct image making normalization, out of 188,880 events, 9552 events passed the 1111 cut right before the 75 cm track length cut which is 5.1% passing rate and is comparable 1112 to figure 8.1. In time cosmics were also run over for efficiency and purity calculations. Out of 14395 in time cosmic events, 175 passed the cut right before the 75 cm track 1114 length cut which is a passing rate of 1.2% compared to 1.3% shown in figure 8.1.

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Table 3: Selection I: Original The table shows passing rates for the above described event selection. Numbers are absolute event counts and Cosmic background is not scaled appropriately. The BNB+Cosmic sample contains all events, not just ν_{μ} CC inclusive. The selected events are further broken up in the following subsection. The numbers in brackets give the passing rate wrt the step before (first percentage) and wrt the generated events (second percentage). In the BNB+Cosmic MC Truth column shows how many true ν_{μ} CC inclusive events (in FV) are left in the sample. This number includes possible mis-identifications where a cosmic track is picked by the selection instead of the neutrino interaction in the same event. The cosmic only sample has low statistics, but please note that it is not used in any plots, it is just for illustrating the cut efficiency. The last column Signal:Cosmic only gives an estimate of the ν_{μ} CC events wrt the cosmic only background at each step. For this number, the cosmic background has been scaled as described in chapter 2. Note that this numbers is not a purity, since other backgrounds can't be determined at this step.

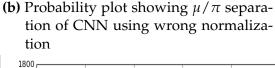
	BNB + Cosmic				Cosmic only		Signal:
	Selection		MC-Truth				Cosmic only
Generated events	191362		45273		4804		1:22
$\geq 1 \text{ flash with } \geq 50 \text{PE}$	136219	(71%/71%)	44002	(97%/97%)	2979	(62/%62%)	1:14
≥ 1 vertex in FV	131170	(96%/69%)	43794	(99%/97%)	2805	(94%/58%)	1:13
≥ 1 track within 5 cm of vertex	129784	(99%/68%)	43689	(99%/97%)	2756	(98%/58%)	1:13
flash matching of longest track	44775	(34%/23%)	23647	(54%/52%)	647	(23%/13%)	1:5.7
track containment	10114	(23%/5.3%)	6882	(29%/15%)	61	(9.4%/1.3%)	1:1.9
$\mathrm{track} \geq 75\mathrm{cm}$	7358	(73%/3.8%)	5801	(84%/13%)	31	(51%/0.6%)	1:1.1

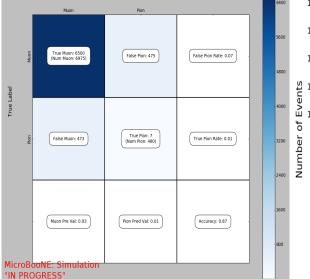
Figure 8.1: Snapshot of passing rates of Selection I from CC-Inclusive Filter

Figures 8.2a, 8.2b, 8.2c and 8.2d show the accuracy and μ/π separation of both the correct and incorrect normalized images. The confusion matrices are only composed of μ/π data. Other particles passed the cc-inclusive filter before the 75 cm track length cut and were all mis-id'ed as muons. Since CNN10000 has not seen any particles other than muons and pions, it makes sense that those get mis-id'ed. Figures 8.2b and 8.2d don't have μ/π separation comparable to 7.2c, but 8.2b does skew to higher probabilities compared to 8.2d. This is to be expected and further work on quantifying the performance of CNN10000 should use the incorrect image making normalization. It is also expected that the separation isn't as defined as the testing dataset for CNN10000. CNN10000 was trained and tested using single particle muons and pions and the track candidate dataset come from BNB+Cosmic events, not to mentions all track candidates have passed the cc-inclusive filter that tags "muon-like" tracks therefore the pions in this sample look much closer in muon topology than the network has seen. Also, these images were made from wire and time ticks associated to hits from the track candidate that passed the cc-inclusive filter. This is different from the training images where a bounding box was drawn over the total μ or π interaction. Spurious energy deposition from a π – Ar interaction is most likely not included in the BNB+Cosmic images due to the tracking algorithm. To remedy this, the neural network needs to see more "muon-like" pions and muons and pions from a neutrino interaction passing the cc-inclusive filter as well as a larger particle variety including protons, photons

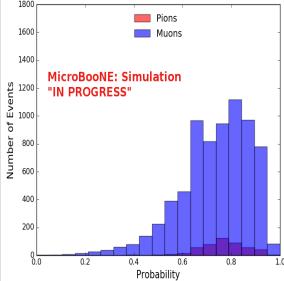


(a) Confusion Matrix showing Accuracy of CNN using data with wrong normilazion



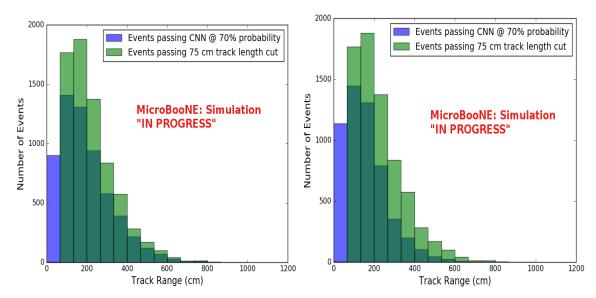


(c) Confusion Matrix showing Accuracy of CNN using data with correct normilazion

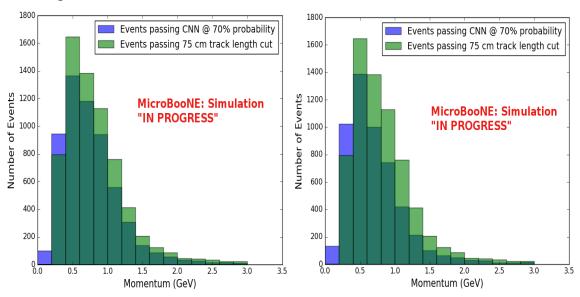


(d) Probability plot showing μ/π separation of CNN using correct normalization

Figure 8.2: Results of CNN10000 classification of track candidate images output from ccinclusive filter.



- (a) Track range distribution of events from Selection I Original passing CNN with 70% accuracy using image data with wrong normilazion
- **(b)** Track range distribution of events from Selection I Original passing CNN with 70% accuracy using image data with correct normilazion



- (c) Momentum distribution of events from Selection I Original passing CNN with 70% accuracy using image data with wrong normilazion
- (d) Momentum distribution of events from Selection I Original passing CNN with 70% accuracy using image data with correct normilazion

Figure 8.3: CNN10000 distributions of track candidate images output from Selection I Original cc-inclusive filter with different image data normalizations

and electrons. Although μ/π separation is lacking, CNN10000 does an excellent job of classifying muons and using higher CNN probability can increase purity. Figures 8.3a, 8.3b, 8.3c and 8.3d show the track and momentum distributions for these two datasets. In both sets you have an increase in data in the bin below 75 cm and at bins below 0.5 GeV. These distributions were made with events classified with 70% probability of being a muon regardless of true particle type.

8.1.2 Classification of MC data using Selection I Modified CC-Inclusive Filter

Table 5: Selection I: Modified The table shows passing rates for the above described event selection. Numbers are absolute event counts and Cosmic background is not scaled appropriately. The BNB+Cosmic sample contains all events, not just ν_{μ} CC inclusive. The selected events are further broken up in the following subsection. The numbers in brackets give the passing rate wrt the step before (first percentage) and wrt the generated events (second percentage). In the BNB+Cosmic Mc Truth column shows how many true ν_{μ} CC inclusive events (in FV) are left in the sample. This number includes possible mis-identifications where a cosmic track is picked by the selection instead of the neutrino interaction in the same event. The cosmic only sample has low statistics, but please note that it is not used in any plots, it is just for illustrating the cut efficiency. The last column Signal:Cosmic only gives an estimate of the ν_{μ} CC events wrt the cosmic only background at each step. For this number, the cosmic background has been scaled as described in chapter 2. Note that this numbers is not a purity, since other backgrounds can't be determined at this step.

	BNB + Cosmic			Cosmic only		Signal:	
	Se	election	M	C-Truth			Cosmic only
Generated events	191362		45273		4804		1:22
≥ 1 flash with $\geq 50 \text{PE}$	136219	(71%/71%)	44002	(97%/97%)	2979	(62%/62%)	1:14
≥ 1 track within 5 cm of vertex	135830	(99%/71%)	43974	(99%/97%)	2975	(99%/62%)	1:14
vertex candidate in FV	79112	(58%/41%)	34891	(79%/77%)	1482	(50%/31%)	1:8.9
flash matching of longest track	40267	(51%/21%)	25891	(74%/57%)	340	(23%/7.1%)	1:2.8
track containment	19391	(48%/10%)	11693	(45%/26%)	129	(38%/2.7%)	1:2.3
$track \ge 75 cm$	6920	(36%/3.6%)	5780	(49%/13%)	17	(13%/0.4%)	1:0.6

Figure 8.4: Snapshot of passing rates of all cuts from Selection I Modified cc-inclusive filter

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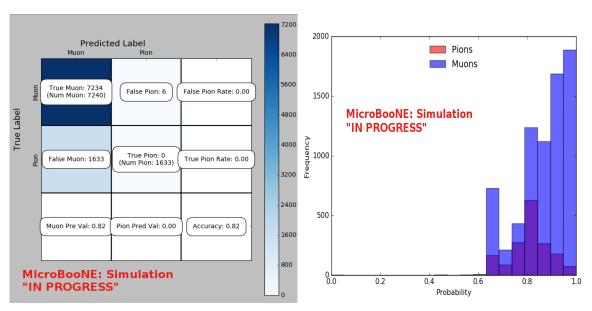
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CNN10000 was also used to classify track candidate images that were identified by the selection I modified cc-inclusive filter described in [?]. Passing rates for each cut in this filter are shown in figure 8.4. As seen in section 8.1.1, wrong image normalization had a higher muon classification probability so all work done using selection I modified cc-inclusive filter was done using this normalization. Out of 188,880 events, 19,112 passed the cut right before the 75 cm track length cut which is a 10.1% passing rate and comparable to the 10% passing rate shown in figure 8.4. In time cosmics were also run over, out of 14,606 in time cosmics events, 302 passed the cut right before the 75 cm track length cut which is a 2.1% passing rate comparable to the 2.7% passing rate in the cc-inclusive tech-note. Figures 8.5a and 8.5b show the accuracy and μ/π separation. Both plots are only composed of muons and pions and like selection I original data,

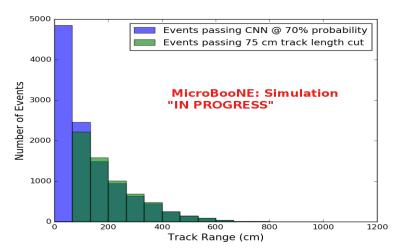
all other particles were id'ed as muons. Also like selection I original data, muons are being identified at a very high rate. Figure 8.6a shows the track range distributions of all events from selection I modified being classified by the CNN as a muon with a probability of 70% regardless of true particle type. We get entries for the CNN curve in the lowest bin and none for the 75 cm curve. To see how many true CC events were identified by CNN10000 breaking down figure 8.6a by event type was necessary. Figures 8.6b and 8.6c show track range distributions separated by signal and various backgrounds. Particle type was not taken into consideration in these plots so true CC event images can be any track candidate particle passing selection I modified cut right before track length cut including pions and protons.

To gain an even deeper understanding on how CNN10000 is performing, plotting these distributions with only muons and pions was done due to the fact that CNN10000 was trained with only those particles for μ/π separation. Figures 8.6d-8.7d show the stacked histograms of signal and background of the track range distributions with varying CNN probabilities starting from 70% and ending at 90% probability. With higher probabilities we get a purer sample in the lower bin but we end up losing events as well. Momentum distributions for all signal/background events are shown in figure 8.8.

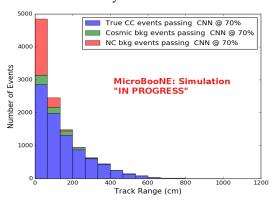


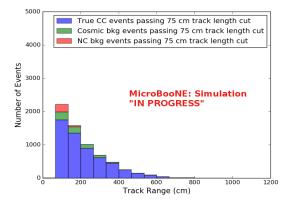
- (a) Confusion Matrix for CNN10000 classified events from selection I modified
- **(b)** Probability plot for CNN10000 classified events from selection I modified

Figure 8.5: Confusion matrix and probability plot of events passing selection I modified ccinclusive cuts right before 75cm track length cut

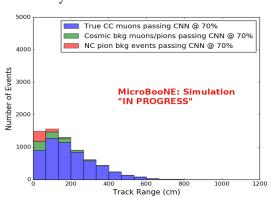


(a) Track range distribution of events from Selection I Modified passing CNN with 70% accuracy

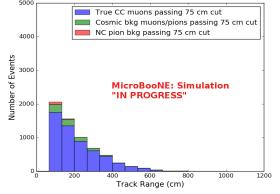




(b) Stacked signal and background track range distributions from Selection I Modified passing CNN with 70% accuracy



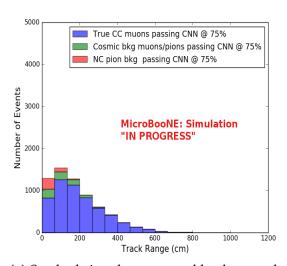
(c) Stacked signal and background track range distributions from Selection I Modified passing 75 cm track length cut



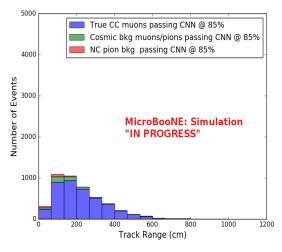
(d) Stacked signal muons and background muons/pions of track range distributions from Selection I Modified passing CNN with 70% accuracy

(e) Stacked signal muons and background muons/pions of track range distributions from Selection I Modified passing 75 cm track length cut

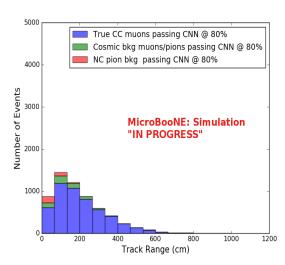
Figure 8.6: CNN10000 distributions of track candidate images output from Selection I Modified cc-inclusive filter



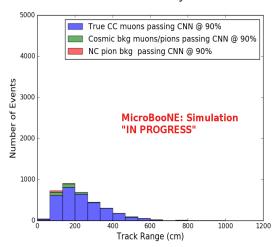
(a) Stacked signal muons and background muons/pions of track range distributions from Selection I Modified passing CNN with 75% accuracy



(c) Stacked signal muons and background muons/pions of track range distributions from Selection I Modified passing CNN with 85% accuracy

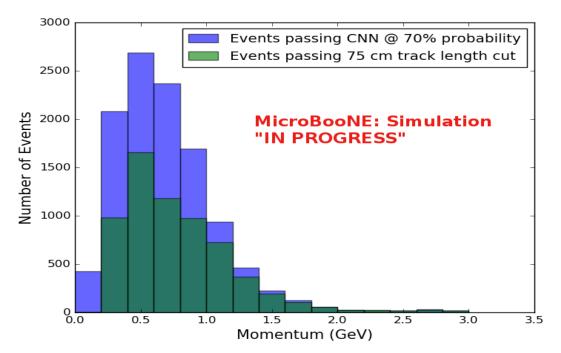


(b) Stacked signal muons and background muons/pions of track range distributions from Selection I Modified passing CNN with 80% accuracy

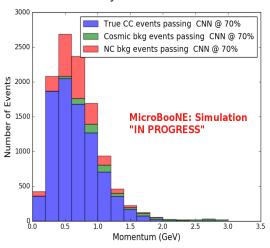


(d) Stacked signal muons and background muons/pions of track range distributions from Selection I Modified passing CNN with 90% accuracy

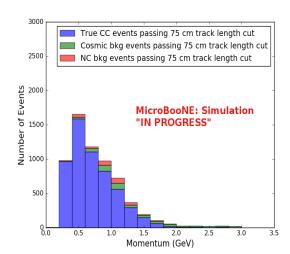
Figure 8.7: CNN10000 stacked signal/background track range distributions of track candidate images output from Selection I Modified cc-inclusive filter



(a) Momentum distribution of events from Selection I Modified passing CNN with 70% accuracy



(b) Stacked signal and background momentum distributions from Selection I Modified passing CNN with 70% accuracy



(c) Stacked signal and background momentum distributions from Selection I Modified passing 75 cm track length cut

Figure 8.8: CNN10000 momentum distributions of track candidate images output from Selection I Modified cc-inclusive filter

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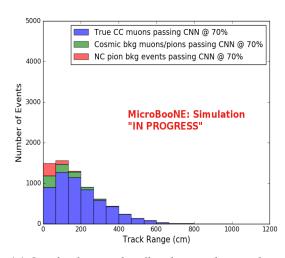
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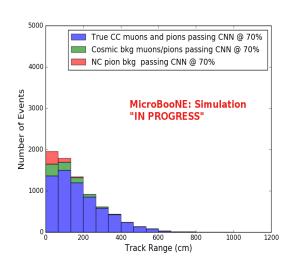
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Another check was to see if any true CC pions were passing through the cut right before the 75 cm track length cut. Figure 8.9 shows the comparison of the stacked track range distribution with only true CC muon signal versus the stacked distribution with true CC muons and pions signal. As you can see, we gain more events when plotting CC events with a particle type of either muons or pions due to the CNN classifying all pions in this dataset as muons. This is an interesting scenario and a sample of topologies of these images are represented in figure 8.10, at least 3 tracks are coming out of the vertex for these types of events. With the 75 cm track length cut, the selection is cutting event topologies like this where the pion is the tagged track candidate. Figure 8.10a has a defined longer muon track, but because of dead wires through the track, the reconstructed range is 1. less than 75 cm and 2. shorter than the reconstructed pion whose length is also less than 75 cm. This is a very interesting event, but because of issues with the tracking algorithm, the 75 cm cut would get rid of this event. The CNN was able to recover this event only because it has classified all pions as muons. Figure 8.10b shows the second case to think about, the pion, while still less than 75 cm has a reconstructed track length longer than the muon. Again, the CNN recovered this event due to pions being classified as muons. Lastly, figure 8.10c shows a pion with a reconstructed track length greater than 75 cm and the muon. These three cases show that a broader question must be asked when training the network other than is it a muon or pion. There are different routes to recover interesting events like these. One route is to ask the network "Is it a CC event or is it an NC event?" and obtain an image dataset consisting of whole CC/NC events that will train the network to answer this question. The other route is to ask the network "Is this a $\mu/\pi/p/$ from a CC event or NC event and obtain an image dataset consisting of primary particles from a CC/NC event. Both these paths will be explored in future work.





- (a) Stacked signal μ /backround μ and π track range distribution of CNN @ 70%
- **(b)** Stacked signal $\mu \& \pi$ /backround $\mu \& \pi$ track range distribution of CNN @ 70%

Figure 8.9: Track distribution comparisons of true CC muons plotted vs true CC muons and pions plotted



(a) Pion recontructed track range is less than 75 cm and longer than muon track due to dead wires



(b) Pion recontructed track range is less than 75 cm and larger than muon reconstructed track



(c) Pion reconstructed track range is greater than 75 cm and larger than muon reconstructed track

Figure 8.10: Images of true CC events where the pion was the tagged track candidate

		BNB + C Selection	Cosmics MC Truth	Cosmic Only	Signal: Cosmic Only
75 cm Cut passing rates	Generated Events	191362	45723	4804	1:22
	Track Containment	19391 (48%/10%)	11693 (45%/26%)	129 (38%/2.7%)	1:2.3
	track ≥ 75 cm	6920 (36%/3.6%)	5780 (49%/13%)	17 (13%/0.4%)	1:0.6
CNN passing rates	Generated Events	188880	44689	14606	1:21
	Track Containment	19112 (/10%)	11554 (/26%)	302 (/2.1%)	1:1.73
	CNN cut @ 70% Probability	16502 (86%/8.7%)	10605 (92%/23%)	205 (68%/14%)	1:1.28
	CNN cut @ 83% Probability	7511 (46%/4.0%)	6142 (58%/14%)	32 (16%/0.2%)	1:0.4

Table 8.1: Comparing passing rates of CNN at different probabilities versus 75 cm track length cut: Numbers are absolute event counts and Cosmic background is not scaled appropriately. The BNB+Cosmic sample contains all events. The numbers in brackets give the passing rate wrt the step before (first percentage) and wrt the generated events (second percentage). In the BNB+Cosmic MC Truth column shows how many true ν_{μ} CC-inclusive events (in FV) are left in the sample. This number includes possible mis-identifications where a cosmic track is picked by the selection instead of the neutrino interaction in the same event. The CNN MC True generated events were scaled wrt the MC True generated events for the 75 cm cut passing rates due to only running over 188,880 generated events versus the 191362 generated events. The last column Signal:Cosmic only gives an estimate of the ν_{μ} CC events wrt the cosmic only background at each step. For this number, the cosmic background has been scaled as described in [?]. Note that these numbers are not a purity, since other backgrounds canâ $\check{A}\check{Z}t$ be determined at this step.

		#Events(Fraction)	#Events(Fraction)	
		passing CNN @ 70% Probability	passing CNN @ 83% Probability	
Signal	ν_{μ} CC events with true vertex in FV	10605(35%)	6142(61%)	
Backgrounds	Cosmics Only Events	13573(45%)	2582(26%)	
	Cosmics in BNB Events	2249(7.4%)	492(4.9%)	
	NC Events	3412(11%)	778(7.7%)	
	ν_e and $ar{ u}_e$ Events	139(0.5%)	32(0.3%)	
	$ar{v}_{\mu}$ Events	97(0.3%)	67(0.7%)	

Table 8.2: Signal and background event numbers at modified selection level with CNN cut estimated from a BNB+Cosmic sample and Cosmic only sample normalized to $5*10^{19}$ PoT. The last column gives the fraction of this signal or background type to the total selected events per CNN probability.

Table 8.1 shows the passing rates for the 75 cm track length cut and the CNN cut at 70% and 83%. The passing rates at the track containment level for the 75 cm track length cut compared to the CNN are comparable with only a 0.6% difference in the in time cosmic bin which may be due in part to the larger in time cosmic statistics used for the CNN dataset. These passing rates need to be comparable to then be able to compare the passing rates after the CNN cut to the 75 cm cut. Again, the same BNB+Cosmic sample was used for both selection I modified with 75 cm cut and selection I modified with CNN cut. As it stands, a CNN cut at 83% probability has

a MC true CC event passing rate of 14% compared to the 13% passing rate of the 75 cm track length cut. The Signal:Cosmic Only background is also reduced from 1:0.6 to 1:0.4 The total passing rate is also higher than the 75 cm cut, 3.6% vs 4.0%. Table 8.2 shows the breakdown of signal and backgrounds for the CNN at the different probabilities. We have a 61% signal passing rate with the CNN cut @ 83% versus the 53.8% signal passing rate of the 75 cm cut.

Based on these numbers, the following performance values of the modified selection with 75 cm cut versus modified selection with CNN @ 83% probability cut were calculated:

- Efficiency: Number of selected true ν_{μ} CC events divided by the number of expected true ν_{μ} CC events with interaction in the FV.
 - Selection I modified: 13%

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- Selection I modified with CNN cut @ 83% probability: 14%
- Purity: Number of selected true ν_{μ} CC events divided by sum of itself and the number of all backgrounds.
 - Selection I modified: 53.8%
 - Selection I modified with CNN cut @ 83% probability: 61%

Lastly, figure 8.12 shows a more representative performance of the CNN. Due to the fact that the CNN was trained on muons and pions, showing the performance of CC muon events versus NC pion events with respect to CNN probability gives a better picture of how the network is performing. Figure 8.12 shows that at 83% we are below the 75 cm cut NC pion threshold and still above the CC muon threshold. Using 83% probability not only reduced the NC pion background, it also dramatically reduced the in time cosmics and cosmics in the BNB.

8.1.3 Conclusions and Future Work

It was shown that even though CNN10000 was trained with single particle generated muons and pions, it performs fairly well at classifying track candidate images from BNB+Cosmic events. Events have been regained below the 75 cm track length cut and the momentum and track range distributions have similar shapes to the distributions of Selection I original and modified. Efficiencies and purities were calculated for selection

Table 8: **Selection I: Modified** Signal and background event numbers at modified selection level estimated from a BNB+Cosmic sample and Cosmic only sample normalized to 5×10^{19} PoT. The last column gives the fraction of this signal or background type to the total 2189 selected events.

		#Events	
Signal	ν_{μ} CC events with true vertex in FV	1168	53.8%
Backgrounds	Cosmics only events	725	33.4%
	Cosmics in BNB events	144	6.6%
	NC events	75	3.5%
	ν_e and $\bar{\nu}_e$ events	4	0.2%
	$\bar{\nu}_{\mu}$ events	15	0.7%
	ν_{μ} CC events with true vertex outside FV	40	1.8%

Figure 8.11: Snapshot of signal and background event numbers of Selection I modified from cc-inclusive note [?]

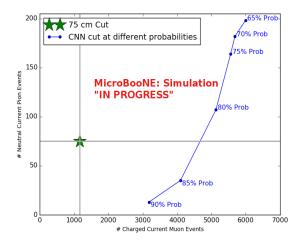


Figure 8.12: CNN performance of classified muons and pions compared to the already implemented 75 cm track length cut

I modified events before 75 cm track length cut with the CNN at 83% probability and 1236 are 14% and 62% respectively. Although the CNN doesn't have separation between 1237 muons and pions and although all particles passing CNN are classified as muon, increasing CNN probability allows us to increase the purity as well as maintain an 1239 efficiency comparable to the 75 cm track length cut all while recovering events below 1240 that 75 cm cut. Out of the 6142 events that passed the CNN @ 83% 1470 events were 1241 below the 75 cm cut, a recovery of 3.3% of data with an purity of 15%. Although 1242 these numbers are low, it is an improvement from the selection I modified in both total efficiency and purity and an increase in phase space by recovering these events. 1244

8.2 Classification using CNN100000

All future classifications will be done using Selection I Modified CC-Inclusive Filter because it has a higher efficiency and purity than Selection I Original CC-Inclusive Filter. To reiterate, CNN100000 was trained using 20,000 images of each $\mu/\pi/p/\gamma/e$. The results of using CNN100000 to classify BNB+Cosmics will be outlined below.

8.2.1 Classification of MC data using Selection I Modified CC-Inclusive Filter

Chapter 9

Using Convolutional Neural Networks on MicroBooNE Data

Chapter 10

Comparing two CC-Inclusive Cross
Section Selection Filters

1262 Chapter 11

Conclusion

Your Conclusions here.

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