



1 | Exercises with the app

1. Base fit

- a) The fitted line is the OLS regression $\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x$.
- b) The estimated slope $\hat{\beta}_1$ will be close to the true β_1 on average, but not exactly equal due to sampling variability (random noise ε).

2. Heteroscedasticity on/off

- a) With the slider at 0, the p-value is large, showing no evidence of heteroscedasticity.
- b) As heteroscedasticity increases, $SE(OLS)$ underestimates variability while $SE(HC3)$ corrects for it. The HC3 p-value is more conservative, sometimes turning insignificant when OLS still shows significance.

3. Reading the bowtie guide

- a) The dashed curve shows how the conditional variance of ε changes with x .
- b) As the curve steepens (variance grows with x), the Breusch-Pagan test statistic increases, and its p-value drops, indicating heteroscedasticity.

4. Functional form: keeping the same sample

- a) With $\beta_2 = 0$, the data match the base sample; the linear fit coincides with the true model.
- b) For $\beta_2 > 0$, the scatter curves upward (U-shape), and the F-test p-value becomes small, indicating nonlinearity.
- c) For $\beta_2 < 0$, the curve bends downward (inverted U), and the RESET test also flags misspecification.

5. Comparing linear vs quadratic coefficients

- a) The coefficient on x^2 corresponds to curvature.
- b) It becomes significant when the true curvature (β_2) is large enough. This aligns with the F-test and the dashed quadratic overlay, which fits the data better.

6. Multicollinearity: creating instability

- a) VIF values rise sharply toward infinity as $\rho_x \rightarrow 1$, showing inflated standard errors.
- b) The coefficient estimate for β_1 changes drastically depending on whether x_2 is included. This instability illustrates how collinearity makes coefficients unreliable.
- c) Collinearity does not bias OLS coefficients; instead, it increases their variance, making estimates unstable and inference weak.

7. Equation comparison panel

- a) For nonlinearity, the card shows only the linear fit because the app is demonstrating how misspecification occurs when a quadratic term is omitted.
- b) For collinearity, the model is written as $\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x_1 + \hat{\beta}_2 x_2$, highlighting that interpretation of each coefficient depends heavily on the other due to overlap between x_1 and x_2 .

2 | Testing the Classical Linear Assumptions

see [RScript](#).