# ${\tt PO12Q-Introduction\ to\ Quantitative\ Political\ Analysis\ II:}$

Worksheet Week 10 - Solutions



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# 1 Testing the Classical Linear Assumptions

see RScript.

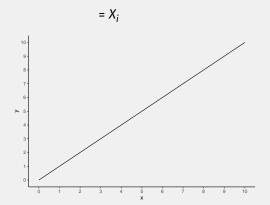
### 2 The Gauss-Markov Theorem

2. According to Malinvaud, the assumption that  $E(u_i|X_i)=0$  is quite important. To see this, consider the PRF:  $Y=\beta_1+\beta_2X_i+u_i$ . Now consider two situations: (1)  $\beta_1=0$ ,  $\beta_2=1$  and  $E(u_i)=0$ ; and (2)  $\beta_1=1$ ,  $\beta_2=0$  and  $E(u_i)=X_i-1$ . Now take the expectation of the PRF conditional upon X in those two cases, and see if you agree with Malinvaud about the significance of the assumption  $E(u_i|X_i)=0$ .

#### 2.1 Situation 1

$$Y = \beta_0 + \beta_1 X_i + \epsilon_i$$

$$= 0 + X_i + 0$$
(1)





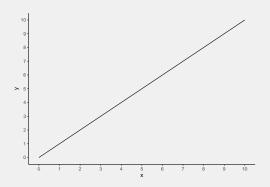
### 2.2 Situation 2

$$Y = \beta_0 + \beta_1 X_i + \epsilon_i$$

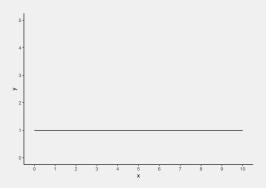
$$= 1 + 0 + X_i - 1$$

$$= X_i$$
(2)

So what we get is:



What we **should** get is:



## 2.3 Conclusion

- The second PRF is the same as the first, even though according to the betas it should be a flat line
- This is only possible, because the error term is not zero and has an interdependence with  $X_i$ .