

**The Algebra of Derivatives - Day 8**

1. Suppose that  $P(t)$  gives the number of fish in a lake, where  $t$  is time in weeks.

(a) If 130 fish are born each week, what is  $\frac{dP}{dt}$  equal to (including units)?

(b) If state wildlife managers add 60 fish to the lake each week, what is  $\frac{dP}{dt}$  in this case?

(c) In reality both of those things are happening at the same time. So what is  $\frac{dP}{dt}$  overall?

(d) Conclusion: If  $P(t) = f(t) + g(t)$ , then, using  $f'(t)$  and  $g'(t)$ ,

$$P'(t) =$$

2. Suppose that  $C(x)$  is the cost to a manufacturer of producing  $x$  yoga mats.

(a) What is the meaning of  $C(50)$ ? What are the units of  $C(50)$  and what does it mean in the context of the problem?

(b) What is the meaning of  $C'(50)$ ? What are the units of  $C'(50)$  and what does it mean in the context of the problem?

(c) Suppose that  $C'(50) = 3.50$ . If costs in the yoga mat industry suddenly double, what is the new value of  $C'(50)$ ?

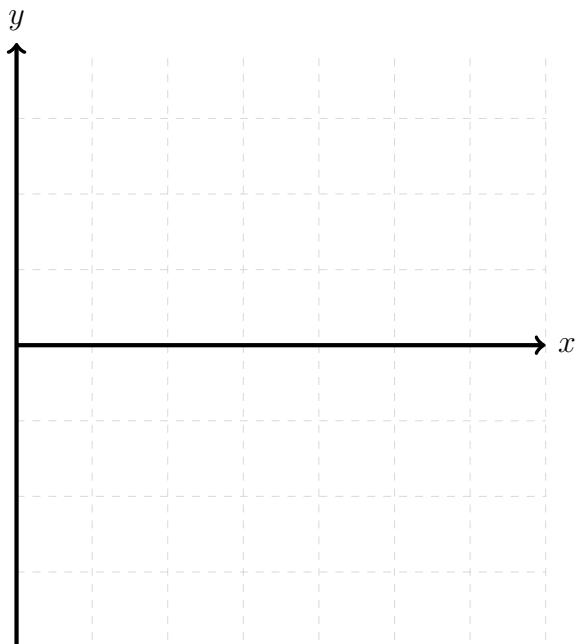
(d) What if the costs had instead tripled?

(e) Conclusion: If  $C(x) = kf(x)$  for a constant  $k$ , then (use  $f'(x)$  in your answer)

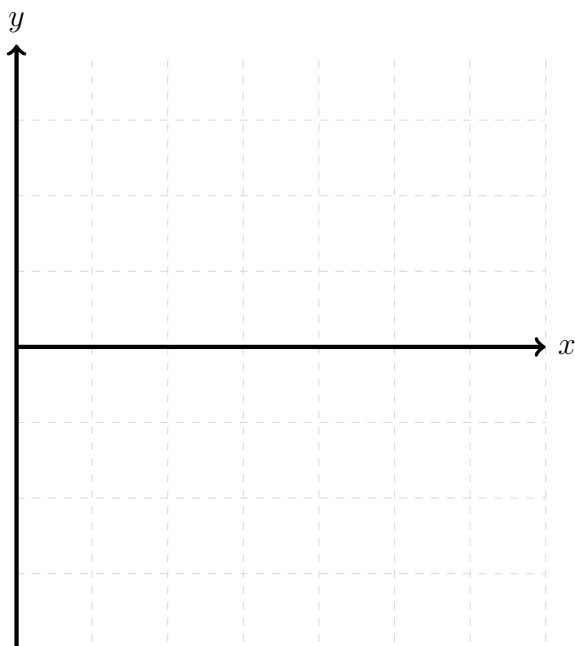
$$C'(x) =$$

3. Adding a constant:  $+C$ :

(a) Sketch both  $f(x) = \sin(2x)$  and  $g(x) = \sin(2x) + 2$  for  $0 \leq x \leq \pi$  into the axes below.



(b) Now use those graphs to sketch  $f'(x)$  and  $g'(x)$  into the axes below.



(c) What do you notice? Complete the sentence:

If  $g(x) = f(x) + C$  for a constant  $C$ , then  $g'(x) = \dots$