

From Autoencoders to Variational Autoencoders: The Loss Function

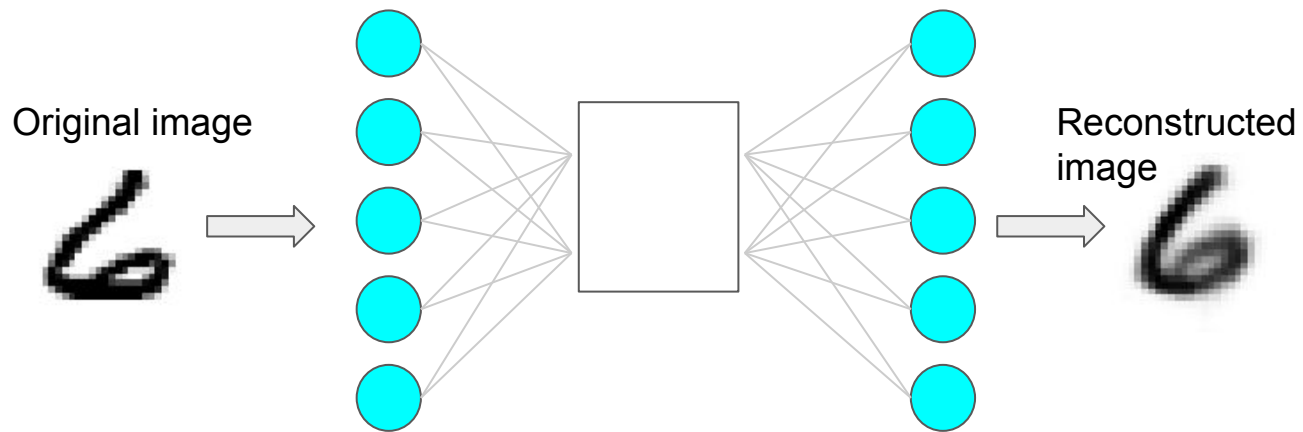
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- Modify encoder component
- Modify loss function

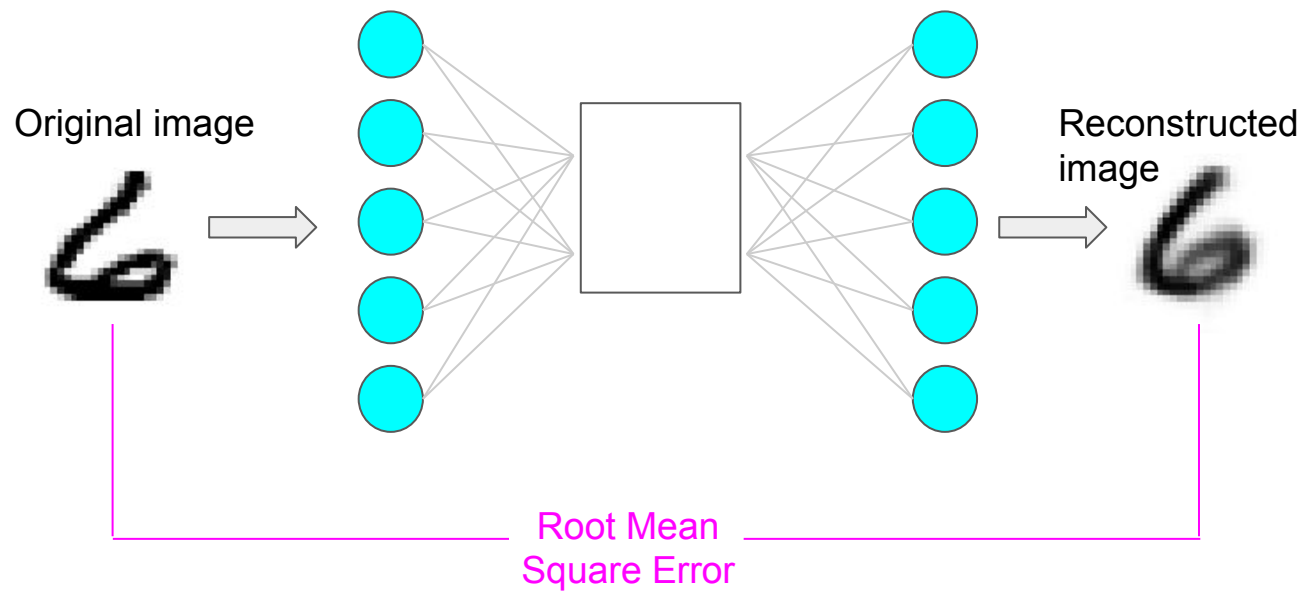
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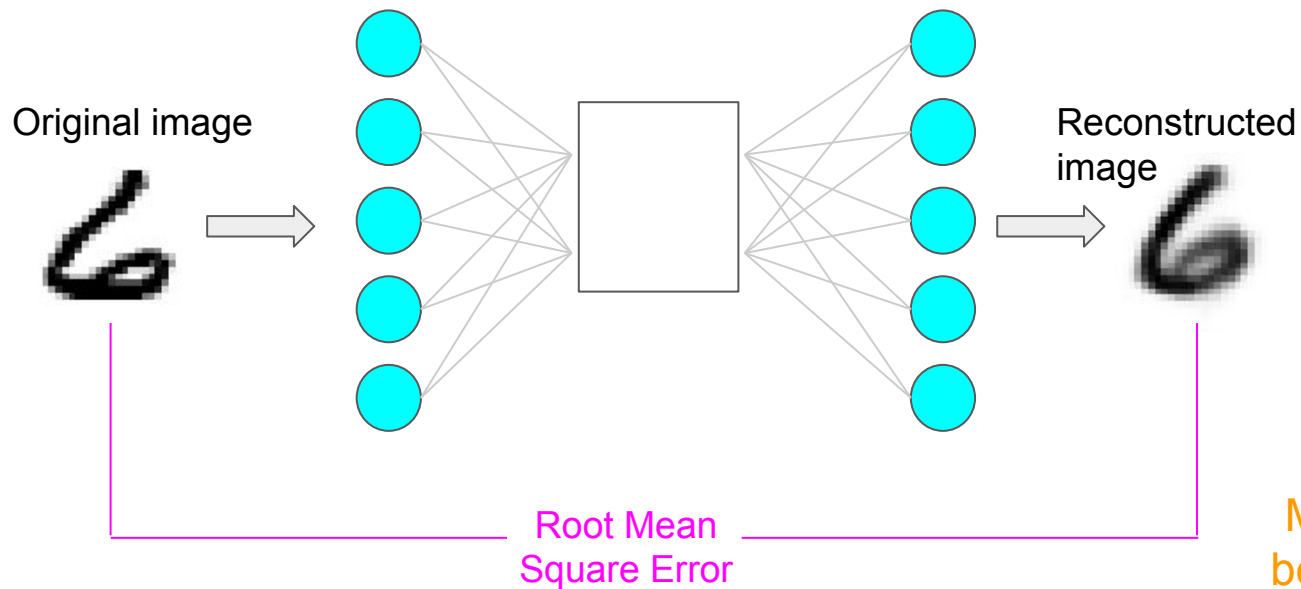
Loss function: Autoencoder



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Loss function: Autoencoder



Training goal:
Minimise difference
between original and
reconstructed image

Loss function: Autoencoder

$$LOSS = RMSE$$

Loss function: Variational Autoencoder

Kullback–Leibler Divergence

$$LOSS = RMSE + KL$$

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Reconstruction error

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Difference between
normal distribution
(mean vector, log
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standard normal
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Kullback–Leibler Divergence: The intuition

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- It's not a *distance*
 - KL divergence isn't symmetric
 - $KL(A, B) \neq KL(B, A)$
- Can be given in “closed” form with normal distributions

Kullback–Leibler Divergence (Closed form)

$$D_{KL}(N(\mu, \sigma) || N(0, 1)) = \frac{1}{2} \sum (1 + \log(\sigma^2) - \mu^2 - \sigma^2)$$

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Sum across all
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Loss function: Variational Autoencoder

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$$LOSS = RMSE + KL$$

Reconstruction error

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What does the KL loss term do?

Penalize observations where mean and log variance vectors differ significantly from the parameters of a standard normal distribution (mean vector = 0 and log variance = 0)

KL divergence loss term fixes

- Promotes symmetry around the origin
- Decreases chance of large gaps between clusters of points

Weighting the loss function

$$LOSS = \alpha \cdot RMSE + KL$$

reconstruction loss weight

Weighting the loss function

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- Finding the correct value for α is a delicate exercise
- If α is too small -> poorly reconstructed images
- If α is too large -> same issues as with AE
- α can be treated as a hyper-parameter to optimise

What next?

- Implement VAE