

H.W. 1

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- a) The height of the recursion tree is n at LoD n , because SnowFlake-Edge decrements n once for each recursive call it makes.
- b) The number of nodes corresponds to the number of edges at a given level. At each level of recursion, each edge splits into 4 edges. Since we start with 3 edges, there are $3 \cdot 4^i$ nodes.
- c) There's only 1 triangle at each node, so the asymptotic rendering time is $\Theta(1)$.
- d) At each level of the recursion tree, the number of triangles is equal to the number of edges from the last step, so it's $\Theta(\text{numtriangles}) = \Theta(\text{numedges}) = \Theta(4^i)$.
- e) Since rendering triangles of arbitrary size all takes the same amount of time, the total asymptotic cost is just the total number of triangles, which is $\Theta(4^n)$.
- f) The height of the recursion tree is still n .
- g) The number of nodes is still $3 \cdot 4^i$.
- h) The line segments aren't rendered til the end, so the asymptotic rendering time is 0.
- i) $\Theta(1)$, since there is 1 line rendered for each node.
- j) Nodes aren't rendered til the last level, so 0.
- k) The number of line segments that need to be rendered is a constant times the number of nodes. The number of nodes is 3×4^n , so the asymptotic rendering time is $\Theta(4^n)$.
- l) It's the cost of rendering the last level, which is $\Theta(4^n)$.
- m) The height of the recursion tree is still n .
- n) The number of nodes at a level is still $r \times 4^i$.
- o) It's 0 because nodes are only rendered at the last level.
- p) Rasterizing a line segment takes resources proportional to the length of the line. At each level, the line segment lengths get divided by 3. Thus, it is $\theta((1/3)^n)$.
- q) It's 0 since the lines aren't rasterized til the last level.
- r) We have to multiply the number of nodes by the length of the segments, which results is $3 \times 4^n \times (1/3)^n = \Theta((4/3)^n)$.
- s) It's $\Theta((4/3)^n)$.