# exploring\_word\_vectors

February 25, 2019

## 1 CS224N Assignment 1: Exploring Word Vectors (25 Points)

Welcome to CS224n!

Before you start, make sure you read the README.txt in the same directory as this notebook.

```
In [1]: # All Import Statements Defined Here
       # Note: Do not add to this list.
        # All the dependencies you need, can be installed by running .
        # -----
        import sys
       assert sys.version_info[0]==3
       assert sys.version_info[1] >= 5
       from gensim.models import KeyedVectors
       from gensim.test.utils import datapath
       import pprint
       import matplotlib.pyplot as plt
       plt.rcParams['figure.figsize'] = [10, 5]
       import nltk
       nltk.download('reuters')
       from nltk.corpus import reuters
        import numpy as np
        import random
       import scipy as sp
       from sklearn.decomposition import TruncatedSVD
       from sklearn.decomposition import PCA
       START_TOKEN = '<START>'
       END_TOKEN = '<END>'
       np.random.seed(0)
       random.seed(0)
        # -----
[nltk_data] Downloading package reuters to
[nltk_data] /Users/DrMatters/nltk_data...
```

### 1.1 Please Write Your SUNet ID Here:

#### 1.2 Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from *co-occurrence matrices*, and those derived via *word2vec*.

**Assignment Notes:** Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

**Note on Terminology:** The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

## 1.3 Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (Firth, J. R. 1957:11)

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, *co-occurrence matrices* (for more information, see here or here).

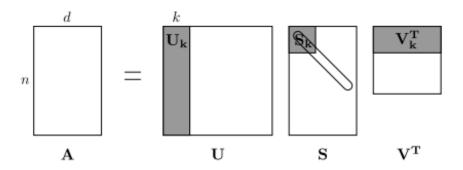
#### 1.3.1 Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word  $w_i$  occurring in the document, we consider the *context window* surrounding  $w_i$ . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document, i.e. words  $w_{i-n} \dots w_{i-1}$  and  $w_{i+1} \dots w_{i+n}$ . We build a *co-occurrence matrix* M, which is a symmetric word-by-word matrix in which  $M_{ij}$  is the number of times  $w_j$  appears inside  $w_i$ 's window.

## **Example: Co-Occurrence with Fixed Window of n=1**:

Document 1: "all that glitters is not gold" Document 2: "all is well that ends well"

*	START	all	that	glitters	is	not	gold	well	ends	END
START	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0



Picture of an SVD

*	START	all	that	glitters	is	not	gold	well	ends	END
gold	0	0	0	0	0	1	0	0	0	1
well	0	0	1	0	1	0	0	0	1	1
ends	0	0	1	0	0	0	0	1	0	0
END	0	0	0	0	0	0	1	1	0	0

**Note:** In NLP, we often add START and END tokens to represent the beginning and end of sentences, paragraphs or documents. In thise case we imagine START and END tokens encapsulating each document, e.g., "START All that glitters is not gold END", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on wordword co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run *dimensionality reduction*. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is A with n rows corresponding to n words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal S matrix, and our new, shorter length-k word vectors in  $U_k$ .

This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. *doctor* and *hospital* will be closer than *doctor* and *dog*.

**Notes:** If you can barely remember what an eigenvalue is, here's a slow, friendly introduction to SVD. If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures 7, 8, and 9 of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing pre-programmed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k— known as  $Truncated\ SVD$ — then there are reasonably scalable techniques to compute those iteratively.

#### 1.3.2 Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-

RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see https://www.nltk.org/book/ch02.html. We provide a read\_corpus function below that pulls out only articles from the "crude" (i.e. news articles about oil, gas, etc.) category. The function also adds START and END tokens to each of the documents, and lowercases words. You do **not** have perform any other kind of pre-processing.

Let's have a look what these documents are like....

```
[['<START>', 'japan', 'to', 'revise', 'long', '-', 'term', 'energy', 'demand', 'downwards', 't
   'ministry', 'of', 'international', 'trade', 'and', 'industry', '(', 'miti', ')', 'will', 're
   'its', 'long', '-', 'term', 'energy', 'supply', '/', 'demand', 'outlook', 'by', 'august', 'term', 'energy', 'supply', 'demand', 'outlook', 'by', 'august', 'term', '
   'meet', 'a', 'forecast', 'downtrend', 'in', 'japanese', 'energy', 'demand', ',', 'ministry',
   'officials', 'said', '.', 'miti', 'is', 'expected', 'to', 'lower', 'the', 'projection', 'for
   'primary', 'energy', 'supplies', 'in', 'the', 'year', '2000', 'to', '550', 'mln', 'kilolitre
   '(', 'kl', ')', 'from', '600', 'mln', ',', 'they', 'said', '.', 'the', 'decision', 'follows'
   'the', 'emergence', 'of', 'structural', 'changes', 'in', 'japanese', 'industry', 'following'
   'the', 'rise', 'in', 'the', 'value', 'of', 'the', 'yen', 'and', 'a', 'decline', 'in', 'domes'
   'electric', 'power', 'demand', '.', 'miti', 'is', 'planning', 'to', 'work', 'out', 'a', 'rev
   'energy', 'supply', '/', 'demand', 'outlook', 'through', 'deliberations', 'of', 'committee',
   'meetings', 'of', 'the', 'agency', 'of', 'natural', 'resources', 'and', 'energy', ',', 'the'
   'officials', 'said', '.', 'they', 'said', 'miti', 'will', 'also', 'review', 'the', 'breakdow
   'of', 'energy', 'supply', 'sources', ',', 'including', 'oil', ',', 'nuclear', ',', 'coal', 'a
   'natural', 'gas', '.', 'nuclear', 'energy', 'provided', 'the', 'bulk', 'of', 'japan', "'", 's
   'electric', 'power', 'in', 'the', 'fiscal', 'year', 'ended', 'march', '31', ',', 'supplying'
   'an', 'estimated', '27', 'pct', 'on', 'a', 'kilowatt', '/', 'hour', 'basis', ',', 'followed'
   'by', 'oil', '(', '23', 'pct', ')', 'and', 'liquefied', 'natural', 'gas', '(', '21', 'pct',
   'they', 'noted', '.', '<END>'],
 ['<START>', 'energy', '/', 'u', '.', 's', '.', 'petrochemical', 'industry', 'cheap', 'oil',
   'feedstocks', ',', 'the', 'weakened', 'u', '.', 's', '.', 'dollar', 'and', 'a', 'plant',
   'utilization', 'rate', 'approaching', '90', 'pct', 'will', 'propel', 'the', 'streamlined', '
   '.', 's', '.', 'petrochemical', 'industry', 'to', 'record', 'profits', 'this', 'year', ',',
   'with', 'growth', 'expected', 'through', 'at', 'least', '1990', ',', 'major', 'company',
   'executives', 'predicted', '.', 'this', 'bullish', 'outlook', 'for', 'chemical', 'manufactur
   'and', 'an', 'industrywide', 'move', 'to', 'shed', 'unrelated', 'businesses', 'has', 'prompte
```

'gaf', 'corp', '&', 'lt', ';', 'gaf', '>,', 'privately', '-', 'held', 'cain', 'chemical', 'i:

',', 'and', 'other', 'firms', 'to', 'aggressively', 'seek', 'acquisitions', 'of', 'petrochem 'plants', '.', 'oil', 'companies', 'such', 'as', 'ashland', 'oil', 'inc', '&', 'lt', ';', 'a '>,', 'the', 'kentucky', '-', 'based', 'oil', 'refiner', 'and', 'marketer', ',', 'are', 'alse 'shopping', 'for', 'money', '-', 'making', 'petrochemical', 'businesses', 'to', 'buy', '.', 'i', 'see', 'us', 'poised', 'at', 'the', 'threshold', 'of', 'a', 'golden', 'period', ',"', ' 'paul', 'oreffice', ',', 'chairman', 'of', 'giant', 'dow', 'chemical', 'co', '&', 'lt', ';', 'dow', '>,', 'adding', ',', '"', 'there', "'", 's', 'no', 'major', 'plant', 'capacity', 'bei 'added', 'around', 'the', 'world', 'now', '.', 'the', 'whole', 'game', 'is', 'bringing', 'ou 'new', 'products', 'and', 'improving', 'the', 'old', 'ones', '."', 'analysts', 'say', 'the', 'chemical', 'industry', "'", 's', 'biggest', 'customers', ',', 'automobile', 'manufacturers' 'and', 'home', 'builders', 'that', 'use', 'a', 'lot', 'of', 'paints', 'and', 'plastics', ',' 'are', 'expected', 'to', 'buy', 'quantities', 'this', 'year', '.', 'u', '.', 's', '.', 'petrochemical', 'plants', 'are', 'currently', 'operating', 'at', 'about', '90', 'pct', 'capacity', ',', 'reflecting', 'tighter', 'supply', 'that', 'could', 'hike', 'product', 'pri 'by', '30', 'to', '40', 'pct', 'this', 'year', ',', 'said', 'john', 'dosher', ',', 'managing 'director', 'of', 'pace', 'consultants', 'inc', 'of', 'houston', '.', 'demand', 'for', 'some 'products', 'such', 'as', 'styrene', 'could', 'push', 'profit', 'margins', 'up', 'by', 'as', 'much', 'as', '300', 'pct', ',', 'he', 'said', '.', 'oreffice', ',', 'speaking', 'at', 'a', 'meeting', 'of', 'chemical', 'engineers', 'in', 'houston', ',', 'said', 'dow', 'would', 'eas 'top', 'the', '741', 'mln', 'dlrs', 'it', 'earned', 'last', 'year', 'and', 'predicted', 'it' 'would', 'have', 'the', 'best', 'year', 'in', 'its', 'history', '.', 'in', '1985', ',', 'whe 'oil', 'prices', 'were', 'still', 'above', '25', 'dlrs', 'a', 'barrel', 'and', 'chemical', 'exports', 'were', 'adversely', 'affected', 'by', 'the', 'strong', 'u', '.', 's', '.', 'dollar ',', 'dow', 'had', 'profits', 'of', '58', 'mln', 'dlrs', '.', '"', 'i', 'believe', 'the', 'entire', 'chemical', 'industry', 'is', 'headed', 'for', 'a', 'record', 'year', 'or', 'close 'to', 'it', ',"', 'oreffice', 'said', '.', 'gaf', 'chairman', 'samuel', 'heyman', 'estimated 'that', 'the', 'u', '.', 's', '.', 'chemical', 'industry', 'would', 'report', 'a', '20', 'pc 'gain', 'in', 'profits', 'during', '1987', '.', 'last', 'year', ',', 'the', 'domestic', 'industry', 'earned', 'a', 'total', 'of', '13', 'billion', 'dlrs', ',', 'a', '54', 'pct', 'le 'from', '1985', '.', 'the', 'turn', 'in', 'the', 'fortunes', 'of', 'the', 'once', '-', 'sick' 'chemical', 'industry', 'has', 'been', 'brought', 'about', 'by', 'a', 'combination', 'of', ' 'and', 'planning', ',', 'said', 'pace', "'", 's', 'john', 'dosher', '.', 'dosher', 'said', ' 'year', "'", 's', 'fall', 'in', 'oil', 'prices', 'made', 'feedstocks', 'dramatically', 'chea 'and', 'at', 'the', 'same', 'time', 'the', 'american', 'dollar', 'was', 'weakening', 'agains' 'foreign', 'currencies', '.', 'that', 'helped', 'boost', 'u', '.', 's', '.', 'chemical', 'exports', '.', 'also', 'helping', 'to', 'bring', 'supply', 'and', 'demand', 'into', 'balance 'has', 'been', 'the', 'gradual', 'market', 'absorption', 'of', 'the', 'extra', 'chemical', 'manufacturing', 'capacity', 'created', 'by', 'middle', 'eastern', 'oil', 'producers', 'in', 'the', 'early', '1980s', '.', 'finally', ',', 'virtually', 'all', 'major', 'u', '.', 's', '. 'chemical', 'manufacturers', 'have', 'embarked', 'on', 'an', 'extensive', 'corporate', 'restructuring', 'program', 'to', 'mothball', 'inefficient', 'plants', ',', 'trim', 'the', 'payroll', 'and', 'eliminate', 'unrelated', 'businesses', '.', 'the', 'restructuring', 'touc 'off', 'a', 'flurry', 'of', 'friendly', 'and', 'hostile', 'takeover', 'attempts', '.', 'gaf' 'which', 'made', 'an', 'unsuccessful', 'attempt', 'in', '1985', 'to', 'acquire', 'union', 'carbide', 'corp', '&', 'lt', ';', 'uk', '>,', 'recently', 'offered', 'three', 'billion', 'd 'for', 'borg', 'warner', 'corp', '&', 'lt', ';', 'bor', '>,', 'a', 'chicago', 'manufacturer' 'of', 'plastics', 'and', 'chemicals', '.', 'another', 'industry', 'powerhouse', ',', 'w', '. 'r', '.', 'grace', '&', 'lt', ';', 'gra', '>', 'has', 'divested', 'its', 'retailing', ',',

'restaurant', 'and', 'fertilizer', 'businesses', 'to', 'raise', 'cash', 'for', 'chemical', 'acquisitions', '.', 'but', 'some', 'experts', 'worry', 'that', 'the', 'chemical', 'industry 'may', 'be', 'headed', 'for', 'trouble', 'if', 'companies', 'continue', 'turning', 'their', 'back', 'on', 'the', 'manufacturing', 'of', 'staple', 'petrochemical', 'commodities', ',', 's 'as', 'ethylene', ',', 'in', 'favor', 'of', 'more', 'profitable', 'specialty', 'chemicals', 'that', 'are', 'custom', '-', 'designed', 'for', 'a', 'small', 'group', 'of', 'buyers', '.', 'companies', 'like', 'dupont', '&', 'lt', ';', 'dd', '>', 'and', 'monsanto', 'co', '&', 'lt' 'mtc', '>', 'spent', 'the', 'past', 'two', 'or', 'three', 'years', 'trying', 'to', 'get', 'or' 'of', 'the', 'commodity', 'chemical', 'business', 'in', 'reaction', 'to', 'how', 'badly', 't 'market', 'had', 'deteriorated', ',"', 'dosher', 'said', '.', '"', 'but', 'i', 'think', 'the 'will', 'eventually', 'kill', 'the', 'margins', 'on', 'the', 'profitable', 'chemicals', 'in' 'the', 'niche', 'market', '."', 'some', 'top', 'chemical', 'executives', 'share', 'the', 'concern', '.', '"', 'the', 'challenge', 'for', 'our', 'industry', 'is', 'to', 'keep', 'from 'getting', 'carried', 'away', 'and', 'repeating', 'past', 'mistakes', ',"', 'gaf', "'", 's', 'heyman', 'cautioned', '.', '"', 'the', 'shift', 'from', 'commodity', 'chemicals', 'may', 'be 'ill', '-', 'advised', '.', 'specialty', 'businesses', 'do', 'not', 'stay', 'special', 'long '."', 'houston', '-', 'based', 'cain', 'chemical', ',', 'created', 'this', 'month', 'by', 't 'sterling', 'investment', 'banking', 'group', ',', 'believes', 'it', 'can', 'generate', '700 'mln', 'dlrs', 'in', 'annual', 'sales', 'by', 'bucking', 'the', 'industry', 'trend', '.', 'chairman', 'gordon', 'cain', ',', 'who', 'previously', 'led', 'a', 'leveraged', 'buyout', ' 'dupont', "'", 's', 'conoco', 'inc', "'", 's', 'chemical', 'business', ',', 'has', 'spent', '.', '1', 'billion', 'dlrs', 'since', 'january', 'to', 'buy', 'seven', 'petrochemical', 'pla 'along', 'the', 'texas', 'gulf', 'coast', '.', 'the', 'plants', 'produce', 'only', 'basic', 'commodity', 'petrochemicals', 'that', 'are', 'the', 'building', 'blocks', 'of', 'specialty' 'products', '.', '"', 'this', 'kind', 'of', 'commodity', 'chemical', 'business', 'will', 'ne 'be', 'a', 'glamorous', ',', 'high', '-', 'margin', 'business', ',"', 'cain', 'said', ',', 'adding', 'that', 'demand', 'is', 'expected', 'to', 'grow', 'by', 'about', 'three', 'pct', 'annually', '.', 'garo', 'armen', ',', 'an', 'analyst', 'with', 'dean', 'witter', 'reynolds' 'said', 'chemical', 'makers', 'have', 'also', 'benefitted', 'by', 'increasing', 'demand', 'fe 'plastics', 'as', 'prices', 'become', 'more', 'competitive', 'with', 'aluminum', ',', 'wood' 'and', 'steel', 'products', '.', 'armen', 'estimated', 'the', 'upturn', 'in', 'the', 'chemic 'business', 'could', 'last', 'as', 'long', 'as', 'four', 'or', 'five', 'years', ',', 'provid 'the', 'u', '.', 's', '.', 'economy', 'continues', 'its', 'modest', 'rate', 'of', 'growth', '<END>'], ['<START>', 'turkey', 'calls', 'for', 'dialogue', 'to', 'solve', 'dispute', 'turkey', 'said', 'today', 'its', 'disputes', 'with', 'greece', ',', 'including', 'rights', 'on', 'the', 'continental', 'shelf', 'in', 'the', 'aegean', 'sea', ',', 'should', 'be', 'solved', 'throug 'negotiations', '.', 'a', 'foreign', 'ministry', 'statement', 'said', 'the', 'latest', 'cris 'between', 'the', 'two', 'nato', 'members', 'stemmed', 'from', 'the', 'continental', 'shelf' 'dispute', 'and', 'an', 'agreement', 'on', 'this', 'issue', 'would', 'effect', 'the', 'secur ',', 'economy', 'and', 'other', 'rights', 'of', 'both', 'countries', '.', '"', 'as', 'the', 'issue', 'is', 'basicly', 'political', ',', 'a', 'solution', 'can', 'only', 'be', 'found', ' 'bilateral', 'negotiations', ',"', 'the', 'statement', 'said', '.', 'greece', 'has', 'repeate 'said', 'the', 'issue', 'was', 'legal', 'and', 'could', 'be', 'solved', 'at', 'the',

'international', 'court', 'of', 'justice', '.', 'the', 'two', 'countries', 'approached', 'arg' confrontation', 'last', 'month', 'after', 'greece', 'announced', 'it', 'planned', 'oil', 'exploration', 'work', 'in', 'the', 'aegean', 'and', 'turkey', 'said', 'it', 'would', 'also' 'search', 'for', 'oil', '.', 'a', 'face', '-', 'off', 'was', 'averted', 'when', 'turkey',

```
'confined', 'its', 'research', 'to', 'territorrial', 'waters', '.', '"", 'the', 'latest', 'crises', 'created', 'an', 'historic', 'opportunity', 'to', 'solve', 'the', 'disputes', 'bet' 'the', 'two', 'countries', ',"', 'the', 'foreign', 'ministry', 'statement', 'said', '.', 'tw' "'", 's', 'ambassador', 'in', 'athens', ',', 'nazmi', 'akiman', ',', 'was', 'due', 'to', 'prime', 'minister', 'andreas', 'papandreou', 'today', 'for', 'the', 'greek', 'reply', 'to', 'message', 'sent', 'last', 'week', 'by', 'turkish', 'prime', 'minister', 'turgut', 'ozal', 'the', 'contents', 'of', 'the', 'message', 'were', 'not', 'disclosed', '.', '<END>']]
```

## 1.3.3 Question 1.1: Implement distinct\_words [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with for loops, but it's more efficient to do it with Python list comprehensions. In particular, this may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information.

You may find it useful to use Python sets to remove duplicate words.

```
In [4]: def distinct_words(corpus):
           """ Determine a list of distinct words for the corpus.
                   corpus (list of list of strings): corpus of documents
               Return:
                   corpus_words (list of strings): list of distinct words across the corpus,
                   num corpus words (integer): number of distinct words across the corpus
           corpus_words = []
           num\_corpus\_words = -1
           # -----
           # Write your implementation here.
           flat = [item for sublist in corpus for item in sublist]
           corpus_words = sorted(list(set(flat)))
           num_corpus_words = len(corpus_words)
           # -----
           return corpus_words, num_corpus_words
In [5]: # -----
       # Run this sanity check
       # Note that this not an exhaustive check for correctness.
       # -----
       # Define toy corpus
       test_corpus = ["START All that glitters isn't gold END".split(" "), "START All's well "
       test_corpus_words, num_corpus_words = distinct_words(test_corpus)
       # Correct answers
```

ans\_test\_corpus\_words = sorted(list(set(["START", "All", "ends", "that", "gold", "All';

```
ans_num_corpus_words = len(ans_test_corpus_words)

# Test correct number of words
assert(num_corpus_words == ans_num_corpus_words), "Incorrect number of distinct words.

# Test correct words
assert (test_corpus_words == ans_test_corpus_words), "Incorrect corpus_words.\nCorrect

# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

## 1.3.4 Question 1.2: Implement compute\_co\_occurrence\_matrix [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use numpy (np) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n Python NumPy tutorial.

```
In [6]: def compute_co_occurrence_matrix(corpus, window_size=4):
            """ Compute co-occurrence matrix for the given corpus and window_size (default of .
                Note: Each word in a document should be at the center of a window. Words near
                      number of co-occurring words.
                      For example, if we take the document "START All that glitters is not gol
                      "All" will co-occur with "START", "that", "glitters", "is", and "not".
                Params:
                    corpus (list of list of strings): corpus of documents
                    window_size (int): size of context window
                Return:
                    M (numpy matrix of shape (number of corpus words, number of corpus words))
                        Co-occurence matrix of word counts.
                        The ordering of the words in the rows/columns should be the same as th
                    word2Ind (dict): dictionary that maps word to index (i.e. row/column numbe
            11 11 11
            words, num_words = distinct_words(corpus)
            M = None
            word2Ind = {}
            # -----
```

```
# Write your implementation here.
           M = np.zeros((num_words, num_words))
            for index, word in enumerate(words):
               word2Ind[word] = index
            for sentence in corpus:
               for center_word_pos in range(len(sentence)):
                    center_word_str = sentence[center_word_pos]
                    center_word_index = word2Ind[center_word_str]
                    # get a list of strings that contains center word and its window
                   window_set = sentence[
                       max([center_word_pos - window_size, 0]):
                       min([center_word_pos + window_size + 1, len(sentence)])
                    # remove center word from its window
                   window_set = set(window_set) - set([center_word_str])
                   for word in window_set:
                       word index = word2Ind[word]
                       M[center_word_index, word_index] += 1
            # -----
           return M, word2Ind
In [7]: # -----
        # Run this sanity check
        # Note that this is not an exhaustive check for correctness.
        # Define toy corpus and get student's co-occurrence matrix
       test_corpus = ["START All that glitters isn't gold END".split(" "), "START All's well "
       M_test, word2Ind_test = compute co_occurrence_matrix(test_corpus, window_size=1)
        # Correct M and word2Tnd
       M_test_ans = np.array(
            [[0., 0., 0., 1., 0., 0., 0., 0., 1., 0.,],
             [0., 0., 0., 1., 0., 0., 0., 0., 0., 1.,],
             [0., 0., 0., 0., 0., 0., 1., 0., 0., 1.,],
             [1., 1., 0., 0., 0., 0., 0., 0., 0., 0., ],
             [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
             [0., 0., 0., 0., 0., 0., 1., 1., 0.,],
             [0., 0., 1., 0., 0., 0., 0., 1., 0., 0.,],
             [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
             [1., 0., 0., 0., 1., 1., 0., 0., 0., 1.,],
             [0., 1., 1., 0., 1., 0., 0., 0., 1., 0.,]]
       )
```

```
word2Ind_ans = {'All': 0, "All's": 1, 'END': 2, 'START': 3, 'ends': 4, 'glitters': 5,
        # Test correct word2Ind
        assert (word2Ind_ans == word2Ind_test), "Your word2Ind is incorrect:\nCorrect: {}\nYour
        # Test correct M shape
        assert (M_test.shape == M_test_ans.shape), "M matrix has incorrect shape.\nCorrect: {}
        # Test correct M values
        for w1 in word2Ind_ans.keys():
            idx1 = word2Ind_ans[w1]
            for w2 in word2Ind_ans.keys():
                idx2 = word2Ind_ans[w2]
                student = M_test[idx1, idx2]
                correct = M_test_ans[idx1, idx2]
                if student != correct:
                    print("Correct M:")
                    print(M_test_ans)
                    print("Your M: ")
                    print(M_test)
                    raise AssertionError("Incorrect count at index ({}, {})=({}, {}) in matrix
        # Print Success
        print ("-" * 80)
        print("Passed All Tests!")
        print ("-" * 80)
Passed All Tests!
```

## 1.3.5 Question 1.3: Implement reduce\_to\_k\_dim [code] (1 point)

Params:

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

**Note:** All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD.

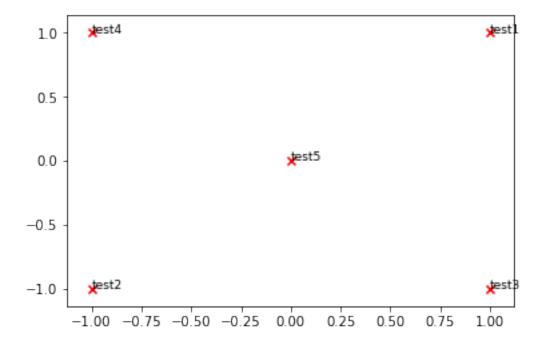
```
M (numpy matrix of shape (number of corpus words, number of corpus words))
                   k (int): embedding size of each word after dimension reduction
               Return:
                   M_{reduced} (numpy matrix of shape (number of corpus words, k)): matrix of k
                           In terms of the SVD from math class, this actually returns U * S
           n iters = 10
                          # Use this parameter in your call to `TruncatedSVD`
           M_reduced = None
           print("Running Truncated SVD over %i words..." % (M.shape[0]))
           # -----
           # Write your implementation here.
           svd = TruncatedSVD(n_components=k, n_iter=n_iters, random_state=42)
           M_reduced = svd.fit_transform(M)
           # -----
           print("Done.")
           return M_reduced
In [9]: # -----
        # Run this sanity check
        # Note that this not an exhaustive check for correctness
        # In fact we only check that your M_reduced has the right dimensions.
        # -----
       # Define toy corpus and run student code
       test_corpus = ["START All that glitters isn't gold END".split(" "), "START All's well '
       M_test, word2Ind_test = compute_co_occurrence_matrix(test_corpus, window_size=1)
       M_test_reduced = reduce_to_k_dim(M_test, k=2)
        # Test proper dimensions
       assert (M_test_reduced.shape[0] == 10), "M_reduced has {} rows; should have {}".format
       assert (M_test_reduced.shape[1] == 2), "M_reduced has {} columns; should have {}".form
        # Print Success
       print ("-" * 80)
       print("Passed All Tests!")
       print ("-" * 80)
Running Truncated SVD over 10 words...
Done
Passed All Tests!
```

#### 1.3.6 Question 1.4: Implement plot\_embeddings [code] (1 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code. In the future, a good way to make a plot is to look at the Matplotlib gallery, find a plot that looks somewhat like what you want, and adapt the code they give.

```
In [10]: def plot_embeddings(M_reduced, word2Ind, words):
             """ Plot in a scatterplot the embeddings of the words specified in the list "word
                NOTE: do not plot all the words listed in M_reduced / word2Ind.
                Include a label next to each point.
                Params:
                    M_reduced (numpy matrix of shape (number of unique words in the corpus ,
                    word2Ind (dict): dictionary that maps word to indices for matrix M
                    words (list of strings): words whose embeddings we want to visualize
             11 11 11
             # -----
             # Write your implementation here.
            for word in words:
                word index = word2Ind[word]
                word_x_emb = M_reduced[word_index, 0]
                word_y_emb = M_reduced[word_index, 1]
                plt.scatter(word_x_emb, word_y_emb, marker='x', color='red')
                plt.text(word_x_emb, word_y_emb, word, fontsize=9)
            plt.show()
             # -----
In [11]: # -----
        # Run this sanity check
         # Note that this not an exhaustive check for correctness.
         # The plot produced should look like the "test solution plot" depicted below.
        print ("-" * 80)
        print ("Outputted Plot:")
        M_reduced_plot_test = np.array([[1, 1], [-1, -1], [1, -1], [-1, 1], [0, 0]])
        word2Ind_plot_test = {'test1': 0, 'test2': 1, 'test3': 2, 'test4': 3, 'test5': 4}
        words = ['test1', 'test2', 'test3', 'test4', 'test5']
        plot_embeddings(M_reduced_plot_test, word2Ind_plot_test, words)
        print ("-" * 80)
Outputted Plot:
```



-----

#### **Test Plot Solution**

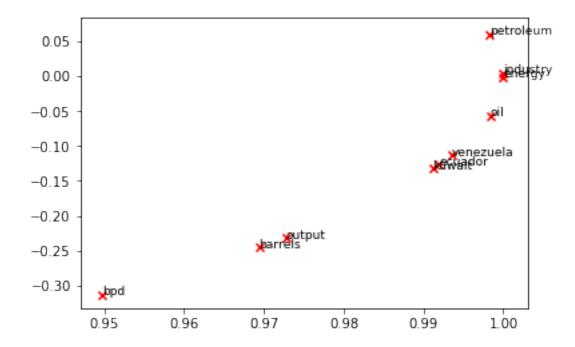
## 1.3.7 Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4, over the Reuters "crude" corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns U\*S, so we normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness). **Note**: The line of code below that does the normalizing uses the NumPy concept of *broadcasting*. If you don't know about broadcasting, check out Computation on Arrays: Broadcasting by Jake VanderPlas.

Run the below cell to produce the plot. It'll probably take a few seconds to run. What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? **Note:** "bpd" stands for "barrels per day" and is a commonly used abbreviation in crude oil topic articles.

```
# Rescale (normalize) the rows to make them each of unit-length
M_lengths = np.linalg.norm(M_reduced_co_occurrence, axis=1)
M_normalized = M_reduced_co_occurrence / M_lengths[:, np.newaxis] # broadcasting
words = ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output'
plot_embeddings(M_normalized, word2Ind_co_occurrence, words)
```

Running Truncated SVD over 8185 words... Done.



- ('industry', 'energy'), ('venezuela', 'ecuador', 'kuwait') and ('output', 'barrels') clusters together.
- ('bpd', 'barrels') probably should be clustered together

## 1.4 Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have come into fashion, e.g. word2vec. Here, we shall explore the embeddings produced by word2vec. Please revisit the class notes and lecture slides for more details on the word2vec algorithm. If you're feeling adventurous, challenge yourself and try reading the original paper.

Then run the following cells to load the word2vec vectors into memory. **Note**: This might take several minutes.

Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please follow the Piazza instructions, as how to run remotely

#### 1.4.1 Reducing dimensionality of Word2Vec Word Embeddings

Let's directly compare the word2vec embeddings to those of the co-occurrence matrix. Run the following cells to:

1. Put the 3 million word2vec vectors into a matrix M

word2Ind = {}

Loaded vocab size 3000000

on Stanford Farmshare machines.

2. Run reduce\_to\_k\_dim (your Truncated SVD function) to reduce the vectors from 300-dimensional to 2-dimensional.

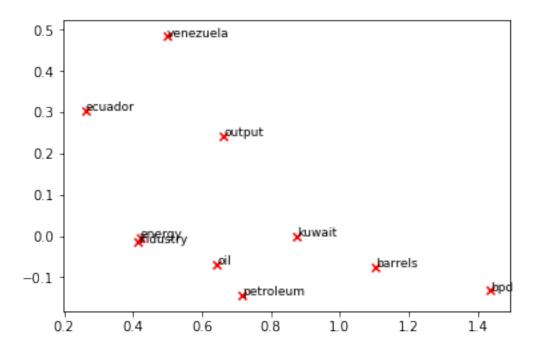
print("Putting %i words into word2Ind and matrix M..." % len(words))

```
M = \Gamma
            curInd = 0
            for w in words:
               try:
                   M.append(wv_from_bin.word_vec(w))
                   word2Ind[w] = curInd
                   curInd += 1
                except KeyError:
                   continue
            for w in required_words:
               try:
                   M.append(wv_from_bin.word_vec(w))
                   word2Ind[w] = curInd
                   curInd += 1
                except KeyError:
                   continue
            M = np.stack(M)
            print("Done.")
            return M, word2Ind
In [16]: # -----
        # Run Cell to Reduce 300-Dimensinal Word Embeddings to k Dimensions
        # Note: This may take several minutes
        M, word2Ind = get matrix of vectors(wv from bin)
        M_reduced = reduce_to_k_dim(M, k=2)
Shuffling words ...
Putting 10000 words into word2Ind and matrix M...
Done.
Running Truncated SVD over 10010 words...
Done.
```

## 1.4.2 Question 2.1: Word2Vec Plot Analysis [written] (4 points)

Run the cell below to plot the 2D word2vec embeddings for ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output', 'petroleum', 'venezuela'].

What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? How is the plot different from the one generated earlier from the co-occurrence matrix?



- ('energy', 'industry') clusters together
- ('pbd', 'barrels'), ('ecuador', 'venezuela', 'kuwait') probably should be clustered together
- Items were aligned with a single parabola on the first plot. Here they are aligned with two lines.

## 1.4.3 Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective L1 and L2 Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:

Instead of computing the actual angle, we can leave the similarity in terms of *similarity* =  $cos(\Theta)$ . Formally the Cosine Similarity s between two vectors p and q is defined as:

$$s = \frac{p \cdot q}{||p||||q||}$$
, where  $s \in [-1, 1]$ 

## 1.4.4 Question 2.2: Polysemous Words (2 points) [code + written]

Find a polysemous word (for example, "leaves" or "scoop") such that the top-10 most similar words (according to cosine similarity) contains related words from *both* meanings. For example, "leaves" has both "vanishes" and "stalks" in the top 10, and "scoop" has both "handed\_waffle\_cone" and "lowdown". You will probably need to try several polysemous words

before you find one. Please state the polysemous word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous words you tried didn't work?

**Note**: You should use the wv\_from\_bin.most\_similar(word) function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance please check the **GenSim documentation**.

Word 'head': 'heads' be in the leading position on. 'director' a person who is in charge of an activity, department, or organization.

It's hard to find polysemous words probably because word2vec model assumes a single vector per word type without considering polysemy. Link to original paper.

#### 1.4.5 Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words (w1,w2,w3) where w1 and w2 are synonyms and w1 and w3 are antonyms, but Cosine Distance(w1,w3) < Cosine Distance(w1,w2). For example, w1="happy" is closer to w3="sad" than to w2="cheerful".

Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the wv\_from\_bin.distance(w1, w2) function here in order to compute the cosine distance between two words. Please see the **GenSim documentation** for further assistance.

distance('easy', 'difficult') is small because these words are placed in same context more often, than ('easy', 'effortless'). It's possible to replace 'easy' for 'difficult' in many cases (This a difficult/easy climb). While it's not possible to use 'effortless' in this example.

#### 1.4.6 Solving Analogies with Word Vectors

Word2Vec vectors have been shown to sometimes exhibit the ability to solve analogies.

As an example, for the analogy "man: king:: woman: x", what is x?

In the cell below, we show you how to use word vectors to find x. The most\_similar function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list. The answer to the analogy will be the word ranked most similar (largest numerical value).

**Note:** Further Documentation on the most\_similar function can be found within the **GenSim** documentation.

## 1.4.7 Question 2.4: Finding Analogies [code + written] (2 Points)

Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y :: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

Note: You may have to try many analogies to find one that works!

```
In [30]: # ------
# Write your analogy exploration code here.
```

'old' is negative to 'young' and 'buy' is opposite to 'sell'

## 1.4.8 Question 2.5: Incorrect Analogy [code + written] (1 point)

Find an example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the (incorrect) value of b according to the word vectors.

'France' - 'Paris' should be similar to 'Spain' - 'Madrid' which is not presented here

## 1.4.9 Question 2.6: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit to our word embeddings.

Run the cell below, to examine (a) which terms are most similar to "woman" and "boss" and most dissimilar to "man", and (b) which terms are most similar to "man" and "boss" and most dissimilar to "woman". What do you find in the top 10?

```
In [32]: # Run this cell
    # Here `positive` indicates the list of words to be similar to and `negative` indicat
    # most dissimilar from.
    pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'boss'], negative=['man']))
    print()
    pprint.pprint(wv_from_bin.most_similar(positive=['man', 'boss'], negative=['woman']))
```

```
[('bosses', 0.5522644519805908),
('manageress', 0.49151360988616943),
('exec', 0.45940813422203064),
('Manageress', 0.45598435401916504),
('receptionist', 0.4474116563796997),
('Jane_Danson', 0.44480544328689575),
('Fiz_Jennie_McAlpine', 0.44275766611099243),
('Coronation_Street_actress', 0.44275566935539246),
('supremo', 0.4409853219985962),
('coworker', 0.43986251950263977)]
[('supremo', 0.6097398400306702),
('MOTHERWELL_boss', 0.5489562153816223),
('CARETAKER_boss', 0.5375303626060486),
('Bully_Wee_boss', 0.5333974361419678),
('YEOVIL_Town_boss', 0.5321705341339111),
('head_honcho', 0.5281980037689209),
('manager_Stan_Ternent', 0.525971531867981),
('Viv_Busby', 0.5256162881851196),
('striker_Gabby_Agbonlahor', 0.5250812768936157),
('BARNSLEY_boss', 0.5238943099975586)]
```

- (a) Neutral: 'bosses', 'exec'. Appropriate: 'manageress'. Biased: 'receptionist'.
- (b) "Bosses" of different sport teams.

('nurse\_practitioner', 0.6218312978744507),

('obstetrician', 0.6072014570236206),

('ob\_gyn', 0.5986712574958801),

## 1.4.10 Question 2.7: Independent Analysis of Bias in Word Vectors [code + written] (2 points)

Use the most\_similar function to find another case where some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

```
('midwife', 0.5927063226699829),
('dermatologist', 0.5739566683769226)]

[('doctors', 0.5891627073287964),
('physician', 0.5288864374160767),
('orthopedists', 0.4788447618484497),
('physicians', 0.4695263206958771),
('urologist', 0.467624306678772),
('surgeon', 0.45575428009033203),
('orthopedist', 0.4482683539390564),
('cardiologist', 0.4382314085960388),
('cardiologists', 0.4380047917366028),
('clinics', 0.43412768840789795)]
```

- Words that are similar to ('woman' + 'doctor' 'man') contain biased variants: ('nurse', 'midwife')
- Words that are similar to ('men' + 'doctor' 'women') contain different variants: ('physician', 'surgeon'), but they have smaller similarity (0.58 at maximum), thus they are not so strongly distinct.

## 1.4.11 Question 2.8: Thinking About Bias [written] (1 point)

What might be the cause of these biases in the word vectors?

Bias is the result of creating word vectors on not ideal corpuses. This happens because any bias in the articles that make up the Word2vec corpus is inevitably captured in the geometry of the vector space.

## 2 Submission Instructions

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Please make sure to have entered your SUNET ID above.
- 3. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of ll cells).
- 4. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 5. Once you've rerun everything, select File -> Download as -> PDF via LaTeX
- 6. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
- 7. Submit your PDF on Gradescope.