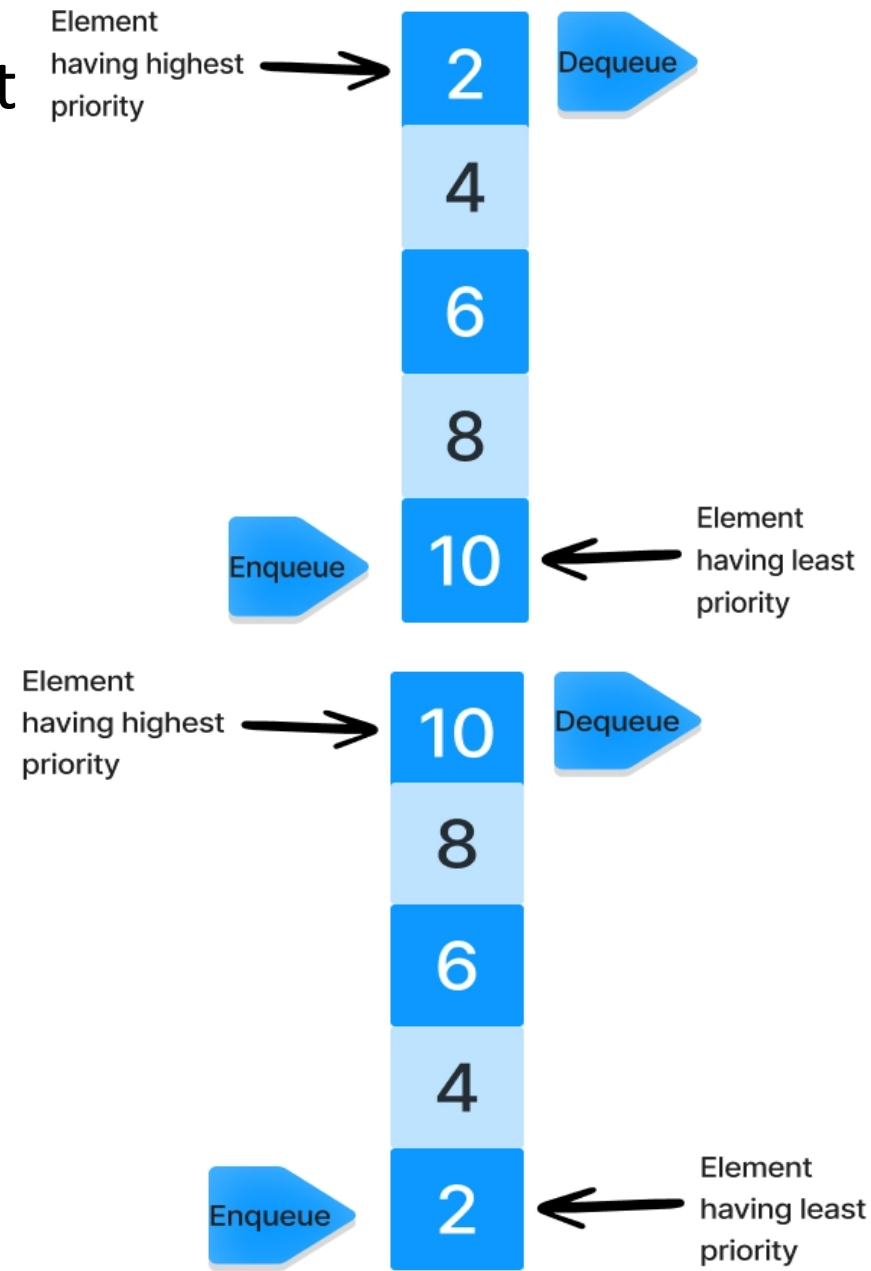


# Priority Queues

# Priority Queue



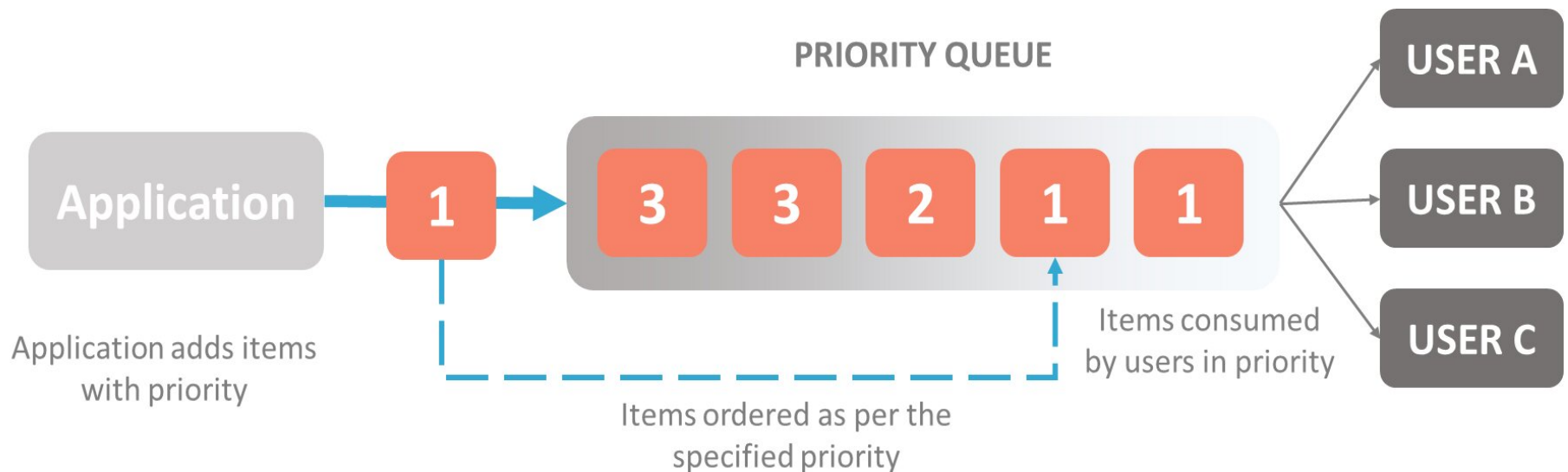
- A Priority Queue – a different kind of queue.
- Similar to a regular queue:
  - insert at rear,
  - remove from front.
- Items in priority queue are ordered by some key
- Item with the lowest key / highest key is always at the front from where they are removed.



# Priority Queue



- Items then 'inserted' in 'proper' position
- Idea behind the Priority Queue is simple:
  - Is a queue
  - But the items are ordered by a key.
  - Implies your 'position' in the queue may be changed by the arrival of a new item.

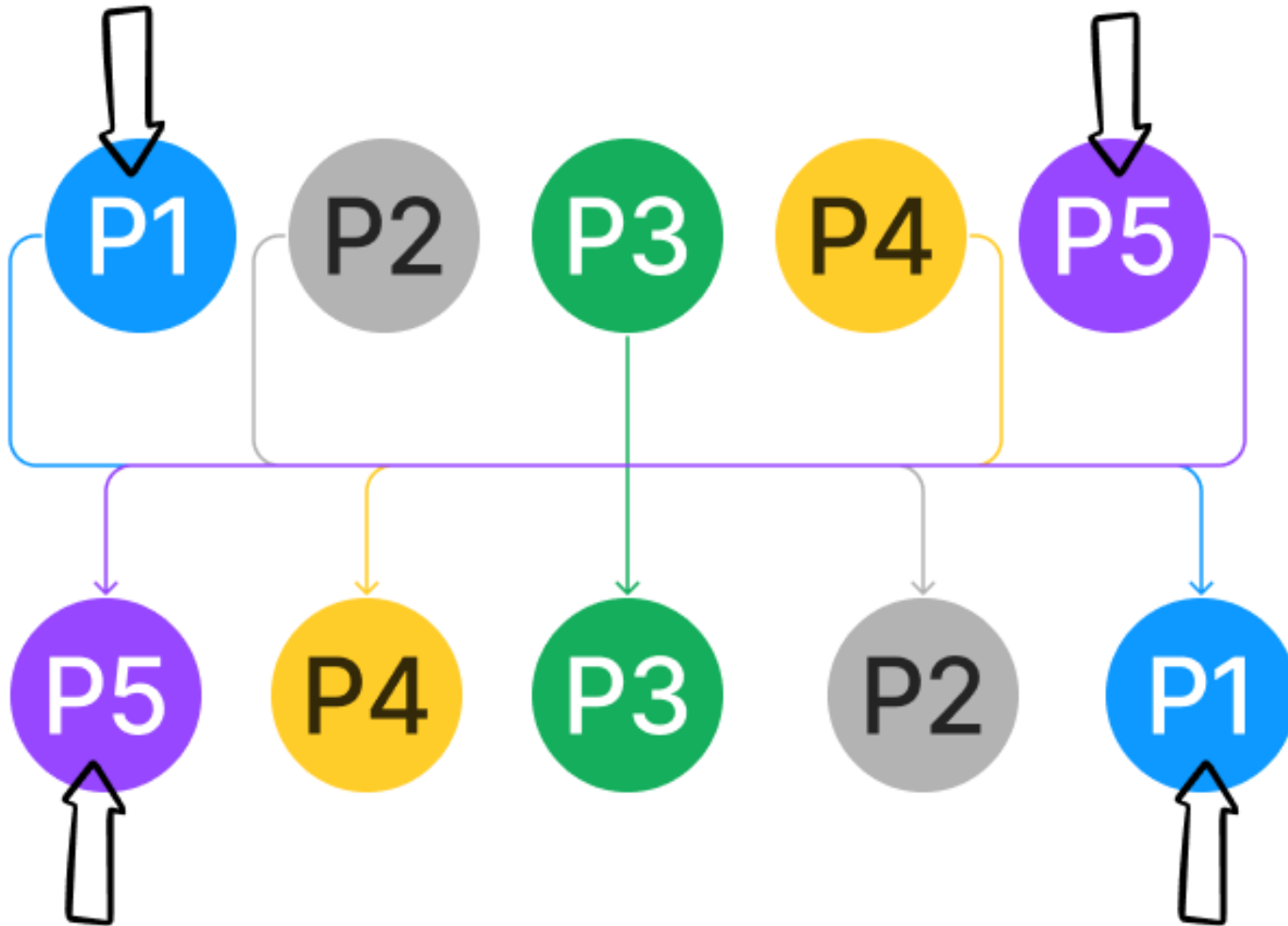


# Normal Queue



Entered the room first

Entered the room last



In case of  
Normal  
Queue

Leaves the room last

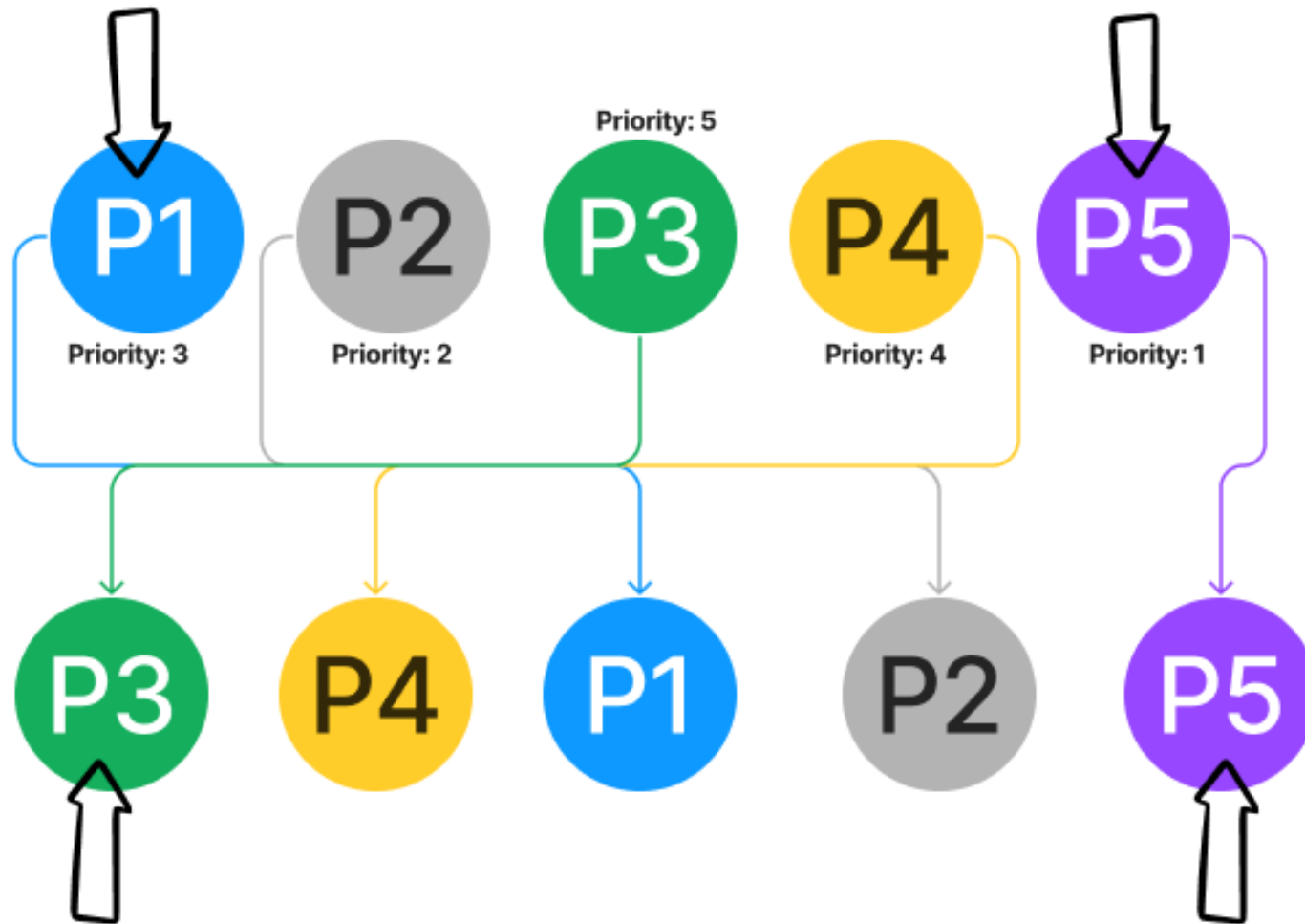
Leaves the room first

# Priority Queue



Entered the room first

Entered the room last



Leaves the room last

Leaves the room first



- Many, many applications.
  - Scheduling queues for a processor, print queues, transmit queues, disk scheduler etc.

Note: a priority queue is **no longer FIFO!**

You will still **remove from** the front of the queue, but **insertions** are governed by a **priority**.



- `remove()`
  - So, the first item has priority and can be retrieved (removed) quickly and returned to calling environment.
  - Hence, '`remove()`' is easy and will take  $O(1)$  time
- `insert()`
  - But, we want to insert quickly. Must go into proper position.



Implementing using **array**:

- **slow** to **insert()**, but this is the simplest and best approach where
- Number of items in the **pqueue** small, and
- **Insertion** speed is not critical.





- **Min Priority Queue**

- Minimum value gets the highest priority and
- Maximum value gets the lowest priority.

**Also called Ascending Order Priority Queue**

- **Max Priority Queue:**

- Maximum value gets the highest priority and
- Minimum value gets the lowest priority

**Also called Descending Order Priority Queue**



- **Priority Queue** can be implemented in **two** ways:
  - **Using ordered Array:** In ordered array **enqueue** operation takes  $O(n)$  time complexity because it enters elements in sorted order in queue. **Deletion** takes  $O(1)$  time complexity.
  - **Using unordered Array:** In unordered array **deletion** takes  $O(n)$  time complexity because it search for the element in Queue for the deletion and **enqueue** takes  $O(1)$  time complexity.



- **Enqueue** – Insert the item at the end of the priority queue takes  $O(1)$  time
- **Dequeue** – Remove the item with the highest priority
- **Peek** – Return item with highest priority

# Max Priority Queue (Unordered) Implementation in C

# C program to demonstrate Priority Queue



```
#include<stdio.h>
#include<limits.h>
#define MAX 100
int idx = -1;
// denotes where the last item in priority queue is
// initialized to -1 since no item is in queue
int pqVal[MAX];
// pqVal holds data for each index item
int pqPriority[MAX];
// pqPriority holds priority for each index item
```



```
int isEmpty( )  
{   return idx == -1;  
}
```

```
int isFull( )  
{   return idx == MAX - 1;  
}
```

# C program to demonstrate Priority Queue



//**enqueue** adds item to the end of the priority queue  $O(1)$

```
void enqueue(int data, int priority)
{  if(!isFull())
    {  idx++;
        pqVal[idx] = data;
        // Insert the element in priority queue
        pqPriority[idx] = priority;
    }
}
```



```
// peek returns item with highest priority  
// Max Priority Queue High priority number  
// means higher priority |  $O(N)$ 
```

```
int peek( )
```

```
{ // Max Priority, so assigned min value as initial value
```

```
    int maxPriority = INT_MIN;
```

```
    int indexPos = -1;
```





```
// Linear search for highest priority
for (int i = 0; i <= idx; i++)
{ // If two items have same priority choose the one
  // with higher data value
  if ( maxPriority == pqPriority[i] && indexPos > -1
      && pqVal[indexPos] < pqVal[i] )
  { maxPriority = pqPriority[i];
    indexPos = i;
  }
}
```



```
// MAX Priority so higher priority number means
// higher priority
    else if (maxPriority < pqPriority[i])
    {   maxPriority = pqPriority[i];
        indexPos = i;
    }
}
return indexPos;
}
```

# C program to demonstrate Priority Queue



```
// dequeue() removes the element with highest priority
// from the priority queue | O(N)
void dequeue( )
{ if( !isEmpty() )
    { // Get element with highest priority
        int indexPos = peek();
        // reduce size of priority queue by first shifting all elements
        // one position left from index where the
        // highest priority item was found
```



```
for (int i = indexPos; i < idx; i++)
{
    pqVal[i] = pqVal[i + 1];
    pqPriority[i] = pqPriority[i + 1];
}
// reduce size of priority queue by 1
idx--;
}
}
```



```
void display( )
{
    for (int i = 0; i <= idx; i++)
    {
        printf ( "(%d, %d) \n",
                  pqVal[i], pqPriority[i]);
    }
}
```

# C program to demonstrate Priority Queue



```
int main( )
{ enqueue(5, 1);    enqueue(10, 3);    enqueue(15, 4);
  enqueue(20, 5);    enqueue(500, 2);
  printf("Before Dequeue : \n");
  display();
  // Dequeue the top element
  dequeue();    // 20 dequeued
  dequeue();    // 15 dequeued
  printf("\nAfter Dequeue : \n");
  display();
}
```



- **Dequeue** – Remove the item from the end takes  $O(1)$  time
- **Enqueue** – Insert item according to their priority, lowest priority at the start and highest priority at the end. Items are arranged in ascending order of their priority value
- **Peek** – Return item with highest priority. Last item in the array itself will have highest priority

# Max Priority Queue (Ordered) Implementation in C



```
#include<stdio.h>
#include<limits.h>
#define MAX 100
// denotes where the last item in priority queue is
// initialized to -1 since no item is in queue
int idx = -1;
// pqVal holds data for each index item
// pqPriority holds priority for each index item
int pqVal[MAX];
int pqPriority[MAX];
```

```
int isEmpty( )  
{   return idx == -1;  
}
```

```
int isFull( )  
{   return idx == MAX - 1;  
}
```



```
void enqueue(int data, int priority)
{
    if( !isFull( ) )
    {
        if( idx == -1 )    // If empty, insert the New item
        {
            idx++;
            pqVal[idx] = data;
            pqPriority[idx] = priority;
            return;
        }
        else {    idx++;
```

```
// shift all items rightwards with higher
// priority than the element we trying to insert
for(int i = idx-1; i >= 0;i--)
{ if (pqPriority[i] >= priority)
  { pqVal[i+1] = pqVal[i];
    pqPriority[i+1] = pqPriority[i];
  }
```

else

```
{ // insert item just before where
  // lower priority index was found
  pqVal[i+1] = data;
    pqPriority[i+1] = priority;
    break;
  } // else
} // for
} // outer else
} // if
} // enqueue
```

```
// peek( ) returns item with highest priority  
// note highest priority in max priority queue is last  
// item in array
```

```
int peek( )  
{ return idx;  
}
```

```
void dequeue( )
```

```
{    idx--;  
}
```

```
// just reducing index would mean we have dequeued the  
// value would be still there but we can say that  
// no more than a garbage value
```

```
void display( )
```

```
{    for (int i = 0; i <= idx; i++)  
    {    printf ( "(%d, %d)\n",  
                pqVal[i], pqPriority[i]);  
    }  
}
```

```
int main()
{ // To enqueue items as per priority
    enqueue(25, 1); enqueue(10, 10); enqueue(15, 50);
    enqueue(20, 100); enqueue(30, 5); enqueue(40,
7);
    printf("Before Dequeue : \n");    display();
    // // Dequeue the top element
    dequeue(); // 20 dequeued
    dequeue(); // 15 dequeued
    printf("\nAfter Dequeue : \n");    display();
}
```