

Trigram Model

$$p(w_1, w_2, w_3, \dots, w_n) \approx p(w_1) p(w_2 | w_1) p(w_3 | w_2, w_1) \dots p(w_n | w_{n-1}, w_{n-2})$$

$$\begin{aligned} \text{Perplexity}(C) &= N \sqrt[N]{\frac{1}{\prod_{i=1}^N p(s_i)}} \\ &= 2^{-\frac{1}{N} \sum_{i=1}^N \log_2(p(s_i))} \end{aligned}$$

N = total length of test sentences

Sentence s with n words, $n \sqrt[n]{\frac{1}{p(w^n)}}$

$$\text{Perplexity}(C) = N \sqrt[N]{\frac{1}{p(s_1, s_2, \dots, s_N)}} \quad \text{Perplexity of corpus}$$

$$\text{Perplexity}(C) = 2^{-\frac{1}{N} \sum_{i=1}^N \log_2(p(w_1, w_2, w_3, \dots, w_n))}$$