

exercise 4: test diagnostics.

tuberculosis $\frac{15}{1000}$

- ① problem : "before" "after" \Rightarrow so better to use a table.

T = tuberculosis

\bar{T} = not tube

	before (B)	after (A)
T	15/10000	15 - 5 + 3 / 10000 = 13/10000
\bar{T}	9985/10000	9987/10000

- a) tuberculosis at "before" ?

$$P(T \cap B) = \frac{15}{10000} = 0,0015 //$$

- b) incidence

$$R = \text{Incidence proportion} = \frac{\text{Number of new cases during period}}{\text{Population at risk at start of period ("during these 5 years")}}$$

$$R(T) = \frac{3}{9985} = 3,005 \cdot 10^{-4} \approx 0,03\% //$$

- ② At the start, 15 people already had T, so people at risk was $10.000 - 15 = 9985$

c) incident rate (absolute risk) = $\frac{\text{no of new cases during period}}{\text{total person-time at risk}} =$

$$= \frac{3}{(9985) \cdot 5 \text{ years}} = \frac{3}{49.925} = 6 \cdot 10^{-5} // \text{ per person-years}$$

\uparrow
total time

- d) prevalence: proportion of individuals with tuberculosis.

At the end of 5 years (after)

$$P(T) = \frac{13}{10000} = 0,0003 = 3 \cdot 10^{-4}$$

exercise 4: test diagnostics

(2)

$C = \text{varicella/chickenpox}$

$V = \text{vaccinated}$

$\bar{V} = \text{unvaccinated}$

$$P(C \cap V) = \frac{18}{160}$$

$$P(\bar{C} \cap V) = \frac{142}{160}$$

$$P(C \cap \bar{V}) = \frac{30}{70}$$

$$P(\bar{C} \cap \bar{V}) = \frac{40}{70}$$

	Chicken pox	not chickenpox	Total
Vaccinated	18/160	142/160	160
not vacci	30/70	40/70	70

a) relative risk = RR(C) = $\frac{18/160}{30/70} = \frac{0,1125}{0,4286} = 0,2625$

\rightarrow UP (numerator)

0,26 = 26% \Rightarrow means that

vaccinated children had only a 26% risk of chickenpox compared to unvaccinated.

26% are less likely to get chickenpox

b) Odds ratio = $\frac{\text{event } C(C)}{\text{non-event } (\bar{C})}$

varicella of vaccinated people

$$\text{Vaccinated Odds}_V = \frac{C}{\bar{C}} = \frac{18}{142} = 0,127$$

$$\text{no vacu Odds}_U = \frac{C}{\bar{C}} = \frac{30}{40} = 0,75$$

c) what's more suitable?

- RR(C): seguir a las personas para ver quien desarrolla la enfermedad teniendo gente expuesta (vaccinate) y no expuesta (unvaccinated)
- Odds(OR): estudio convierte con gente ya enferma (casos) y se compara con gente no enferma (controles).

so 0,127 is the odds of V children of getting chickenpox

OR = $\frac{0,127}{0,75} \approx 0,169 //$

can also \rightarrow use this formula

therefore, RR(C) is more suitable.

(3)

	Test +	Test -	Total	
$D = \text{sick}$	2020	140	2160	
$\bar{D} = \text{healthy}$	80	7760	7840	
				$\rightarrow 10.000 \text{ people in total}$

a) sensitivity $P(+|D) = \frac{P(C \cap D)}{P(D)} = \frac{2020}{2160} \approx 0,93518$

specificity $P(-|\bar{D}) = \frac{P(\bar{C} \cap \bar{D})}{P(\bar{D})} = \frac{7760}{7840} \approx 0,9898$

b) PPV = $P(D|+) = \frac{P(D \cap +)}{P(+)} = \frac{2020}{2020 + 80} = \frac{2020}{2100} = 0,962 //$

NPV = $P(\bar{D}|-) = \frac{P(\bar{D} \cap -)}{P(-)} = \frac{7760}{7760 + 140} = 0,982 //$

c) P(correct diagnosis) = $P(D|+) + P(\bar{D}|-) = \frac{2020 + 7760}{10.000} = 0,978 //$