

# exercise 4: test diagnostics.

tuberculosis  $\frac{15}{10000}$

① problem: "before" "after"  $\Rightarrow$  so better to use a table.

T = tuberculosis  
 $\bar{T}$  = not tube.

	before (B)	after (A)
T	15/10000	15 - 5 + 3 / 10000 = 13/10000
$\bar{T}$	9985/10000	9.987/10000

a) tuberculosis at "before"?

$$P(T \cap B) = \frac{15}{10000} = 0,0015 \%$$

b) incidence

R = Incidence proportion =  $\frac{\text{Number of new cases during period}}{\text{population at risk at start of period}}$  ("during these 5 years")

$$R(T) = \frac{3}{9985} = 3,005 \cdot 10^{-4} \approx 0,03 \%$$

⊗ At the start, 15 people already had T, so people at risk was  $10.000 - 15 = 9985$

c) Incident rate (absolute risk) =  $\frac{\text{no of new cases during period}}{\text{Total person time at risk}}$

$$= \frac{3}{(9985) \cdot 5 \text{ years}} = \frac{3}{49.925} = 6 \cdot 10^{-5} \text{ per person-years}$$

↑  
total time

d) prevalence = proportion of individuals with tuberculosis.

At the end of 5 years (after)

$$P(T) = \frac{13}{10000} = 0,0003 = 3 \cdot 10^{-4}$$



# exercise 4: test diagnostics

②

C = varicella/chickenpox

V = vaccinated

$\bar{V}$  = unvaccinated

$$P(C \cap V) = \frac{18}{160}$$

$$P(\bar{C} \cap V) = \frac{142}{160}$$

$$P(C \cap \bar{V}) = \frac{30}{70}$$

$$P(\bar{C} \cap \bar{V}) = \frac{40}{70}$$

	chicken pox	not chickenp.	Total
vaccinated	18/160	142/160	160
not vacci	30/70	40/70	70

a) relative risk  $\Rightarrow RR(C) = \frac{18/160}{30/70} = \frac{0,1125}{0,4286} = 0,2625$

of varicella  
of vaccinated  
people  $\rightarrow$  up (numerator)

0,26 = 26% means that

vaccinated children had only a 26% risk of chickenpox compared to unvaccinated.

26% are less likely to get chickenpox

b) Odd ratio =  $\frac{\text{event} + (C)}{\text{non-event} + (\bar{C})}$

varicella of vaccinated people

Vaccinated Odds<sub>V</sub> =  $\frac{C}{\bar{C}} = \frac{18}{142} = 0,127$

no vacc Odds =  $\frac{C'}{\bar{C}'} = \frac{30}{40} = 0,75$

OR =  $\frac{\text{exposed (vacc)}}{\text{unexp. (unvaccinated)}}$

OR =  $\frac{0,127}{0,75} \approx 0,169$

can also just use the formula

so 0,169 is the odds of V children of getting chickenpox

• RR(C): seguir a las personas para ver quien desarrolla la enfermedad teniendo gente expuesta (vaccinated) y no expuesta (unvaccinated)

• Odds(OR): estudio coherente con gente ya enferma (casos) y se compara con gente no enferma (controls)

Therefore, RR(C) is more suitable.

③

	Test +	Test -	Total
D = sick	2020	140	2160
$\bar{D}$ = healthy	80	7760	7840

} = 10.000 people in total

a) sensitivity  $P(+|D) = \frac{P(+ \cap D)}{P(D)} = \frac{2020}{2160} \approx 0,93518$

specificity  $P(-|\bar{D}) = \frac{P(- \cap \bar{D})}{P(\bar{D})} = \frac{7760}{7840} \approx 0,9898$

b) PPV =  $P(D|+) = \frac{P(D \cap +)}{P(+)} = \frac{2020}{2020 + 80} = \frac{2020}{2100} = 0,962$

NPV =  $P(\bar{D}|-) = \frac{P(\bar{D} \cap -)}{P(-)} = \frac{7760}{7760 + 140} = 0,982$

c) P(correct diagnosis) =  $P(D \cap +) + P(\bar{D} \cap -) = \frac{2020 + 7760}{10.000} = 0,978$

people tested