Relational Model

CS 377: Database Systems

ER Model: Recap

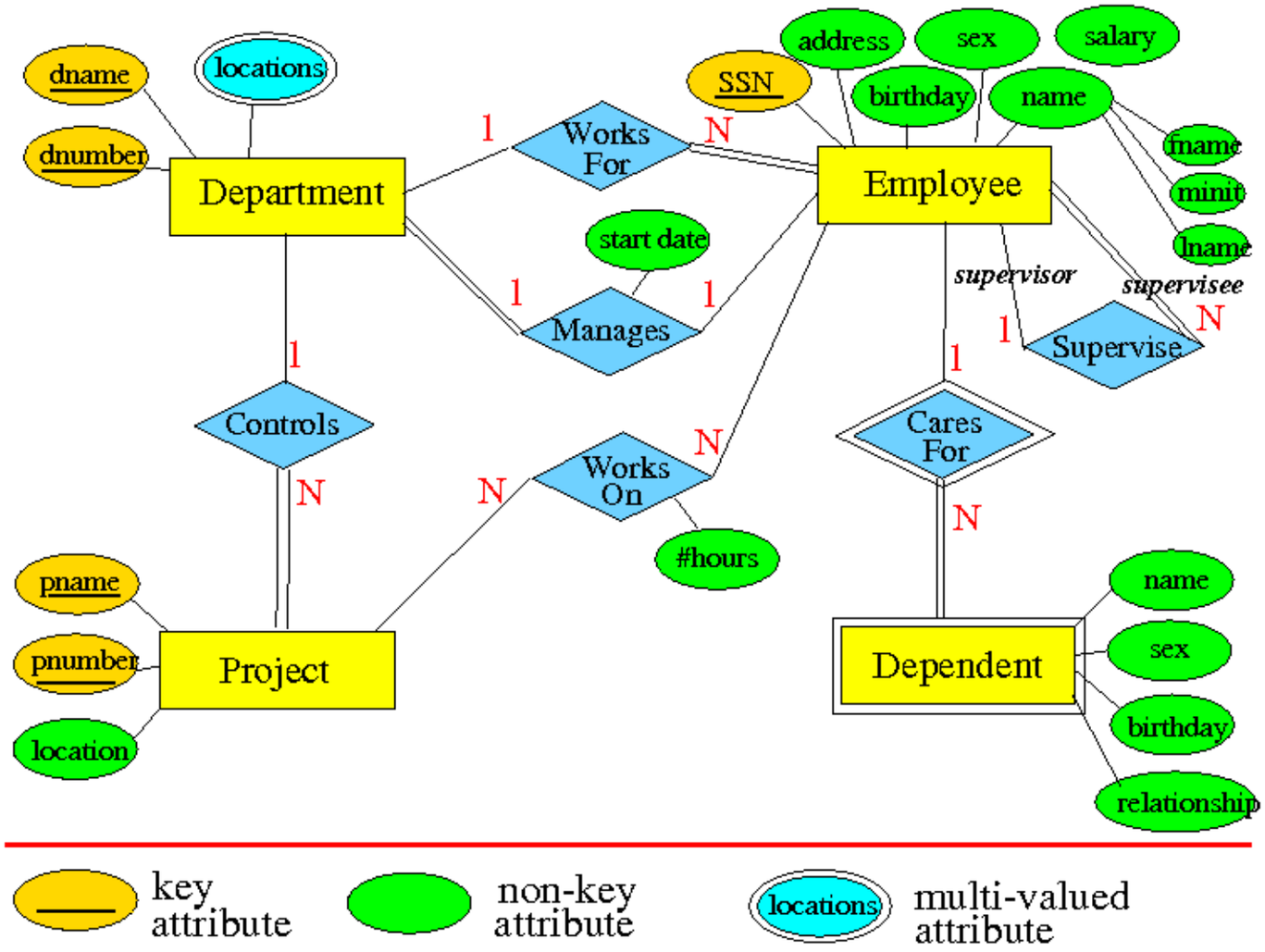
Recap: Conceptual Models

- A high-level description of the database
- Sufficiently precise that technical people can understand it
- But, not so precise that non-technical people can participate in the process

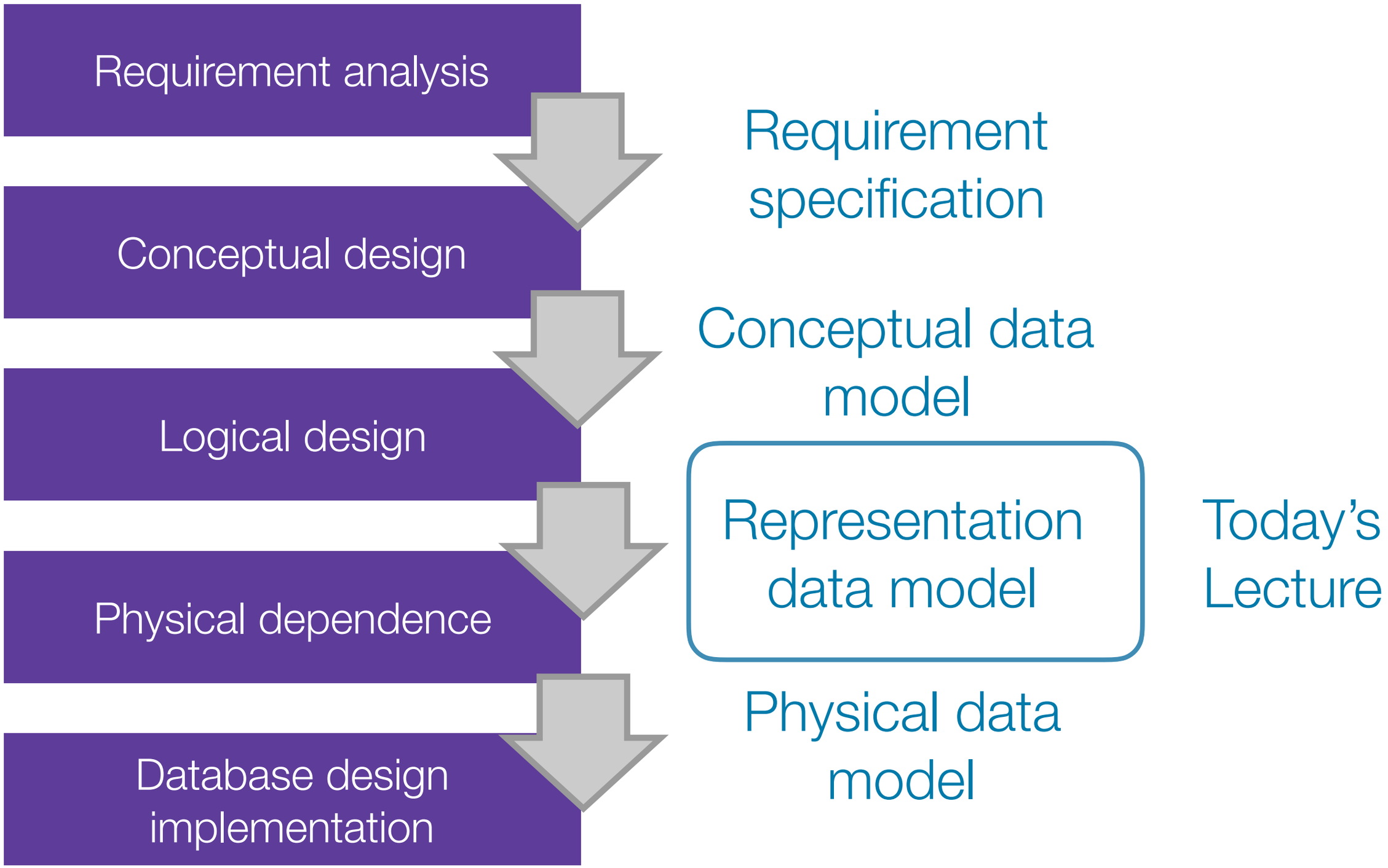
This is where ER models fit in

Recap: ER Model

- Entities
  - Attributes
- Relationships
  - Degree
  - Cardinality
  - Participation



Recap: Building a Database System



Today's Lecture

1. Relational Model
2. ER to Relational Mapping
   - Example: Company Database
   - Exercise: Football

Relational Model

- First formal database model
- Introduced by Ted Codd in 1970
- Conceptual basis of relational databases
  - Simple and based on the mathematical relations
  - Declarative method for specifying data and queries
- Previous models include hierarchical and network models

Relational Model: Relation

Data is stored in **tables** (**relations**)

PRODUCT

Name	Category	Price	Manufacter
iPad	Tablet	$399.00	Apple
Surface	Tablet	$299.00	Microsoft
Kindle	eReader	$79.00	Amazon
…	…	…	…

Relational Model: Schema

Relational schema R(A_1, A_2, …, A_n): made of of a relation name R and a set of attributes A_1, A_2, …, A_n

Product(name, category, price, manufacturer)

PRODUCT

Name	Category	Price	Manufacter
iPad	Tablet	$399.00	Apple
Surface	Tablet	$299.00	Microsoft
Kindle	eReader	$79.00	Amazon
…	…	…	…

Relational Model: Attribute

Attribute is a column header in the table

PRODUCT

Name	Category	Price	Manufacter
iPad	Tablet	$399.00	Apple
Surface	Tablet	$299.00	Microsoft
Kindle	eReader	$79.00	Amazon
…	…	…	…

Relational Model: Tuple

Tuple or **row** or **record** is a single entry in the table having the attributes specified by the schema

PRODUCT

Name	Category	Price	Manufacter
iPad	Tablet	$399.00	Apple
Surface	Tablet	$299.00	Microsoft
Kindle	eReader	$79.00	Amazon
…	…	…	…

Relational Model: Instance

Instance of a relation is a set of tuples or records

PRODUCT

Name	Category	Price	Manufacter
iPad	Tablet	$399.00	Apple
Surface	Tablet	$299.00	Microsoft
Kindle	eReader	$79.00	Amazon
…	…	…	…

Relation Definitions

- **Domain**: set of atomic values that are assigned to an attribute (e.g., name: string, category: string, price: real)
    - In practice, the domain is added for each attribute of the relational schema
- **Degree of a relation**: number of attributes in the relation schema
    - this is different than the degree in ER model!

Database: Schema & Instance

- **Database schema**: a collection of relation schemas
- **Instance of a database**: a collection of relation instances
- Schemas are stable over long periods of time while instance changes constantly with data inserts, updates, and deletions

Can view schemas as types while instances as values in a programming language

Relational Model Notation

Notation	Description
$R(A_1, A_2, \ldots, A_n)$	Relation schema R of degree n
Q, R, S	Relation names
q, r, s	Relations
t, u, v	Tuples
$t(a_1, a_2, \ldots, a_n)$	tuple t of a relation
$t[A_i]$	the value of the attribute A_i in the tuple t
$t[A_i, A_j, A_k]$	value of the attributes A_i, A_j ,A_k in the tuple t

Relational Model Constraints

- Restrictions on actual values in a database

- **Inherent model-based constraints** or **implicit constraints**: inherent in the data model (e.g., no duplicate tuples)

- **Schema-based constraints** or **explicit constraints**: can be directly expressed in schemas of the data model

- **Application-based / semantic constraints**, or **business rules**: cannot be directly expressed in schemas and can only be enforced and expressed in the application program

Schema-based Constraints: Domain Constraints

- Value of attribute A: atomic value from the domain of A
- Typical data types associated with domains

PRODUCT

Should be numeric, not string

Name	Category	Price	Manufacter
iPad	Tablet	$399.00	Apple
Surface	Tablet	$299.00	Microsoft
Kindle	eReader	$79.00	Amazon
...	...	...	...

Schema-based Constraints: Key Constraints

- No two tuples can have the same combination of values for all their attributes

- **Superkey**: set of attributes in a relation R such that no 2 different tuples will have the same values for that set of attributes

$$\forall t_1, t_2 \in R : t_1[SK] \neq t_2[SK]$$

Schema-based Constraints: Key Constraints

- **Key**: minimal set of attributes in relation R such that no 2 tuples have the same values (i.e., key is a minimal superkey)
- **Candidate key**: any key

PERSON

key(s)

PID	SSN	Name	Address
52032	111-12-2345	John Doe	123 My Street
12345	444-23-1234	Jane Smith	555 South Street
79823	555-67-8910	Tom Thumb	224 First Street
…	…	…	…

Schema-based Constraints: Key Constraints

- **Primary key**: key chosen to be used to identify tuples in a relation

  - Once chosen, you must use that primary key throughout the database

  - Other candidate keys are unique keys

  - Every relation schema must have a primary key

- **Foreign key**: set of attributes inside some relation *R1* that is a primary key of another relation *R2*

Example: Primary & Foreign Key

primary key

PERSON

PID	SSN	Name	Address
52032	111-12-2345	John Doe	123 My Street
12345	444-23-1234	Jane Smith	555 South Street
79823	555-67-8910	Tom Thumb	224 First Street
…	…	…	…

primary key

foreign key

PURCHASE

TID	PID	Product	Price
123456778	52032	iPad Air 2	$399.00
123470901	52032	Kindle	$79.00
234096701	79823	Surface	$499.00
…	…	…	…

Schema-based Constraints: Entity Integrity

- Primary key values cannot have NULL values
- Primary key is used to identify a tuple
- NULL value means not applicable or not available which hinders the ability to identify a tuple

PERSON

PID	SSN	Name	Address
52032	111-12-2345	John Doe	123 My Street
NULL	444-23-1234	Jane Smith	555 South Street
…	…	…	…

Not allowed!

Schema-based Constraints: Referential Integrity

- A tuple in one relation (t_1 in R_1) that refers to another relation (t_2 in R_2) must refer to an existing tuple in that relation (t_2 must exist): $t_1[FK] = t_2[PK]$
- R_1 is the referencing relation and R_2 is the referenced relation

tuple must exist in PERSON table

PURCHASE

TID	PID	Product	Price
123456778	52032	iPad Air 2	$399.00
123470901	52032	Kindle	$79.00
234096701	79823	Surface	$499.00
…	…	…	…

Relational Model Virtues

- Physical & logical independence
- Declarative
- Simple, elegant and clean: everything is a relation

Why did it take so long?
Doubted it could be done efficiently

ER Model vs Relational Model

ER model (conceptual model)

- Several concepts: entities, relationships, attributes
- Well-suited for capturing application requirements
- Not well-suited for computer implementation

Relational model (implementation model)

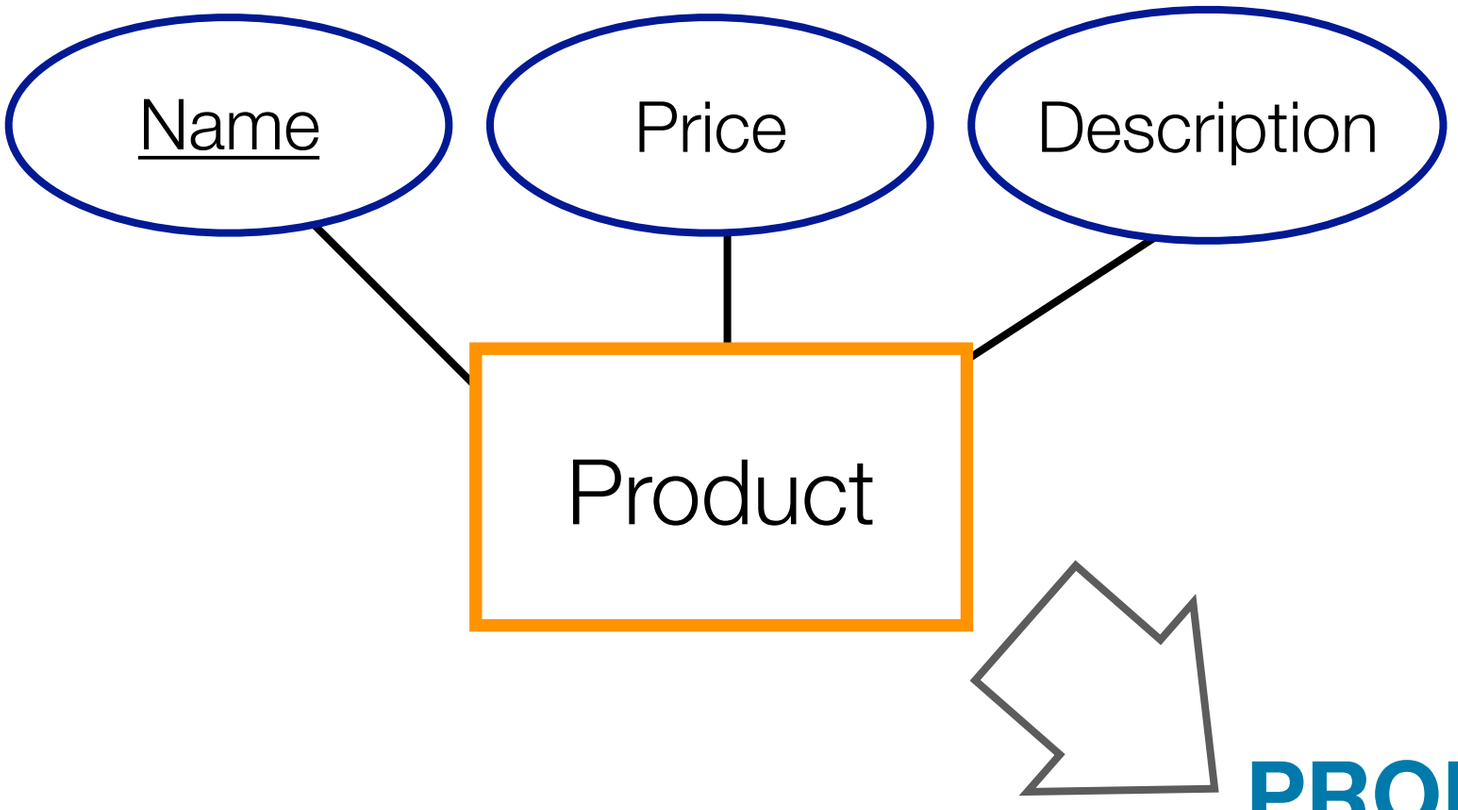
- Single concept: relation (not same as mathematical concept!)
- Everything is represented with a collection of tables
- Well-suited for efficient manipulations on computers

ER-to-Relational Mapping: Step 1

Convert Entities to Relations

- Basic case: entity set E —> relation with attributes of E
- Special case: weak entity & multi-valued attributes

Basic Case: Entity to Relation



PRODUCT

Name	Price	Description
...	...	...

Special Case: Multi-valued Attribute

- Naive storing of multi-valued attributes:
  - Variable-length records causes inefficient in storage
  - Multiple tuples leads to lots of redundancy

STORE

Number	Name	{Locations}
1	Apple	Cumberland Mall
1	Apple	Lenox Square
2	Macys	Lenox Square
2	Macys	Cumberland Mall
…	…	…

Special Case: Multi-valued Attribute

- Naive storing of multi-valued attributes:
  - Variable-length records causes inefficient in storage
  - Multiple tuples leads to lots of redundancy
- Use the key concept
  - Convert multi-valued attribute to new relation X
  - Add foreign key to that relation

Special Case: Multi-valued Attribute

STORE_LOC

locID	Location
1	Lenox Square
2	Cumberland Mall
…	…

foreign key: referential integrity

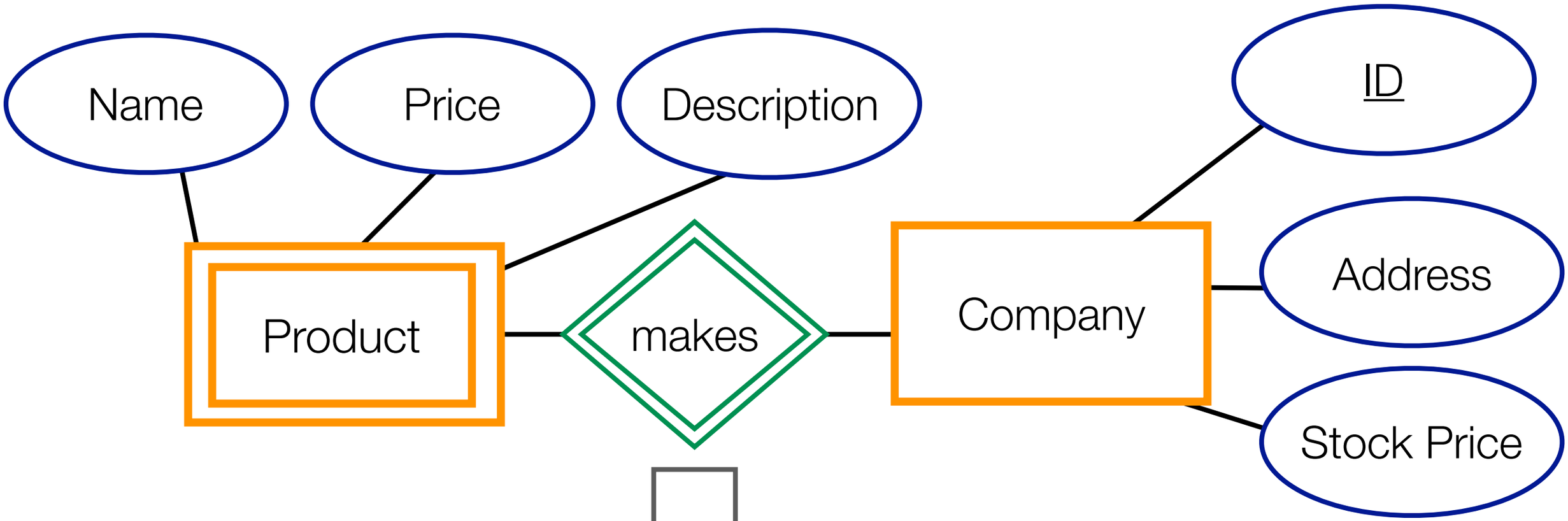
STORE

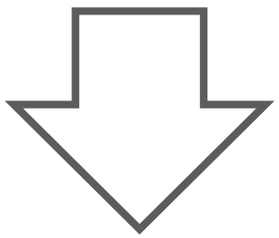
sNumber	Name	locID
1	Apple	1
1	Apple	2
2	Macys	1
2	Macys	2
…	…	…

Special Case: Weak Entity

- Weak entity does not have a key —> relation violation
- Borrow key from the other entity in the identifying relationship (E) and add it to the weak entity (W)
- Result: key of weak entity consists of the key of the related entity and some identifying attribute of the weak entity

Special Case: Weak Entity





PRODUCT

foreign key

Name	cID	Price	Manufacter
...	...	...	...

weak entity key

ER-to-Relational Mapping: Step 2

Map Relationships to Relations

- Basic case: relationship R —> relation with attributes being keys of related entity sets and attributes of R

- Special case: expansion, merging, & n-ary relationship types

Basic Case: Relationship to Entity

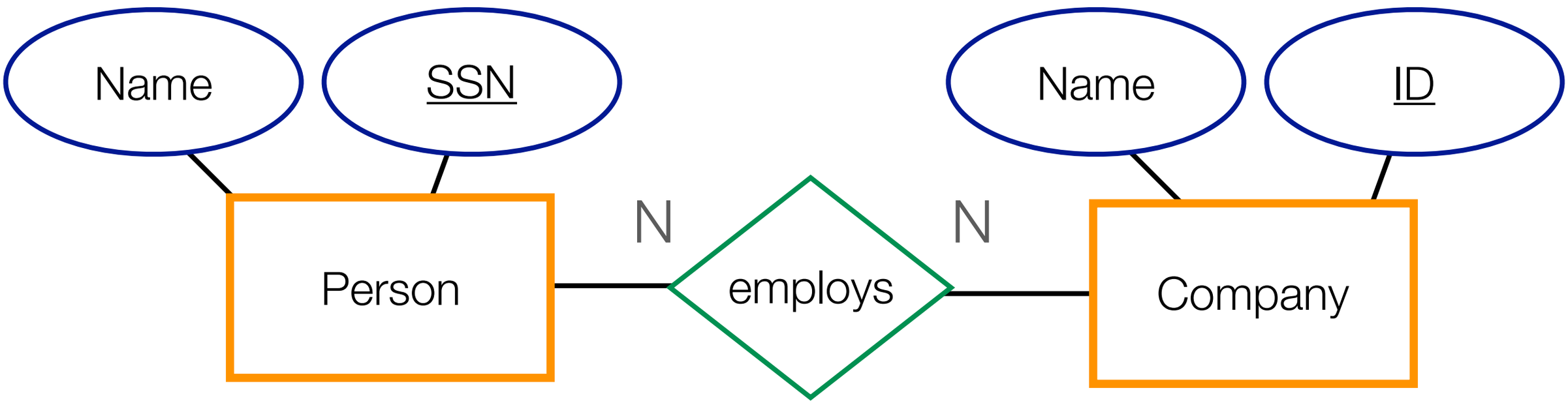
Create a new relation (S — R — T)

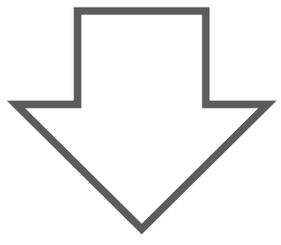
- New tuples of relationship R stored in this table with foreign keys from the entities S and T

- Pro: always possible

- Con: Increasing the number of relations

Basic Case: Relationship to Entity





EMPLOY

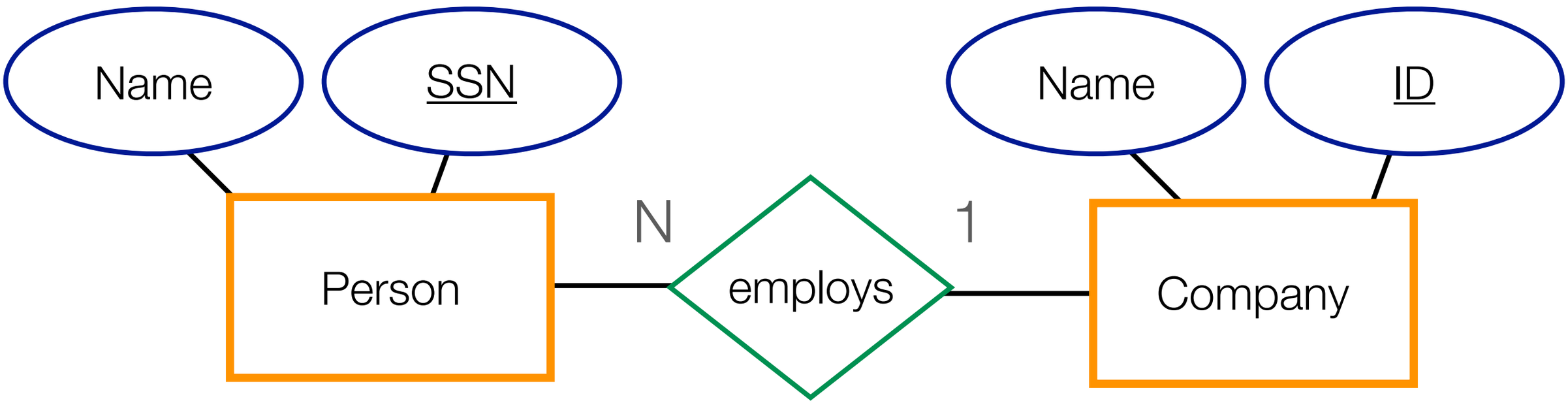
SSN	cID
…	…

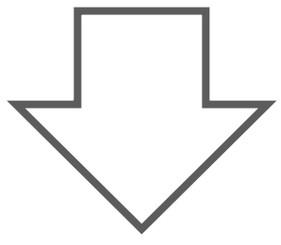
Special Case: Expansion

Expand an existing relation (foreign key approach)

- Tuples of relationship are stored inside the table of an existing entity
- Use key of that entity to store tuples of the relationship
- Pro: only makes an existing relation a bit larger
- Con: not always possible

Special Case: Expansion





PERSON

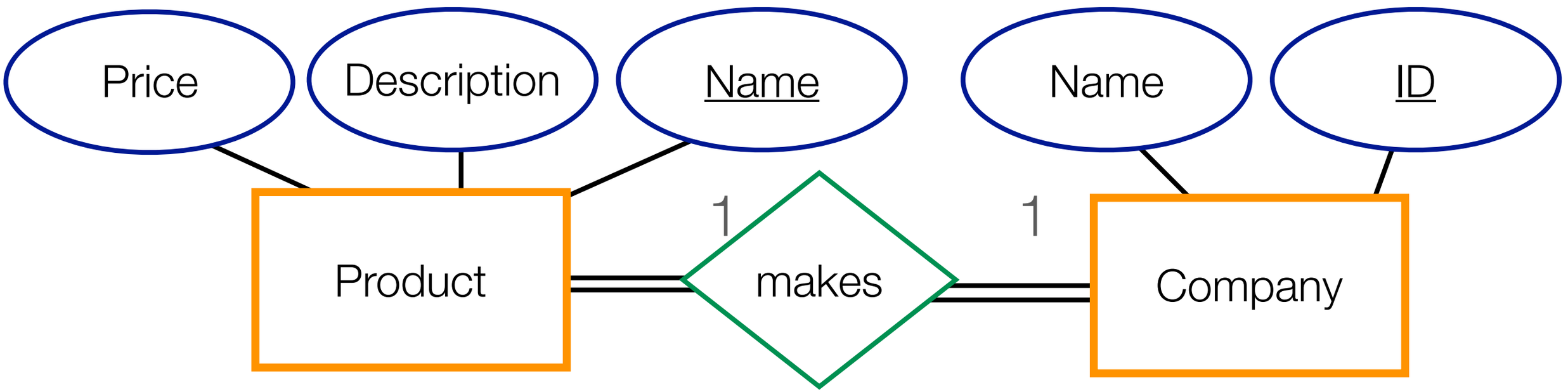
SSN	Name	cID
…	…	…

Special Case: Merging

Merge two existing relations

- Merge two entity types and relationship into one relation
- Only possible in 1:1 mapping and both have total participation
- Pro: reduction of relations
- Con: rarely used

Special Case: Merging



COMPANY_PROD

pName	cName	cID	Price	Description
...	...	...		

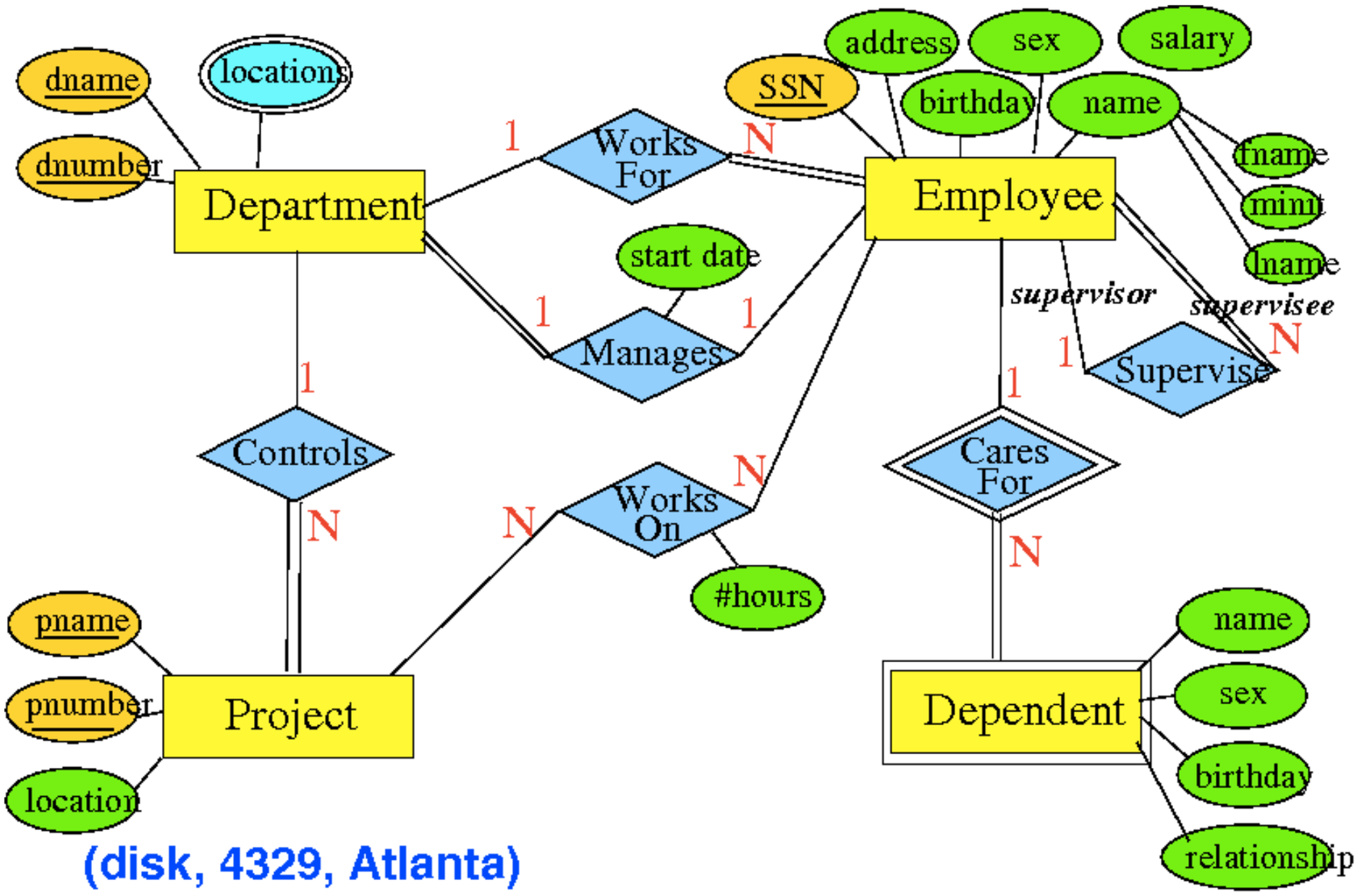
Relation Mapping Design Principles

- Relationship R where Entity1: Entity2 = 1:N —> expand the relation that represents Entity2

- Relationship R where Entity1: Entity2 = 1:1 -> expand either Entity1 or Entity2

- Avoid having attributes that can take on NULL values (e.g., expand a relationship where entity is total participation over entity with partial participation)

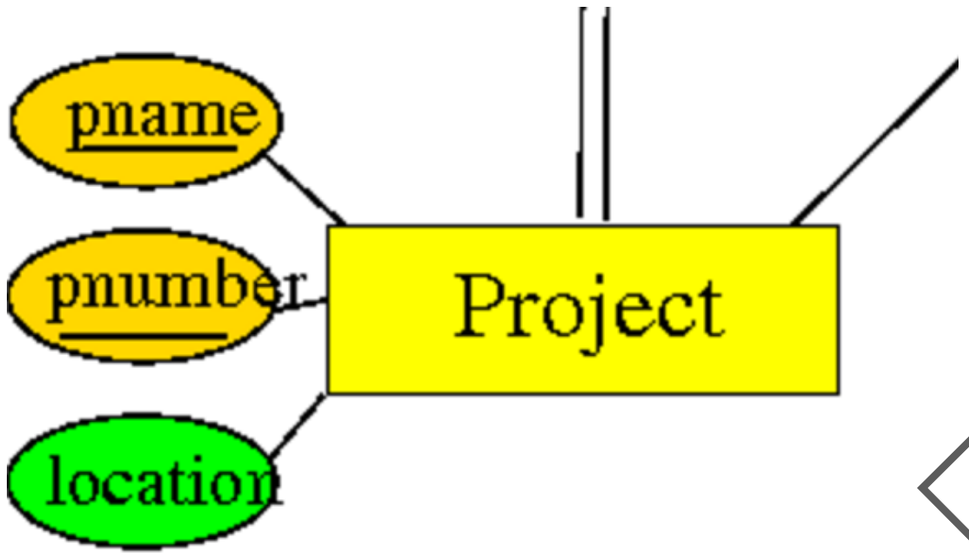
Example: Company database



(disk, 4329, Atlanta)
(CPU, 1562, Boston)
(Printer, 7862, Denver)
...

Example from Prof Cheung's lectures

Step 1: Project Entity

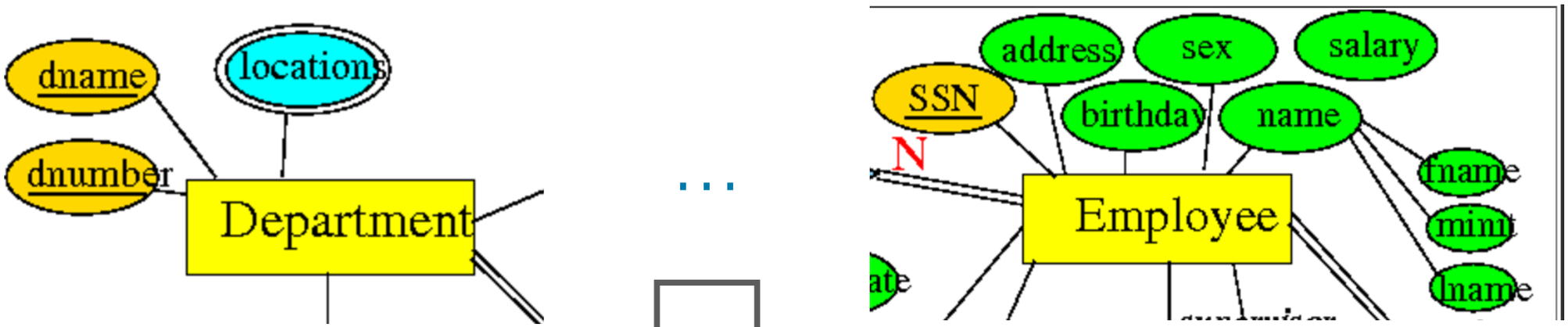


Pick one of the candidate keys to be primary key

PROJECT

PName	PNumber	Location
...	...	...

Step 1: Employee & Department Entities



EMPLOYEE

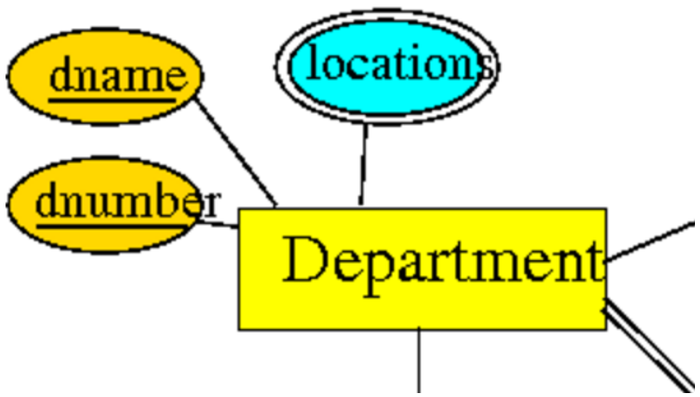
SSN	FName	MI	LName	Sex	Address	BDate	Salary
...	...	...					

DEPARTMENT

DNumber	DName	{Locations}
...	...	...

Attribute values are not ATOMIC!

Step 1: Department Location



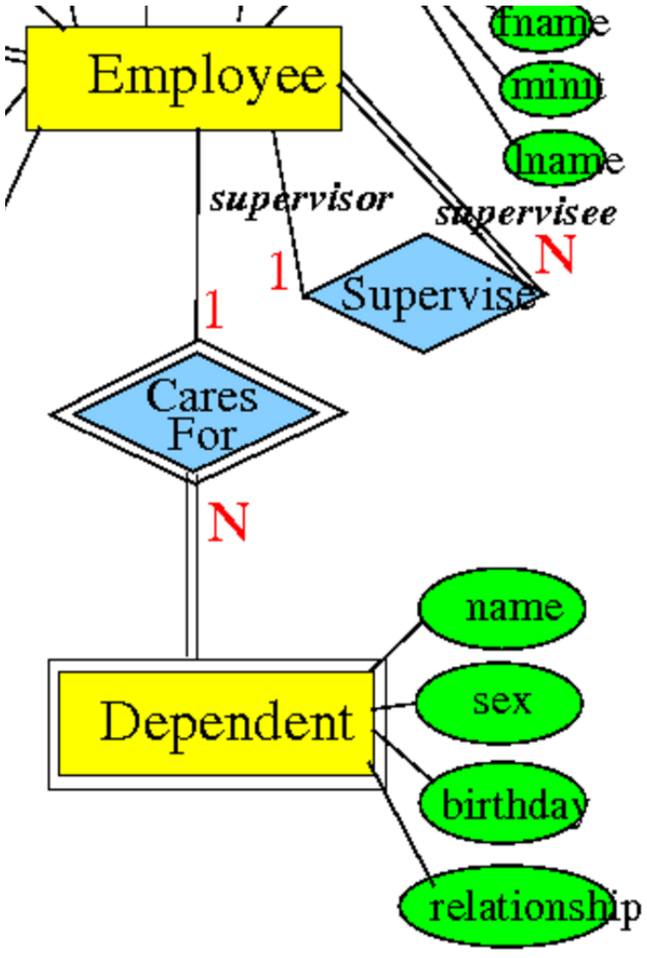
DEPARTMENT

DName	DNumber
Manufacturing	D1234
Research	D7652
…	…

DEPT_LOC

DNumber	Location
D1234	Atlanta
D1234	New York
D1234	Denver
D7652	San Jose
D7652	Austin
…	…

Step 1: Dependent Entity

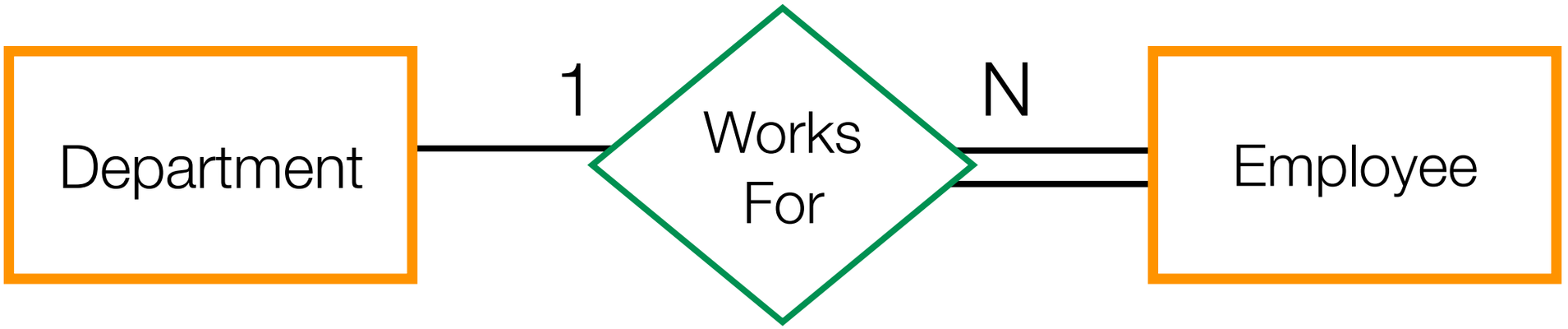


Necessary to identify weak entity

DEPENDENT

ESSN	FName	Sex	BDate	Relationship
	...	...	...	

Step 2: WorksFor Relationship



Use expansion by adding attribute to Employee because 1:N relationship

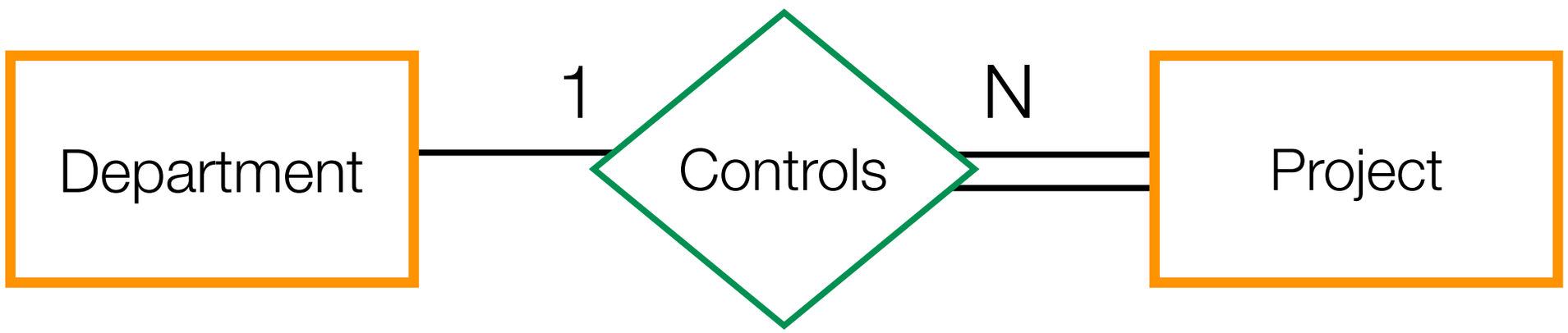
EMPLOYEE

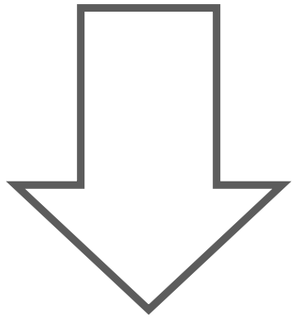
SSN	FName	MI	LName	Sex	Addres	BDate	Salary	DNo
...	...	...						

DEPARTMENT

DName	DNumber
...	...

Step 2: Controls-Project



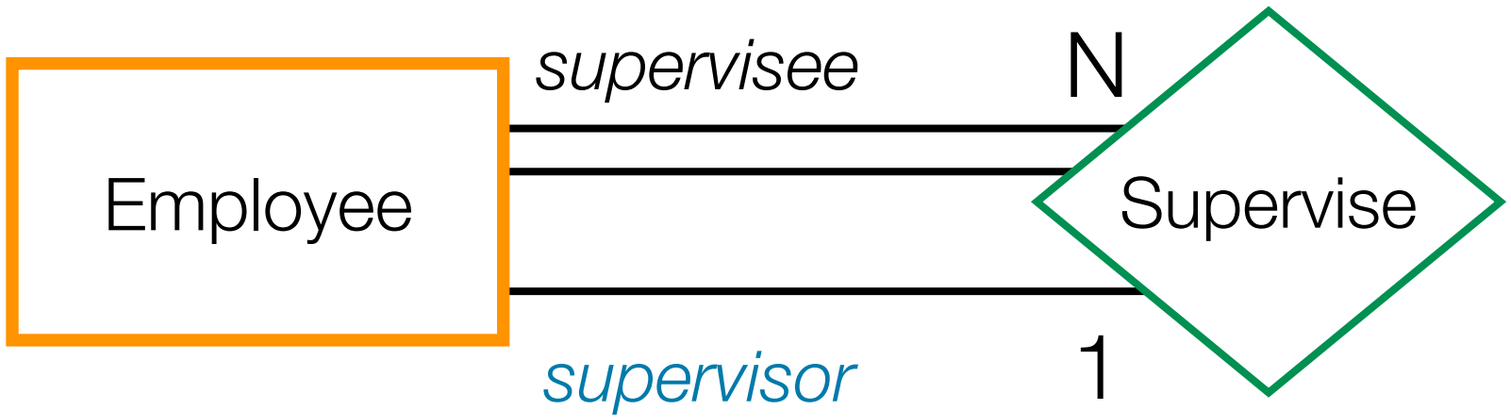


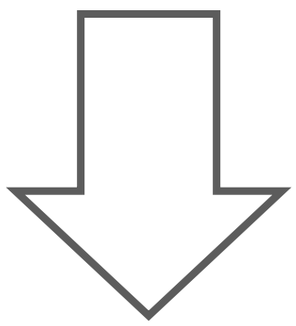
Expand Project because of the 1:N relationship

PROJECT

PName	PNumber	Location	DNum
...	...	...	

Step 2: Supervisor



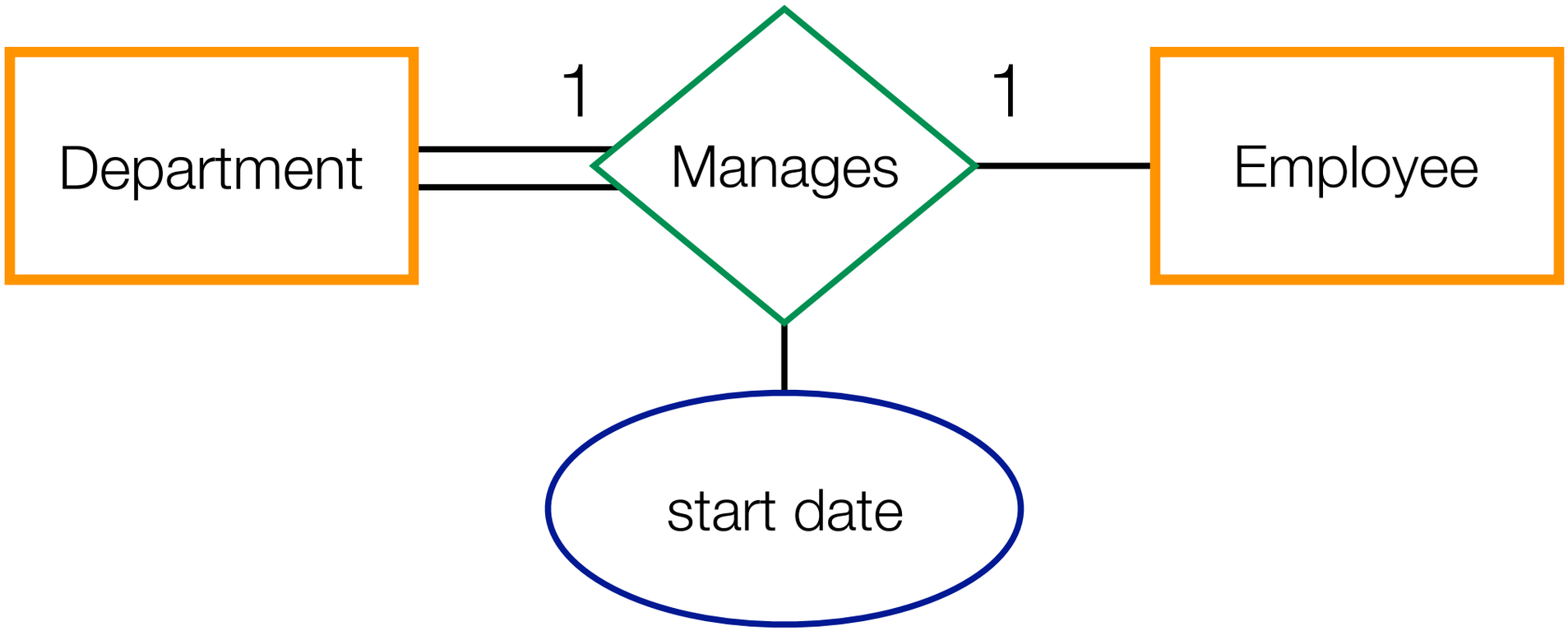


Expand supervisor because of the 1:N relationship

EMPLOYEE

SSN	FName	MI	LName	Sex	Address	BDate	Salary	superSSN	DNo
...	...	...							

Step 2: Manager

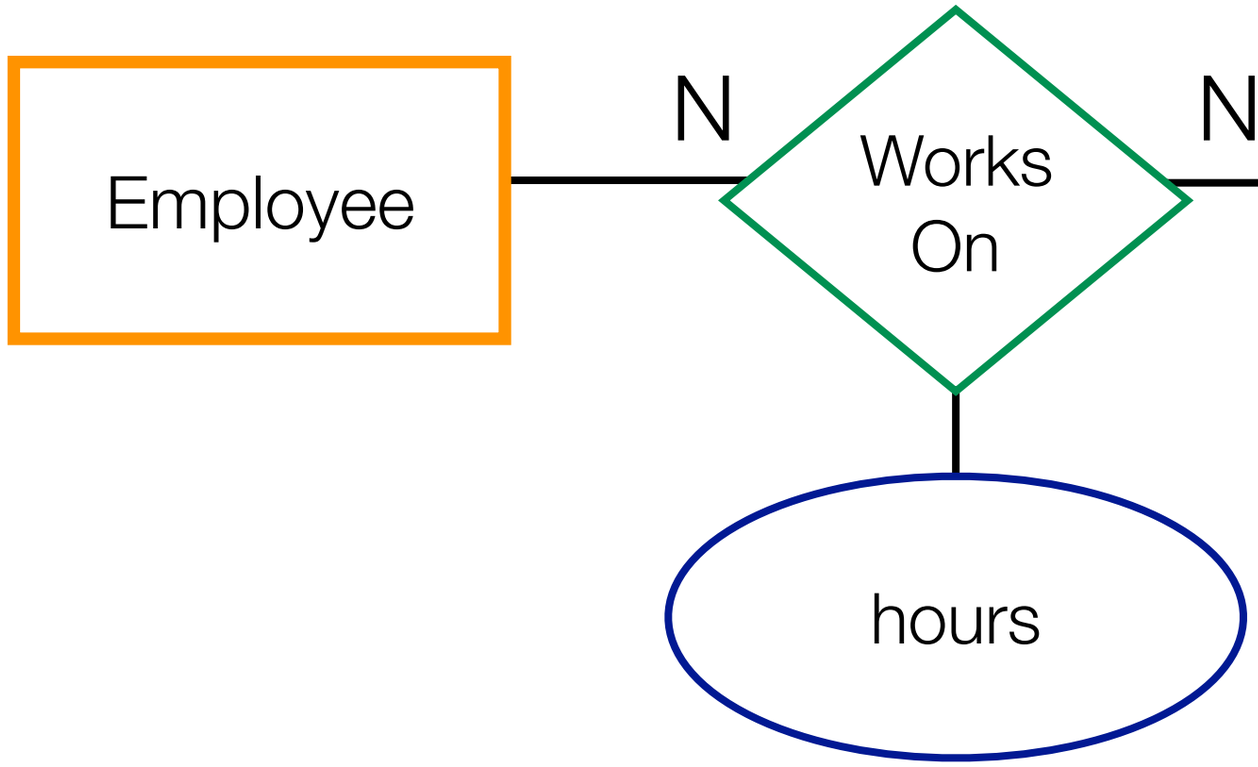


Expand Department because of total participation

DEPARTMENT

DName	DNumber	mgrSSN	mgrStart
...	...		

Step 2: Works On



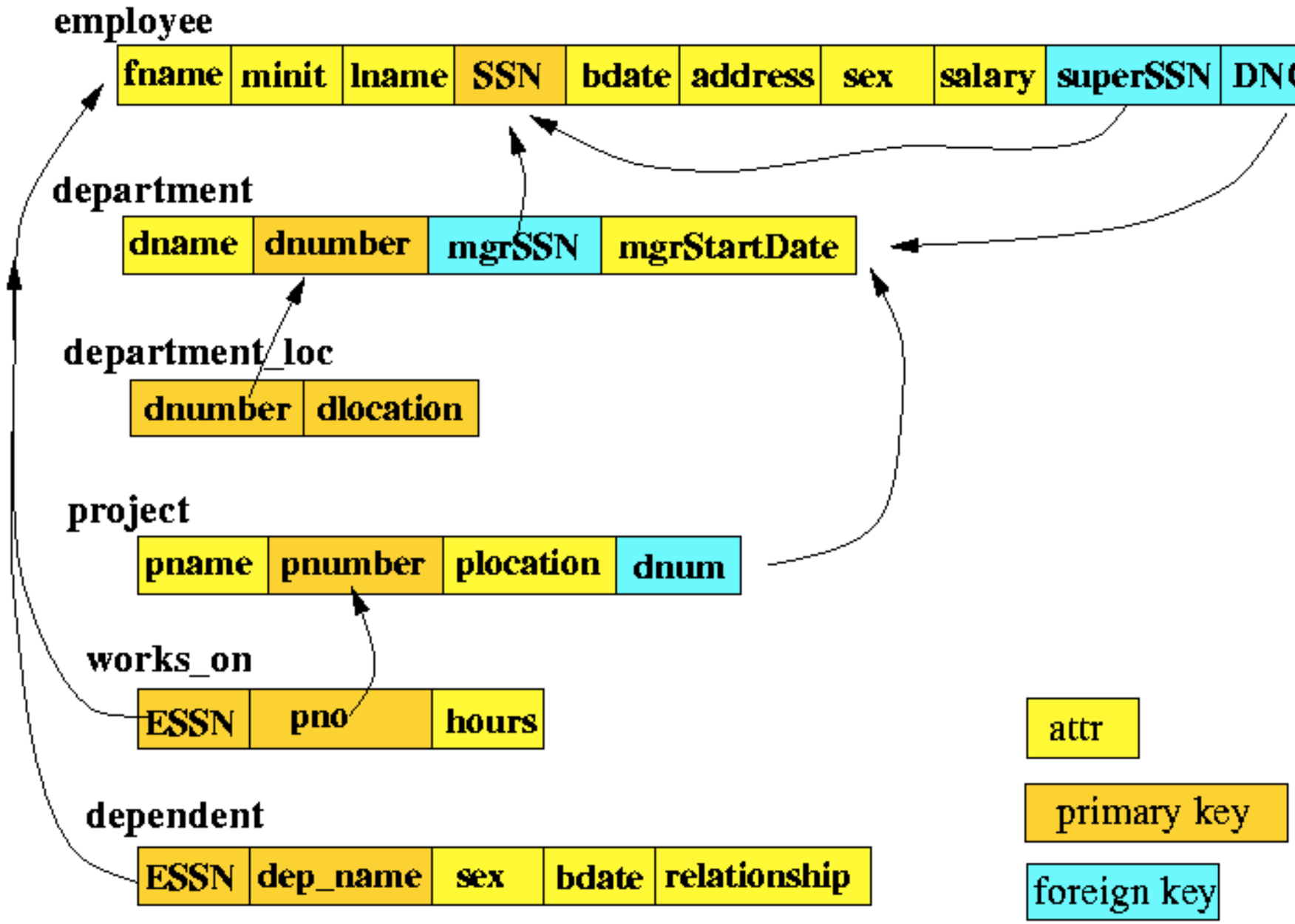
Expansion?

- Employee w/ attribute WorkedOnProject leads to multi-valued attribute
- Project w/ attribute WorkerSSN also results in multi-valued attribute

WORKS_ON

ESSN	PNO	Hours
…	…	

Example: Full Relational Model



http://www.mathcs.emory.edu/~cheung/Courses/377/Syllabus/3-Relation/rel-db-design2.html

Mapping Summary

ER Model	Relational model
Entity type	Entity relation
1:1 or 1:N relationship	Expand (or create R relation)
M:N relationship	Create R relation with two foreign keys
n-ary relationship type	Create R relation with n foreign keys
Simple attribute	Attribute
Composite attribute	Set of simple component attributes
Multivalued attribute	Relation and foreign key
Key attribute	Primary (or secondary) key

Exercise: Football ER Model

Relational Model: Recap

- Relational Model
  - Relation, attributes
  - Schema vs instance
  - Relational model constraints
- ER to Relational
  - Entity set, relationship —> relation