

Semiconductor Fundamentals – (II)

2.3 **Energy Bands**

2.4 Doping of Semiconductors

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HW-1: solution

- Si atomic **density**:

$$\frac{\# \text{Atoms}}{\text{Volume}} = \frac{8 \times (1/8) + 6 \times (1/2) + 4}{a_0^3} = \frac{8}{(5.43 \times 10^{-8} \text{ cm})^3} = 5 \times 10^{22} \text{ cm}^{-3}$$

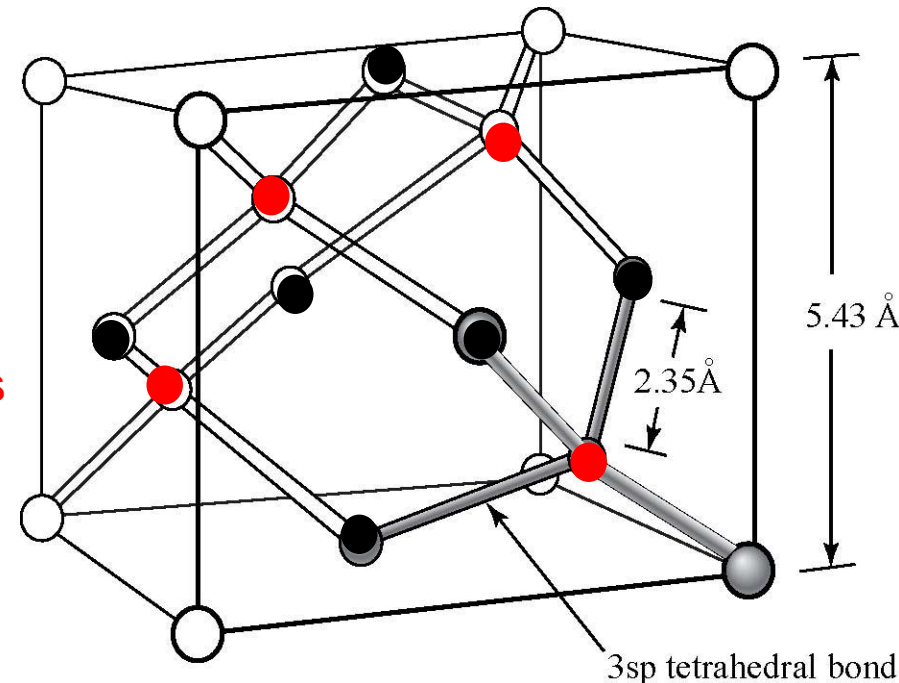
- Number of atoms in a **unit cell**:

- **4 atoms** completely inside cell
- Each of the **8 atoms** on corners are shared among cells → count as **1 atom** inside cell
- Each of the **6 atoms** on the faces are shared among 2 cells → count as **3 atoms** inside cell

Total number inside the cell = **4 + 1 + 3 = 8**

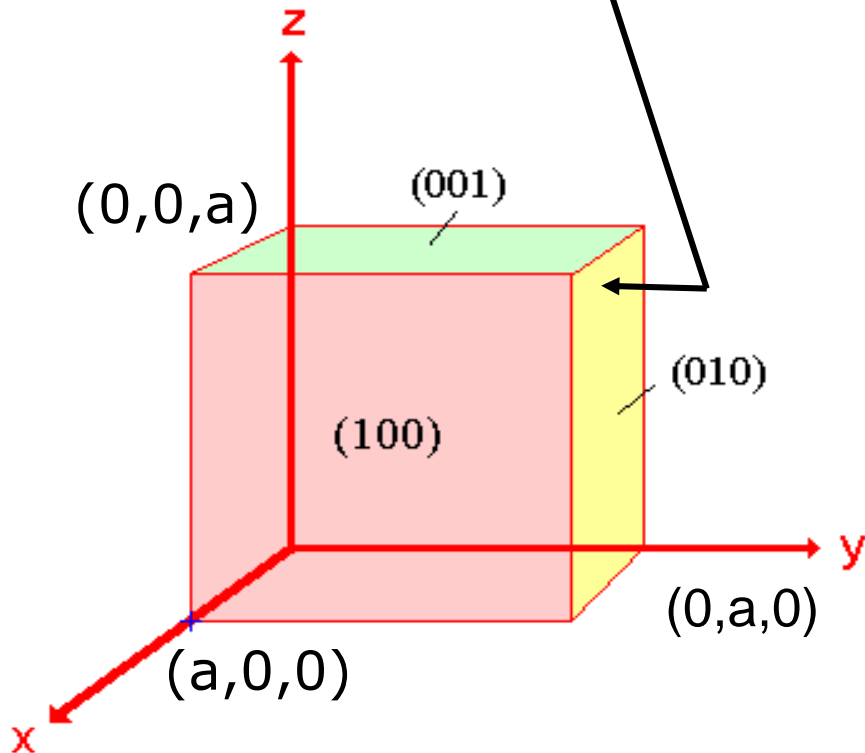
- Cell volume:

$$(0.543 \text{ nm})^3 = 1.6 \times 10^{-22} \text{ cm}^3$$



HW-2: solution

Why the **Miller indices** of this plane is (010)?

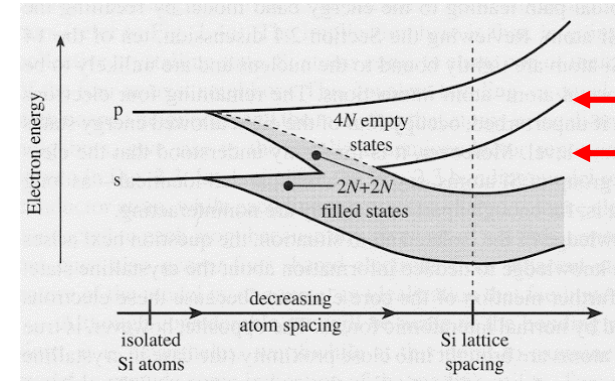
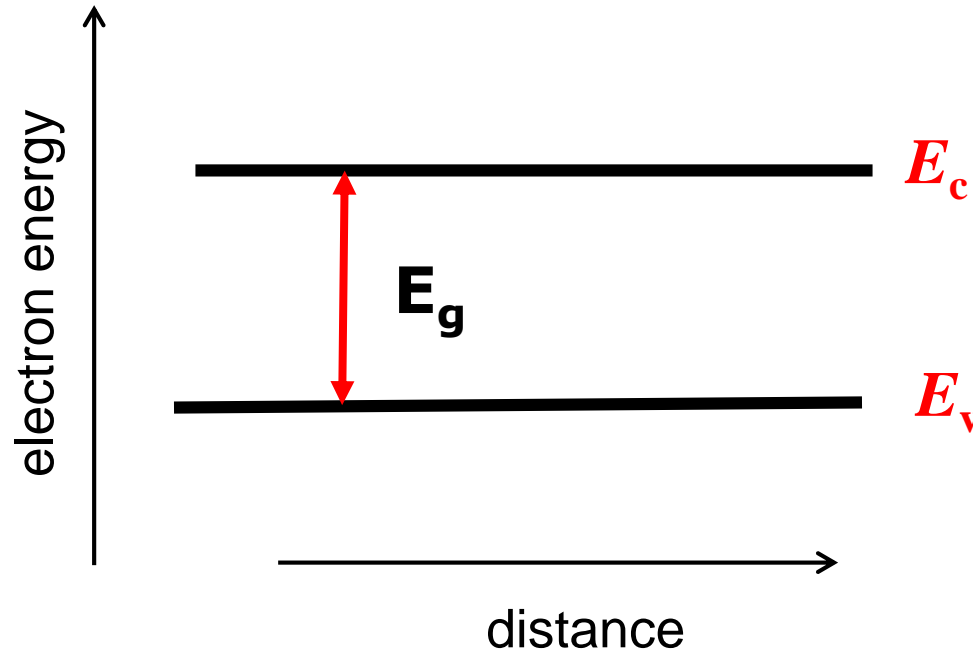


x-intercept of plane
y-intercept of plane
z-intercept of plane

h: **inverse** x-intercept of plane
k: **inverse** y-intercept of plane
l: **inverse** z-intercept of plane

h*, *k* and *l are reduced/enlarged
to **3 integers** having the same
ratio. **(010)**

Last lecture:



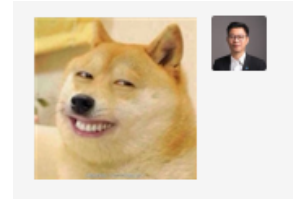
Simplified version of **energy band model**, indicating

- **bottom edge** of the **conduction band** (E_c)
- **top edge** of the **valence band** (E_v)
- E_c and E_v are separated by the **band gap energy** E_g

2.3

Energy Bands

- **Band theory**
 - What's a Semiconductor
 - Fermi Level
 - Band model of e & h
 - Bond model of e & h
- Generation and recombination
- Intrinsic semiconductor

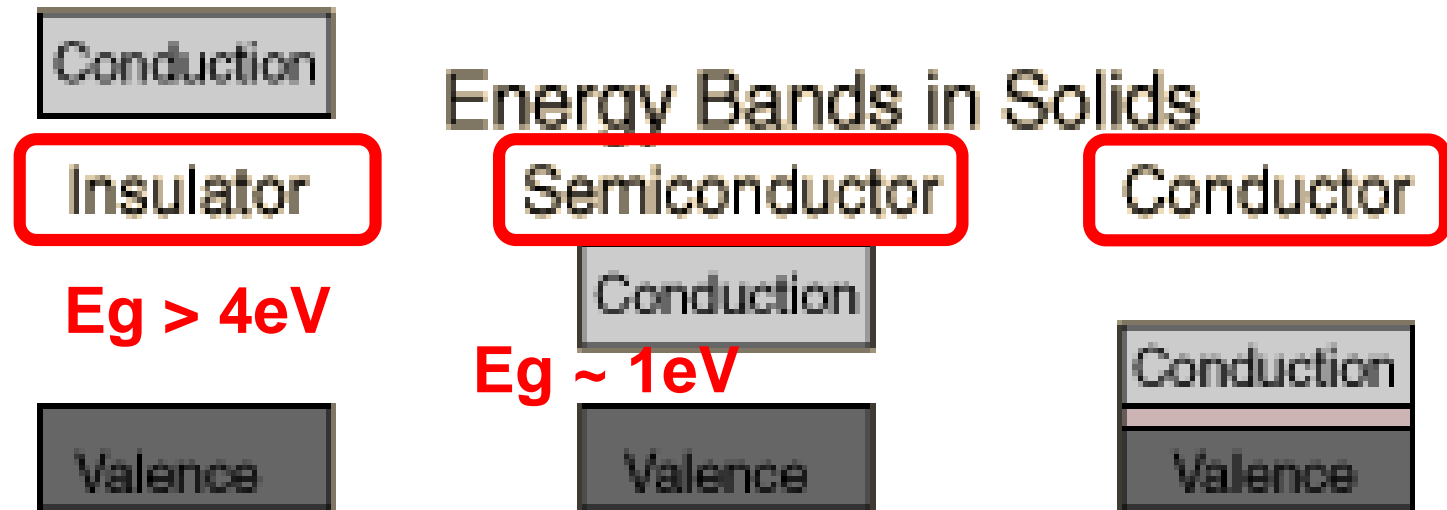


What is a **Semiconductor**?

- Low resistivity => “**conductor**” e.g. Al, Cu
- High resistivity => “**insulator**” e.g. SiO₂
- Intermediate resistivity => “**semiconductor**”
 - **conductivity** lies between that of **conductors** and **insulators**

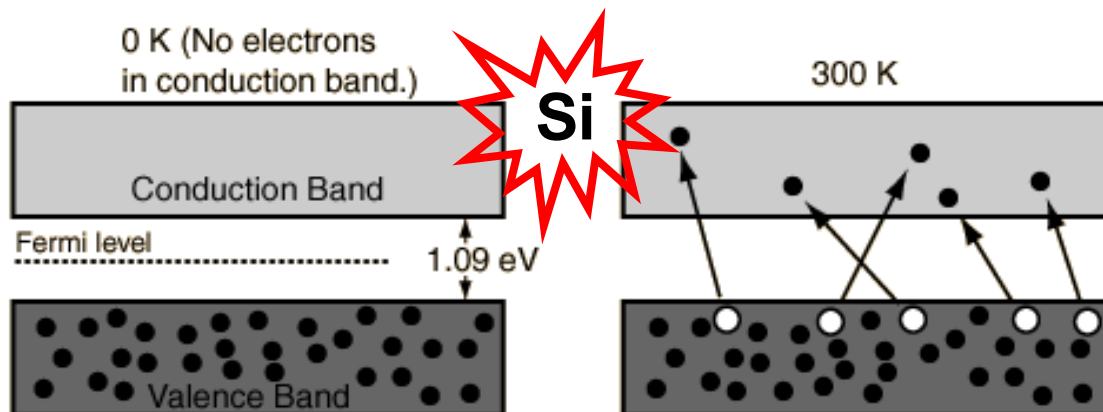
Band Theory of Solids

- A useful way to **visualize** the difference between conductors, insulators and semiconductors is to plot the available energies for electrons in the materials. In **conductors** the **valence band overlaps** the **conduction band**, and in **semiconductors** or **insulator** there is a **small or big gap** between the **valence** and conduction bands.
- An important **parameter** in the band theory is the Fermi level.



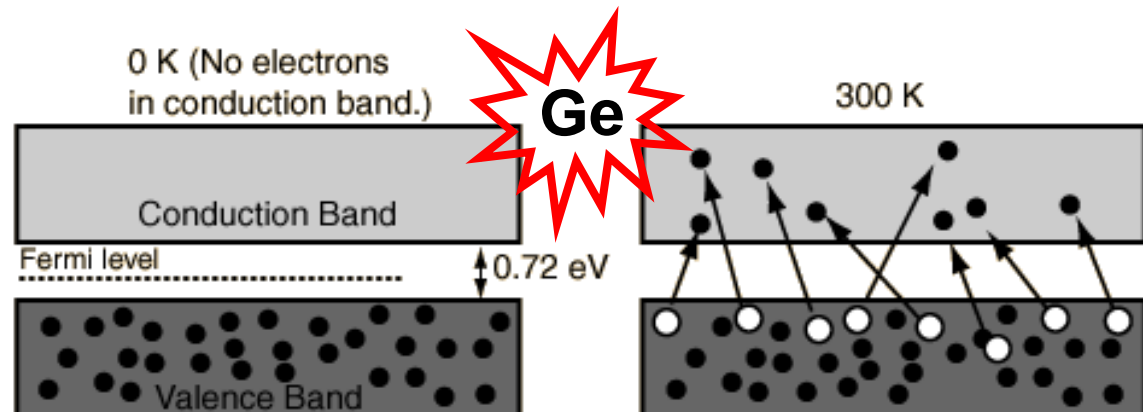
Energy Bands of Silicon & Germanium

- At finite temperatures, the number of electrons which reach the **conduction band** and contribute to current can be modeled by the Fermi function.



1) Fermi level?

2) “holes”?



Fermi function and Fermi level

Probability that a **state** at **energy level**, E , is occupied by **one electron** is,

$$f(E) = \frac{1}{1 + \exp\left(\frac{E - E_F}{kT}\right)}$$

Students → electrons

Seat row → energy level, E .

Seat → state



Example: Students in a theatre class room.

Every **row** has different **energy level**, E . For example, for **row 7**, its **energy level** is E_7 .

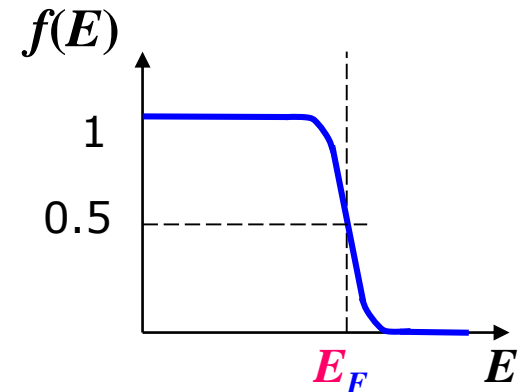
The probability for one **student** to **occupy** a **seat** on **row 7** can be calculated by $f(E_7)$.

E_F is a energy level at which $f(E)$ is 50%.

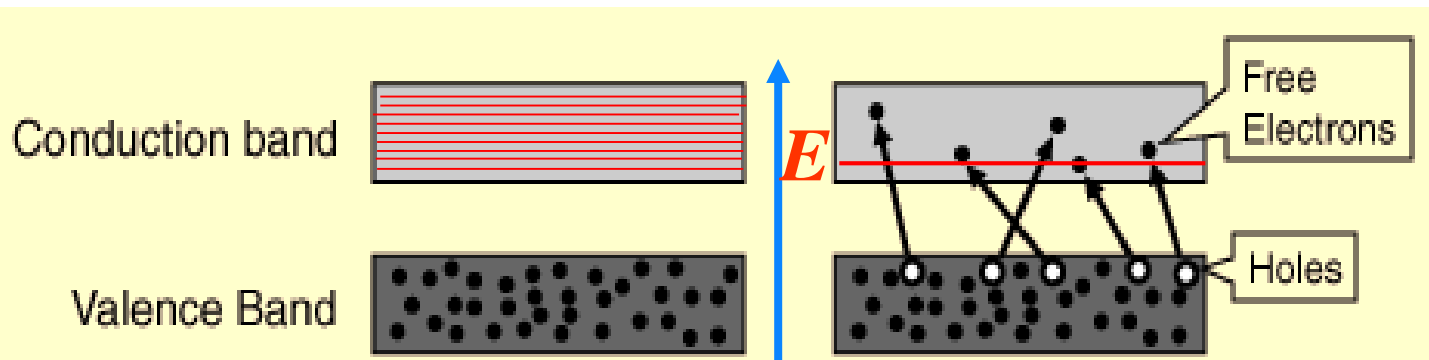
Fermi function and Fermi level

- **Probability** that a **state** at **energy level, E** , is occupied by one electron is,

$$f(E) = \frac{1}{1 + \exp\left(\frac{E - E_F}{kT}\right)}$$



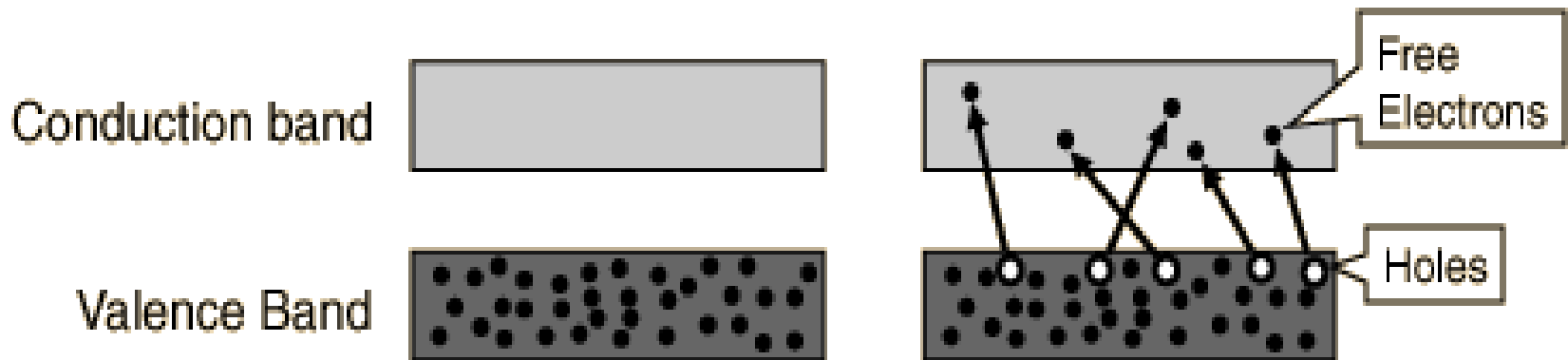
- $f(E)$: **Fermi**-Dirac **function**
- An **increase** in E will **reduce** $f(E)$
- E_F --- **Fermi-level**
 - **When $E = E_F$, $f(E=E_F) = 0.5$.**



textbook
P.66

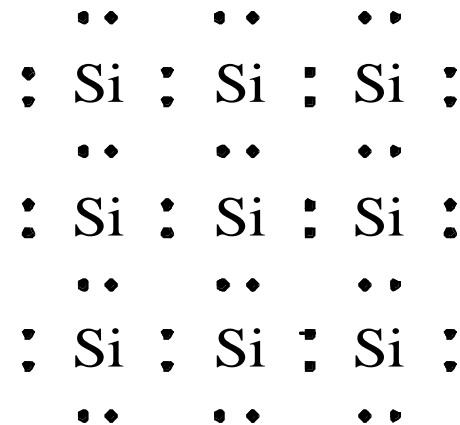
Band Model of Electrons and Holes

- In an pure semiconductor like silicon at temperatures above absolute zero, there will be some **electrons** which are **excited** across the band gap into the **conduction band** and which can produce **current**.
- When the **electron** in pure silicon **crosses** the **gap**, it leaves behind an **electron vacancy** or "**hole**" in the regular silicon lattice.
- Under the influence of an **external voltage**, both the **electron** and the **hole** can **move** across the material.

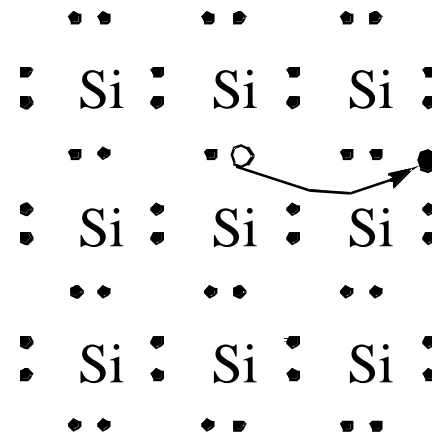


Bond Model of Electrons and Holes

2-D representation:
Covalent Bonds



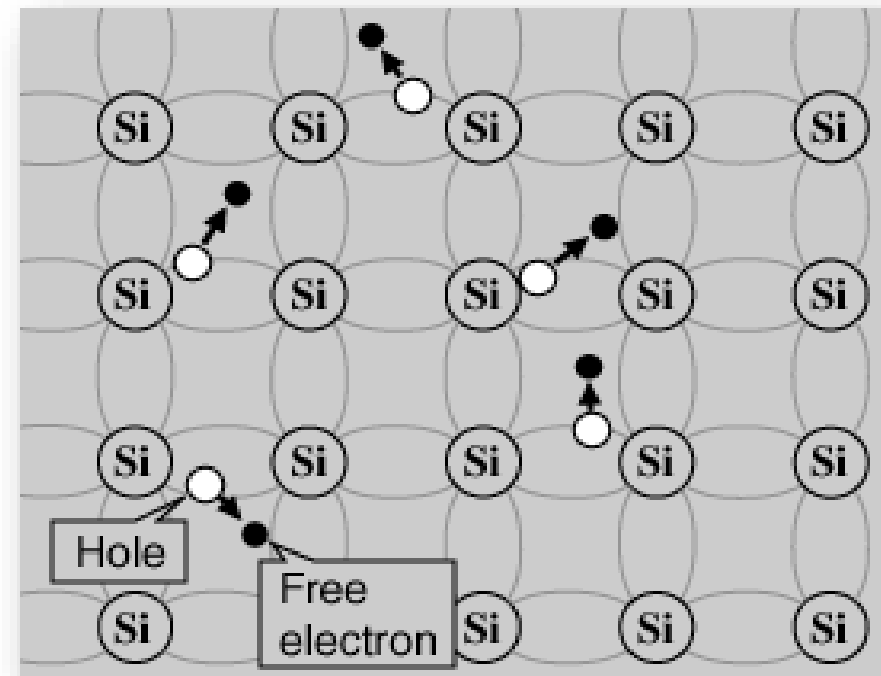
When an **electron breaks loose** and becomes a **conduction electron**, a **hole** is also created.



Bond Model of Electrons and Holes

- When an **electron breaks loose** and becomes a **conduction electron**, a **hole** is also created.
- A **hole** (along with its associated **positive charge**) is **mobile**!
- Hole density = electron density in a pure Si.

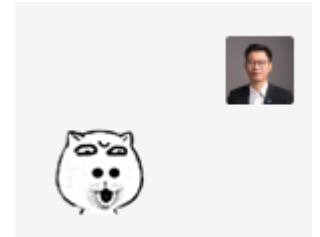
2-D representation:



Pure Si

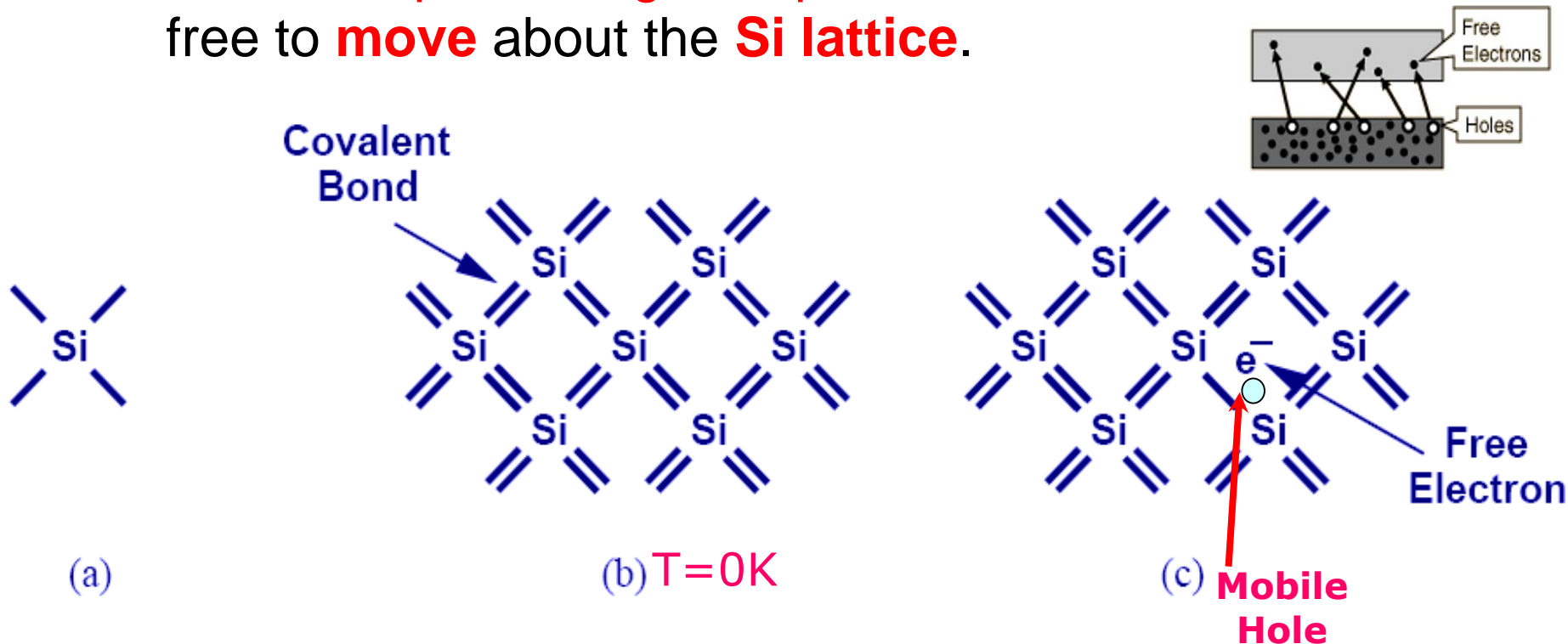
2.3 Energy Bands

- Band theory
 - What's a Semiconductor
 - Fermi Level
 - Band model of e & h
 - Bond model of e & h
- **Generation and recombination**
- Intrinsic semiconductor



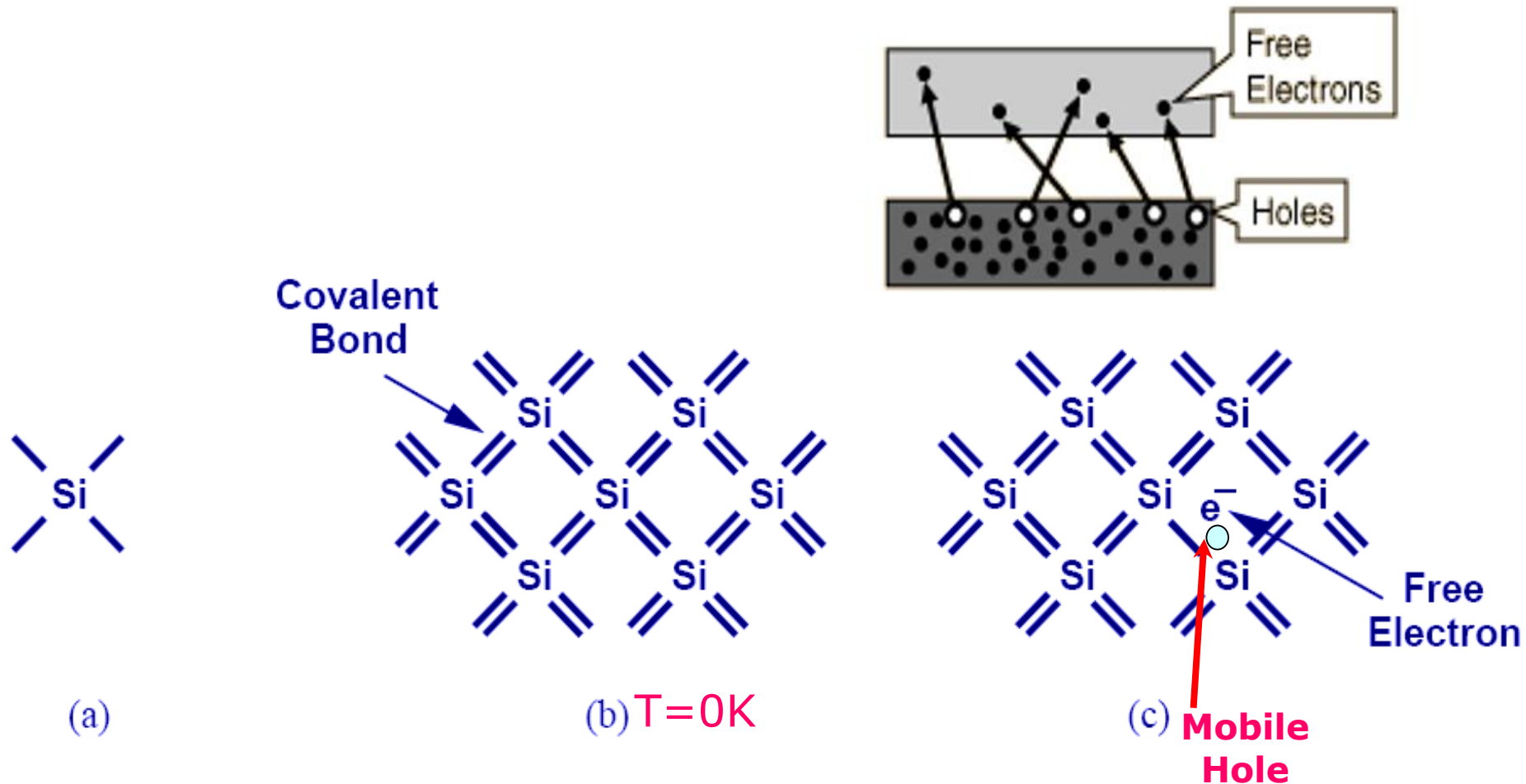
Thermal Generation

- Inverse process: **recombination**
- Si has four valence electrons. Therefore, it can form covalent bonds with four of its nearest neighbors.
- When **temperature goes up**, **electrons** can become free to **move** about the **Si lattice**.



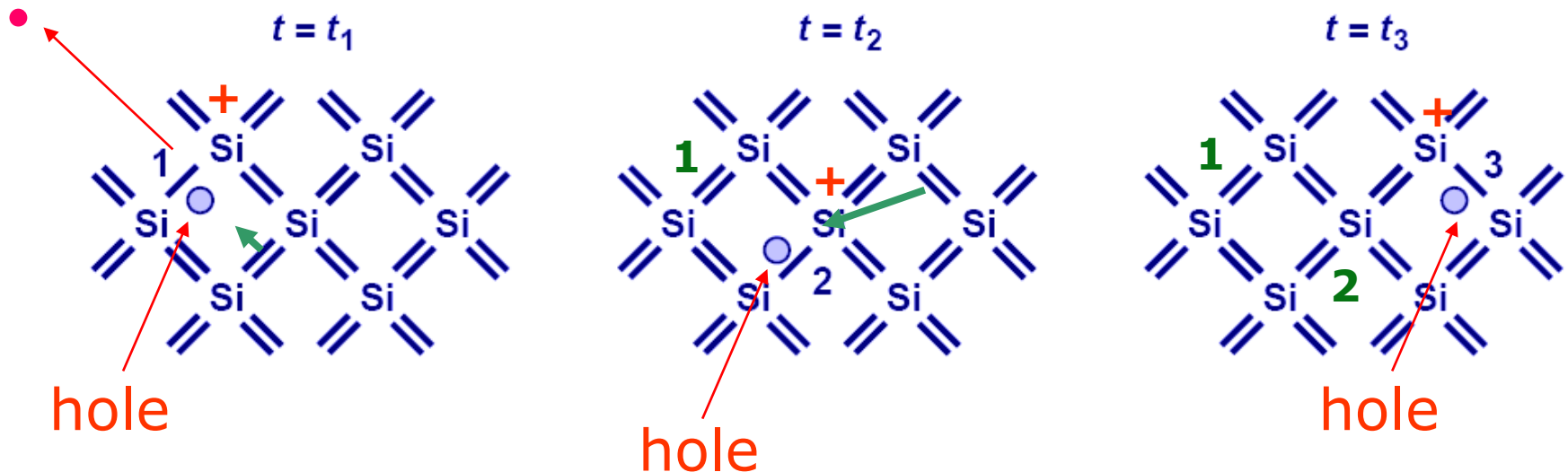
Generation

- **Generation:** A process to create electron-hole pairs.



Electron-Hole Pair Generation

- When a **conduction electron** is thermally **generated**, a “**hole**” is also **generated**.
- A **hole** is associated with a **positive charge**, and is free to **move** about the **Si lattice** as well.



A hole is **mobile!**

Generation

- We have seen that conduction (mobile) electrons and holes can be created in pure (intrinsic) silicon by **thermal generation**.
 - Thermal **generation rate** increases exponentially with **temperature T**
- Another type of generation process which can occur is **optical generation**
 - The energy absorbed from a **photon** frees an **electron** from covalent bond
 - In **Si**, the minimum energy required is **1.1 eV**, which corresponds to **$\sim 1 \mu\text{m}$ wavelength (infrared region)**.
 - $1 \text{ eV} = \text{energy gained by an electron falling through } 1 \text{ V potential} = q_e V = 1.6 \times 10^{-19} \text{ CV} = 1.6 \times 10^{-19} \text{ J}$.
- Note that conduction electrons and holes are continuously generated, if **$T > 0$**

Light interactions with Semiconductors

Absorption of light in a semiconductor:

- For energies of light greater than the bandgap ($h\nu > E_g$), light is absorbed
- For energies less than the bandgap ($h\nu < E_g$), light is out
- **Silicon** is transparent to IR (can see through it with an IR camera)
- **Diamond** is a wide bandgap ($\sim 5.47\text{eV}$) semiconductor
- (transparent to **visible light**)

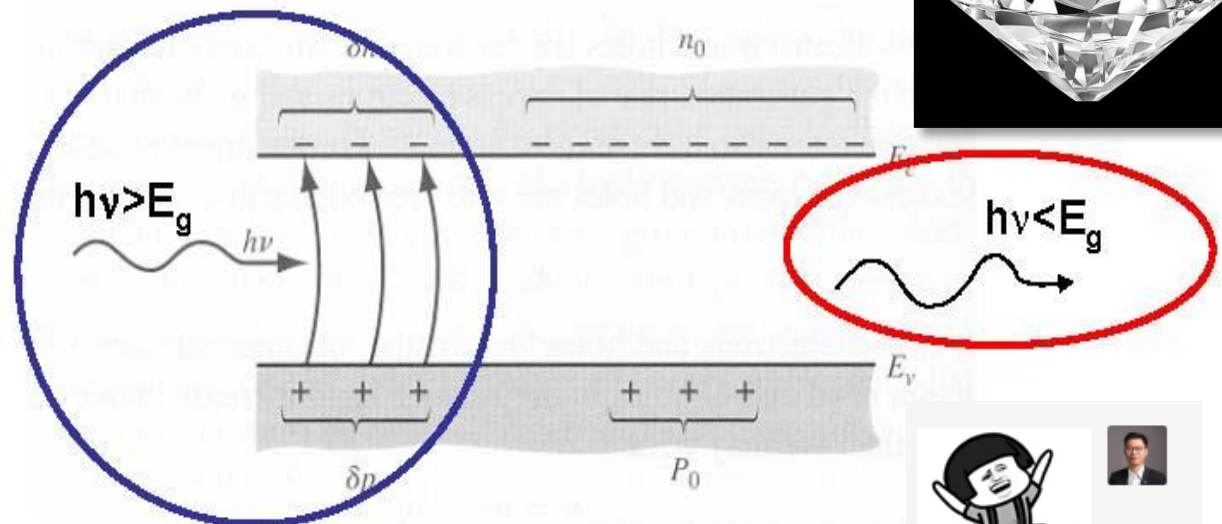
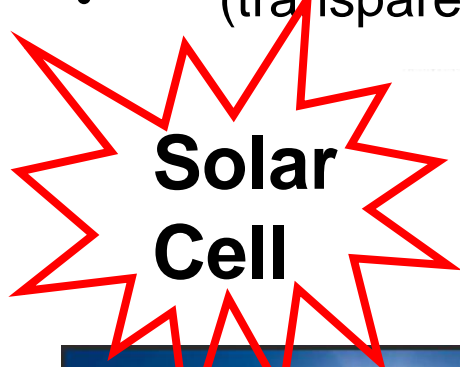


Figure 6.2 | Creation of excess electron and hole densities by photons.

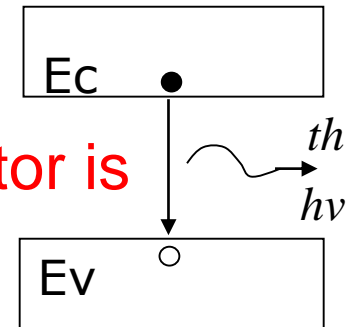


Recombination

- When a **conduction electron** and **hole meet**, each one is **eliminated**, a process called **“recombination”**. The **energy lost** by the conduction electron (when it “falls” back into the covalent bond) can be released in two ways:

- to the semiconductor lattice (vibrations)

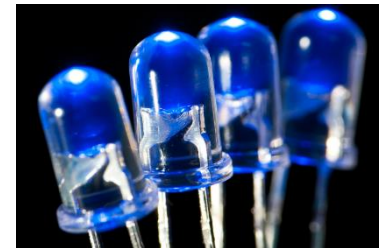
“thermal recombination” → semiconductor is heated



- to photon emission

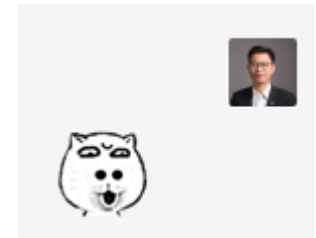
“optical recombination” → light is emitted

- It is the basis for **light-emitting diodes** and laser diodes.



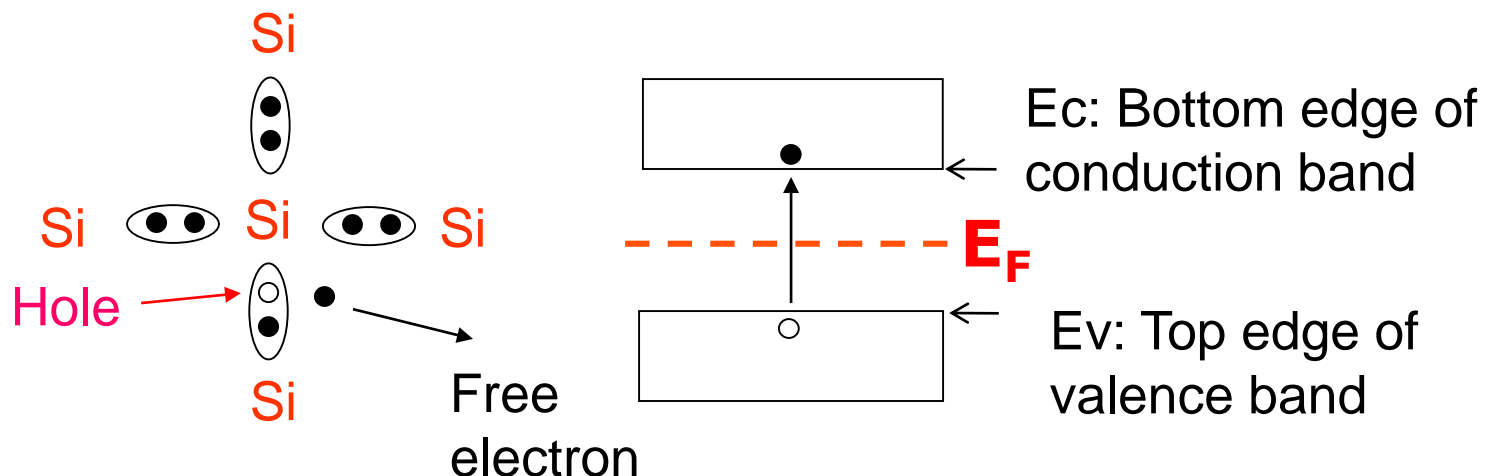
2.3 Energy Bands

- Band theory
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- Generation and recombination
- **Intrinsic semiconductor**



Intrinsic semiconductors

- **Intrinsic:** pure semiconductor
- A **hole** is created simultaneously with a free **electron**
 - n (free electron density) = p (hole density)
- E_F is in the **middle** of the **bandgap** ★



Carrier Concentrations in Intrinsic Si

- The “band-gap energy” E_g is the amount of **energy** needed to remove an **electron** from a **covalent bond**.
- The **concentration of conduction electrons** in intrinsic silicon, n_i , depends exponentially on E_g and the absolute **temperature** (T):

$$n_i = 5.2 \times 10^{15} T^{3/2} \exp \left(-\frac{E_g}{2kT} \right) \text{ electrons/cm}^3$$

Boltzmann constant
8.62E-5 eV/K

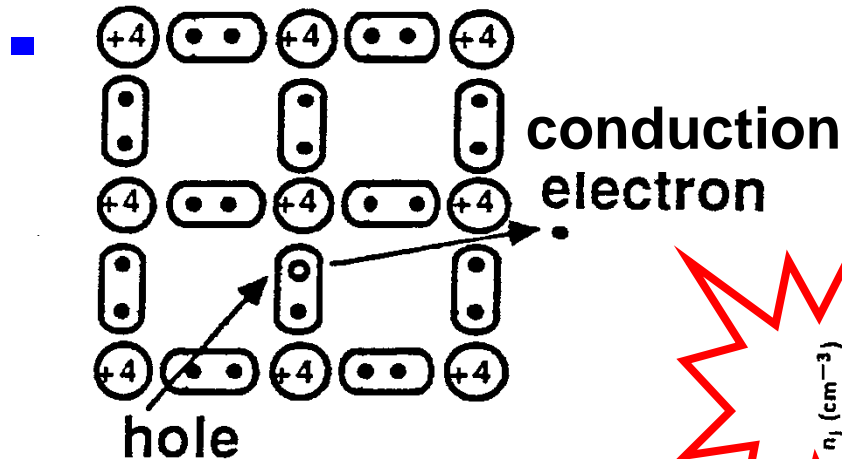
$$n_i \cong 1 \times 10^{10} \text{ electrons/cm}^3 \text{ at } 300\text{K}$$

$$n_i \cong 1 \times 10^{15} \text{ electrons/cm}^3 \text{ at } 600\text{K}$$

RT

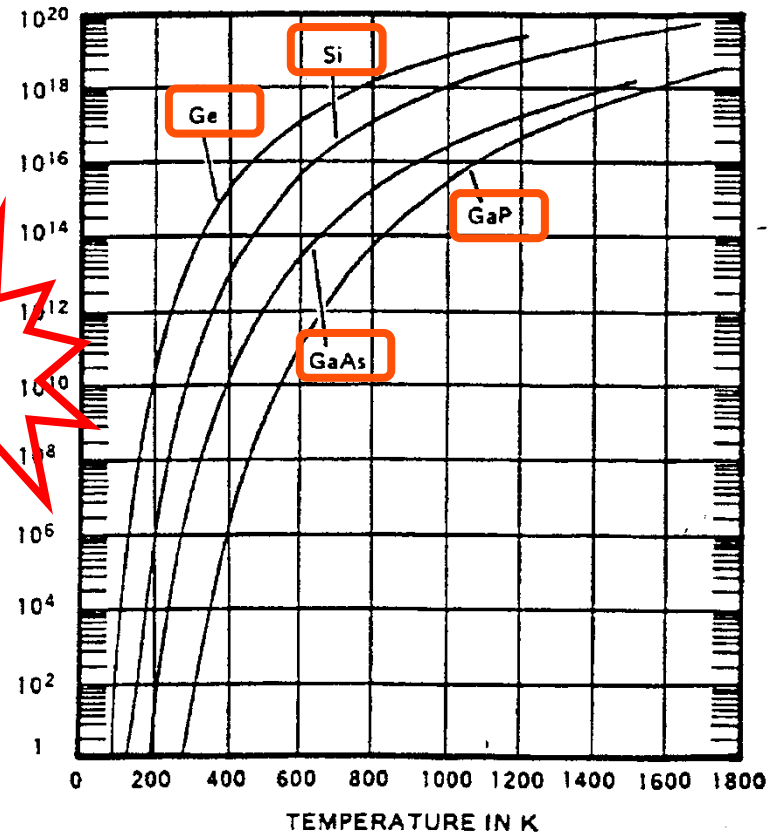
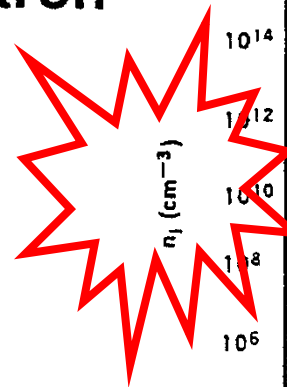
Pure Si

$$n_i = 5.2 \times 10^{15} T^{3/2} \exp \frac{-E_g}{2kT} \text{ electrons/cm}^3$$



Covalent (shared e^-) bonds exist between Si atoms in a crystal. Since the e^- are loosely bound, some will be free at any T , creating hole electron pairs.

p.75



Si:

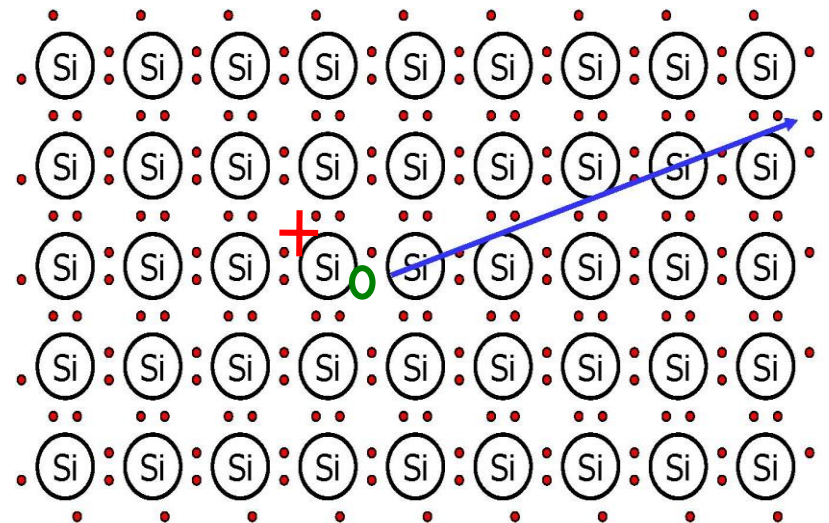
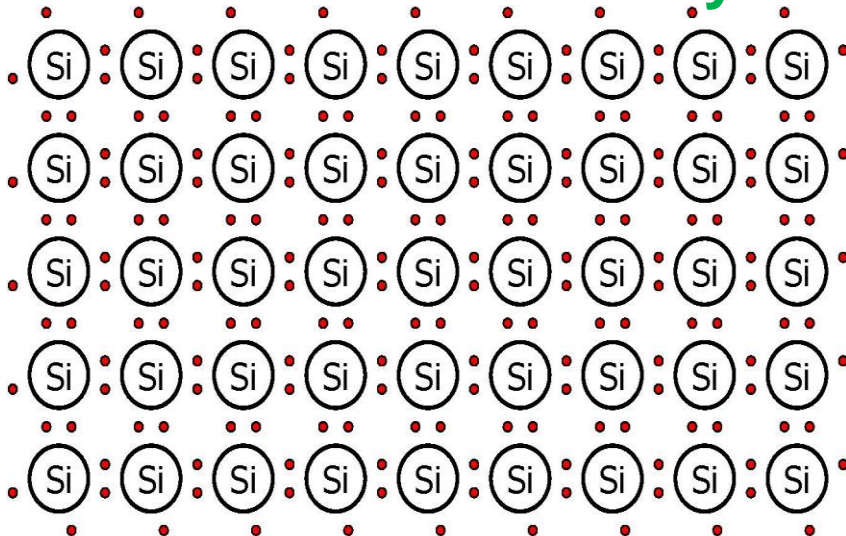
$$n_i = 3.9 \times 10^{16} T^{3/2} e^{-\frac{0.605\text{eV}}{kT}} / \text{cm}^3$$

$n_i \cong 1 \times 10^{10} \text{ cm}^{-3}$ at room temperature

Intrinsic Semiconductor

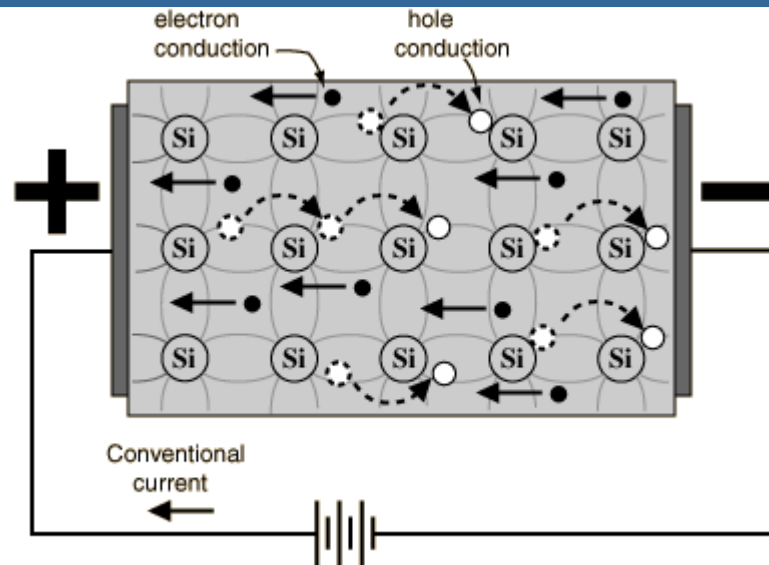
Silicon has four valence electrons

- It covalently bonds with 4 adjacent atoms in the crystal lattice
- Increasing Temperature Causes Creation of Free Carriers. 10^{10}cm^{-3} free carriers at 23°C (out of $2 \times 10^{23}\text{cm}^{-3}$): Intrinsic Conductivity.
- **Si atomic density: $5 \times 10^{22}\text{cm}^{-3}$**



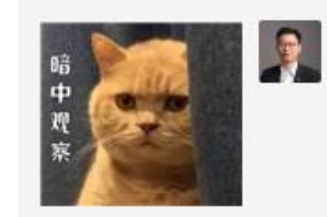
Semiconductor Current

- Both electrons and holes contribute to **current flow** in an intrinsic semiconductor.



2.4 The doping of semiconductors

- **Doping elements**



- Doping: N type

- Doping: P type

- Counter doping

The Doping

- The addition of a **small percentage** of **foreign atoms** in the regular crystal lattice of silicon or germanium produces **dramatic changes** in their electrical properties, producing n-type and p-type semiconductors.
- Definition of Terms:

n = number of electrons/cm³

p = number of holes/cm³

n_i = intrinsic carrier concentration

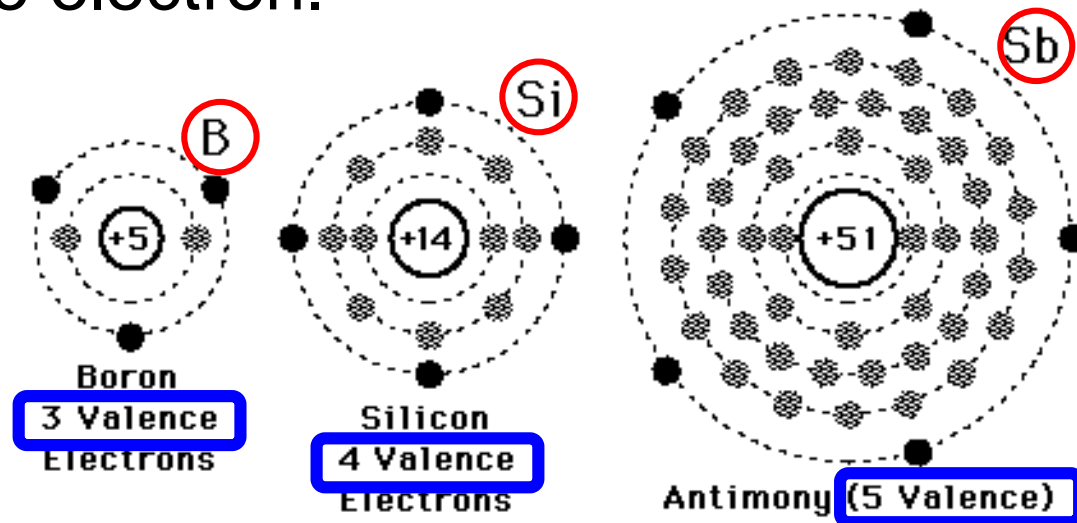
In a pure semiconductor,

$$n = p = n_i$$

Valence Electrons

PL

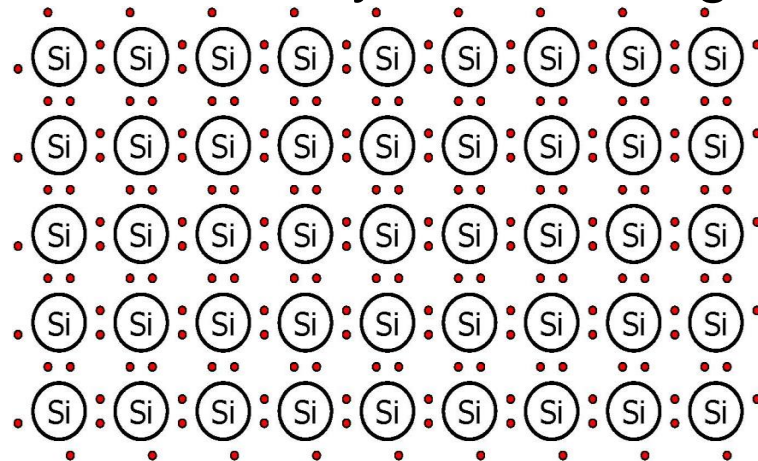
- The electrons in the outermost shell of an atom are called **valence electrons**; they dictate the nature of the **chemical reactions** of the atom and largely determine the **electrical nature** of solid matter. The electrical properties of matter are pictured in the [band theory of solids](#) in terms of how much energy it takes to free a valence electron.



The **Doping** of Semiconductors

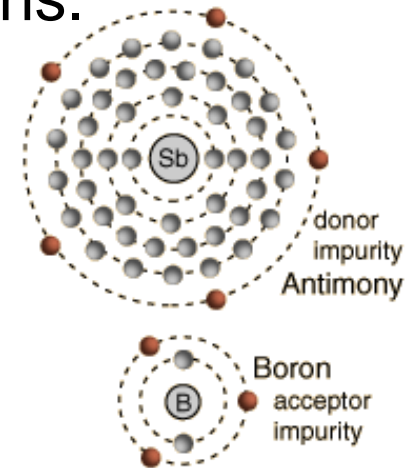
Pentavalent impurities (donor impurities = **donors**)

Impurity atom with **5 valence electrons** produce **n-type** semiconductors by contributing **extra** electrons.



Antimony
Arsenic
Phosphorous

Boron
Aluminum
Gallium



Trivalent impurities (acceptor impurities = **acceptors**)

Impurity atoms with **3 valence electrons** produce **p-type** semiconductors by producing a "**hole**" or **electron deficiency**.

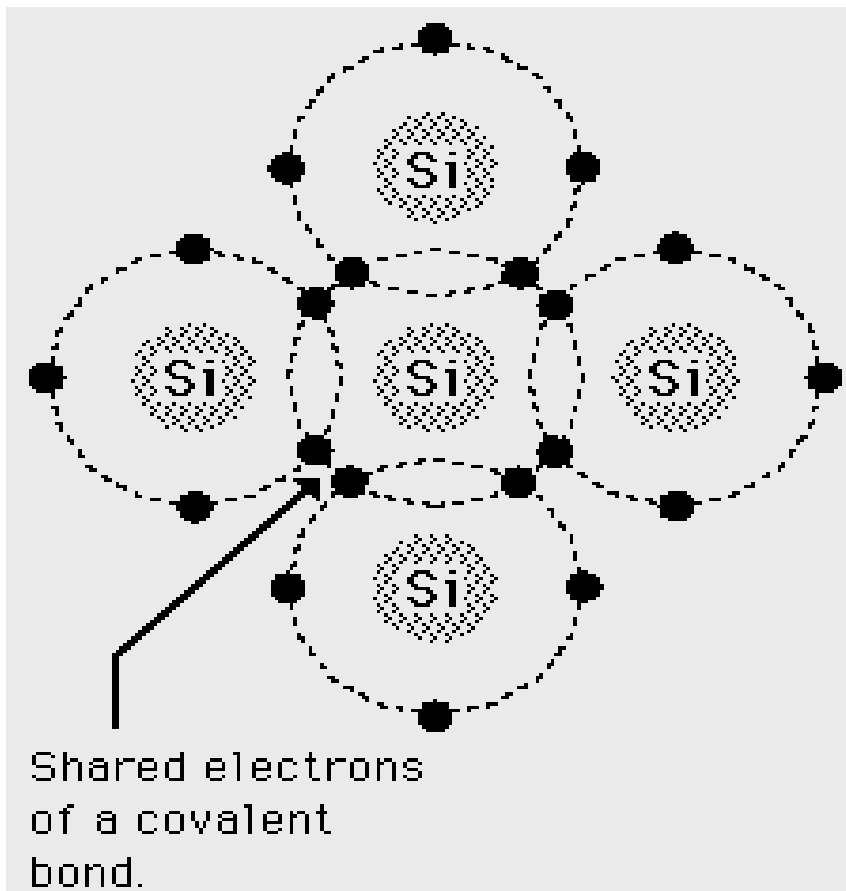
2.4 The doping of semiconductors

- Doping elements
- **Doping: N type**
- Doping: P type
- Counter doping



Doping (**N type**)

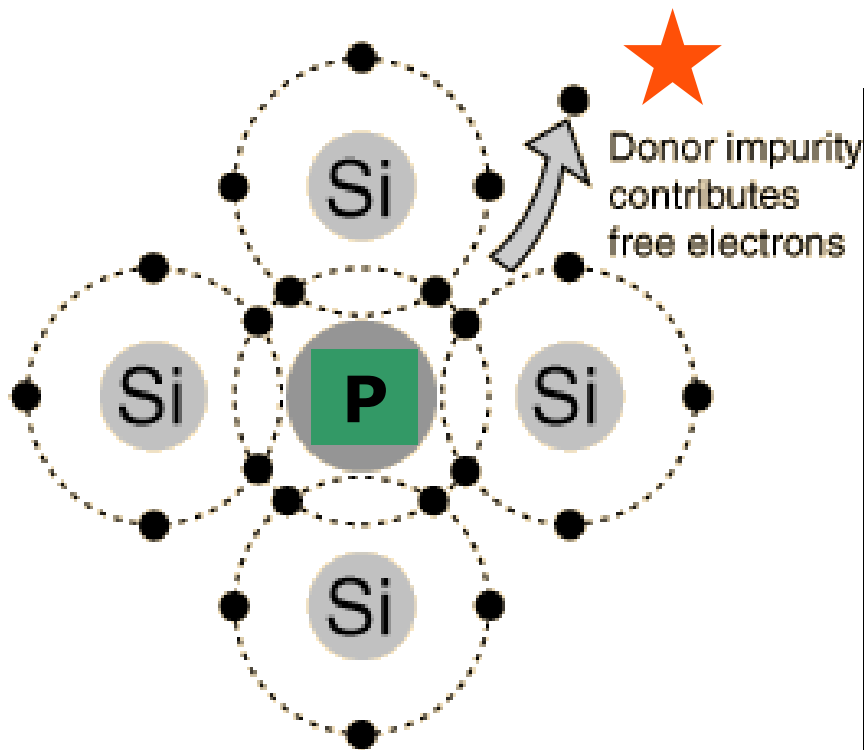
Column **V** elements are **donors**, e.g. P, As, Sb



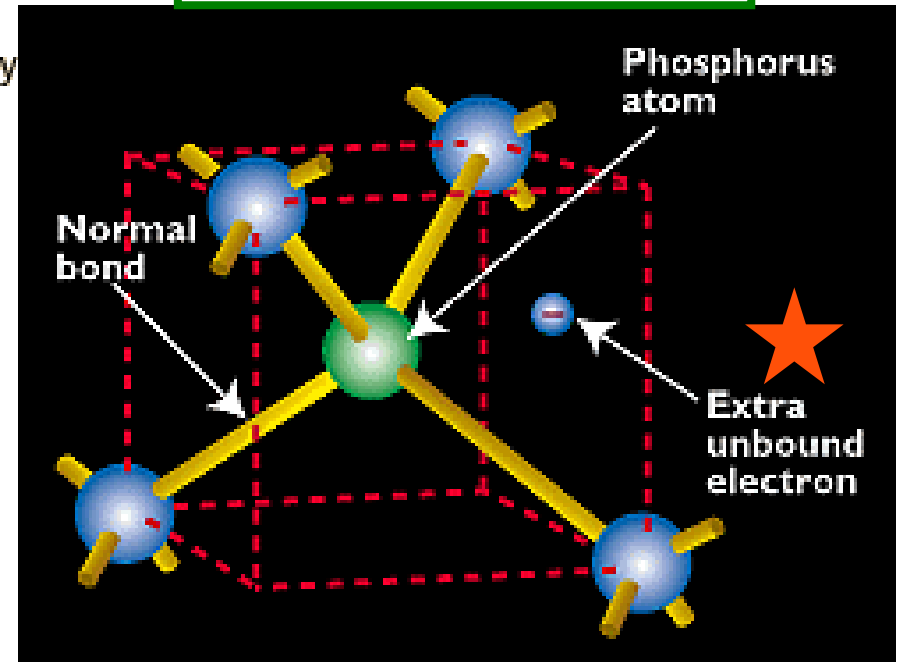
Doping (**N type**)

Column **V** elements are **donors**, e.g. P, As, Sb

By substituting a Si atom with a special impurity atom (**Column V** element), a **conduction electron** is created.



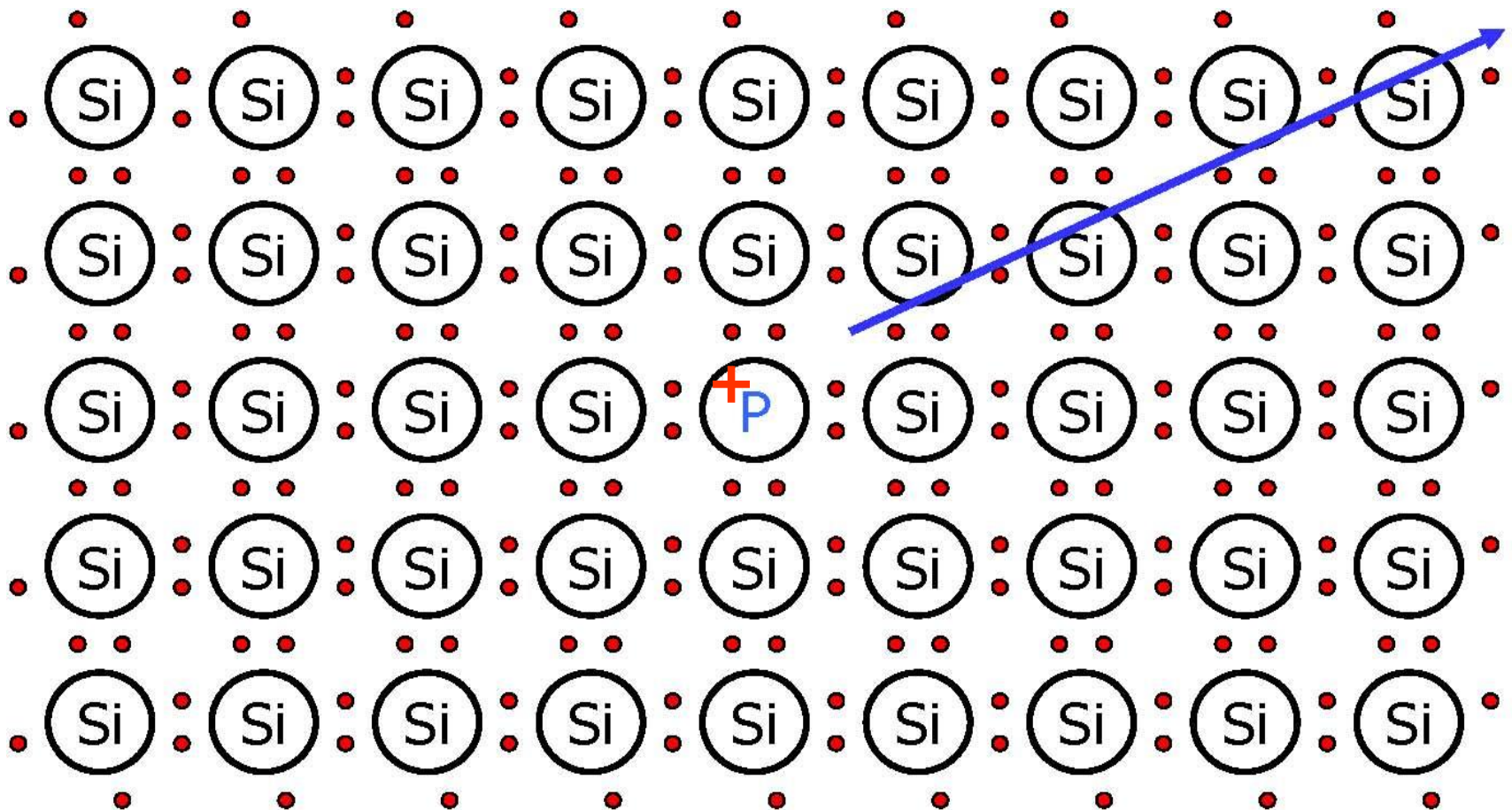
Donors: P, As, Sb



Phosphorus has 5 valence electrons

- 'Donates' **one conduction electron** to lattice
- Our substrate has 10^{15}cm^{-3} phosphorus

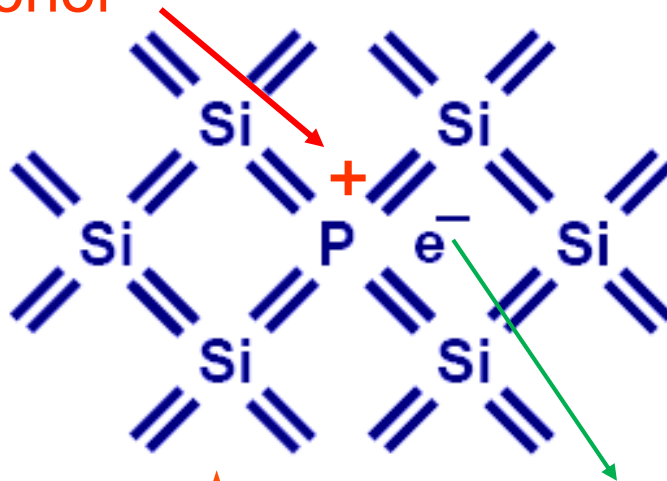
Free
★ ↓



Doping (**N type**)

- If Si is doped with **phosphorus (P)**, each P atom can contribute a conduction **electron**, so that the Si lattice has more electrons than holes, *i.e.* it becomes “**N type**”:

Immobile ion: N_D^+
Ionized donor



n_{iD} ?

$$n = N_D^+ + n_{iD} \star$$

Notation:

N_D = Concentration of donors

n = electron concentration

N_D^+ = Concentration of ionized donors

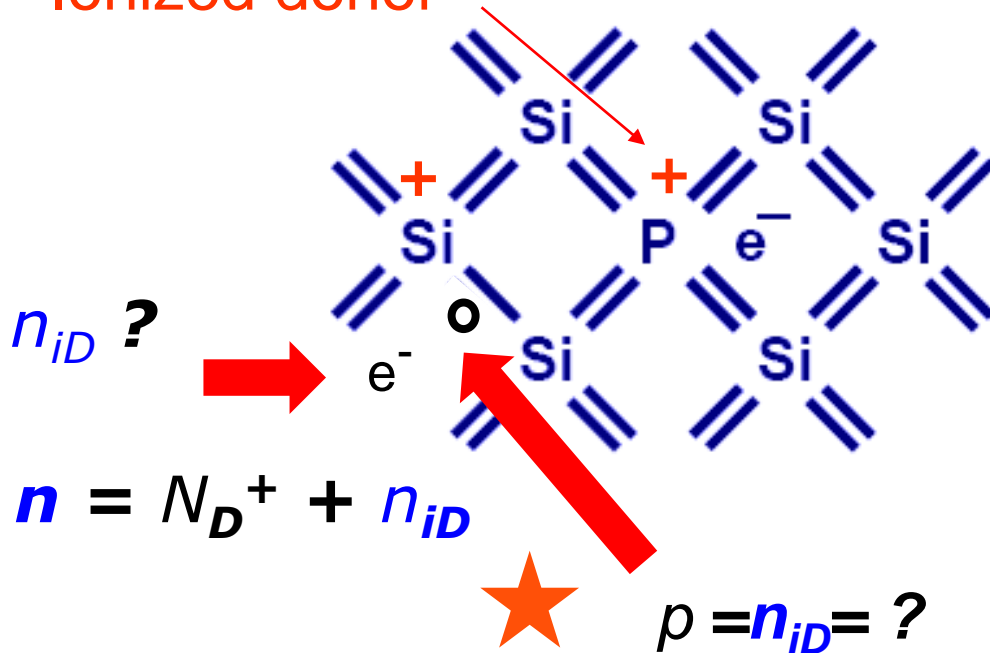
Ionization energy < 50meV:

At RT, $N_D \approx N_D^+ \gg n_{iD}$

Doping (N type)

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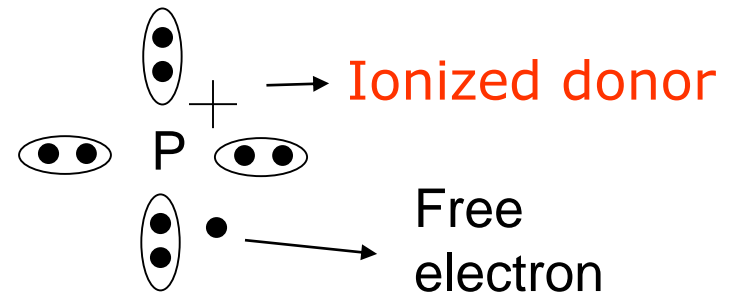
N_D^+ = Concentration of ionized donors

Ionization energy < 50meV:

At RT, $N_D \approx N_D^+ \gg n_{iD}$

N-type

- Doped by impurities of **5 valence electrons (donors)**
- At room temperature, one donor will create **one free electron**.
- Holes are not created
- $n = n_{iD} + N_D$
 - $n_{iD} \ll n_i$ = density of free electrons in the intrinsic semiconductor
 - N_D = **density of donors**
- Normally, $N_D > 10^{14} \text{ cm}^{-3}$ and $n_i \approx 10^{10} \text{ cm}^{-3}$
- Since $N_D \gg n_{iD}$, $n \approx N_D$. The density of free electron can be controlled through **doping**.



Electron and Hole Concentrations

No E field, no B field, no light

- Under thermal equilibrium conditions, the product of the conduction-electron density and the hole density is ALWAYS equal to the square of n_i :



$$np = n_i^2 = (10^{10})^2/\text{cm}^3 \text{ at RT}$$

N-type material at RT

$$n \approx N_D$$
$$p \approx \frac{n_i^2}{N_D}$$

Example: at RT

$$N_D = 10^{15}/\text{cm}^3$$

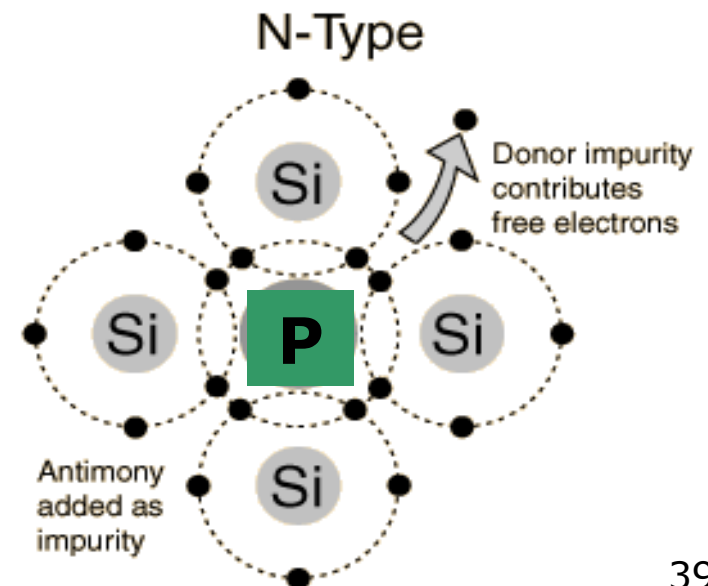
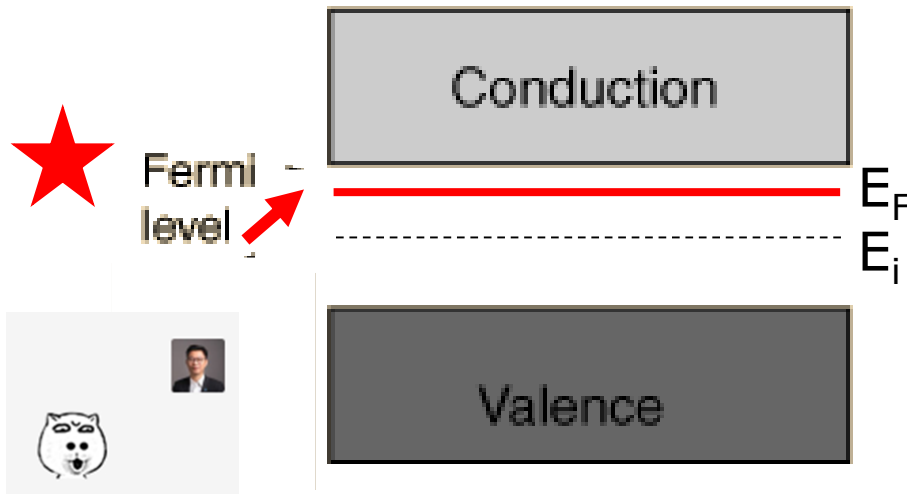
$$n = 10^{15}/\text{cm}^3$$

$$N_D^+ = 10^{15}/\text{cm}^3$$

$$p = 10^5/\text{cm}^3$$

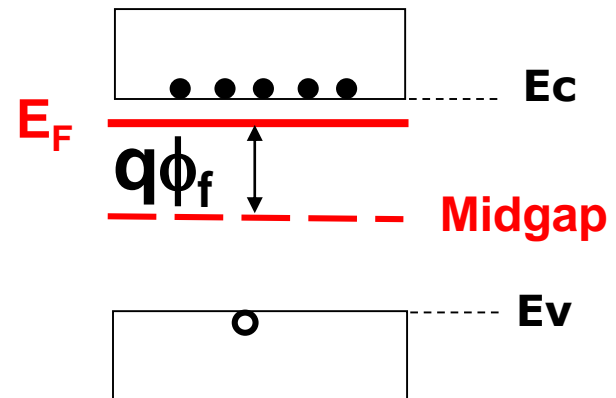
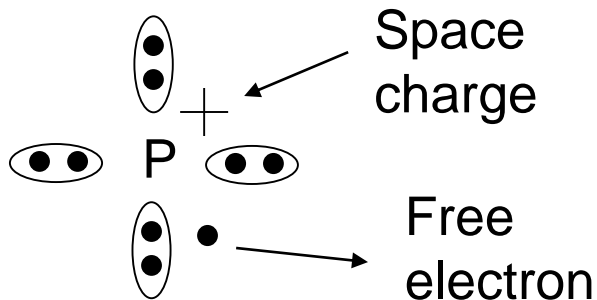
N-Type Semiconductor

- The addition of pentavalent impurities such as Sb, As or P contributes **free electrons**, greatly increasing the **conductivity** of the intrinsic semiconductor.
- **Phosphorus** may be added by diffusion of phosphine gas (PH_3).
- E_F is shifted to the **up-half** of the bandgap for n-type.



Properties of N-type

- $n \gg p$, so “**n-type**”.
- Electrons are ‘**majority**’ charge carriers and holes are ‘**minority**’ charge carriers.
- Space charge: when an electron is freed, it left a positively charged atom behind, which is fixed in space
- **Fermi potential: ϕ_f**
 - How ‘**strong**’ the n-type is



2.4 The doping of semiconductors

- Doping elements
- Doping: N type
- **Doping: P type**
- Counter doping

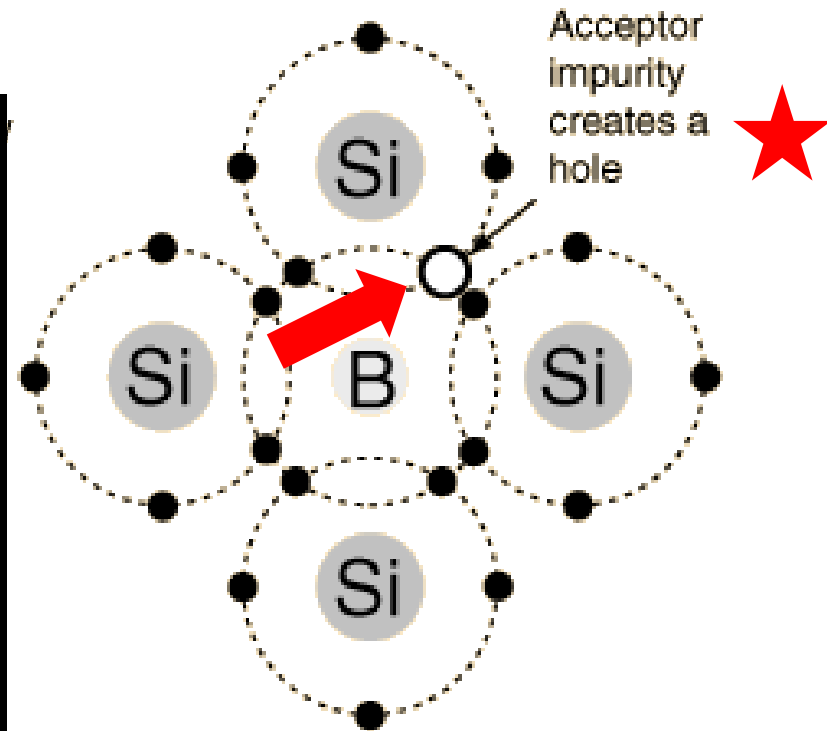
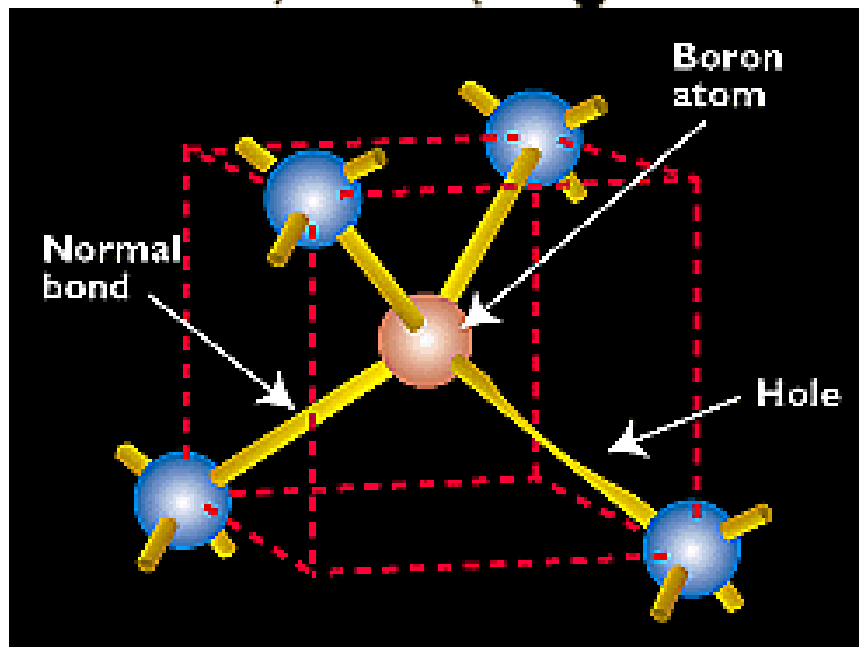


Doping (P type)

Column III elements are acceptors, e.g. B, Al, Ga

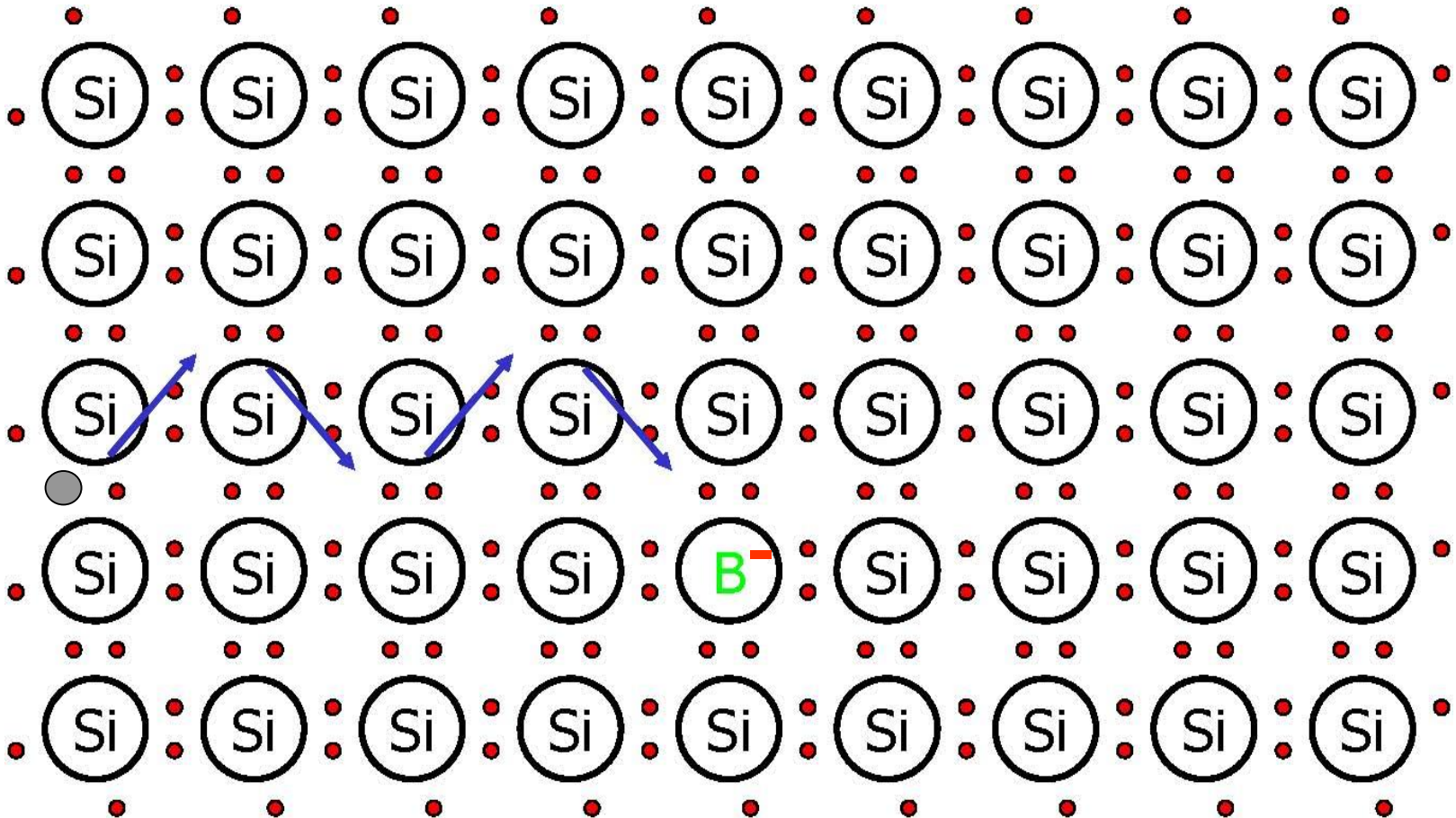
By substituting a Si atom with a special impurity atom (Column III element), a **conduction hole** is created.

Acceptors: B, Al, Ga, In



Boron has 3 valence electrons

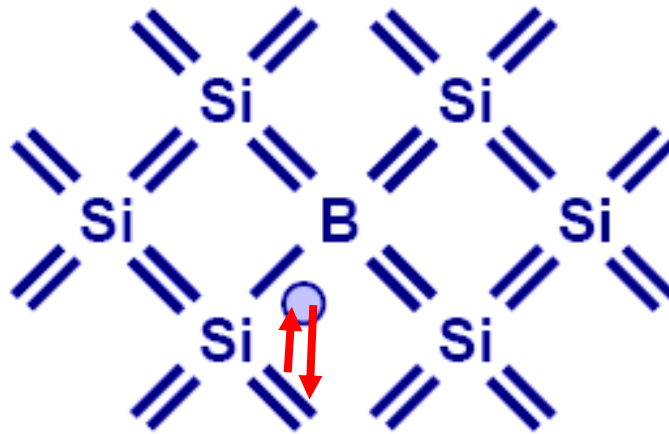
- **'Accepts'** one electron from lattice
- Creates a **'hole'**



Doping (**P type**)

Column III elements are acceptors, e.g. B

- If Si is doped with **Boron (B)**, each B atom can contribute a **hole**, so that the Si lattice has **more holes** than electrons, *i.e.* it becomes “**P type**”:



Notation:

N_A = concentration of acceptors

p = hole concentration

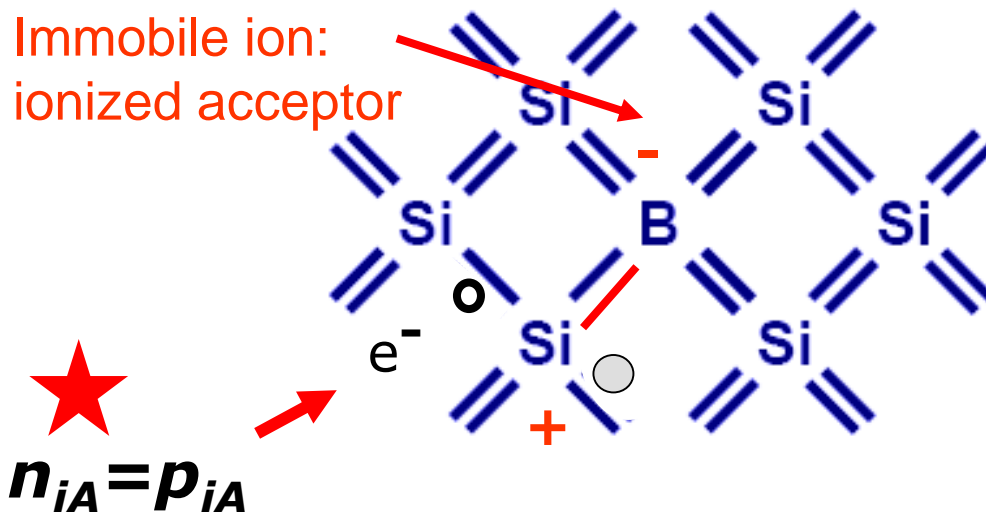
N_A^- = concentration of ionized acceptors

Hole is created when a neighboring valence electron moves to the B atom.

Doping (P type)

Column III elements are acceptors, e.g. B

- If Si is doped with **Boron (B)**, each B atom can contribute a **hole**, so that the Si lattice has **more holes** than electrons, *i.e.* it becomes “**P type**”:



Notation:

N_A = concentration of acceptors

p = hole concentration

N_A^- = concentration of ionized acceptors

Ionization energy < 50meV:

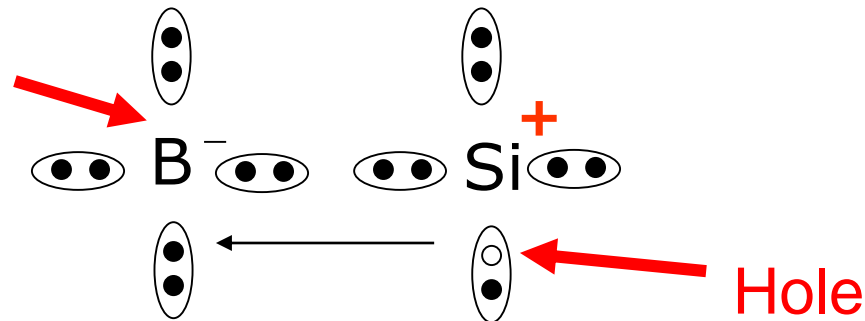
At RT, $N_A \approx N_A^- \gg p_{iA}$

$$p = N_A^- + p_{iA}$$

P-type

- Doped by impurities of **3 valence electrons** (acceptors)
- At room temperature, one acceptor will create one hole.
- Free electrons are not created
- $p = p_{iA} + N_A \approx N_A$.
 - $p_{iA} \ll p_i$ = density of holes in the intrinsic semiconductor
 - N_A = density of acceptors

Immobile ion: N_A^-
ionized acceptor



Electron and Hole Concentrations

- Under **thermal equilibrium conditions**, the product of the **conduction-electron density** and the **hole density** is ALWAYS equal to the **square of n_i** :



$$np = n_i^2 = (10^{10})^2/\text{cm}^3 \text{ at RT}$$

P-type material at RT

$$p \approx N_A$$
$$n \approx \frac{n_i^2}{N_A}$$

Example: at RT

$$N_A = 10^{15}/\text{cm}^3$$

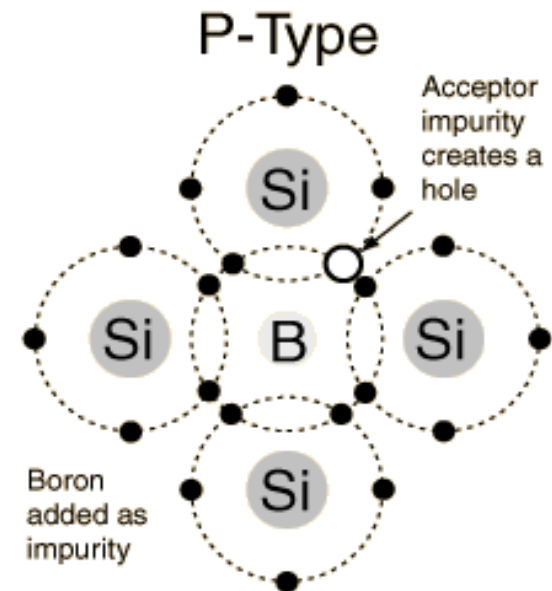
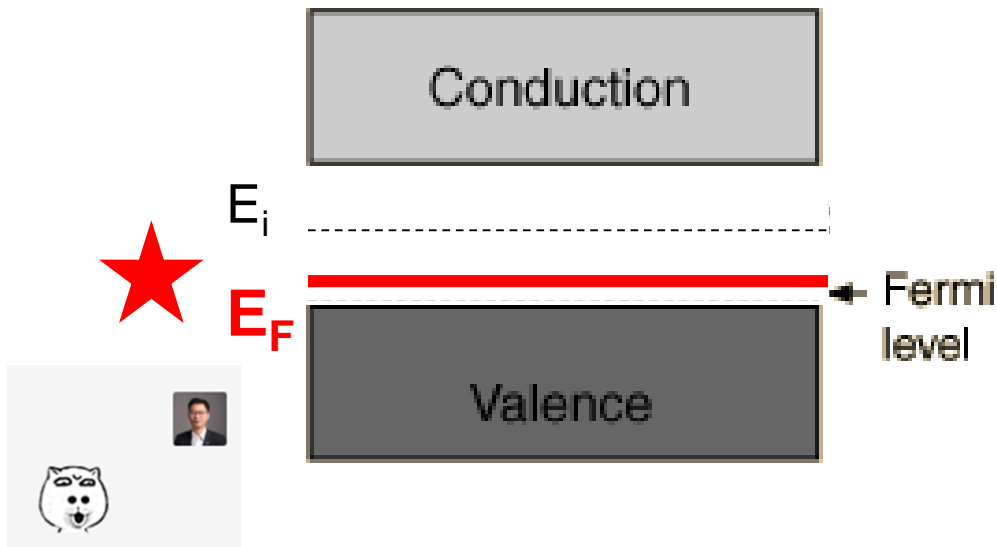
$$p = 10^{15}/\text{cm}^3$$

$$N_A^- = 10^{15}/\text{cm}^3$$

$$n = 10^5/\text{cm}^3$$

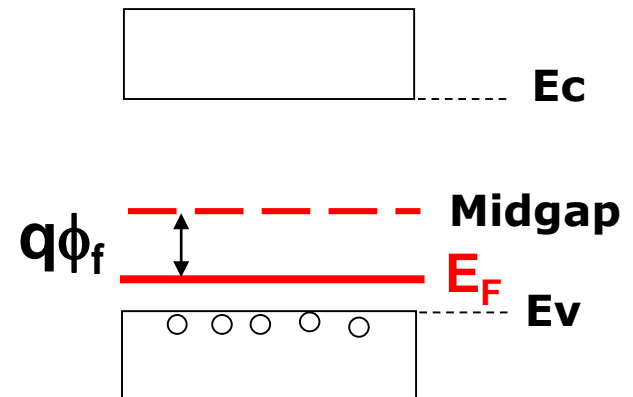
P-Type Semiconductor

- The addition of **trivalent impurities** such as B, Al, or Ga to an intrinsic semiconductor creates deficiencies of valence electrons, called "**holes**".
- It is typical to use B_2H_6 diborane gas to diffuse boron into the silicon material.
- E_F is shifted to the **down-half** of the bandgap for p-type.



Properties of P-type

- $p \gg n$, so “**p-type**”.
- **Holes** are ‘majority’ charge carriers and **electrons** are ‘minority’ charge carriers.
- Space charge: negative charges bonded to Boron atoms
- **Fermi potential: ϕ_f**
 - How ‘**strong**’ the p-type is

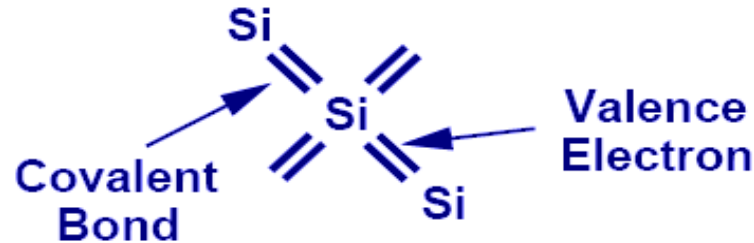


Summary of doping

Intrinsic Semiconductor

Column-V
elements
contribute
conduction
electrons,
and are
called
donors.

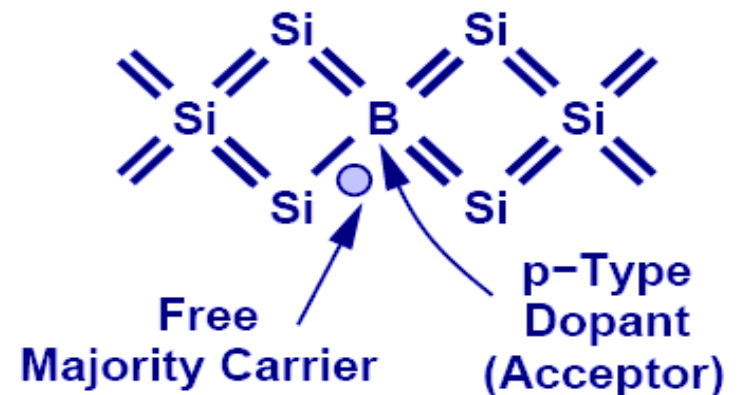
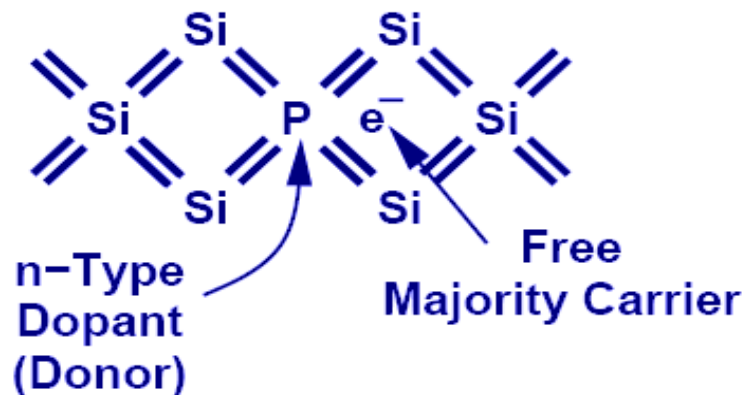
Column-III
elements
contribute
holes, and
are called
acceptors



Extrinsic Semiconductor

Silicon Crystal
 N_D Donors/cm³

Silicon Crystal
 N_A Acceptors/cm³



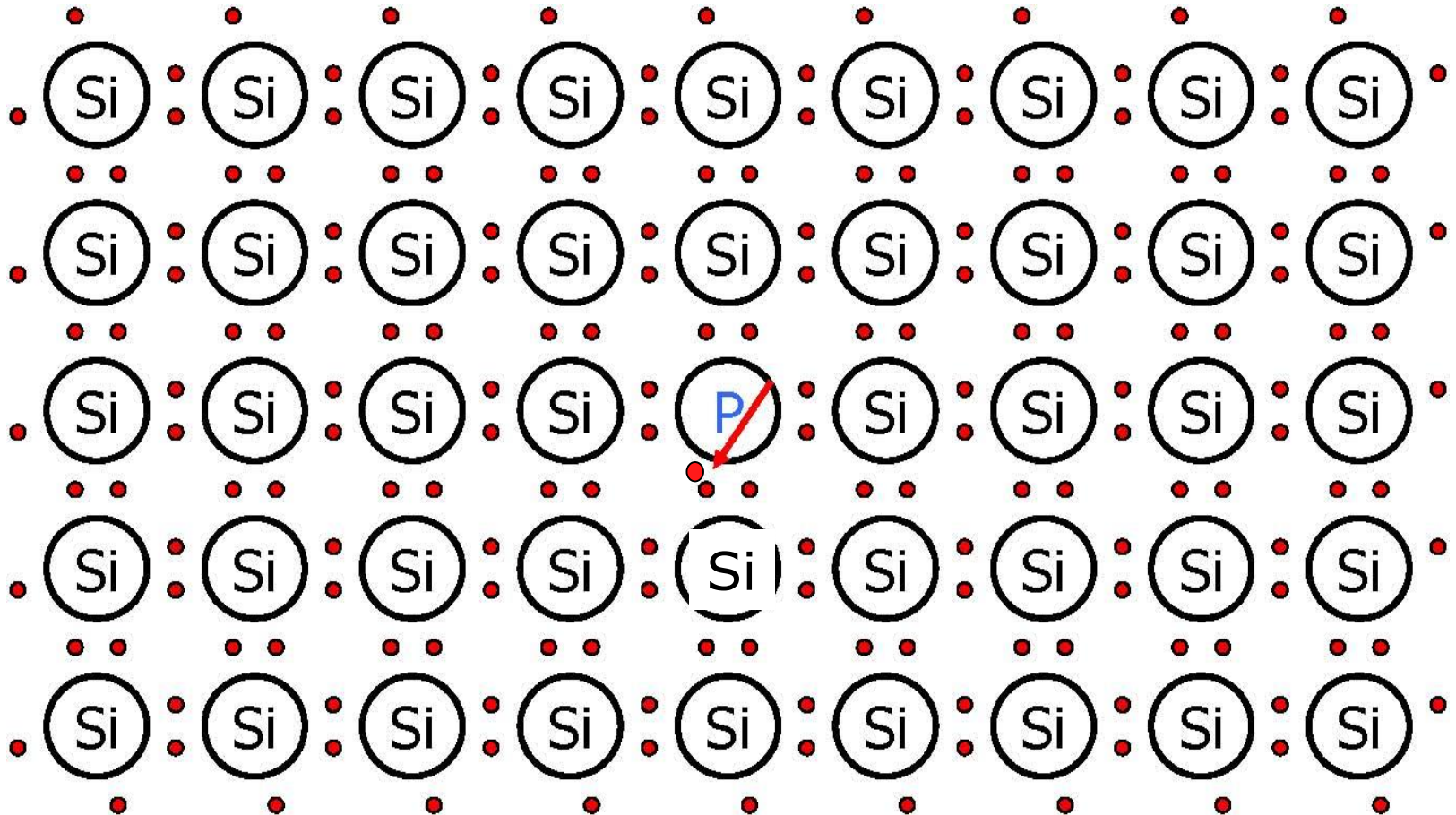
2.4 The doping of semiconductors

- Doping elements
- Doping: N type
- Doping: P type
- **Counter doping**



Counter Doping

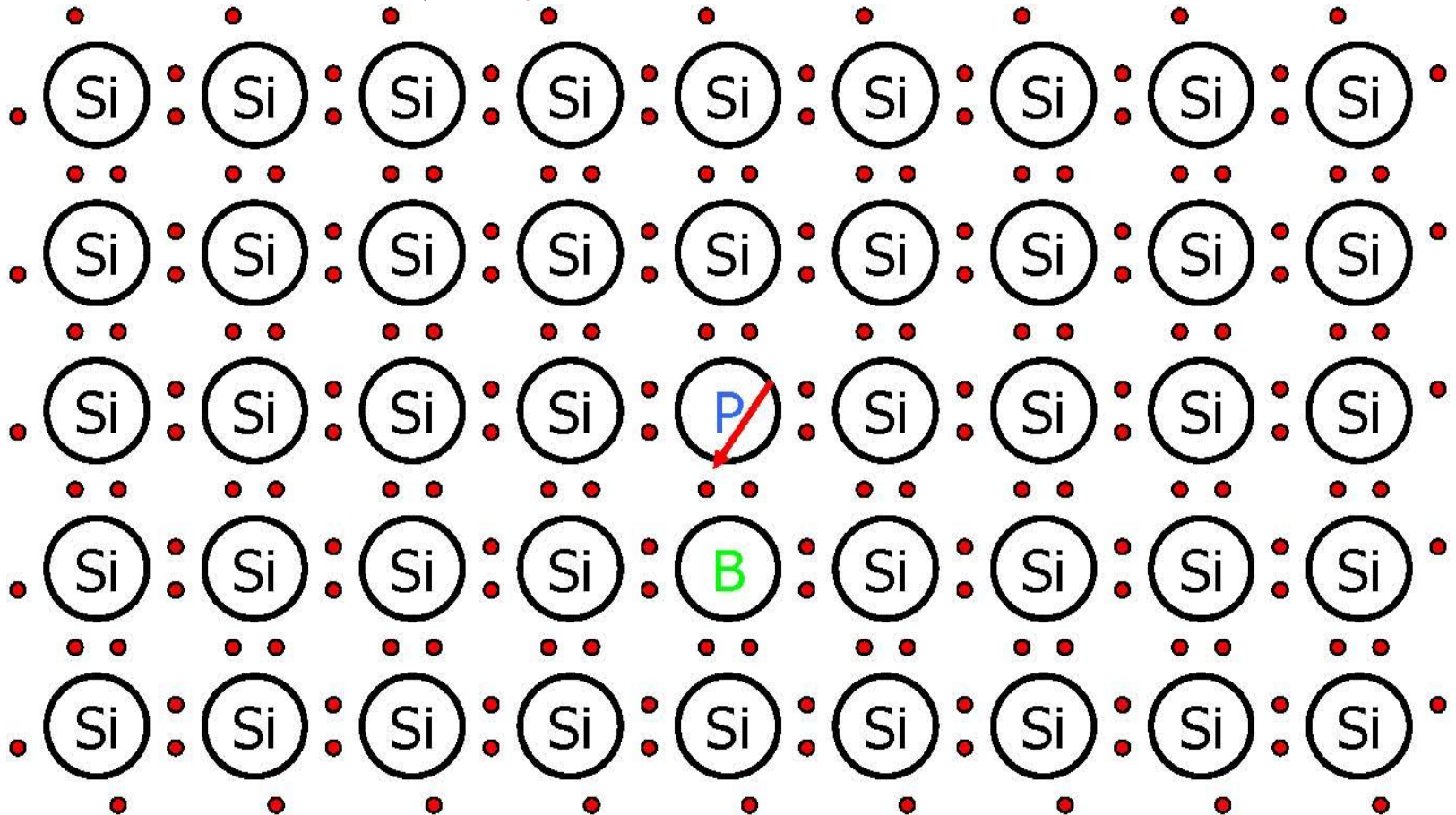
This is a **n-type** Si, $n = N_D + n_i$. Normally $N_D \gg n_i$, so **$n = N_D$**



Counter Doping

Adding the **same B** as **P** causes the doping type to change.

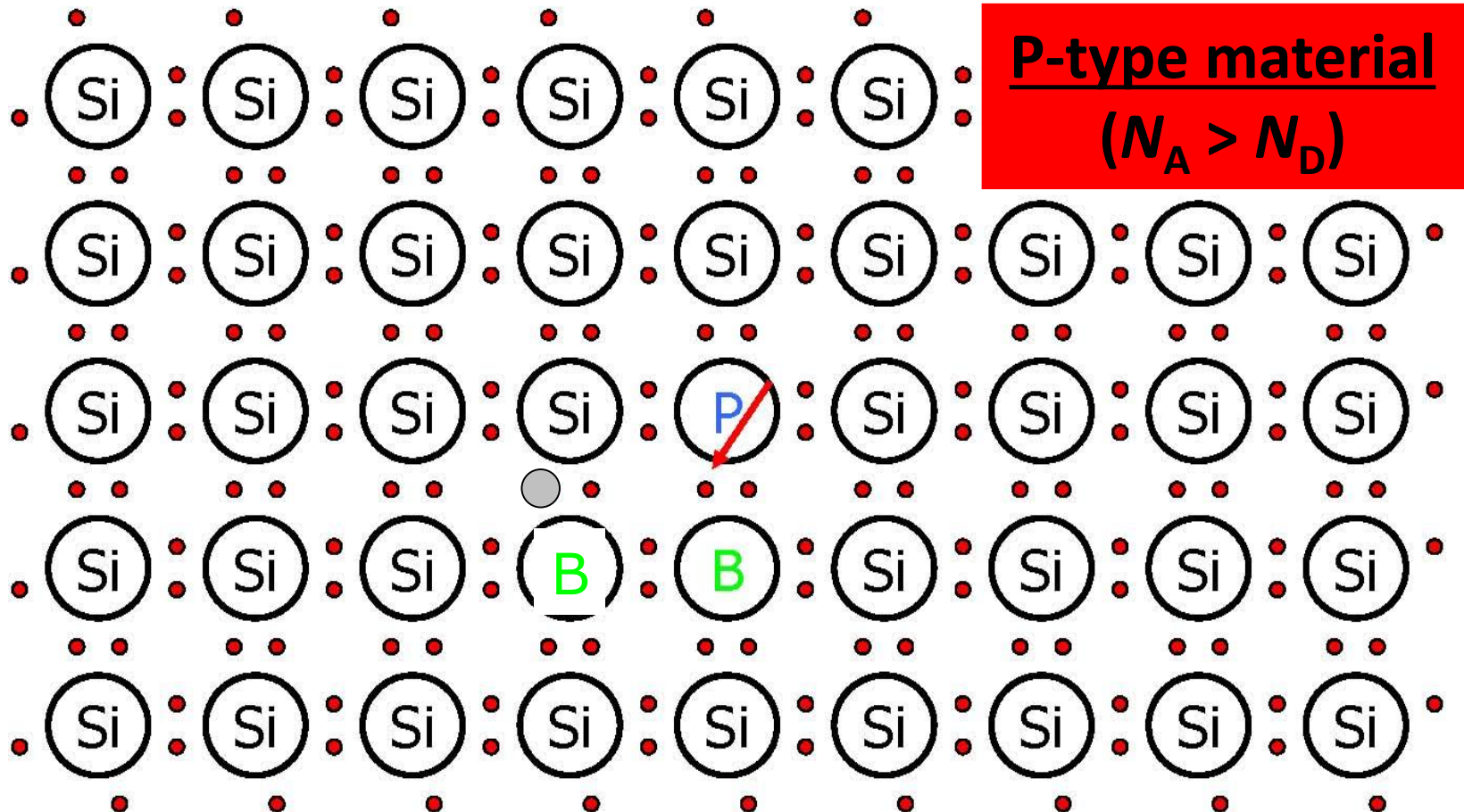
$$n = p = N_D - N_A + n_i = n_i$$



Counter Doping

$$p \approx N_A - N_D, \quad n \approx \frac{n_i^2}{N_A - N_D}$$

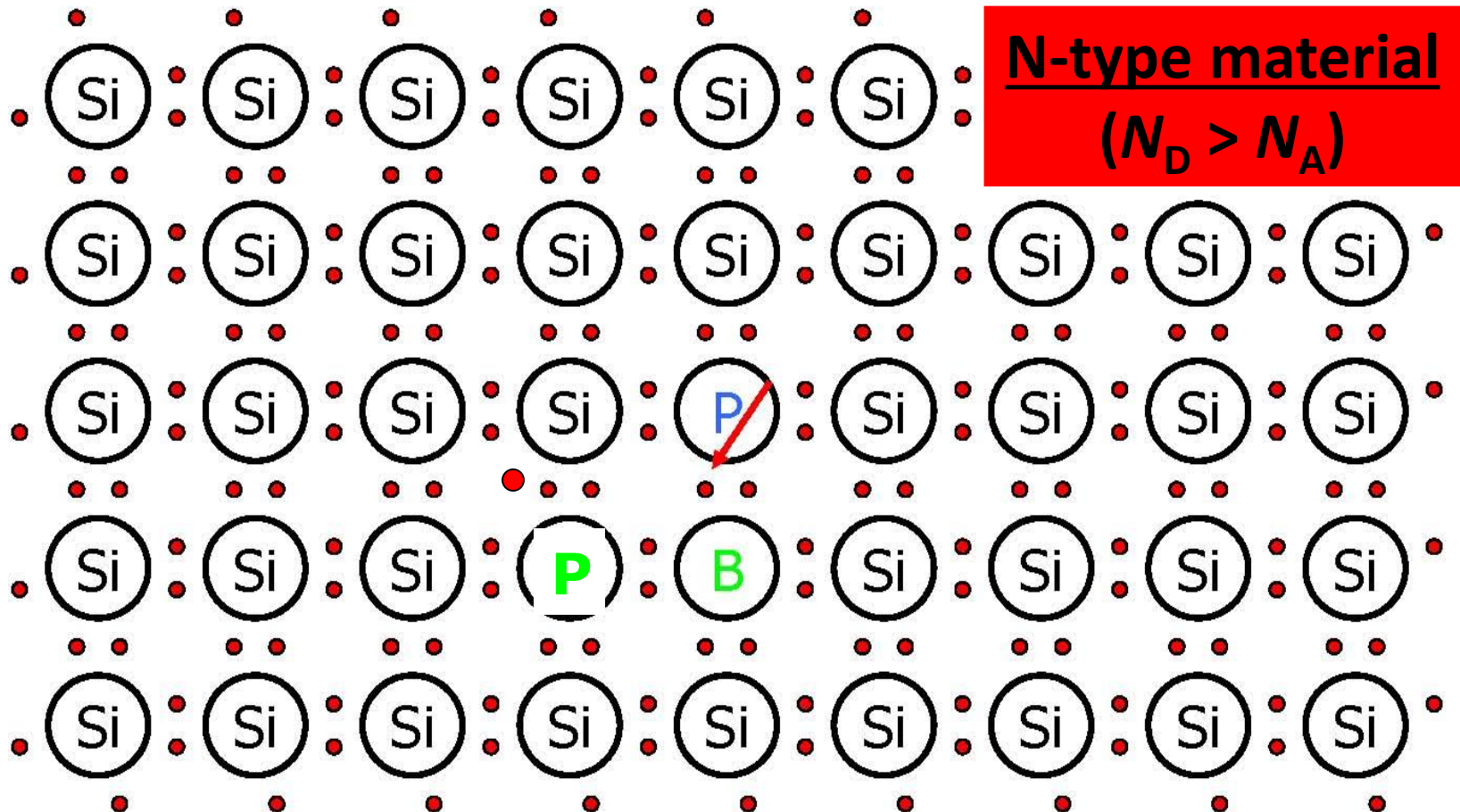
The addition of **one more B** than **P** causes the doping type to change from n-type to **p-type**



Counter Doping

$$n \approx N_D - N_A, \quad p \approx \frac{n_i^2}{N_D - N_A}$$

The addition of **one more P** than **B** causes the doping type to change from p-type to **n-type**



Dopant Compensation

- An **N-type** semiconductor can be **converted** into **P-type** material by **counter-doping** it with acceptors such that $N_A > N_D$.
- A **compensated semiconductor material** has both acceptors and donors.

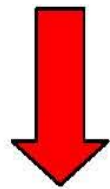
★ <u>N-type material</u>		<u>P-type material</u> ★
$(N_D > N_A)$	“net doping”	$(N_A > N_D)$
$n \approx N_D - N_A$		$p \approx N_A - N_D$
$p \approx \frac{n_i^2}{N_D - N_A}$		$n \approx \frac{n_i^2}{N_A - N_D}$

What is the relationship between E_F and n/p ?

Counter Doping Process

- To form pn junction

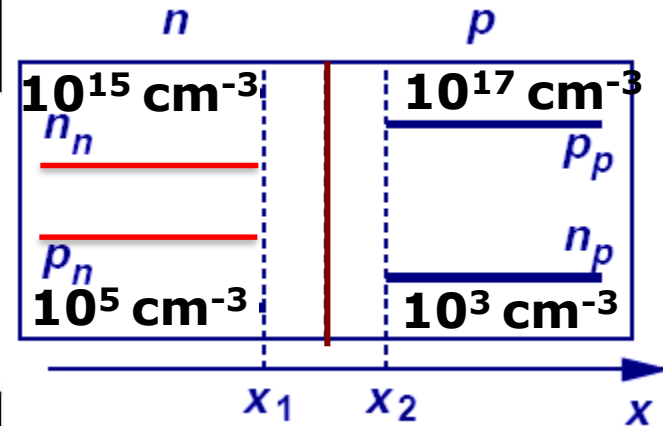
n-type (10^{15} cm^{-3})



Implant Boron
and Anneal

p-type ($> 10^{15} \text{ cm}^{-3}$)

n-type (10^{15} cm^{-3})



Next week:

Semiconductor Fundamentals – (III)

2.5 Boltzmann approximation & E_F , n , p

2.6 Carrier drift and diffusion

