

Q1

(a) Due to the fact that

Silicon is doped with As

we also know that As is "+"

Value in Semiconductors

⇒ When doped with Silicon,

there exists many electrons

⇒ Thus, the material is

N-type

$$\begin{aligned} (b) \quad n_i &= BT^{\frac{3}{2}} e^{\frac{-E_g}{2kT}} \\ &= (5.23 \times 10^{15}) (300)^{\frac{3}{2}} e^{\frac{-1.1}{2(86 \times 10^{-6})(300)}} \\ &= 1.5 \times 10^{10} \text{ cm}^{-3} \end{aligned}$$

$$n_d = n_{\text{electron}} = 5 \times 10^{16} \text{ cm}^{-3}$$

$$\begin{aligned} n_o = n_{\text{hole}} &= \frac{n_i^2}{n_d} \\ &= \frac{2.25 \times 10^{20}}{5 \times 10^{16}} \end{aligned}$$

$$= 4.5 \times 10^3 \text{ cm}^{-3}$$

$$\Rightarrow \text{In Summary } \left\{ \begin{array}{l} \text{electron: } 5 \times 10^{16} \text{ cm}^{-3} \\ \text{hole: } 4.5 \times 10^3 \text{ cm}^{-3} \end{array} \right.$$

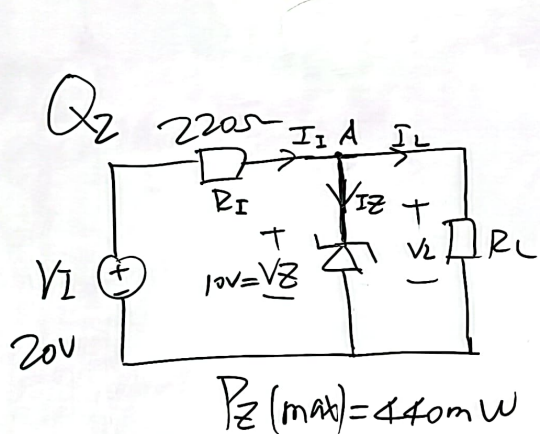
$$\begin{aligned} (c) \quad n_i &= BT^{\frac{3}{2}} e^{\frac{-E_g}{2kT}} \\ &= (5.23 \times 10^{15}) (350)^{\frac{3}{2}} e^{\frac{-1.1}{2(86 \times 10^{-6})(350)}} \\ &= 3.97 \times 10^{10} \text{ cm}^{-3} \end{aligned}$$

$$n_d = n_{\text{electron}} = 5 \times 10^{16} \text{ cm}^{-3}$$

$$\begin{aligned} n_o = n_{\text{hole}} &= \frac{n_i^2}{n_d} \\ &= \frac{(3.97)^2 \times 10^{20}}{5 \times 10^{16}} \end{aligned}$$

$$= 3.15 \times 10^3 \text{ cm}^{-3}$$

$$\Rightarrow \text{In Summary } \left\{ \begin{array}{l} \text{electron: } 5 \times 10^{16} \text{ cm}^{-3} \\ \text{hole: } 3.15 \times 10^3 \text{ cm}^{-3} \end{array} \right.$$



$$\begin{aligned}
 I_Z &= I_1 - I_L \\
 I_1 &= \frac{V_1 - V_Z}{R_1} \\
 I_L &= \frac{V_Z}{R_L} \\
 \Rightarrow I_Z &= \frac{V_1 - V_Z}{R_1} - \frac{V_Z}{R_L} \\
 \Rightarrow I_Z &= \frac{20 - 10}{22} - \frac{10}{38} \\
 \Rightarrow I_Z &= \frac{1}{22} - \frac{1}{38}
 \end{aligned}$$

(a) Apply KCL to node A $\Rightarrow I_Z = \frac{4}{209} A = 19.14mA \Rightarrow 44mW = \frac{1}{22} - \frac{10}{R_L}$

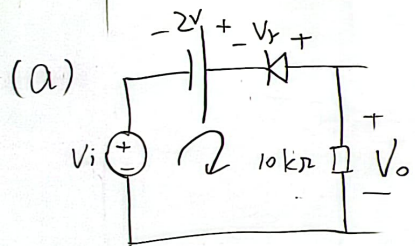
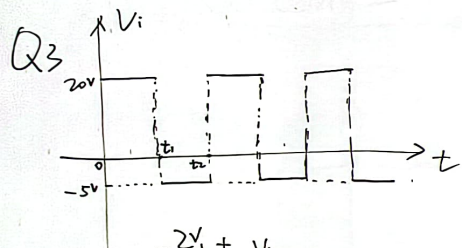
$$\begin{aligned}
 \Rightarrow I_L &= I_1 - I_Z \\
 \Rightarrow I_L &= \frac{V_Z}{R_L} = \frac{1}{38} A = 26.32mA \Rightarrow R_L = 6875 \Omega \\
 \Rightarrow I_1 &= I_Z + I_L = \frac{1}{22} A = 45.45mA
 \end{aligned}$$

(b) From (a)

$$\begin{aligned}
 \Rightarrow I_Z &= \frac{V_1 - V_Z}{R_1} - \frac{V_Z}{R_L} \\
 \Rightarrow I_Z &= \frac{1}{22} - \frac{10}{R_L} \\
 P_{Z(max)} &= V_Z \cdot I_Z \\
 V_Z &= 10 \\
 P_{Z(max)} &= 440mW
 \end{aligned}$$

(c) From (b)

$$\begin{aligned}
 \Rightarrow I_Z &= \frac{V_1 - V_Z}{R_1} - \frac{V_Z}{R_L} \\
 \Rightarrow I_Z &= \frac{10}{175} - \frac{10}{R_L} \\
 P_{Z(max)} &= V_Z \cdot I_Z \\
 V_Z &= 10V \\
 P_{Z(max)} &= 440mW \\
 \Rightarrow R_L &= 760.87\Omega
 \end{aligned}$$



Let us analyze the situation in a period ($0 \leq t \leq t_2$)

1° When $0 \leq t \leq t_1$

\Rightarrow Diode is cut-off

$\Rightarrow i_D = 0$

$\Rightarrow V_o = i_D \cdot 10k\Omega = 0V$

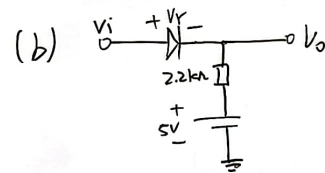
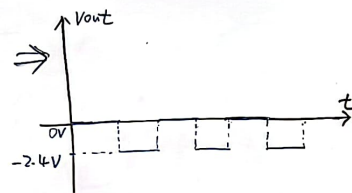
2° when $t_1 < t \leq t_2$

\Rightarrow Diode is on.

\Rightarrow Apply KVL to this loop

$\Rightarrow 2 + V_r - V_o + V_i = 0$

$\Rightarrow V_o = -2.4V$



Let us analyze the situation in a period ($0 \leq t \leq t_2$)

1° When $0 \leq t \leq t_1$

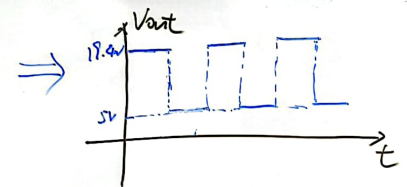
\Rightarrow Diode is on

$\Rightarrow V_o = V_i - V_r = 17.4V$

2° when $t_1 < t \leq t_2$

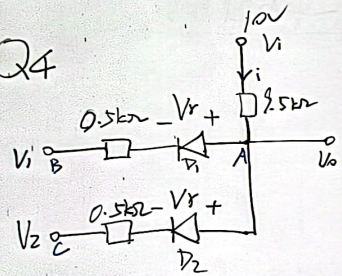
\Rightarrow Diode is cut-off

$\Rightarrow V_o = V_i = -5V$





Q4



(a) $V_1 = 10V$; $V_2 = 0V$

$$\frac{10 - 0.6}{10k} = \frac{V_r}{10k}$$

$$\left. \begin{array}{l} V_1 = 10V \\ V_i = 10V \end{array} \right\} \Rightarrow D_1 \text{ is cut-off} \Rightarrow I_{D1} = 0A$$

$$\left. \begin{array}{l} V_2 = 0V \\ V_i = 10V \end{array} \right\} \Rightarrow D_2 \text{ is on} \Rightarrow I_{D2} = \frac{V_i - V_r}{10k} = 0.94mA$$

AB path is open

$$\Rightarrow V_o = V_r + I_{D2} \cdot 0.5k$$

$$\Rightarrow V_o = 1.07V$$

\Rightarrow In Summary

$$\left\{ \begin{array}{l} V_o = 1.07V \\ I_{D1} = 0A \\ I_{D2} = 0.94mA \end{array} \right.$$

(b) $V_1 = V_2 = 10V$

$$\left. \begin{array}{l} V_1 = V_2 = 10V \\ V_i = 10V \end{array} \right\}$$

\Rightarrow both D_1 and D_2 are cut-off

$$\Rightarrow I_{D1} = I_{D2} = 0A$$

\Rightarrow AB, AC paths are open

$$\Rightarrow V_o = V_i = 10V$$

$$\Rightarrow \text{In Summary} \left\{ \begin{array}{l} V_o = 10V \\ I_{D1} = 0A \\ I_{D2} = 0A \end{array} \right.$$

(c) $V_1 = V_2 = 0V$

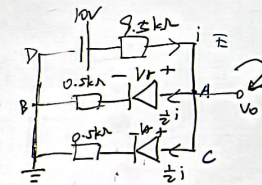
$$\left. \begin{array}{l} V_1 = V_2 = 0V \\ V_i = 10V \end{array} \right\}$$

\Rightarrow both D_1 and D_2 are on

Because the components on path AB and Path AC are totally same

$$\Rightarrow I_{D1} = I_{D2} = \frac{1}{2} i$$

\Rightarrow The circuit can be simplified to



\Rightarrow Apply KVL to closed loop ABDEA

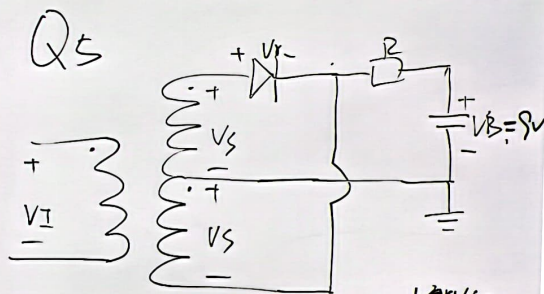
$$\Rightarrow 10 - V_r = 0.5k i + 0.5k \cdot \frac{1}{2} i$$

$$\Rightarrow i = 0.96mA$$

$$\Rightarrow \frac{1}{2} i = I_{D1} = I_{D2} = 0.48mA$$

$$\Rightarrow V_o = V_r + \frac{1}{2} i \cdot 0.5k = 0.84V$$

$$\Rightarrow \text{In Summary} \left\{ \begin{array}{l} V_o = 0.84V \\ I_{D1} = 0.48mA \\ I_{D2} = 0.48mA \end{array} \right.$$



(a) $V_S = 15 \sin[2\pi(60)t]$ *varying*

$V_S(\text{peak}) = 15 \text{ V}$

$R = \frac{V_S(\text{peak}) - V_r - V_B}{1.2 \text{ A}}$

$R = 4.42 \Omega$

(b) From (c)

$\Rightarrow t_1 = \frac{40.28^\circ}{180 \cdot 120\pi} = 1.87 \text{ ms}$
 $t_2 = \frac{139.71^\circ}{180 \cdot 120\pi} = 6.47 \text{ ms}$

$\Rightarrow \Delta t = 4.6 \text{ ms}$

$i(t) = \frac{V_S - V_r}{R}$

$Q = \int_{t_1}^{t_2} i(t) dt$

$\Rightarrow Q = \int_{1.87 \text{ ms}}^{6.47 \text{ ms}} \frac{15 \sin(120\pi t) - 9.7}{4.42} dt$

$\Rightarrow Q = (-3.33) \left[\frac{\cos(120\pi t)}{120\pi} \right]_{1.87 \text{ ms}}^{6.47 \text{ ms}} - 21 \int_{1.87 \text{ ms}}^{6.47 \text{ ms}} dt$

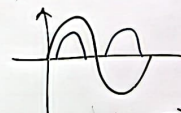
$\Rightarrow Q = 13.47 \text{ mC} - 10.07 \text{ mC} = 3.6 \text{ mC}$
(m = 10⁻³)

$\Rightarrow I_{\text{ave}} = \frac{Q}{t_2 - t_1} = \frac{3.6 \times 10^{-3} \text{ C}}{(6.47 - 1.87) \times 10^{-3} \text{ s}}$

$\Rightarrow I_{\text{ave}} = 0.78 \text{ A}$

\Rightarrow Thus: Average Charging Current is 0.78 A

(c) $V_S = 15 \sin[2\pi(60)t]$
 Fraction of Diode Conduction Cycle



$V_S - V_r \geq V_r$

$\Rightarrow 15 \sin(120\pi t) \geq 9.7$

$\Rightarrow 15 \sin(120\pi t_1) = 9.7$

$\Rightarrow \omega t_1 = 40.28^\circ$

$\Rightarrow \omega t_2 = 180 - 40.28^\circ = 139.71^\circ$

$\Rightarrow \text{Fraction} = \frac{139.71^\circ - 40.28^\circ}{360^\circ} \times 100\%$
 $= 27.62\%$

Because it is a Full-wave

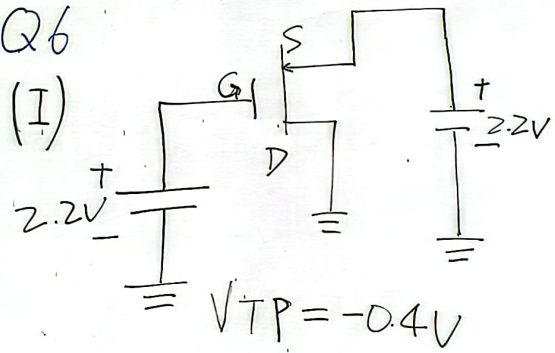
Rectifier, each diode conducts

for the same time in $0 \sim \frac{T}{2}$ and $\frac{T}{2} \sim T$

\Rightarrow Thus the fraction of time that each diode is conducting is 27.62%

Q6

(I)



$$V_G = 2.2V$$

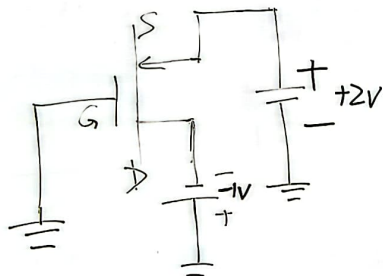
$$V_S = 2.2V$$

$$\Rightarrow V_{SG} = V_S - V_G = 0V$$

$$V_{SG} + V_{TP} = -0.4V < 0$$

\Rightarrow Transistor is cut-off

(II)



$$V_G = 0V$$

$$V_S = 2V$$

$$\Rightarrow V_{SG} = V_S - V_G = 2V$$

$$V_{SG} + V_{TP} = 1.6V > 0$$

\Rightarrow Transistor is on.

$$V_D = 1V$$

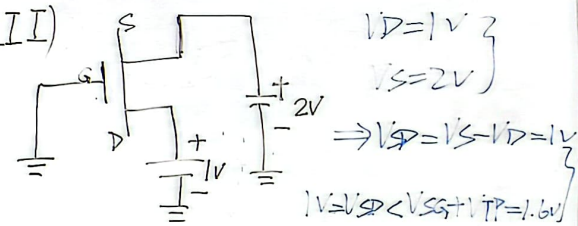
$$V_S = 2V$$

$$\Rightarrow V_{SD} = V_S - V_D = 1V$$

$$1V = V_{SD} < V_{SG} + V_{TP} = 1.6V$$

\Rightarrow Transistor is in
Nonsaturation Region

(III)



$$V_G = 0V$$

$$V_S = 2V$$

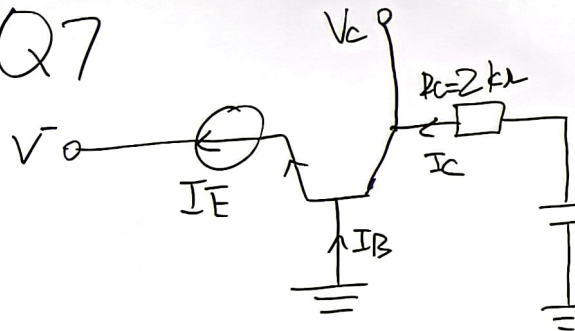
$$\Rightarrow V_{SG} = V_S - V_G = 2V$$

$$V_{SG} + V_{TP} = 1.6V > 0$$

\Rightarrow Transistor is on.

\Rightarrow Transistor is
in Nonsaturation
Region.

Q7



$$\beta = 80$$

$$(a) \quad I_E = (1 + \beta) I_B$$

$$I_E = 1.2 \text{ mA}, \beta = 80$$

$$\Rightarrow I_B = \frac{1.2}{81} \text{ mA} \\ = \frac{1200}{81} \mu\text{A}$$

$$I_C = \beta I_B$$

$$\beta = 80; I_B = \frac{1.2}{81} \text{ mA}$$

$$\Rightarrow I_C = \frac{96}{81} \text{ mA}$$

$$I_C = \alpha I_E$$

$$\Rightarrow \alpha = \frac{I_C}{I_E} = \frac{\frac{96}{81} \text{ mA}}{1.2 \text{ mA}}$$

$$\Rightarrow \alpha = \frac{80}{81}$$

$$V_C = 5 - I_C R_C$$

$$I_C = \frac{96}{81} \text{ mA}; R_C = 2 \text{ k}\Omega$$

$$\Rightarrow V_C = 5 - \frac{192}{81} = \frac{213}{81} \text{ V}$$

In Summary

$$\Rightarrow \left\{ \begin{array}{l} I_B = \frac{1.2}{81} \text{ mA} = 14.81 \mu\text{A} \\ I_C = \frac{96}{81} \text{ mA} = 1.19 \text{ mA} \\ \alpha = \frac{80}{81} = 0.99 \\ V_C = \frac{213}{81} \text{ V} = 2.63 \text{ V} \end{array} \right.$$

(b) $I_E = (1 + \beta) I_B$

$$\beta = 80; I_E = 0.8 \text{ mA}$$

$$\Rightarrow I_B = \frac{0.8}{81} \text{ mA} \\ = \frac{800}{81} \mu\text{A}$$

$$I_C = \beta I_B$$

$$\beta = 80; I_B = \frac{0.8}{81} \text{ mA}$$

$$\Rightarrow I_C = \frac{64}{81} \text{ mA}$$

$$I_C = \alpha I_E$$

$$\Rightarrow \alpha = \frac{I_C}{I_E} = \frac{\frac{64}{81} \text{ mA}}{0.8 \text{ mA}}$$

$$\Rightarrow \alpha = \frac{80}{81}$$

$$V_C = 5 - I_C R_C$$

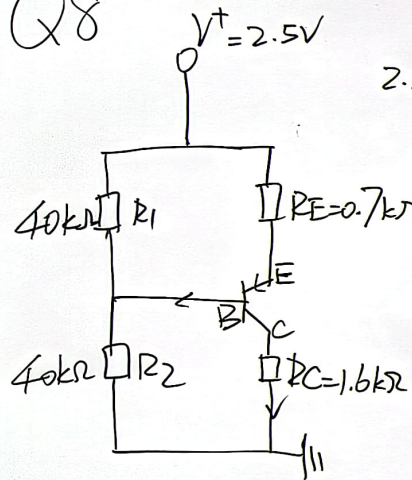
$$I_C = \frac{64}{81} \text{ mA}; R_C = 2 \text{ k}\Omega$$

$$\Rightarrow V_C = 5 - \frac{128}{81} = \frac{277}{81} \text{ V}$$

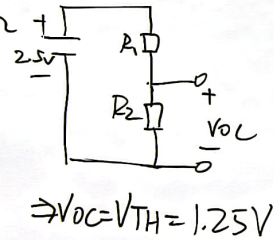
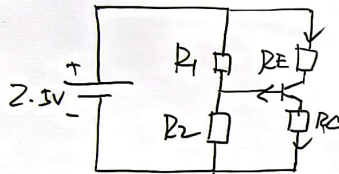
In Summary

$$\Rightarrow \left\{ \begin{array}{l} I_B = \frac{800}{81} \mu\text{A} = 9.88 \mu\text{A} \\ I_C = \frac{64}{81} \text{ mA} = 0.79 \text{ mA} \\ \alpha = \frac{80}{81} = 0.99 \\ V_C = \frac{277}{81} \text{ V} = 3.42 \text{ V} \end{array} \right.$$

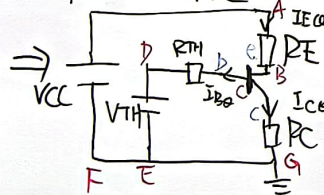
Q8



The circuit can be simplified into



$$\Rightarrow R_{TH} = R_1 \parallel R_2 = 20 \text{ k}\Omega$$



Apply KVL to loop
(A B C D E F A)

$$\begin{aligned} \Rightarrow V_{CC} - V_{EB(\text{on})} - V_{TH} &= I_{EQ} \cdot R_E + I_{BQ} \cdot R_{TH} \\ V_{CC} &= 2.5 \text{ V}; V_{EB(\text{on})} = 0.7 \text{ V} \\ V_{TH} &= 1.25 \text{ V}; R_E = 0.7 \text{ k}\Omega \\ I_{EQ} &= (1 + \beta) I_{BQ} = 9 I_{BQ} \end{aligned}$$

$$\Rightarrow I_{BQ} = 6.57 \mu\text{A}$$

$$I_{EQ} = 9 I_{BQ} = 0.598 \text{ mA}$$

$$\Rightarrow I_{CQ} = \beta I_{BQ} = 0.591 \text{ mA}$$

Apply KVL to loop
(A B C G) ↓

$$2.5 - V_{ECQ} = I_{EQ} \cdot R_E + I_{CQ} \cdot R_C$$

$$\Rightarrow V_{ECQ} = 2.5 - I_{EQ} \cdot R_E - I_{CQ} \cdot R_C$$

$$\Rightarrow V_{ECQ} = 2.5 - 0.598 \text{ mA} \cdot 0.7 \text{ k}\Omega - 0.591 \text{ mA} \cdot 1.6 \text{ k}\Omega$$

$$\Rightarrow V_{ECQ} = 2.5 - 0.419 - 0.946$$

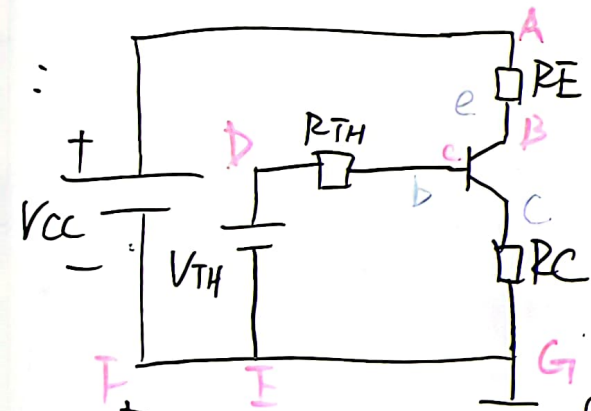
$$\Rightarrow V_{ECQ} = 1.135 \text{ V}$$

$$\Rightarrow \text{In summary } \left\{ \begin{array}{l} R_{TH} = 20 \text{ k}\Omega \\ V_{TH} = 1.25 \text{ V} \\ I_{BQ} = 6.57 \mu\text{A} \\ I_{CQ} = 0.591 \text{ mA} \end{array} \right. \quad V_{ECQ} = 1.135 \text{ V}$$

Q8

(b) From (a)

⇒ the circuit can be simplified into



Despite the change of $\beta \Rightarrow I_{BQ} = 4.375 \mu A$

⇒ V_{TH} keeps $1.25V$ as (a)

R_{TH} keeps $20k\Omega$ as (a) ⇒ $I_{CQ} = 0.656 mA$

Apply KVL to loop
(A B C D E F A)

⌚

$$\Rightarrow V_{CC} - V_{E(B(on))} - V_{TH}$$

$$= I_{EQ} \cdot R_E + I_{BQ} \cdot R_{TH}$$

$$V_{CC} = 2.5V; V_{E(B(on))} = 0.7V$$

$$V_{TH} = 1.25V; R_E = 0.7k\Omega$$

$$I_E = (1 + \beta) I_{BQ} = 151 I_{BQ}$$

Apply KVL to loop
(A B C G) ↓

$$\Rightarrow 2.5 - V_{ECQ} = I_{EQ} \cdot R_E + I_{CQ} \cdot R_C$$

$$\Rightarrow V_{ECQ} = 2.5 - I_{EQ} \cdot R_E - I_{CQ} \cdot R_C$$

$$\Rightarrow V_{ECQ} = 0.988V \quad \text{In Summary}$$

β	I_{CQ}	V_{ECQ}
90	0.591 mA	1.135V
150	0.656 mA	0.988V
$\Delta\%$	$\frac{0.656 - 0.591}{0.591} \times 100\%$	$\frac{0.988 - 1.135}{1.135} \times 100\%$
Result	$= +10.998\%$	$= -12.952\%$