

Ejercicios Algoritmo de Euclides

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Marzo 29 2023

Para cada uno de los siguientes a y n encuentre el cociente y el resto de dividir a sobre n y escriba la ecuación $a = qn + r$.

1. $a = 59, n = 7$

$$\begin{aligned}r &= a - qn \\56 &< 59 < 63 \\7 * 8 &< 59 < 7 * 9 \\8 &< \frac{59}{7} < 9 \\r &= 59 - (8 * 7) = 3 \\59 &= 8 * 7 + 3\end{aligned}$$

2. $a = 84, n = 12$

$$\begin{aligned}72 &< 84 < 96 \\12 * 6 &< 12 * 7 < 12 * 8 \\6 &< 7 < 8 \\r &= 84 - (6 * 12) = 12 \\ \text{Dado que } r &= n \text{ entonces:} \\q+ &= 1 \\r &= 84 - (7 * 12) = 0 \\84 &= 7 * 12\end{aligned}$$

3. $a = 100, n = 9$

$$\begin{aligned}99 &< 100 < 108 \\9 * 11 &< 100 < 9 * 12 \\11 &< \frac{100}{9} < 12 \\r &= 100 - (11 * 9) = 1 \\100 &= 11 * 9 + 1\end{aligned}$$

4. $a = -96, n = 12$

$$\begin{aligned}-108 &< -96 < -84 \\-9 * 12 &< -8 * 12 < -7 * 12\end{aligned}$$

$$\begin{aligned}
& -9 < -8 < -7 \\
& r = -96 - (-9 * 12) = 12 \\
& \text{Dado que } r = n \text{ entonces:} \\
& \quad q+ = 1 \\
& r = -96 - (-8 * 12) = 0 \\
& -96 = -8 * 12
\end{aligned}$$

$$5. \ a = -4, n = 5$$

$$\begin{aligned}
& -5 < -4 < 5 \\
& -1 * 5 < -4 < 1 * 5 \\
& -1 < -\frac{4}{5} < 1 \\
& r = -4 - (-1) * (5) = 1 \\
& -4 = (-1) * (5) + 1
\end{aligned}$$