

# Advanced Projects in Exoplanets

## The RM Effect

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1 The RM Effect

2 Our Model

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# Transiting Exoplanets

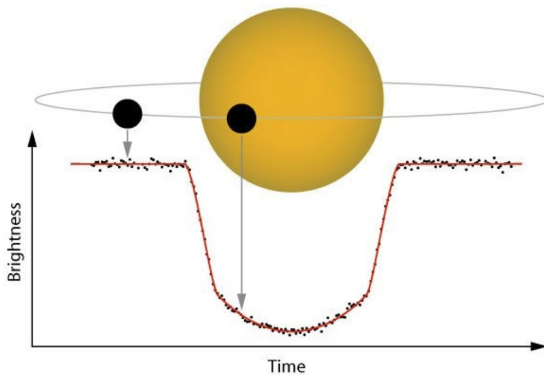


Figure: *Credit ESO*

# Rossiter-McLaughlin Effect

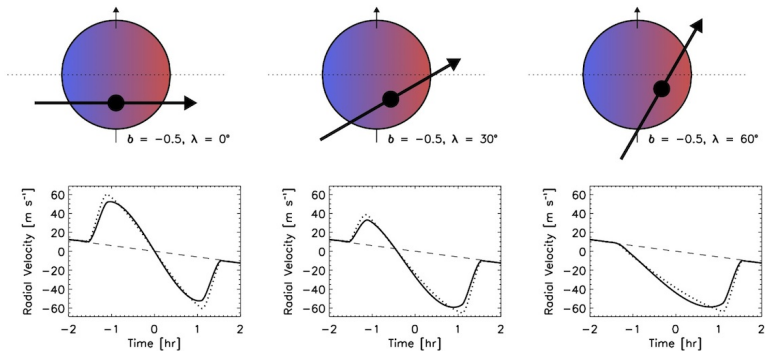


Figure:

<https://wasp-planets.net/tag/rossiter-mclaughlin-effect/>

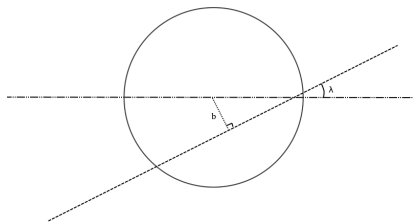
# Our Model - Linear

Planet moves in straight line in front of the star

This path is determined by:

- Projected obliquity
- Impact parameter

This model is not physical



# Keplers Equations

To get  $r(t)$ :

Calculate mean anomaly:

$$M(t) = \sqrt{\frac{G(M_{\star} + M_p)}{a^3}} \cdot (t - t_p).$$

Calculate eccentric anomaly by numerical iteration:

$$E_{n+1} = E_n - \frac{E_n - e \sin(E_n) - M(t)}{1 - e \sin(E - n)}.$$

Calculate true anomaly:

$$\nu(t) = 2 \tan^{-1} \left( \left( \frac{1+e}{1-e} \right)^{1/2} \tan(E(t)/2) \right).$$

Calculate separation:

$$r(t) = a \frac{1 - e^2}{1 + e \cos(\nu(t))}.$$

# Our Model - Physical version

Planet orbits the star.

Keplers equation is solved for input parameters.

The path is determined by:

$a$ ,  $e$ ,  $i$ ,  $\omega$ ,  $M_{\star}$ ,  $M_p$ ,  $t_p$ ,  $\lambda$ ,  $R_p/R_{\star}$   
and  $v \sin(i_{\star})$ .

Much more resource heavy, but  
also correct

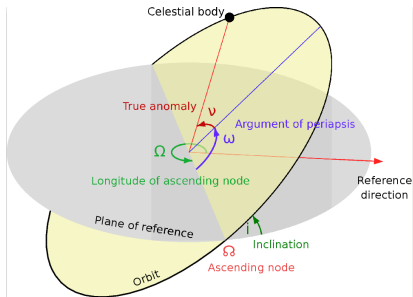


Figure: Credit: Wikipedia user Lassuncty

# Modelling Planet Orbit

Calculate projected coordinates of the planet:

$$\begin{aligned}X_i &= -r \cos(\omega + \nu), \\Y_i &= -r \sin(\omega + \nu) \cos(i).\end{aligned}$$

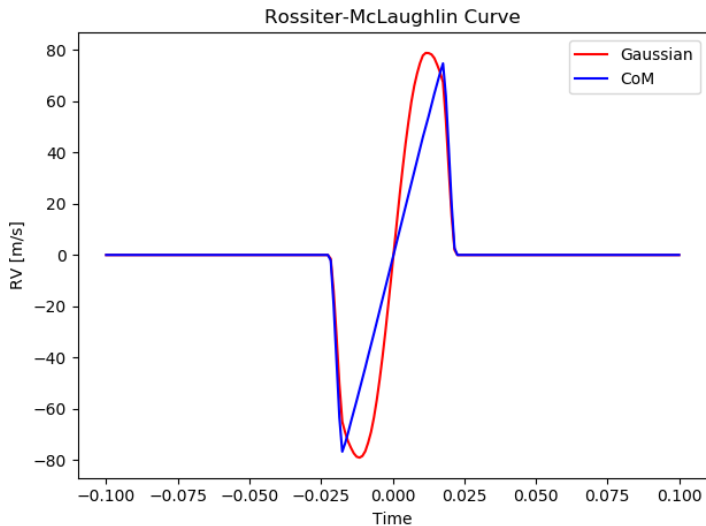
$$\begin{aligned}X &= X_i \cos(\lambda) + Y_i \sin(\lambda), \\Y &= -X_i \sin(\lambda) + Y_i \cos(\lambda), \\Z &= r \sin(\omega + \nu) \sin(i).\end{aligned}$$



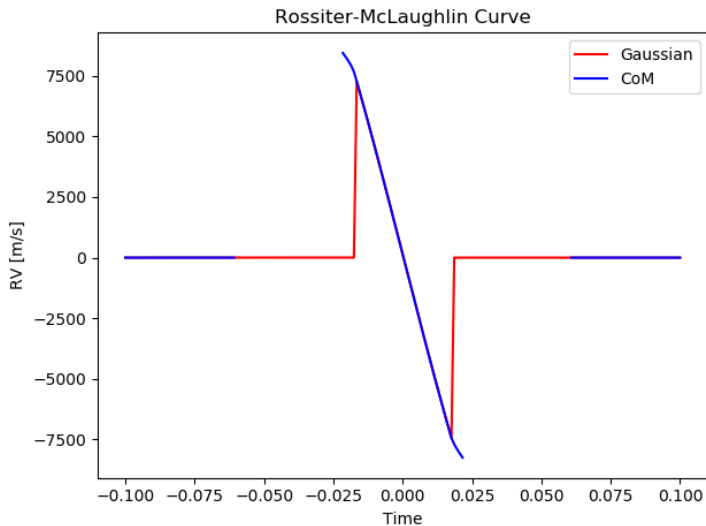
# Our Model - Outputs

[Video here]

# Our Model - Outputs

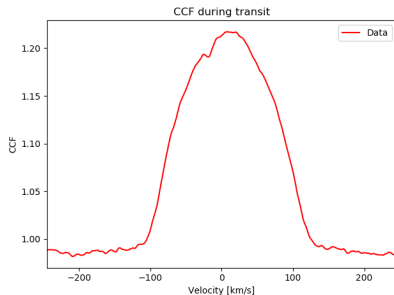


# Our Model - Outputs

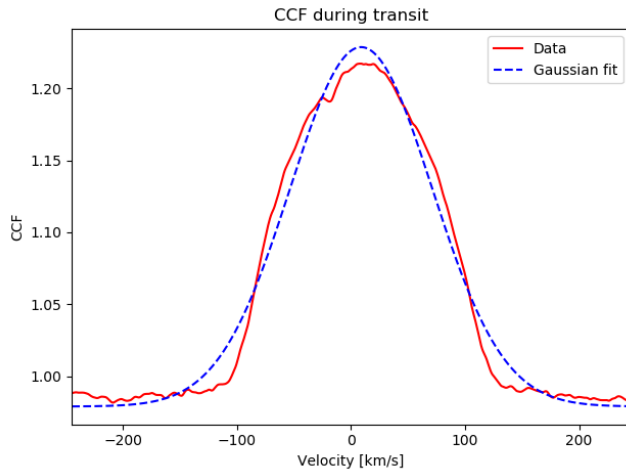


# Data

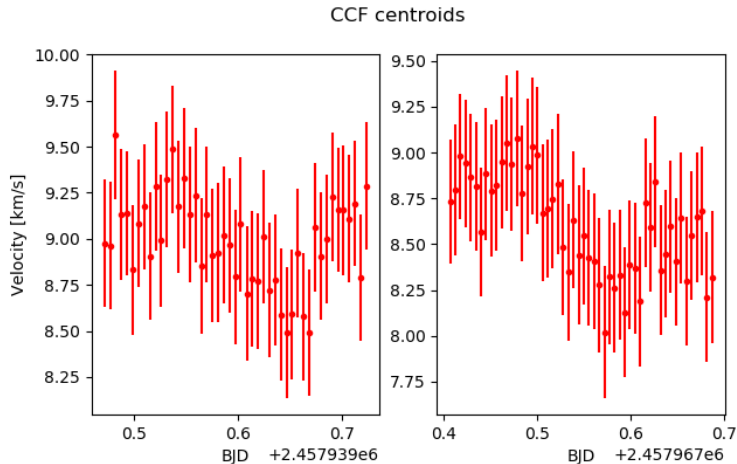
Data is of the star MASCARA-1  
and comes from HARPS.  
Consists of BJD and CCF.



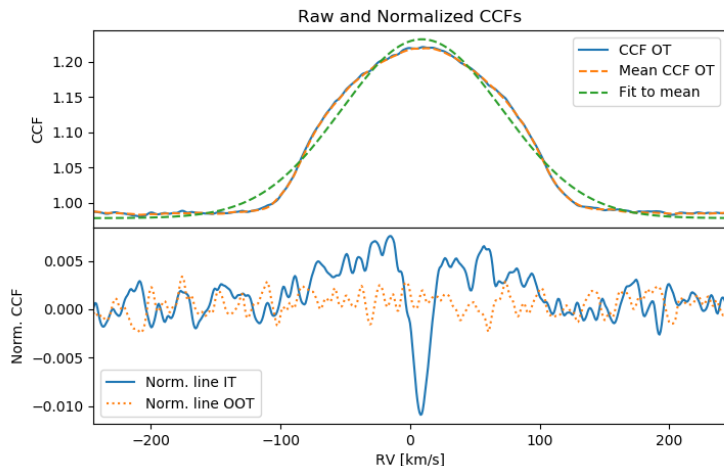
# Data - The stellar line



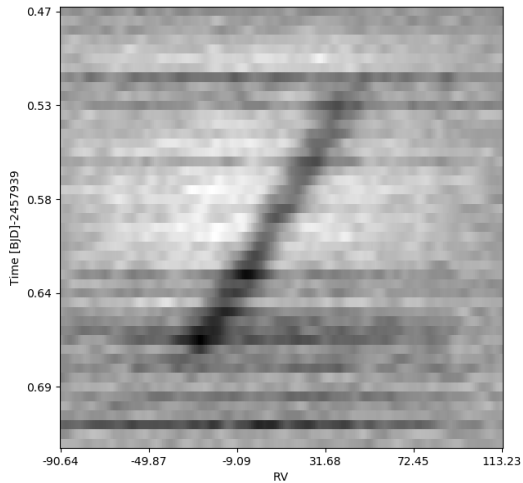
# Data - The Transit



# Data - The 'Planet Line'

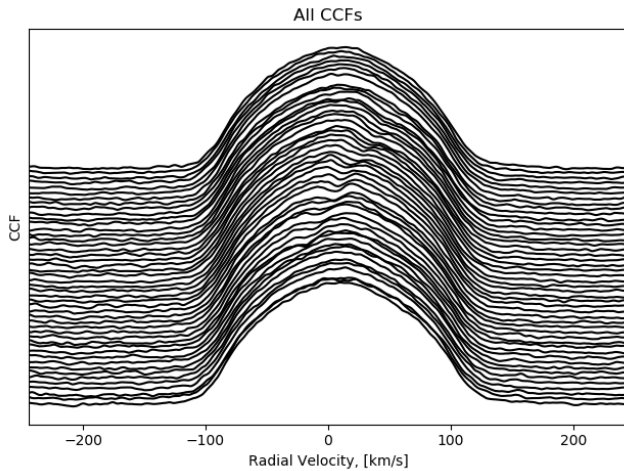


# Data - The RM-effect

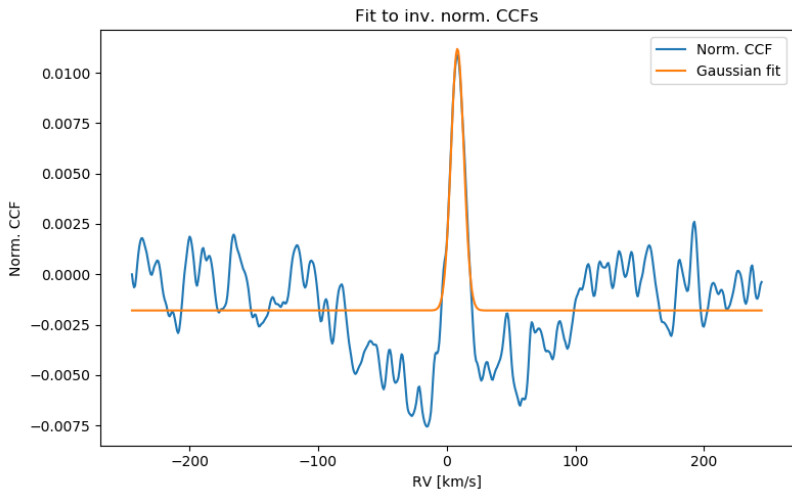




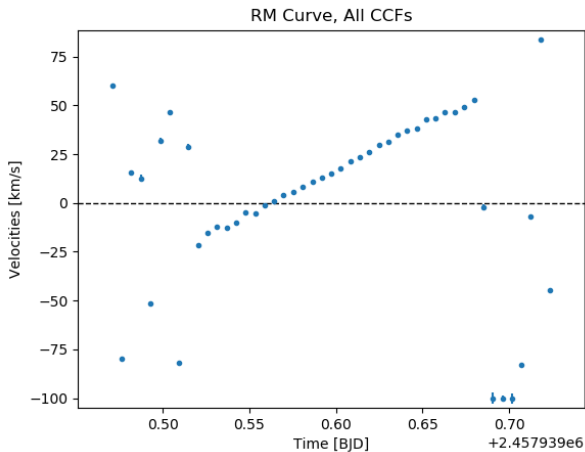
# Data



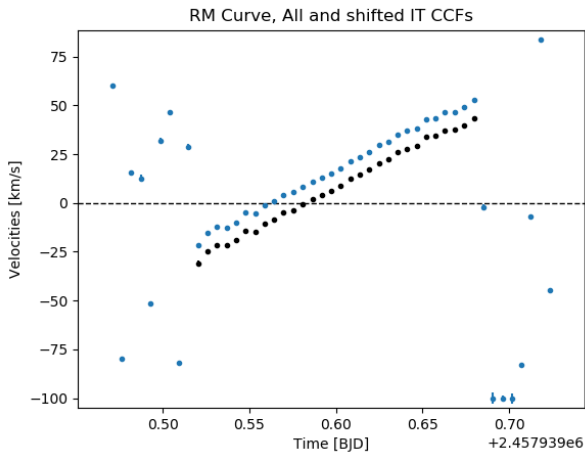
# Data - Fit to CCF



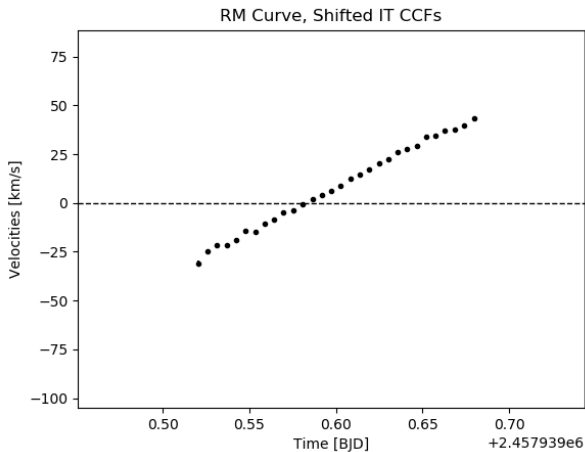
# Data - RM curve



# Data - RM curve



# Data - RM curve



# The Fit - System Parameters

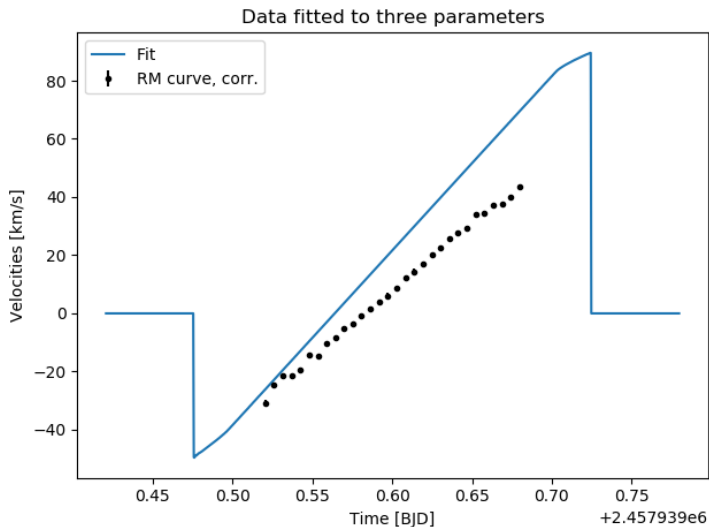
## Variables:

- $\lambda$
- $\omega$
- $v \sin(i_*)$

## Constants:

- $t_p = 0$
- $a = 4.756 R_*$
- $e = 0$
- $M_* = 1.72 M_\odot$
- $M_p = 3.7 M_J$
- $\frac{R_p}{R_*} = 0.0735$
- $\omega = 90^\circ$

# Fitting with curvefit



# Linear fit