Physics Reference

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September 24, 2020

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Introduction

This chapter will offer reference and information that applies to the entire book.

1.1 Standard Units

In physics it's often important to have precisely defined units for the purposes of making very accurate measurements or simply having a coherent unit system. It's possible to derive all necessary units from five measurements of **length**, mass, time, current, and temperature. The standard SI units for these properties are listed bellow:

Type	Unit	Definition		
Length	Meter(m)	Length of distance light in a vacuum travels in $\frac{1}{299792458}$ seconds		
Mass	Kilogram(kg)	Defined by fixing the Planks constant $h = 6.62607015 \times 10^{-34} kg \ m^2 s^{-1}$		
Time	Second(s)	Defined by fixing the ground-state hyperfine transition frequency of the caesium-13:		
		atom, to be $9192631770s^{-1}$		
Current	Ampere(A)	Defined by fixing the charge of an electron as $1.602176634 \times 10^{-19} A \cdot s$		
Temperature	$\operatorname{Kelvin}(K)$	Defined by fixing the value of the Boltzmann constant k to $1.380649 \times 10^{-23} kg \cdot m^2 s^{-2} K^{-1}$		

Common prefixes are listed bellow:

Prefix	Symbol	Definition
mega	M	10^{6}
kilo	k	10^{3}
milli	m	10^{-3}
micro	μ	10^{-6}
nano	n	10^{-9}
pico	p	10^{-12}
femto	f	10^{-15}

Electricity and Magnetism

Law 2.0.1. Maxwells Equations the general laws of electricity and magnetism.

$$\nabla \times \vec{E} = -\vec{B}$$

$$\nabla \times \vec{H} = \vec{J} + \vec{D}$$

$$\nabla \cdot \vec{D} = S$$

$$\nabla \cdot \vec{B} = 0$$

2.1 Electronics

2.1.1 General Components

Definition 2.1.1. Electric Field force per unit charge or N/C

Definition 2.1.2. Voltage or *Potential* is the change in energy per unit charge brought on by traveling through an electric field or J/C or simply V

Remark. The units N/C is equivalent to V/m

Definition 2.1.3. Power can be derived from units of current and voltage for the following formula where P is power(W), V is voltage(V), and I is current(A).

$$P = VI (2.1.1)$$

Law 2.1.1. Ohms Law models the voltage drop across a purely resistive load with the following formula where V is voltage(V), I is current(A), and R is $resistence(\Omega)$.

$$V = IR (2.1.2)$$

Definition 2.1.4. A **Resistor** a device that will produce a voltage drop according to ohms law with a resistance as V/A

Definition 2.1.5. Resistivity(Ω m) is used to calculate how much resistance we expect from a material use the following formula where R is resistence(Ω), ρ is Resistivity(Ω m), l is length(m), and A is cross sectional area(m²).

$$R = \rho \frac{l}{A} \tag{2.1.3}$$

Law 2.1.2. Kirchoff's Voltage Law states precisely that the algebraic sum of all voltages around a closed path is zero.

$$\sum V_n = 0 \tag{2.1.4}$$

Law 2.1.3. Kirchoff's Current Law states precisely that the algebraic sum of all currents entering a node is zero.

$$\sum I_n = 0 \tag{2.1.5}$$

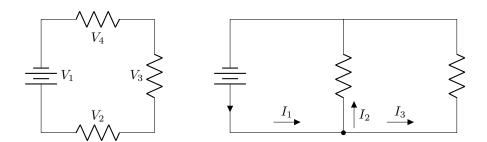


Figure 2.1: Two circuits to demonstrate Krichhoff's Laws

Law 2.1.4. Resistors in Series will simply be the sum of the individual resistance because we are adding the length of the resistors together.

Law 2.1.5. Resistors in Parallel will decrease the overall resistance as indicated by the definition of resistivity 2.1.5.

$$\begin{array}{c}
R_1 \\
R_2 \\
\hline
\frac{1}{R_T} = \sum \frac{1}{R_i}
\end{array} (2.1.7)$$

Definition 2.1.6. Voltage Divider or **Potentiometer** is a arangement of two resistors with a connection between them. A potentiometer refers to a voltage divider where the resistance ratio between the two resistors can be adjusted.

To calculate the voltage we expect at the divider we need to know the voltage across the whole potentiometer V and the ratio between the two resistors $\frac{R_2}{R_1}$.

$$V_{div}$$

$$R_1$$

$$R_2$$

$$V_{div} = V \frac{R_2}{R_1 + R_2}$$

$$(2.1.8)$$

Definition 2.1.7. Ideal Battery - a battery that always produces the same potential difference.

Definition 2.1.8. Real Battery - a battery with some internal resistance that reduces the potential difference across the terminals depending on the amount of current.

$$R_{Internal}$$
 V_{Ideal}
 R_{Load}

$$V_{Real} = V_{Ideal} - IR_{Internal}$$

$$V_{Real} = V_{Ideal} \frac{R_{Load}}{R_{Internal} + R_{Load}} \tag{2.1.9}$$

Definition 2.1.9. Ideal Current Source - a device that always provides that same current to a load.

Definition 2.1.10. Real Current Source - a current source with an internal resistance connected in parallel that reduces the current produced when the load resistance is high.

$$I_{Ideal} \longrightarrow R_{Internal}$$

$$I_{Real} = I_{Ideal} - \frac{V}{R_{Internal}}$$

$$I_{Real} = I_{Ideal} \frac{R_{Internal}}{R_{Internal} + R_{Load}}$$

$$(2.1.10)$$

Definition 2.1.11. A **Capacitor** is a device that accumulates a charge q when a voltage v is applied with a proportionality constant C with units $F(farad) = CV^{-1} = C^2J^{-1}$

$$q = Cv (2.1.11)$$

$$i = C \frac{dv}{dt}$$

$$(2.1.12)$$

Remark. The energy stored in a capacitor can derived by integrating power over time:

$$\omega_C = \frac{1}{2}Cv^2 \tag{2.1.13}$$

Definition 2.1.12. A **Plate Capacitor** is a capacitor made of two conductive plates with area A separated by distance l.

$$C = \frac{\varepsilon_0 \kappa A}{l}$$

Law 2.1.6. Capacitors in Series will decrease the overall capacitance.

Law 2.1.7. Capacitors in Parallel is simply the sum of the individual capacitance.

$$C_1$$

$$C_2$$

$$C_2$$

$$C_3$$

$$C_4$$

$$C_7 = \sum C_i$$

$$(2.1.15)$$

Definition 2.1.13. An **Inductor** is a device which accumulates a magnetic flux $\phi = BA$ when a current is applied with a proportionality constant L with units $H(henry) = J A^{-2}$

$$\phi = Li \tag{2.1.16}$$

$$v = L\frac{di}{dt} \tag{2.1.17}$$

Remark. The energy stored in an inductor can derived by integrating power over time:

$$\omega_L = \frac{1}{2}Li^2 (2.1.18)$$

Law 2.1.8. Inductors in Series is simply the sum of the individual inductance.

$$L_T = \sum_i L_i$$
 (2.1.19)

Law 2.1.9. Inductors in Parallelwill decrease the overall inductance.

$$\frac{L_1}{0000}$$

$$\frac{1}{L_T} = \sum_{i} \frac{1}{L_i}$$
(2.1.20)

2.1.2 RC and RL Circuits

Definition 2.1.14. Charging RC Circuit is a circuit with a resistor, capacitor and voltage source to charge the capacitor. The voltage equation around the loop can be written as

$$V = Ri + \frac{1}{C} \int_{0}^{t} i(\sigma) d\sigma$$

$$i(t) = \frac{V}{R} e^{-t/RC}$$

$$v_{c}(t) = V(1 - e^{-t/RC})$$

$$V = \frac{V}{R}$$

$$C = \frac{V}{R}$$

Figure 2.2: a basic RC circuit in the charging arrangement

Definition 2.1.15. Discharging RC Circuit is a circuit with a capacitor and resistor to discharge the capacitor. The current relation during discharge is symmetric to charge so we can rewrite the equations

$$i(t) = \frac{V}{R}(1 - e^{-t/RC})$$

$$v_c(t) = Ve^{-t/RC}$$

Figure 2.3: a basic RC circuit in the discharging arrangement

Definition 2.1.16. Charging RL Circuit is a circuit with a resistor, inductor and voltage source to charge the inductor.

The current equation can be written as

$$i(t) = \frac{V}{R}(1 - e^{-tR/L})$$
$$v_l(t) = Ve^{-tR/L}$$

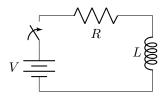


Figure 2.4: a basic RL circuit in the charging arrangement

Definition 2.1.17. Discharging RL Circuit is a circuit with a inductor and resistor to discharge the inductor. The current relation during discharge is symmetric to charging so we can rewrite the equations

$$i(t) = \frac{V}{R}e^{-tR/L}$$

$$v_l(t) = V e^{-tR/L}$$

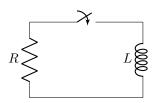


Figure 2.5: a basic RL circuit in the discharging arrangement

2.1.3 AC Circuits

Definition 2.1.18. An AC Voltage source is a voltages source with a alternating voltage. Typically the voltage changes according to the following function:

$$V(t) = V_p \sin(\omega t)$$

Definition 2.1.19. Effective Voltage or **Root Mean Square Voltage** is the voltage $V_p/\sqrt{2}$ where V_p is the peak sinusoidal voltage. This represents the DC voltage that would produce the same power draw as the AC voltage.

Example. Resistor in AC Circuit Bellow is a AC Circuit with a resistor. The current is determined by the following function

$$i(t) = \frac{V_p}{R} \sin \omega t$$



Figure 2.6: a basic AC circuit connected to a resistive load

Definition 2.1.20. Effective Current or **Root Mean Square Current** is the current $I_p/\sqrt{2}$ where I_p is the peak sinusoidal current. This represents the DC current that would produce the same power draw as the AC current.

Example. Capacitor in AC Circuit Bellow is a AC Circuit with a capacitor. The current is determined by the following function

$$i(t) = -\omega C V_p \sin \omega t$$

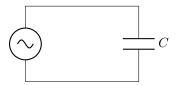


Figure 2.7: a basic AC circuit connected to a capacitive load

Definition 2.1.21. A Phasor Signal is a complex number that we use to represent the output of a wavelike function.

$$Re^{i\theta} = R\cos(\theta) + Ri\sin(\theta)$$

Law 2.1.10. To convert from a phasor signal to the observed signal the following formula applies where x(t) si the observed signal and c is the complex phasor signal.

$$x(t) = Real(c \cdot e^{i\omega t})$$

Law 2.1.11. Generalized Ohm's Law is the complex version of ohm's law that includes complex impedance.

$$\tilde{V} = \tilde{I}Z$$

$$Z = R + iX$$

Where R is circuit resistance and X is circuit reactance.

Thermodynamics

Definition 3.0.1. Thermal Expansion is

Relativity

Theorem 4.0.1. Principle of Relativity states that the laws of physics are the same in all inertial frames. There is no way to detect absolute motion and there is no preferred inertial frame.

Theorem 4.0.2. Constancy of the Speed of Light states that all observers from any inertial frames measure the speed of light as 299792458m/s.

Theorem 4.0.3. Gravitational Equivalence Principle state that inertia mass and gravitational mass are equal.

Definition 4.0.1. Inertia Frames are reference frames where Newtons first law applies.

Law 4.0.1. Lorentz-Fitzgerald's Change of Reference Frame When changing between a reference frame with coordinate x, y, z, t to a reference frame with a relative velocity v in the x direction and coordinates x', y', z', t' the following equations apply:

$$x' = \gamma(x - \beta ct)$$
$$y' = y$$
$$z' = z$$
$$t' = \gamma(t - \beta \frac{x}{c})$$

with β and γ defined as

$$\beta = \frac{v}{c}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

Remark. From this law we can derive an understanding of time dilation and length contraction:

$$T' = \frac{T}{\sqrt{1 - \beta^2}}$$
$$L' = L\sqrt{1 - \beta^2}$$

We can also derive an equation for converting velocities to difference reference frames:

$$U' = \frac{v + U}{1 + \frac{vU}{c^2}}$$

Law 4.0.2. Space-time Interval is the distance than an object travels through space-time.

$$(\Delta s)^2 = (\Delta r)^2 - (c\Delta t)^2 = (x, y, z, ict)$$

The space-time interval will be the same independent to the reference frame.

Definition 4.0.2. Relativistic Doppler Effect is the effect observed from moving sources of waves. Let f_0 be the original frequency, f be the observed frequency, v_{\parallel} be the component of the relative velocity parallel to the observer, and v_{\perp} be the component of the relative velocity away from the observer.

$$f = f_0 \sqrt{1 - \frac{v_{\parallel}^2}{c^2}} \frac{\sqrt{1 - \frac{v_{\perp}}{c}}}{\sqrt{1 + \frac{v_{\perp}}{c}}}$$

Definition 4.0.3. Relativistic Momentum the momentum of an object according to relativity.

$$\rho = \gamma m \vec{v} = \frac{m \vec{v}}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Definition 4.0.4. Relativistic Energy is the energy of objects according to relativity

$$E = \gamma mc^2 = \frac{mc^2}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Definition 4.0.5. Relativistic Energy and Momentum Relations the following equation describes how momentum and energy are related

$$E^{2} = \rho^{2}c^{2} + m^{2}c^{2}$$
$$\frac{\rho}{E} = \frac{\beta}{c}$$

Definition 4.0.6. Relativistic Mass is the mass of objects according to relativity

$$m = \gamma m_0 = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}}$$