Outline of the Course

- 1. The Learning Problem (April 3)
- 2. Is Learning Feasible? (April 5)
- 3. The Linear Model I (April 10)
- 4. Error and Noise (April 12)
- 5. Training versus Testing (April 17)
- 6. Theory of Generalization (April 19)
- 7. The VC Dimension (April 24)
- 8. Bias-Variance Tradeoff (April 26)
- 9. The Linear Model II (May 1)
- 10. Neural Networks (May 3)

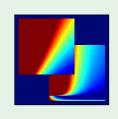
- 11. Overfitting (May 8)
- 12. Regularization (May 10)
- 13. Validation (May 15)
- 14. Support Vector Machines (May 17)
- 15. Kernel Methods (May 22)
- 16. Radial Basis Functions (May 24)
- 17. Three Learning Principles (May 29)
- 18. Epilogue (May 31)
 - theory; mathematical
 - technique; practical
 - analysis; conceptual

Learning From Data

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Lecture 1: The Learning Problem





The learning problem - Outline

- Example of machine learning
- Components of Learning
- A simple model
- Types of learning
- Puzzle

Example: Predicting how a viewer will rate a movie

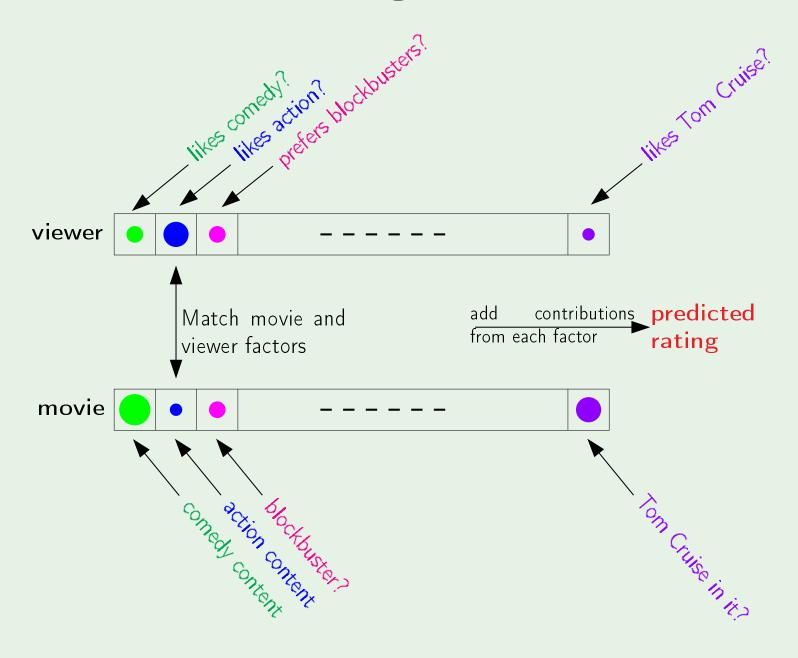
10% improvement = 1 million dollar prize

The essence of machine learning:

- A pattern exists.
- We cannot pin it down mathematically.
- We have data on it.

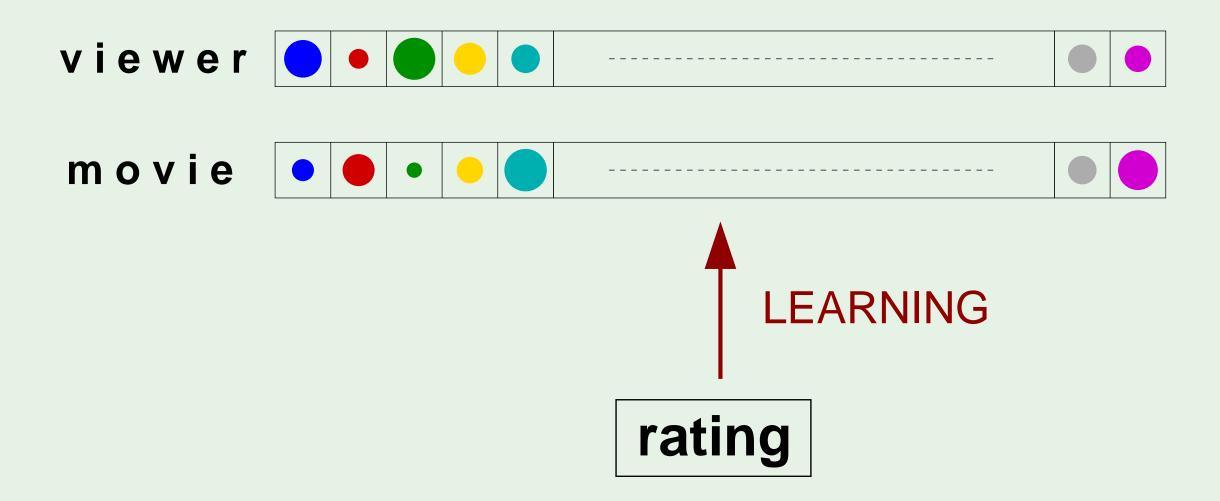
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Movie rating - a solution



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The learning approach



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Components of learning

Metaphor: Credit approval

Applicant information:

age	23 years
gender	male
annual salary	\$30,000
years in residence	1 year
years in job	1 year
current debt	\$15,000
• • •	• • •

Approve credit?

Components of learning

Formalization:

- \bullet Input: \mathbf{x} (customer application)
- Output: y (good/bad customer?)
- ullet Target function: $f:\mathcal{X} o \mathcal{Y}$ (ideal credit approval formula)
- Data: $(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \cdots, (\mathbf{x}_N, y_N)$ (historical records)
 - \downarrow \downarrow
- Hypothesis: $g: \mathcal{X} \to \mathcal{Y}$ (formula to be used)



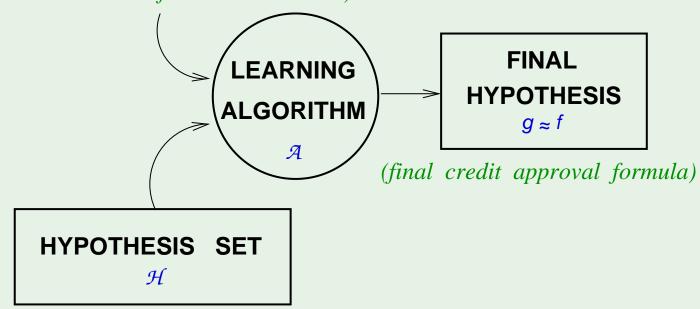
$$f: X \rightarrow \mathcal{Y}$$

(ideal credit approval function)

TRAINING EXAMPLES

$$(\mathbf{x}_{1}, y_{1}), \dots, (\mathbf{x}_{N}, y_{N})$$

(historical records of credit customers)



(set of candidate formulas)

Solution components

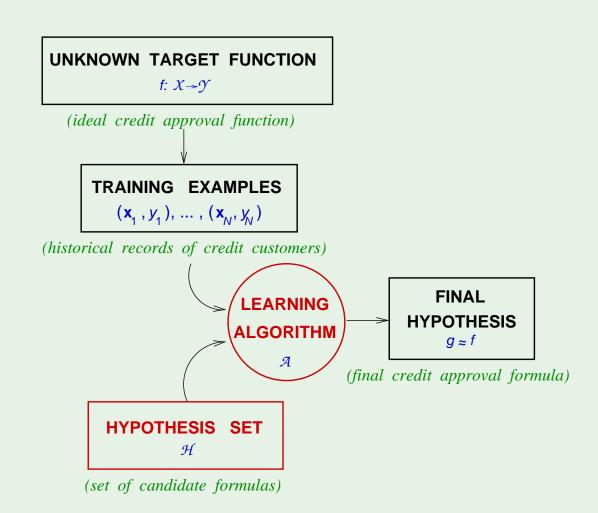
The 2 solution components of the learning problem:

• The Hypothesis Set

$$\mathcal{H} = \{h\} \qquad g \in \mathcal{H}$$

The Learning Algorithm

Together, they are referred to as the *learning* model.



A simple hypothesis set - the 'perceptron'

For input $\mathbf{x}=(x_1,\cdots,x_d)$ 'attributes of a customer'

Approve credit if
$$\sum_{i=1}^d w_i x_i > \mathsf{threshold},$$

Deny credit if
$$\sum_{i=1}^d w_i x_i < \text{threshold.}$$

This linear formula $h \in \mathcal{H}$ can be written as

$$h(\mathbf{x}) = \operatorname{sign}\left(\left(\sum_{i=1}^{d} w_i x_i\right) - \operatorname{threshold}\right)$$

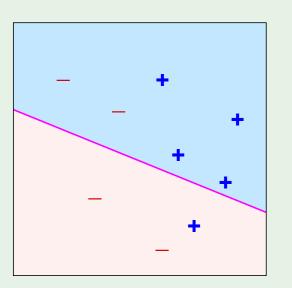
$$h(\mathbf{x}) = \operatorname{sign}\left(\left(\sum_{i=1}^{d} \mathbf{w_i} \ x_i\right) + \mathbf{w_0}\right)$$

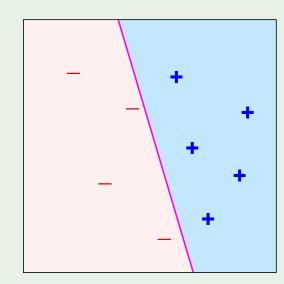
Introduce an artificial coordinate $x_0=1$:

$$h(\mathbf{x}) = \operatorname{sign}\left(\sum_{i=0}^{d} \mathbf{w_i} \ x_i\right)$$

In vector form, the perceptron implements

$$h(\mathbf{x}) = \operatorname{sign}(\mathbf{w}^{\mathsf{T}}\mathbf{x})$$





'linearly separable' data

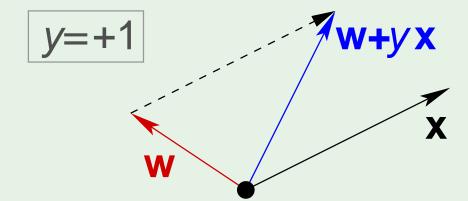
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A simple learning algorithm - PLA

The perceptron implements

$$h(\mathbf{x}) = \operatorname{sign}(\mathbf{w}^{\mathsf{T}}\mathbf{x})$$

A.B = ||A|| ||B|| $\cos\theta$ $\theta = (90,180)$ means negative



Given the training set:

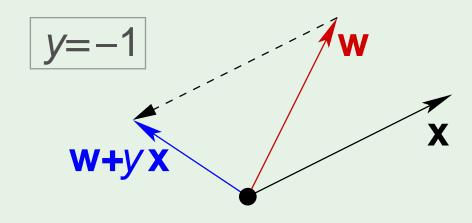
$$(\mathbf{x}_1,y_1),(\mathbf{x}_2,y_2),\cdots,(\mathbf{x}_N,y_N)$$

pick a misclassified point:

$$sign(\mathbf{w}^{\mathsf{T}}\mathbf{x}_n) \neq y_n$$

and update the weight vector:

$$\mathbf{w} \leftarrow \mathbf{w} + y_n \mathbf{x}_n$$



Iterations of PLA

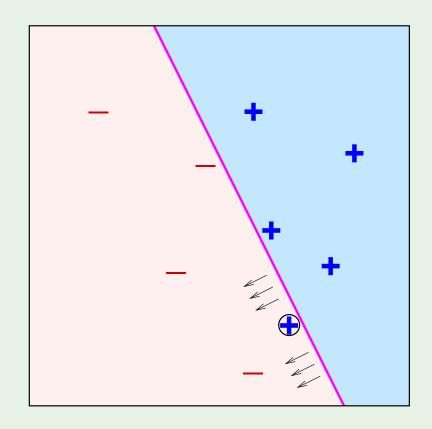
• One iteration of the PLA:

$$\mathbf{w} \leftarrow \mathbf{w} + y\mathbf{x}$$

where (\mathbf{x}, y) is a misclassified training point.

ullet At iteration $t=1,2,3,\cdots$, pick a misclassified point from $(\mathbf{x}_1,y_1),(\mathbf{x}_2,y_2),\cdots,(\mathbf{x}_N,y_N)$

and run a PLA iteration on it.



• That's it!

The learning problem - Outline

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Basic premise of learning

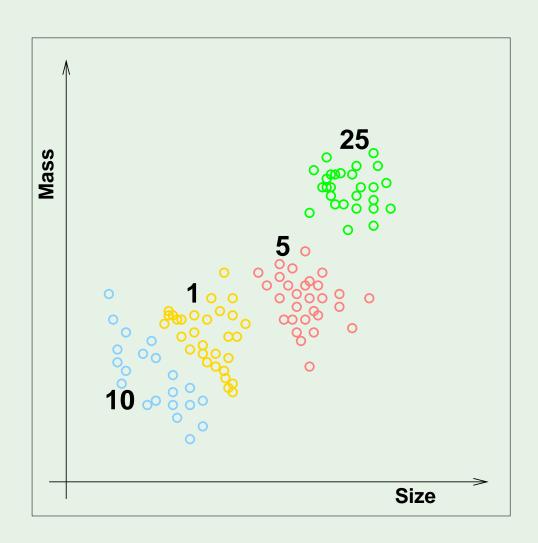
"using a set of observations to uncover an underlying process"

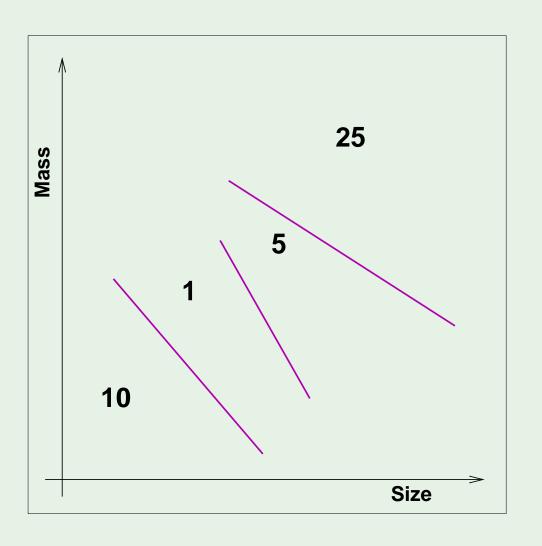
broad premise \implies many variations

- Supervised Learning
- Unsupervised Learning
- Reinforcement Learning

Supervised learning

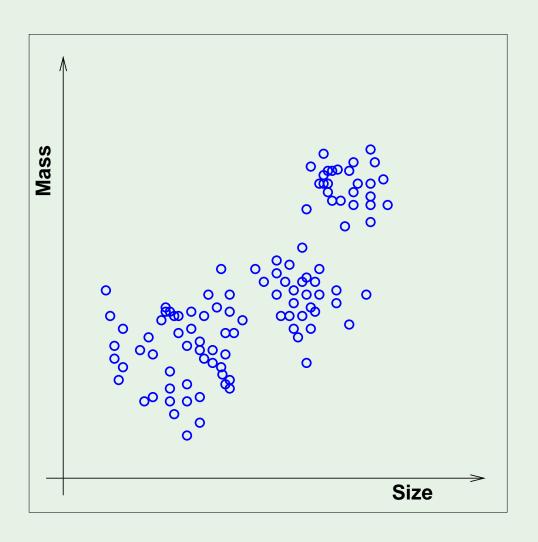
Example from vending machines - coin recognition





Unsupervised learning

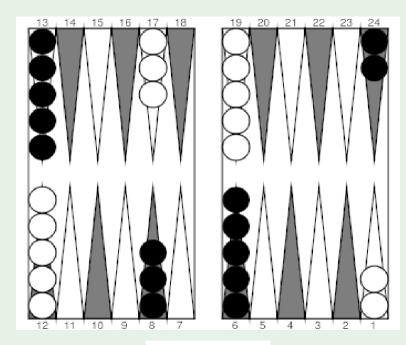
Instead of (input,correct output), we get (input,?)



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Reinforcement learning

Instead of (input,correct output), we get (input,some output,grade for this output)

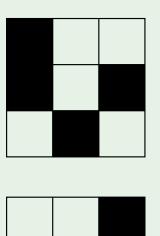


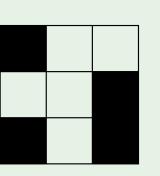
The world champion was a neural network!

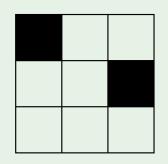


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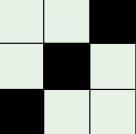
A Learning puzzle

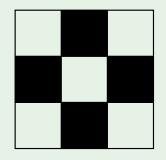


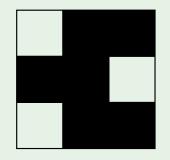




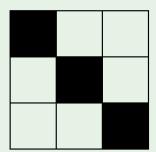
$$f = -1$$







$$f = +1$$



$$f = ?$$