

Today (11/15/15) I finally conceived of a versatile method for describing graphs mathematically, which is outlined below. While it seems simple, getting to this vantage point took a lot of traveling.

Originally I was operating with the layer paradigm but realized it was flawed. Instead, I create the following new paradigm. N is the set of all neurons and N' is the adjacency matrix in which are encoded the weights, if they exist, between each neuron in N . The weight of the connection between N_i and N_{i+n} can be represented by the function $Z(i, n)$. In this way, any graph can be generated and described mathematically.

For example,

The adjacency matrix for a square:

Let X be a directed graph of size l

X' is the adjacency matrix for graph X

$Z(i, n)$ is the weight of the connection from node X_i to node X_{i+n} in X .

$$0 \leq i + n < l$$

$$Z(i, n) = \begin{cases} 1, & \text{if } n = 1 \vee n = l - 1 \\ 0, & \text{otherwise} \end{cases}$$

$$X' = \begin{bmatrix} Z(0, 0) & Z(0, 1) & Z(0, 2) & Z(0, 3) \\ Z(1, -1) & Z(1, 0) & Z(1, 1) & Z(1, 2) \\ Z(2, -2) & Z(2, -1) & Z(2, 0) & Z(2, 1) \\ Z(3, -3) & Z(3, -2) & Z(3, -1) & Z(3, 0) \end{bmatrix}$$

Python code:

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In[1]:

import networkx as nx
import matplotlib.pyplot as plt
import numpy as np

def ngen(z, size):
    a = np.arange(size).reshape([1,size])
    b = np.transpose(a)
    Z = np.vectorize(lambda i,j: z(i, j-i))
    return Z(b,a)

def n_sides_matrix(l):
    z = lambda i,n: 1 if (n==1 or n==(l-1)) else 0
    return ngen(z, l)

G=nx.from_numpy_matrix(n_sides_matrix(4))
nx.draw(G)
```

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plt.show()
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Out[1]:
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