

GENERAL MATHEMATICS 2024

Unit 4 Key Topic Test 3 – Transition Matrices

Recommended writing time*: 45 minutes
Total number of marks available: 25 marks

SOLUTIONS

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SECTION A – Multiple Choice (1 mark per question)

Question 1

Answer: C

from

$$A B$$

to $A \begin{bmatrix} 0.9 & 0.15 \\ 0.1 & 0.85 \end{bmatrix}$

Question 2

Answer: B

$$\begin{bmatrix} 0.9 & 0.15 \\ 0.1 & 0.85 \end{bmatrix}^3 \begin{bmatrix} 100 \\ 100 \end{bmatrix} = \begin{bmatrix} 111.56 \\ 88.44 \end{bmatrix}$$

Question 3

Answer: E

$$100 - (25 + 9) = 66\%$$

Question 4

Answer: A

$$\begin{bmatrix} 0.72 & 0.14 & 0.25 \\ 0.18 & 0.68 & 0.09 \\ 0.1 & 0.18 & 0.66 \end{bmatrix}^{2} \begin{bmatrix} 100 \\ 100 \\ 100 \end{bmatrix} = \begin{bmatrix} 116.72 \\ 93.04 \\ 90.24 \end{bmatrix}$$

$$B = 93$$

Question 5

Answer: E

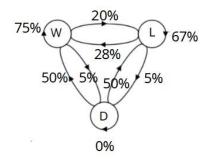
$$\begin{bmatrix} 0.72 & 0.14 & 0.25 \\ 0.18 & 0.68 & 0.09 \\ 0.1 & 0.18 & 0.66 \end{bmatrix}^{\infty} \begin{bmatrix} 100 \\ 100 \\ 100 \end{bmatrix} \approx \begin{bmatrix} 122 \\ 93 \\ 85 \end{bmatrix}$$

C = 85 escooters

SECTION B – Short Answer

Question 1

a.



b.

 $\mathbf{c.} \quad S_0 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{matrix} W \\ L \\ D \end{matrix}$

d.
$$S_1 = TS_0 = \begin{bmatrix} 0.75 \\ 0.2 \\ 0.05 \end{bmatrix}$$

Win=75%

Lose = 20%

Draw = 5%

2 marks

e.
$$S_3 = T^3 S_0$$

$$= \begin{bmatrix} 0.59 \\ 0.36 \\ 0.05 \end{bmatrix}$$

Winning = 59%

2 marks

2 marks

2 marks

1 mark

f. 75% of 4 = 3 teams

1 mark

Question 2

a.
$$m = 100 - 60 - 5 = 35\%$$

 $n = 100 - 70 - 15 = 15\%$
 $p = 100 - 75 - 20 = 5\%$

2 marks

b.
$$S_1 = \begin{bmatrix} 0.75 & 0.15 & 0.35 \\ 0.20 & 0.70 & 0.05 \\ 0.05 & 0.15 & 0.60 \end{bmatrix} S_0$$

$$= \begin{bmatrix} 41 \\ 19.75 \\ 19.25 \end{bmatrix}$$

Yoga = 41 members

2 marks

c.
$$0.75 \times 40 + 0.70 \times 15 + 0.60 \times 25$$

= 55.5
 ≈ 56 members

2 marks

d.
$$S_{20} = S_{21} \approx \begin{bmatrix} 37.5 \\ 27.5 \\ 15 \end{bmatrix}$$

37 in Yoga, 28 in Boxing and 15 in Cardio

2 marks

$$\mathbf{e.} \quad \begin{bmatrix} 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 3 \\ 1 \\ -2 \end{bmatrix} = 2$$

Net effect, 2 members are added each week

1 mark

Net effect, 2 members are added each

f.
$$S_2 = \begin{bmatrix} 0.8 & 0.2 & 0.05 \\ 0.1 & 0.5 & 0.3 \\ 0.1 & 0.3 & 0.65 \end{bmatrix} \begin{bmatrix} 50 \\ 30 \\ 20 \end{bmatrix} + \begin{bmatrix} 3 \\ 1 \\ -2 \end{bmatrix}$$

$$= \begin{bmatrix} 50 \\ 27 \\ 25 \end{bmatrix}$$

1 mark