

Exam on Friday 2pm

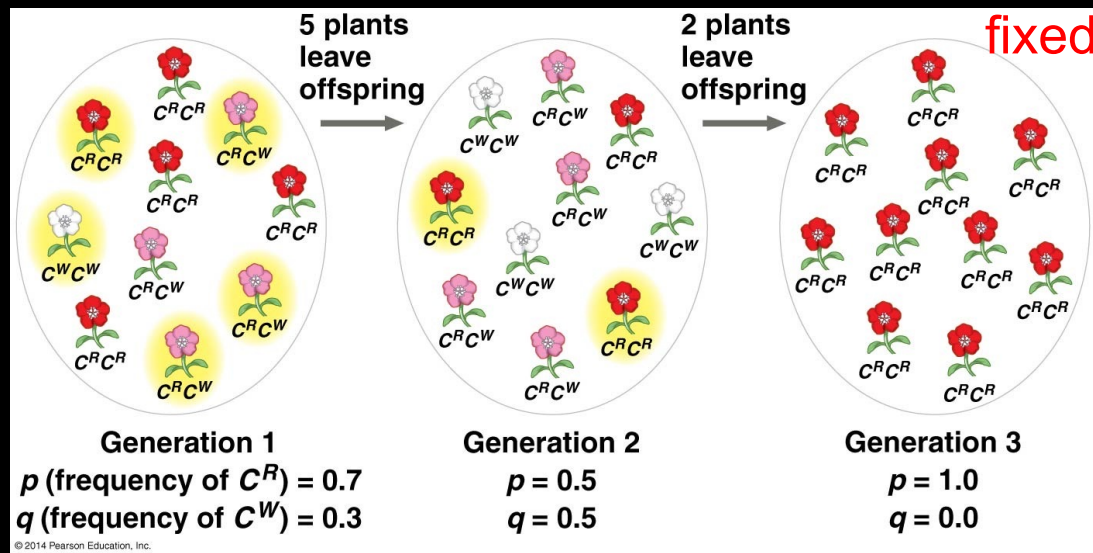
- Bring a pencil and a pen (black or blue)
- student ID (just in case)
- See announcement

Intro to population genetics

- How do alleles and genotypes behave in whole populations?

Gene pool

- A concept denoting the entire genetic makeup of a population i.e. all the alleles present in an interbreeding population
- If only one allele is present, this is allele said to be **fixed** (this can happen by natural selection, or genetic drift)



Intro to population genetics

- **Genotype frequency**: the frequency of individuals with a specific genotype (e.g. homozygous for white C^wC^w)
- **Allele frequency**: the number of copies of one specific allele divided by number of copies of all alleles in that population (for that gene, remember two copies for each individual)
- Allele frequencies in a population; typically denoted by lowercase letters (e.g. alleles C^R , C^w could have allele frequencies p , q)
- If there are only two alleles present, then $p+q = 1$ (100%)
- If there is only one allele for a given locus, then it is said to be **fixed** (e.g. if all individuals are white C^wC^w)

Intro to population genetics

- E.g. a population of 100 plants has two alleles for flower color, C^w and C^R . 10 individuals are homozygous for white, 20 are heterozygous C^wC^R , and 70 are homozygous red.
- Number of white alleles: $(10 \times 2) + (20 \times 1) = 40$. Allele frequency:
 $q = 40 / 2 \times 100 = 0.2$
- Red allele frequency:
 $p = 1 - 0.2 = 0.8$



Intro to the Hardy Weinberg principle



- **Population** = a localized group of interbreeding individuals of the same species
- Hardy and Weinberg studied the allele frequencies in stable populations



Hardy Weinberg principle

- Given a series of assumptions, allele frequencies and genotype frequencies in a population will not change between generations, and genotype frequencies follow a set pattern



$$p^2 + 2pq + q^2 = 1$$

Hardy-Weinberg Equilibrium

If the following **5 assumptions/conditions** are met, the frequency of each allele will remain exactly the same from generation to generation (i.e. no evolution):

1. **No** mutations
2. **No** gene flow
3. **No** natural selection
4. **Random** mating
5. **Large** population

$$p^2 + 2pq + q^2 = 1$$



THE HARDY-WEINBERG EQUATION

		pollen ♂	
		B	b
pistil ♀	B	BB	Bb
	b	Bb	bb

Punnett Square
assuming
complete
dominance

$$p + q = 1$$

p = frequency of the dominant allele in the population

q = frequency of the recessive allele in the population

$$p^2 + 2pq + q^2 = 1$$

p² = freq. of homozygous dominant individuals (genotypes)

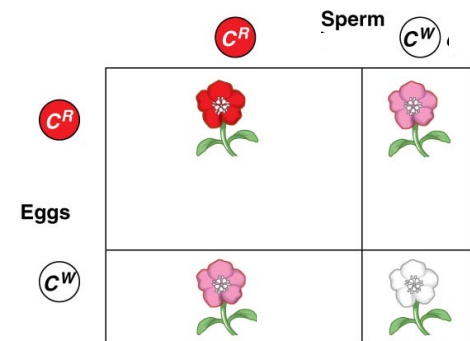
q² = freq. of homozygous recessive individuals (genotypes)

2pq = freq. of heterozygous individuals (genotypes)

Deriving the H-W equation:

Use the Punnett square:

A species of flower occurs in red, pink and white varieties in nature, the alleles for color are all on one locus: what kind of dominance do you think this is?

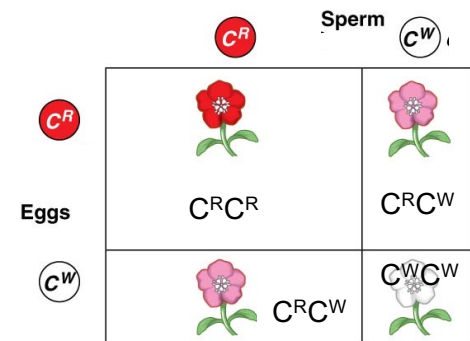


Let's study this example:

A species of flower occurs in red, pink and white varieties in nature:

-Incomplete dominance

1. C^R = allele for red
2. C^W = allele for white
3. $C^R C^W$ genotype will produce pink flowers, $C^R C^R$ red, $C^W C^W$ white.



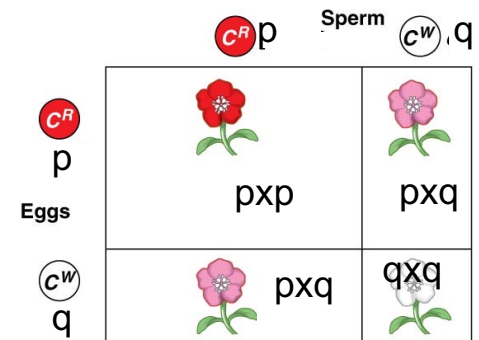
-Note: this is a stable, relatively unchanging population in nature, NOT based on experiments with true breeding etc.

Deriving the H-W equation:

Allele frequencies:

Frequency of $C^R = p$

Frequency of $C^W = q$



Deriving the H-W equation:

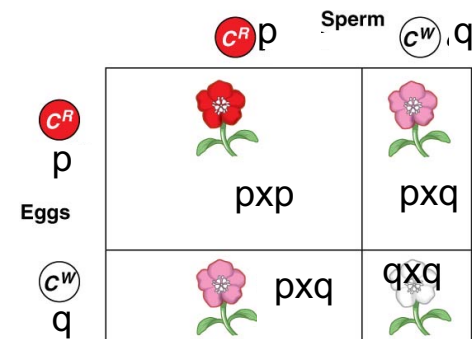
Assume random mating.

Genotype frequencies, based on Punnett square:

Frequency of homozygous dominant genotype = p^2

Frequency of homozygous recessive genotype = q^2

Frequency of heterozygous genotype = $pxq + pxq = 2pq$



Deriving the H-W equation:

Assume random mating.

Genotype frequencies, based on Punnett square:

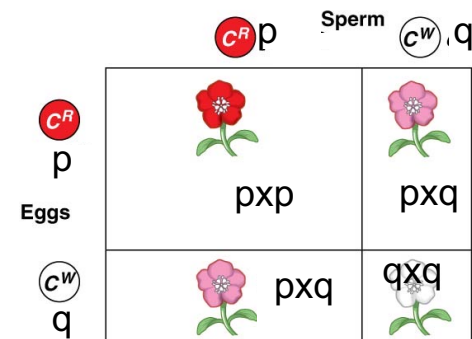
Frequency of homozygous dominant genotype = p^2

Frequency of homozygous recessive genotype = q^2

Frequency of heterozygous genotype = $pxq+pxq= 2pq$




These are all the available genotypes, so they should add up to 1 (=100%)

$$p^2+2pq+q^2 = 1$$



Let's study this example further:

In this case we have 500 individual plants (1000 alleles, remember that each individual has two alleles, when counting allele frequencies):

1. 320 individual flowers are red 
2. 160 are pink 
3. 20 are white 
4. Number of red alleles =
 $(320 \times 2) + (1 \times 160) = 800$
5. Frequency of $C^R = p = 800/1000 = 0.8$
6. Number of white alleles = $1000 - 800 = 200$
7. Frequency of $C^W = q = 200/1000 = 0.2$

Let's study this example:

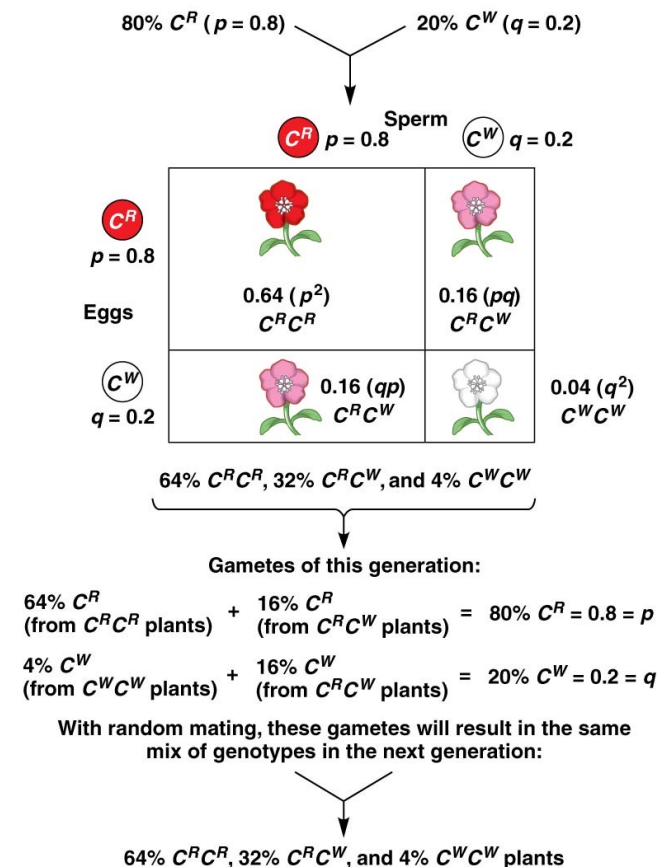
Frequency of genotypes:

1. 320 are red, frequency $320/500 = 0.64$
(same as H-W p^2)
2. 20 are white, frequency $20/500 = 0.04$
(same as H-W q^2)
3. 160 are pink = $160/500 = 0.32$ (same as
H-W $2pq$)

All genotype frequencies should add up to one:

$$0.64 + 0.32 + 0.04 = p^2 + 2pq + q^2 = 1$$

Conclusion: The population is in Hardy Weinberg equilibrium



Don't forget the easy solutions

$$p+q = 1$$

$q = \sqrt{q^2}$ = sq.root of frequency of homozygous recessive genotype.

E.g. eye color:

B = brown (dom.)

b = blue (rec.)

You are told that the frequency (q) of blue eyed (bb) people is 0.25. What is the frequency of the recessive allele (assuming H-W)?

$$p^2 + 2pq + q^2 = 1$$

A simple example....

- Imagine a population made up of 100 individuals, assume H-W equilibrium: A is dominant, a is recessive.
- 4 individuals show the recessive trait
- The allele frequency of A is?
- The allele frequency of a is?

A simple example....

- Imagine a population made up of 100 individuals, assume H-W equilibrium: A is dominant, a is recessive.
- 4 individuals show the recessive trait
- The allele frequency of A is? 0.8
- The allele frequency of a is? 0.2

So what?

- H-W forms the basis of microevolutionary studies
- It serves as a null model: if a population does not conform to the equilibrium equation, we can look at which assumptions are violated (i.e., which evolutionary forces are acting)
- The Hardy-Weinberg Principle can be used to test whether a population is evolving