



# ADJACENT BIT COUNT

0 1 1 0 1 1 0 1

$$0 + 1 + 1 + 0 + 0 + 1 + 0 + 0 = 3$$

$$X_1 * X_2 + X_2 * X_3 + \dots + X_{n-1} * X_n$$

$n, k \leftarrow \text{input}$

$n \leq 100$   
 $t \leq 10^3 \rightarrow \text{iterations}$

Return how many bit string of length  $n$  you can make such that the adj BC is  $k$ .

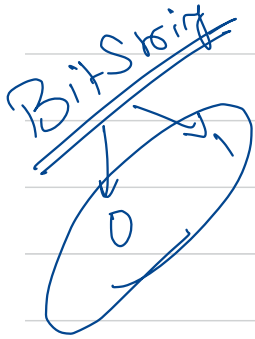
$n = 5$   
 $k = 2 \rightarrow 6$

1100  
 0110  
 0011  
 1011  
 1101  
 1101

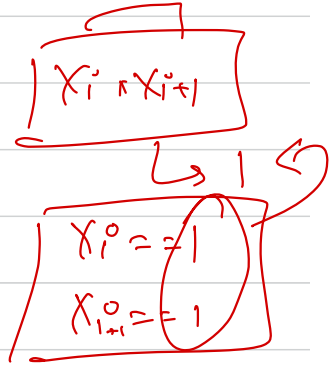
6 string of length  $n=5$   
 with adj BC =  $k(2)$

→ Counting Problem → Count the total no. of strings of length  $n$ , and AdjBitCount =  $k$

bits at adjacent  
↑  
indices



0th index

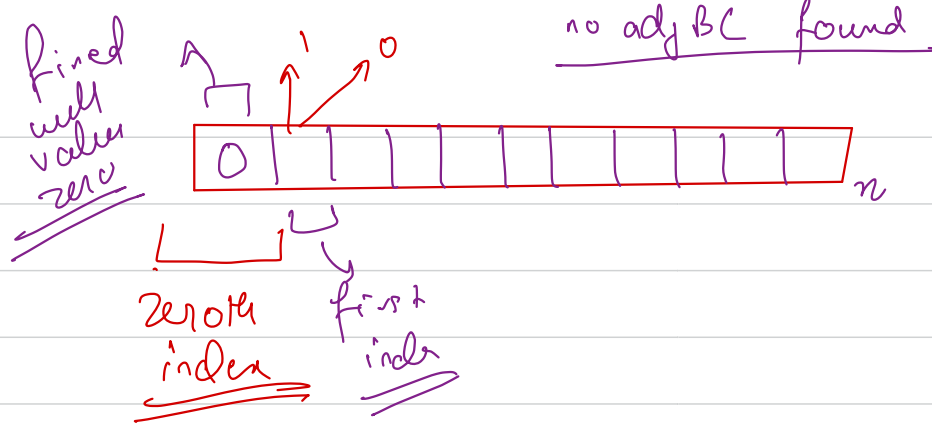


$$0 \times 1 = 0$$

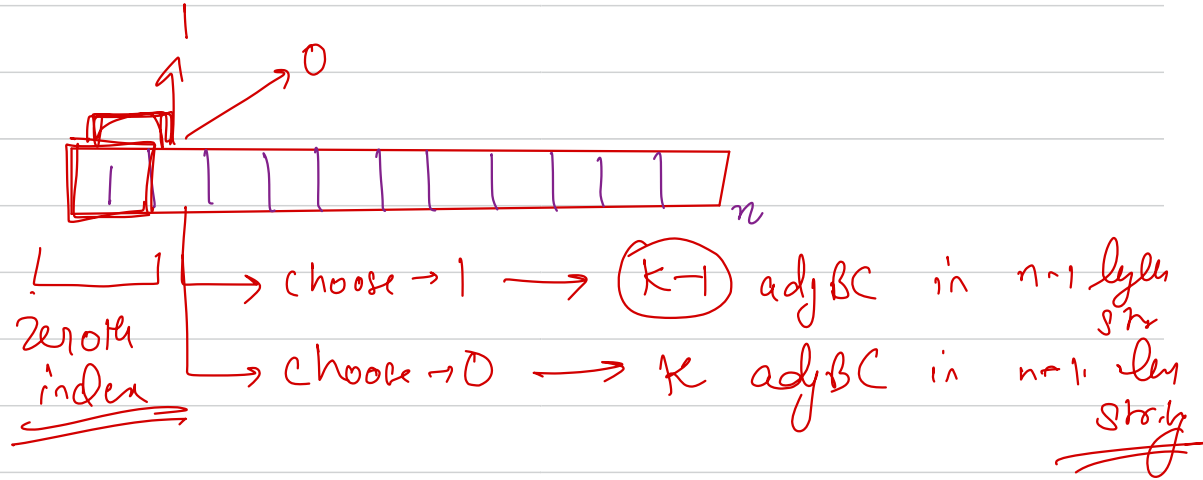
$$0 \times 0 = 0$$

$$1 \times 0 = 0$$

Case 1



Case 2



→ that if zeroth char is 0, and we were finding  
all string with  $adjBC = k$  & length  $n$ , now I need  
to find all strings with  $adjBC = k$  & length  $= n-1$

$$f(n, \underline{k}, 0) = f(n-1, \underline{k}, 0) + f(n-1, k, 1)$$

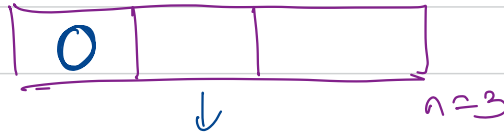
func<sup>n</sup> that returns  
 the no. of strings  
 with adj BC =  $k$ ,  
 length  $n$  and  
 starting from 0.

(assume this works)  
fine

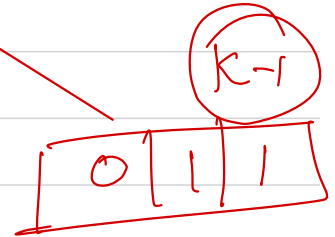
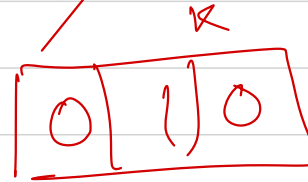
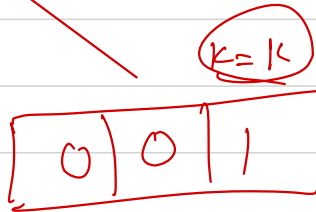
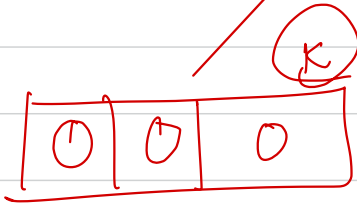
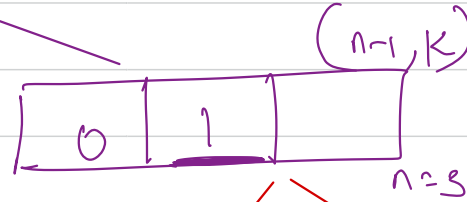
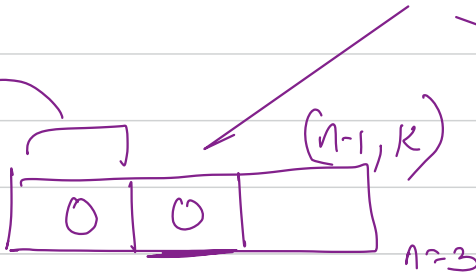
$K=1$

$n=3$


Case I



Contribution of the changes is included



$$f(n, k, 1) = f(n-1, k-1, 1) + f(n-1, k, 0)$$

fnc returns  
count of all  
strings of len = n  
and adj BC = k  
Starting with 1

$f(n, k, \text{first})$

$n \rightarrow$  len of str.'g

$k \rightarrow$  adj BC reqd

$\text{first} \rightarrow$  the zeroth char  
of  $n$  length str.'g  
which we call

first



optimal  $\rightarrow$  most favourable

$\rightarrow$  at max 3D array

$$f(n, k, first) =$$

Bigger problem

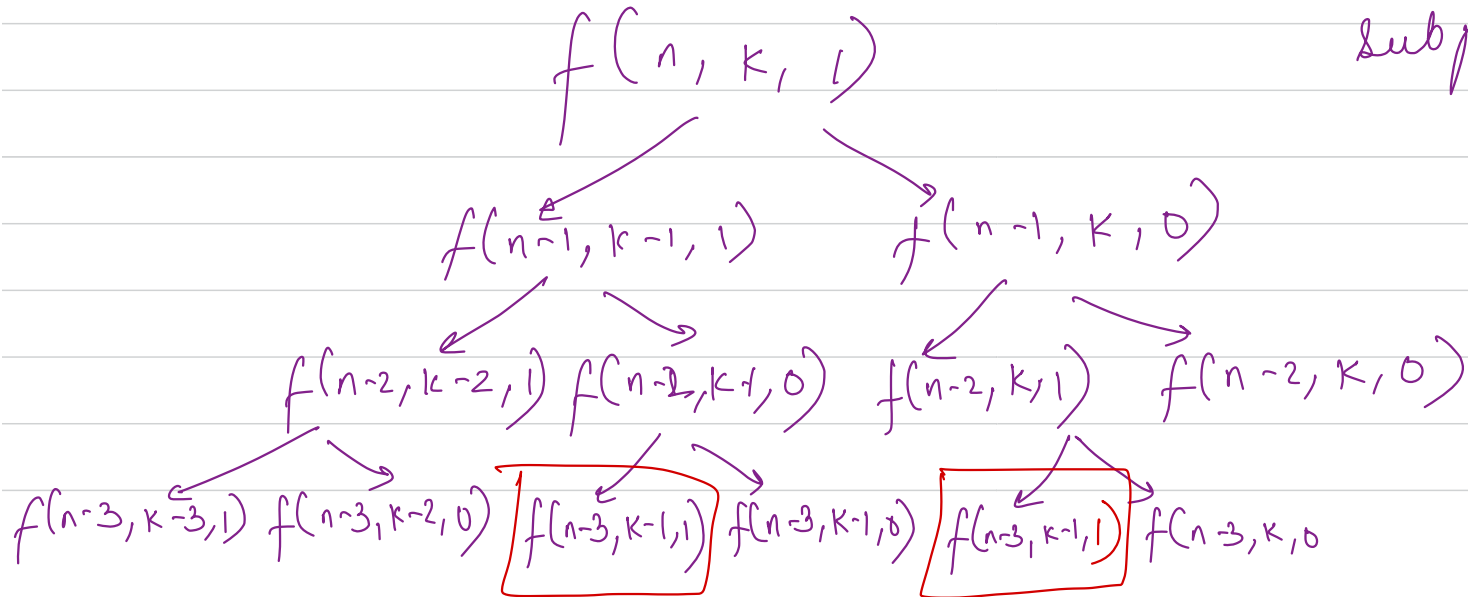
recurrence  
relation

$$\left\{ \begin{array}{l} f(n-1, k, 1) + f(n-1, k, 0) \quad \text{if } first == 0 \\ \hline \text{smaller subproblems} \\ \hline f(n-1, k-1, 1) + f(n-1, k, 0) \quad \text{if } first == 1 \end{array} \right.$$

How many parameters are reqd to uniquely identify  
a subproblem ??  $\Rightarrow$  3  $\rightarrow$  max dimension of space  
reqd

if we have previously computed any subproblem,  
and we encounter it again, then how about  
save it some where.

1) overlapping  
subproblem



2) Optimal Substructure  $\Rightarrow$  If we have optimal ans for a smaller subproblem and they also

contribute optimally to generate ans of bigger problem then it shows optimal substructure

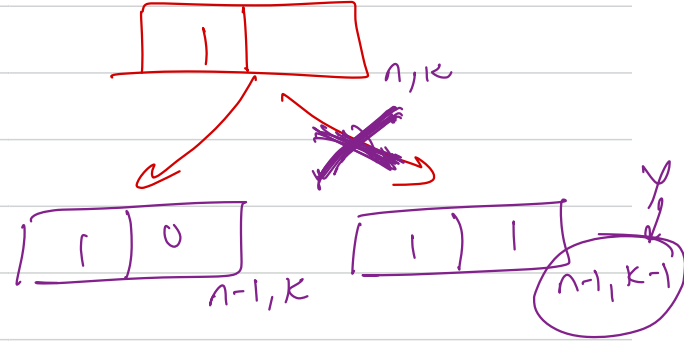
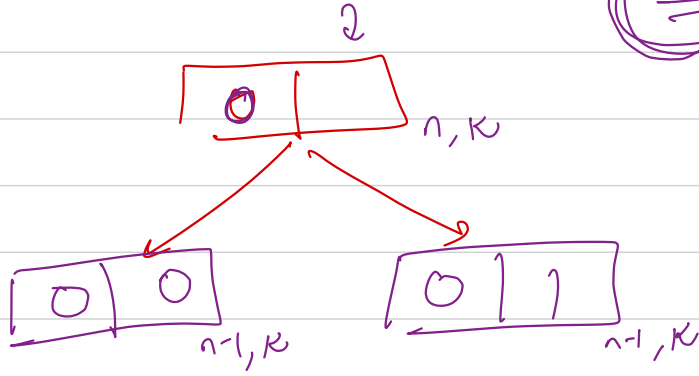
Store common/repeating/overlapping subproblem.

array  $\rightarrow$  dimensions

$$f(n) = f(n-1) + f(n-2)$$

at max  $\rightarrow$  1D array

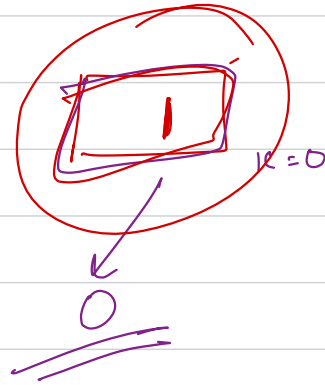
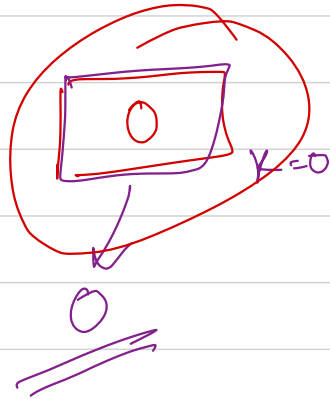
$n=2$   $K=0$



one length  
string



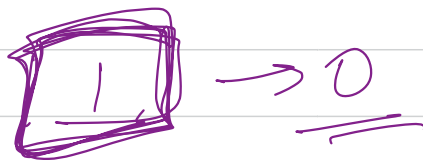
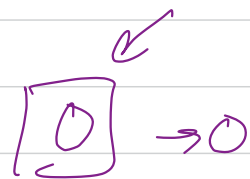
xxxxxx



one length string



$K=0$



1D, 2D, 3D, Probability, Expectation, Symmetric tree, Binary  
search, Combinatorics, Convex hulls etc.

DP with Bitmasking, tree dp

Q.1

Count the no. of binary strings of length  $n$ , such that they don't have any consecutive

ones.

$n=3$   
ans  $\rightarrow 5$

$n=2 \rightarrow$   
 $\downarrow$   
3

0	0
1	0
0	1

$n=1 \rightarrow$   
 $\downarrow$   
2

0
1

$n=4 \rightarrow$   
 $\downarrow$   
8

0	0	0	0
0	0	0	1
0	0	1	0
0	1	0	0
1	0	0	0
1	0	0	1
1	0	1	0

0 0 0  
0 0 1  
0 1 0  
1 0 0  
1 0 1

$n=1 \rightarrow 2$   
 $n=2 \rightarrow 3$   
 $n=3 \rightarrow 5$   
 $n=4 \rightarrow 8$

Fibonacci

0 1 0 1

$$f(n) = f(n-1) + f(n-2)$$



@i san ket Singh