

# CS 481

## *Artificial Intelligence Language Understanding*

March 21, 2023

# Announcements / Reminders

- Enjoy your Spring Break!
- Please follow the Week 09 To Do List instructions
- Written Assignment #03 is due on Sunday 03/26/23 at 11:59 PM CST
- Quiz due on Sunday 03/26/23 at 11:59 PM CST
- Programming Assignment #02 is due on Sunday 04/02/23 at 11:59 PM CST
- Exam dates:
  - Final: 04/27/2023 during Thursday lecture time

# Plan for Today

- Logistic Regression
- Sentiment Analysis
- Words and their meaning

# Text Classification: Supervised ML

- Various Machine Learning supervised learning classifier approaches can be employed:
  - Naïve Bayes
  - Logistic regression
  - Neural networks
  - k-Nearest Neighbors
  - etc.

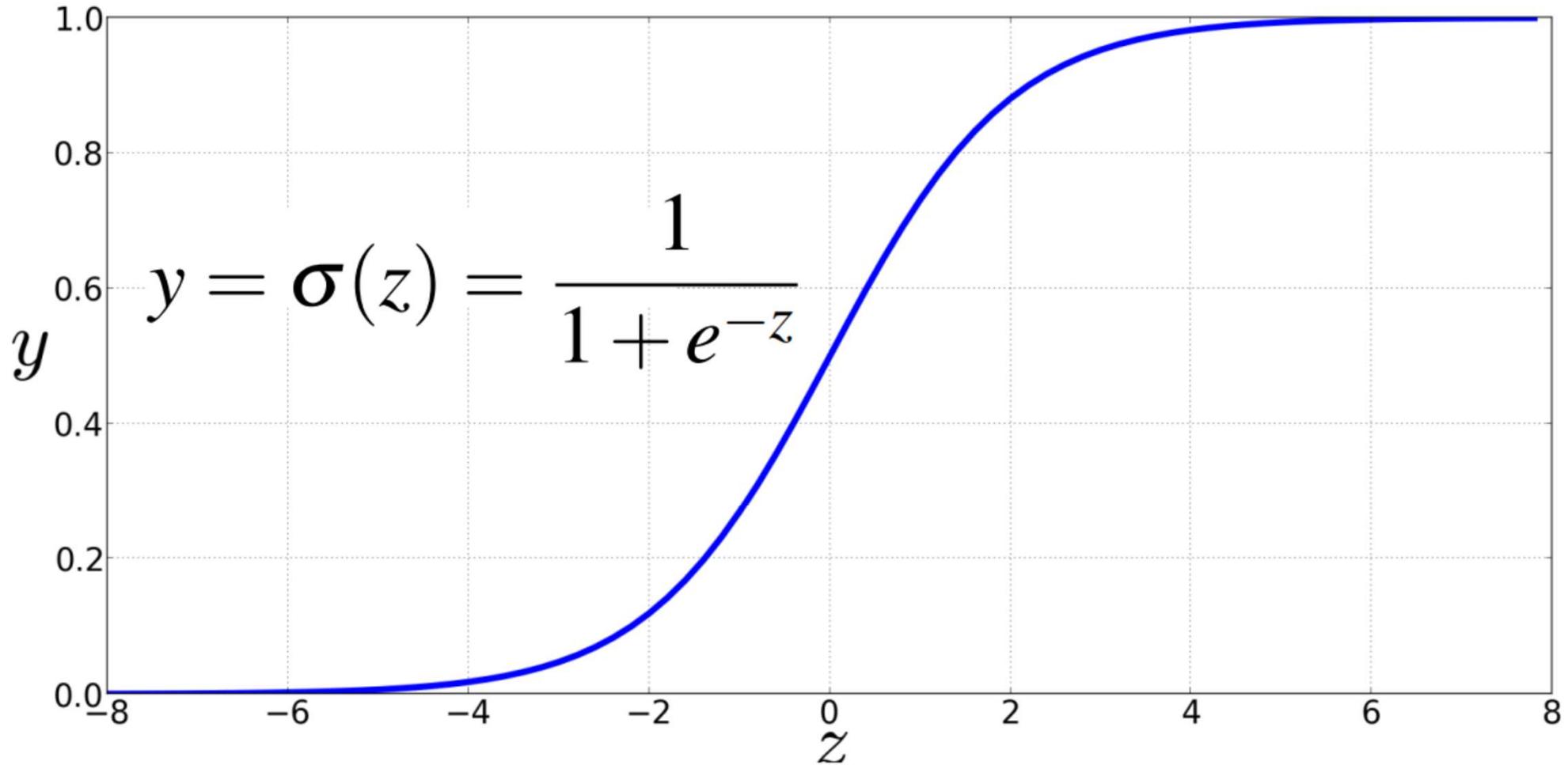
# Logistic Regression: The Idea

- Compute  $w \cdot x + b$  for observation / sample  $x$
- Pass it through the sigmoid function:

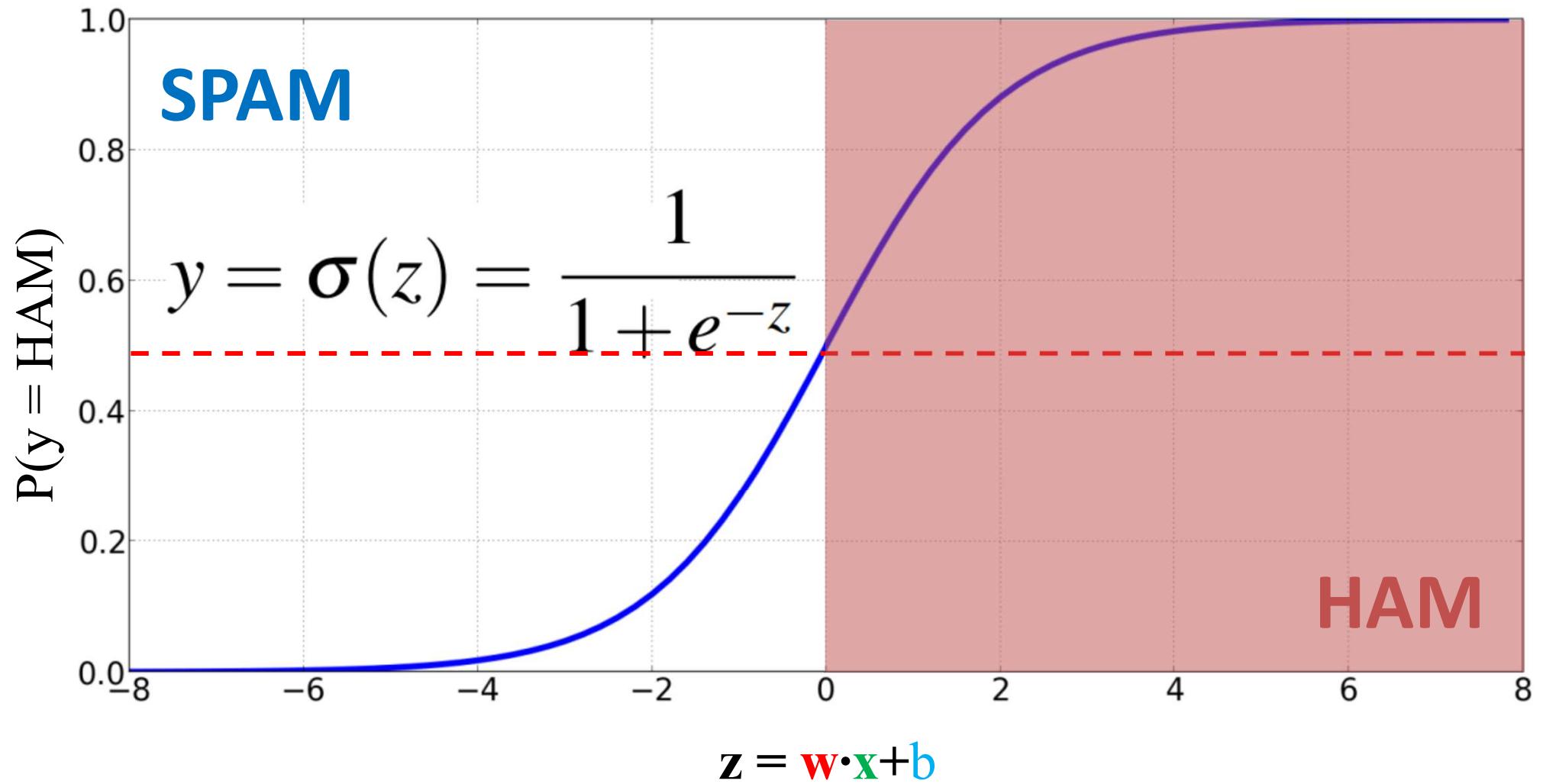
$$\sigma(w \cdot x + b)$$

- Treat the result as probability

# Sigmoid / Logistic Function



# Logistic Regression Classifier



# Probabilities → Classification

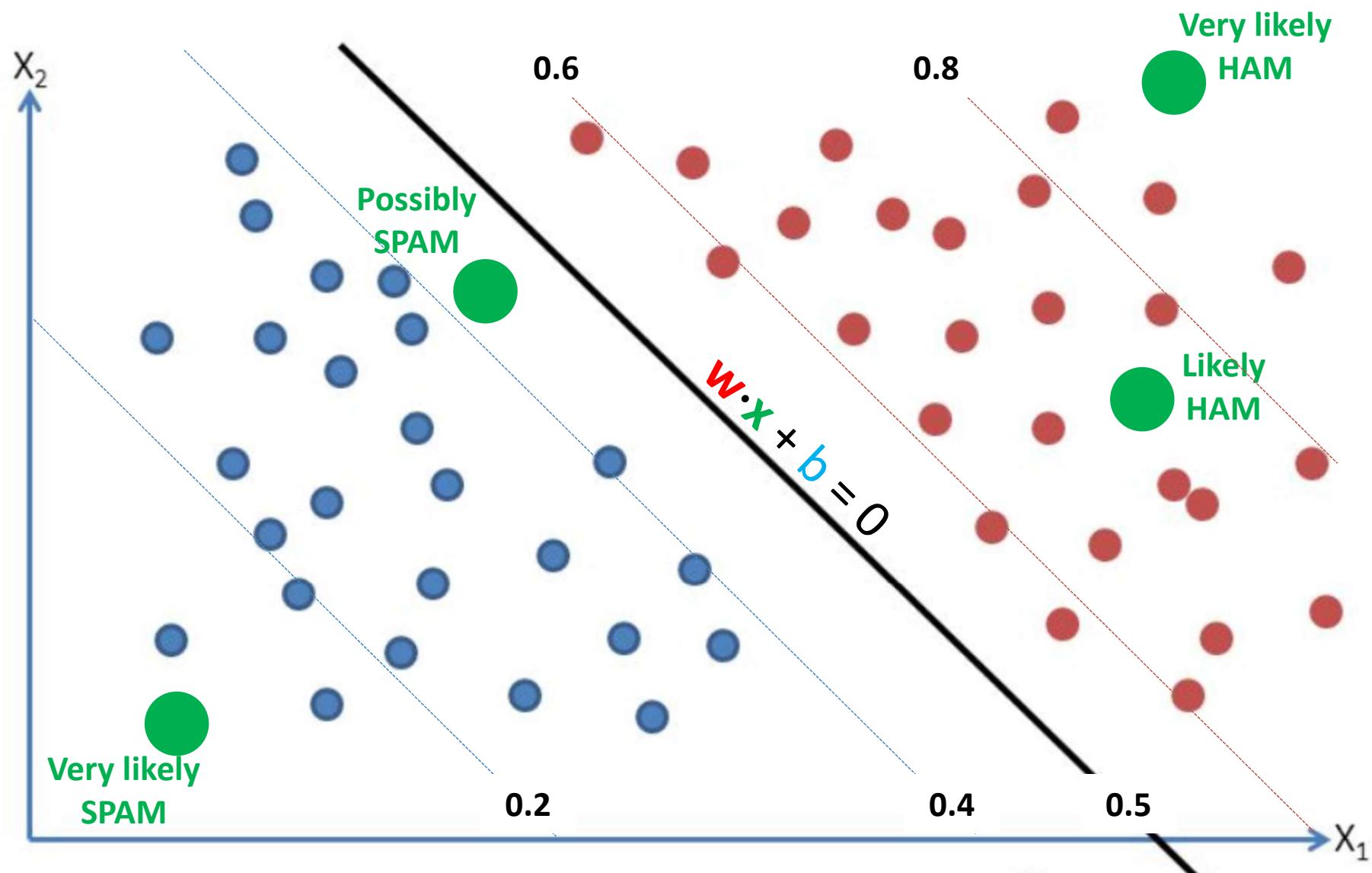
Once we know the probability, we can use it to classify:

$$\hat{y} = \begin{cases} 1 & \text{if } P(y=1|x) > 0.5 \\ 0 & \text{otherwise} \end{cases}$$

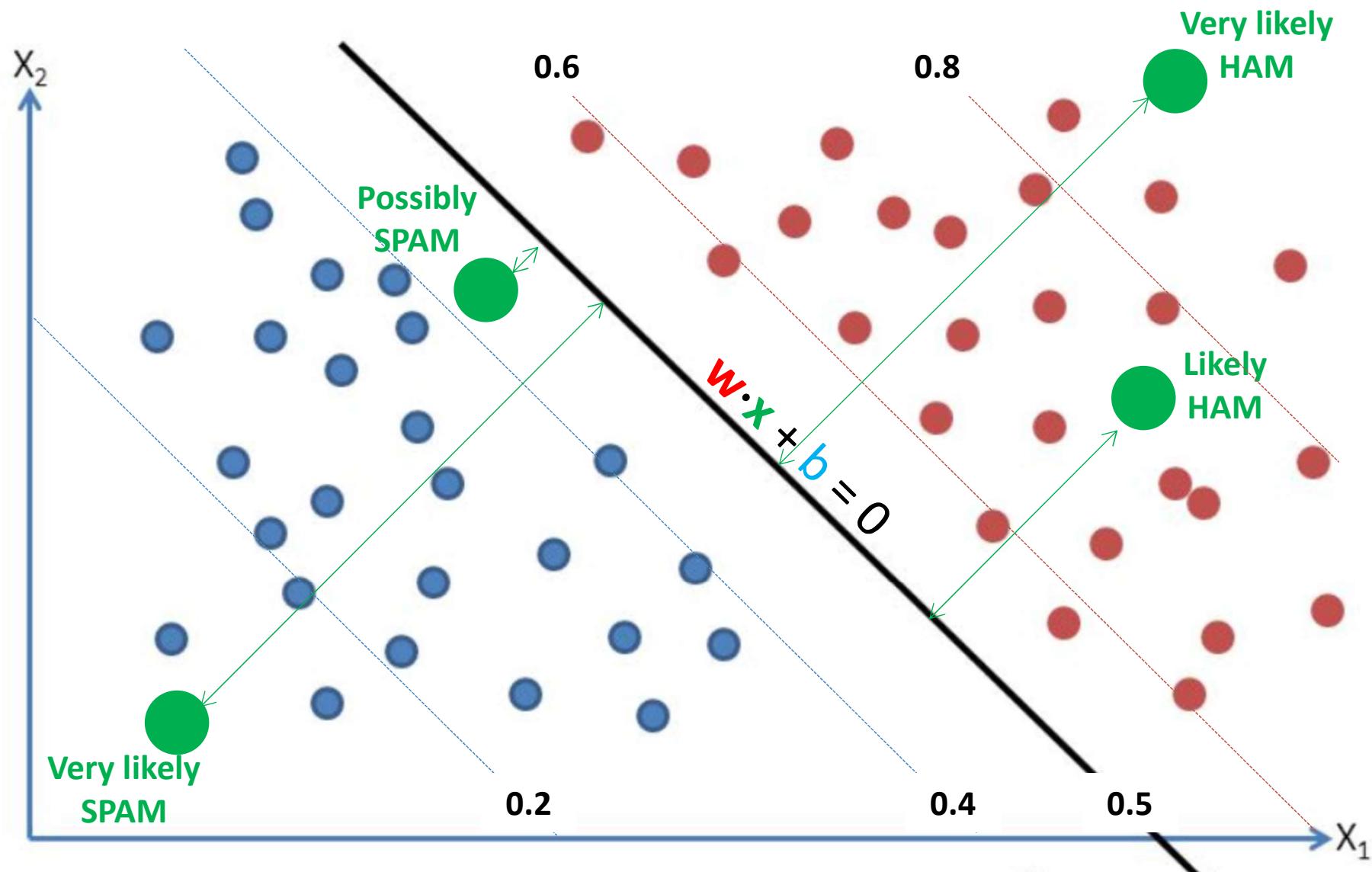
if  $w \cdot x + b > 0$   
if  $w \cdot x + b \leq 0$

Where 0.5 is the **decision boundary**

# Text Classification: Separator



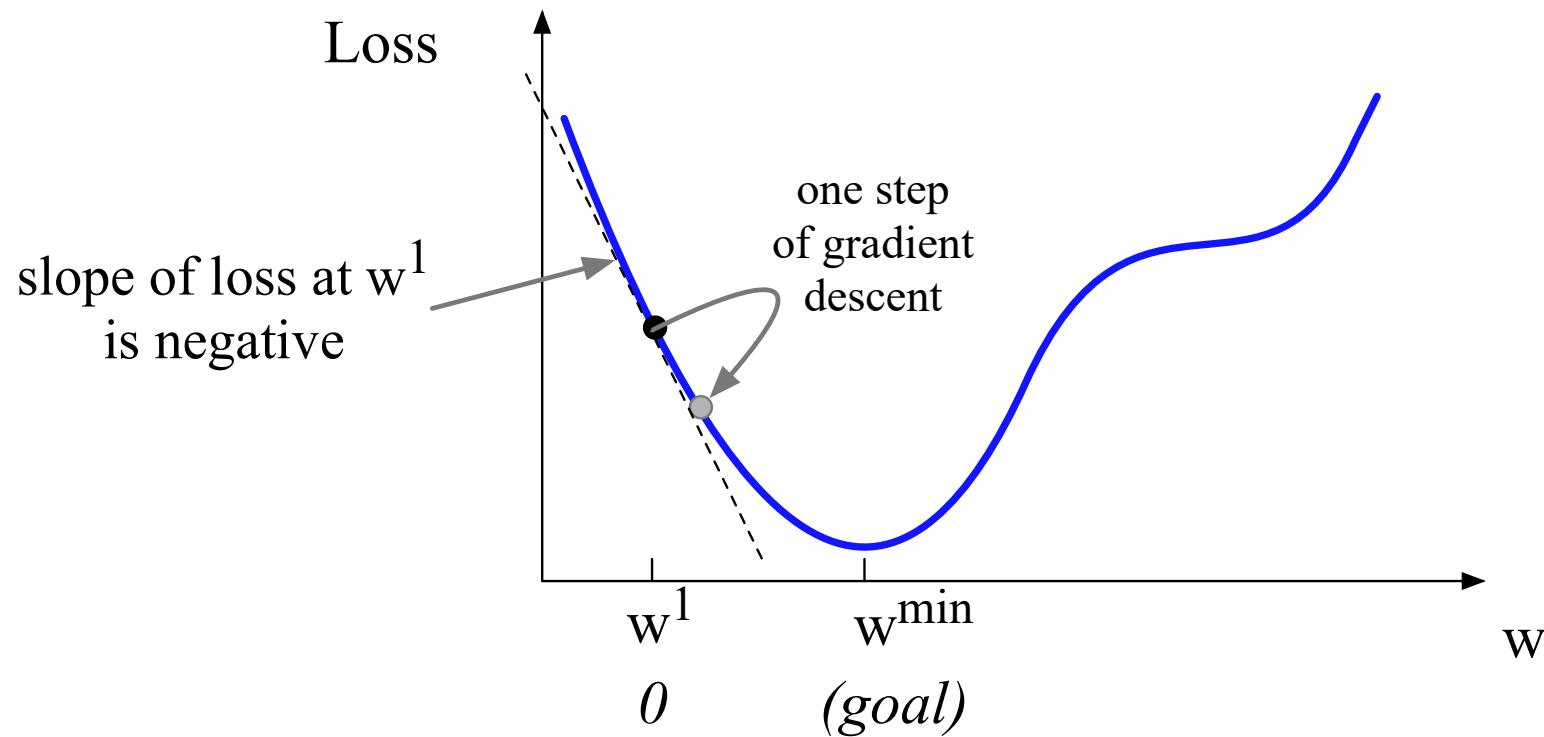
# Text Classification: Separator



# Minimizing Loss

Q: Given current  $w$ , should we make it bigger or smaller?

A: Move  $w$  in the reverse direction from the slope of the loss function



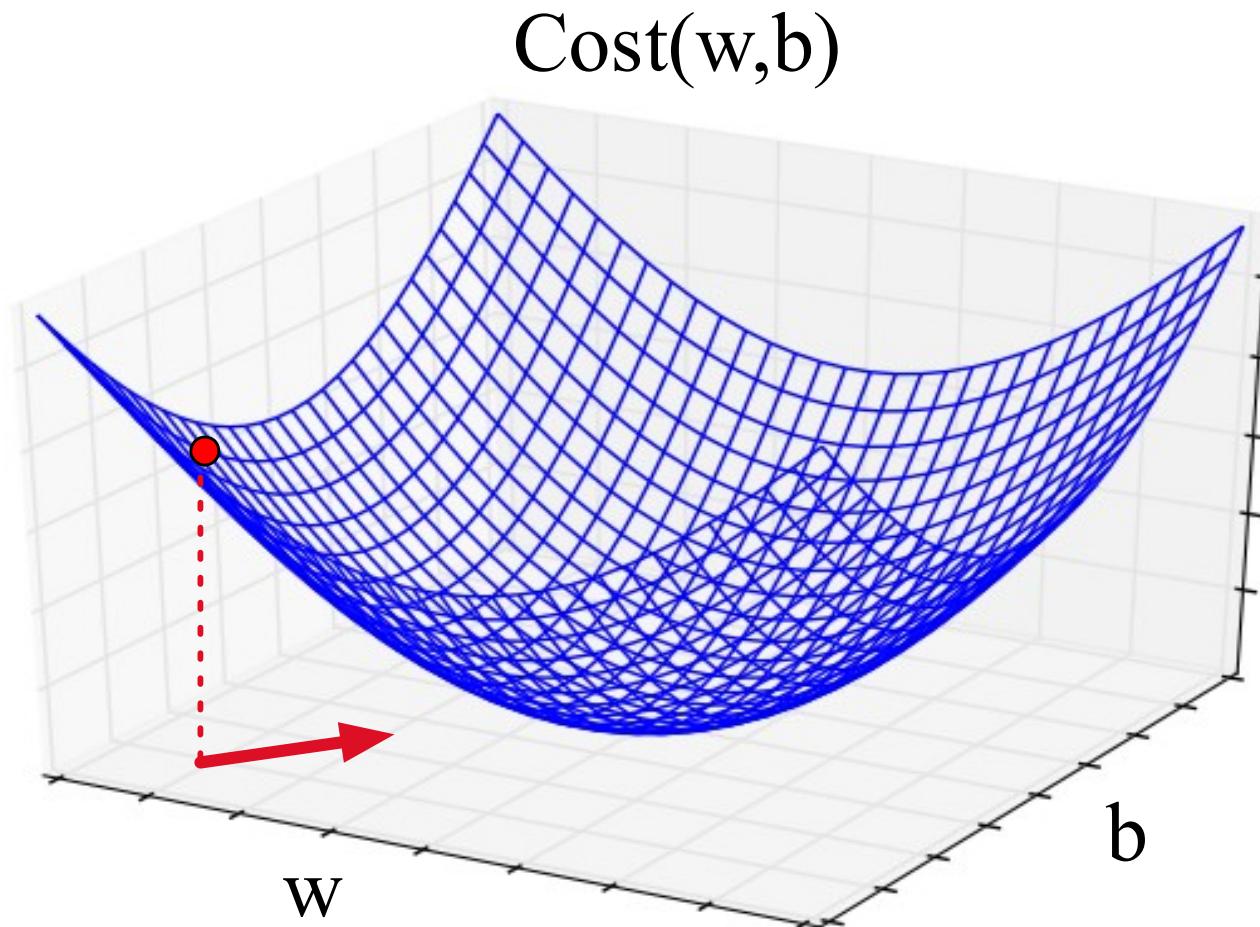
# Gradients and Gradient Descent

The **gradient** of a function of many variables is a **vector pointing in the direction of the greatest increase** in a function.

**Gradient Descent:** Find the gradient of the loss function at the current point and move in the **opposite** direction.

# Gradients: Visualized

Visualizing the gradient vector at the **red** point



# Gradients and Learning Rate

- The value of the gradient (slope in our example)  $\frac{d}{dw} L(f(x; w), y)$  weighted by a **learning rate**  $\eta$
- Higher learning rate means move **w** faster

$$w^{t+1} = w^t - \eta \frac{d}{dw} L(f(x; w), y)$$

# Gradients and Weights/Bias Update

Let's represent  $\hat{y}$  as  $f(\textcolor{red}{x}; \theta)$  to make the dependence on  $\theta$  more obvious:

$$\nabla_{\theta} L(f(x; \theta), y) = \begin{bmatrix} \frac{\partial}{\partial w_1} L(f(x; \theta), y) \\ \frac{\partial}{\partial w_2} L(f(x; \theta), y) \\ \vdots \\ \frac{\partial}{\partial w_n} L(f(x; \theta), y) \end{bmatrix}$$

and the final equation is for updating  $\theta$ :

$$\theta_{t+1} = \theta_t - \eta \nabla L(f(x; \theta), y)$$

# Stochastic Gradient Descent

**function** STOCHASTIC GRADIENT DESCENT( $L()$ ,  $f()$ ,  $x$ ,  $y$ ) **returns**  $\theta$

# where: L is the loss function

# f is a function parameterized by  $\theta$

# x is the set of training inputs  $x^{(1)}, x^{(2)}, \dots, x^{(m)}$

# y is the set of training outputs (labels)  $y^{(1)}, y^{(2)}, \dots, y^{(m)}$

$\theta \leftarrow 0$

**repeat** til done

For each training tuple  $(x^{(i)}, y^{(i)})$  (in random order)

1. Optional (for reporting): # How are we doing on this tuple?

    Compute  $\hat{y}^{(i)} = f(x^{(i)}; \theta)$  # What is our estimated output  $\hat{y}$ ?

    Compute the loss  $L(\hat{y}^{(i)}, y^{(i)})$  # How far off is  $\hat{y}^{(i)}$  from the true output  $y^{(i)}$ ?

2.  $g \leftarrow \nabla_{\theta} L(f(x^{(i)}; \theta), y^{(i)})$  # How should we move  $\theta$  to maximize loss?

3.  $\theta \leftarrow \theta - \eta g$  # Go the other way instead

return  $\theta$

# Hyperparameters

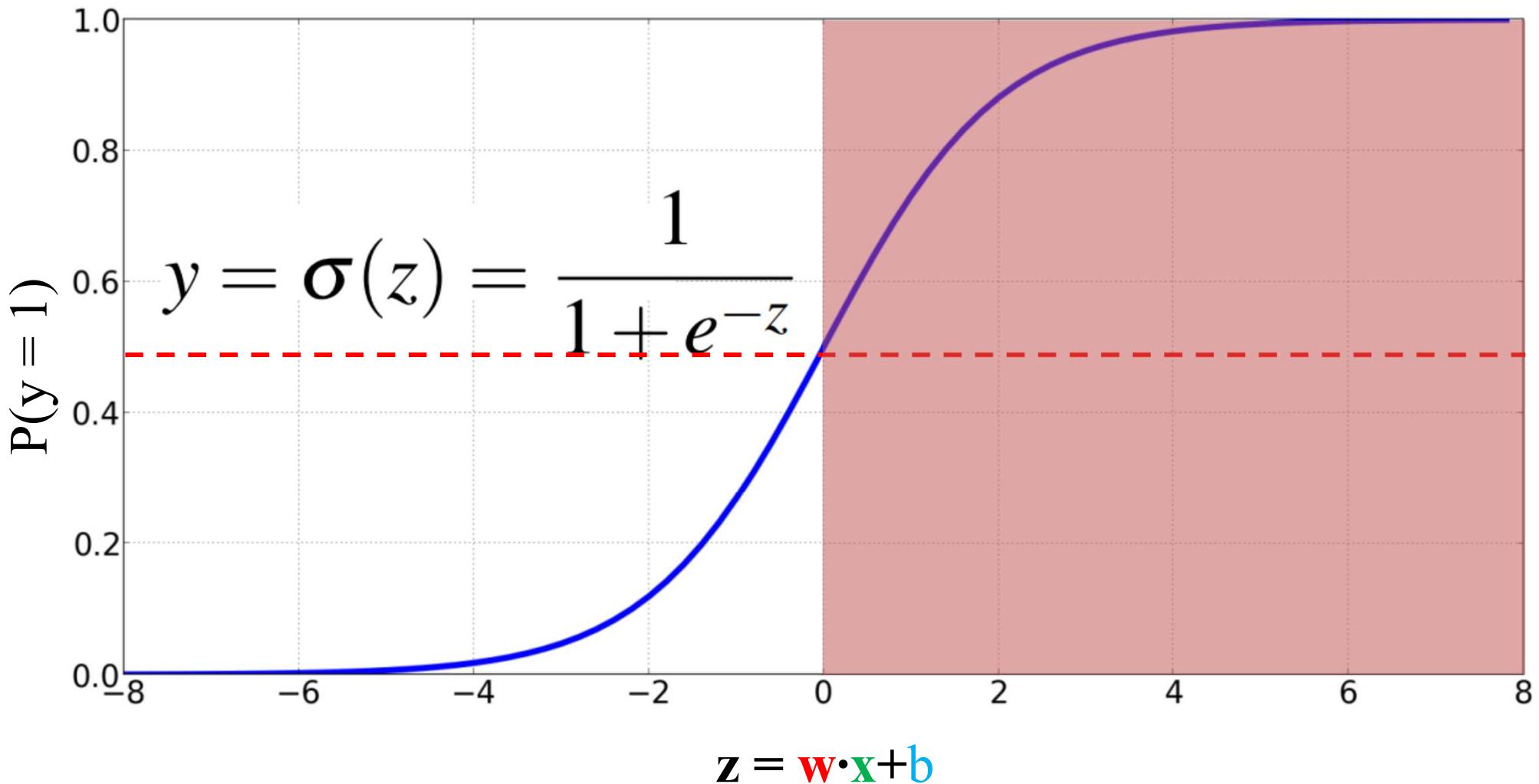
The learning rate  $\eta$  is a **hyperparameter**

- too high: the learner will take big steps and overshoot
- too low: the learner will take too long

Hyperparameters:

- Briefly, a special kind of parameter for an ML model
- Instead of being learned by algorithm from supervision (like regular parameters), they are chosen by algorithm designer.

# Logistic Regression Classifier



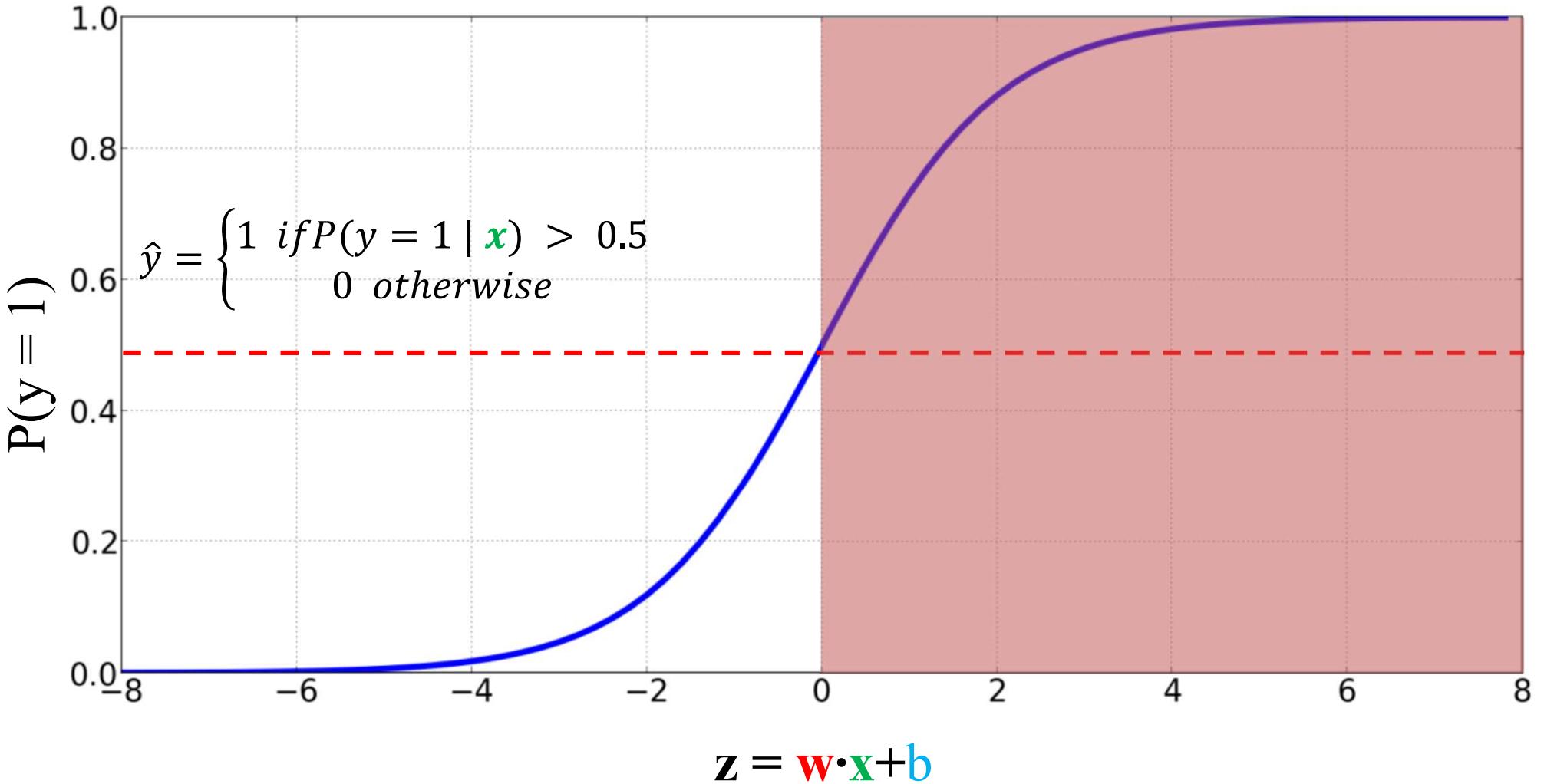
# Probabilities → Classification

Once we know the probability, we can use it to classify:

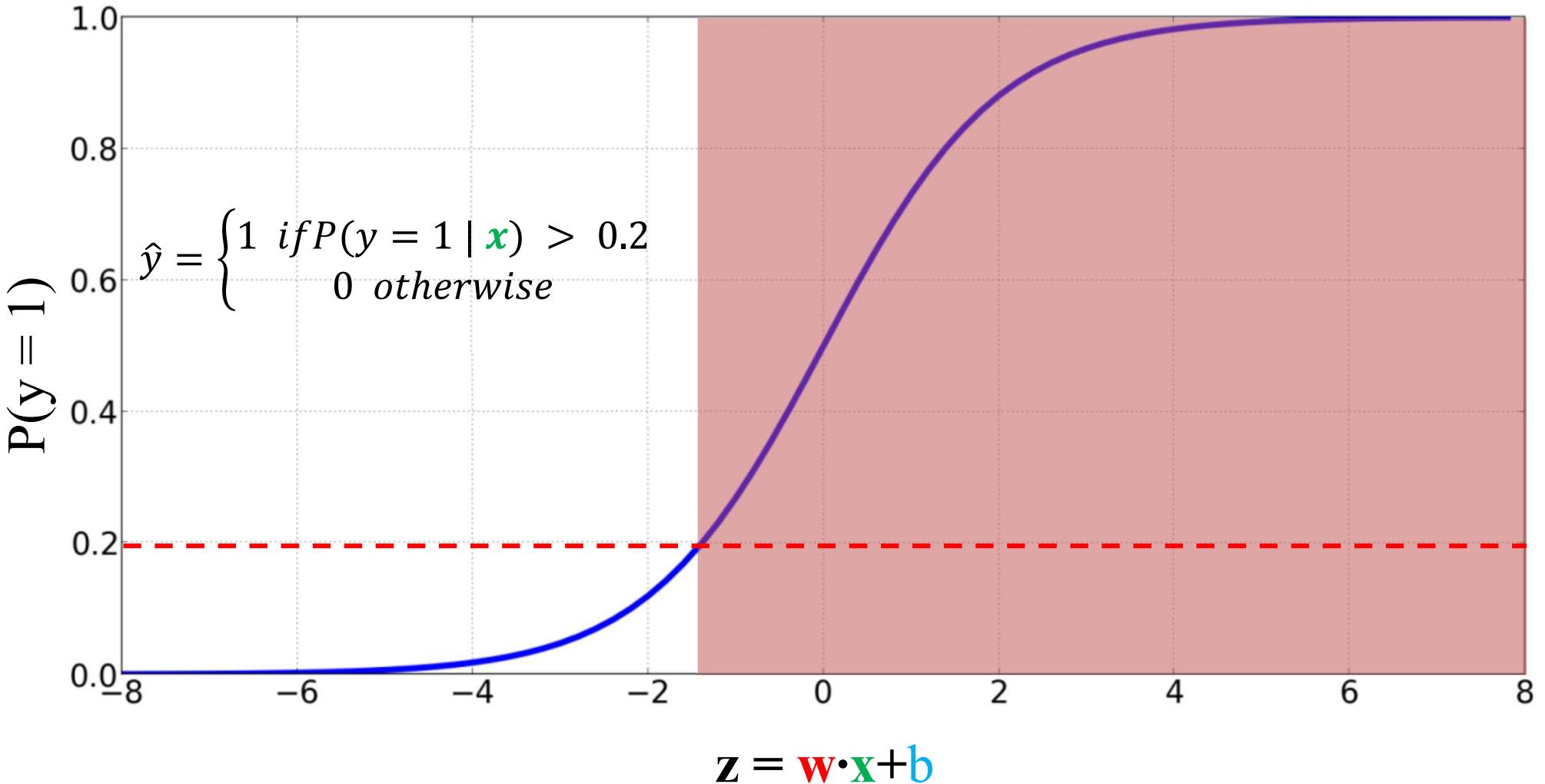
$$\hat{y} = \begin{cases} 1 & \text{if } P(y=1|x) > 0.5 \\ 0 & \text{otherwise} \end{cases}$$

Where 0.5 is the **decision boundary**

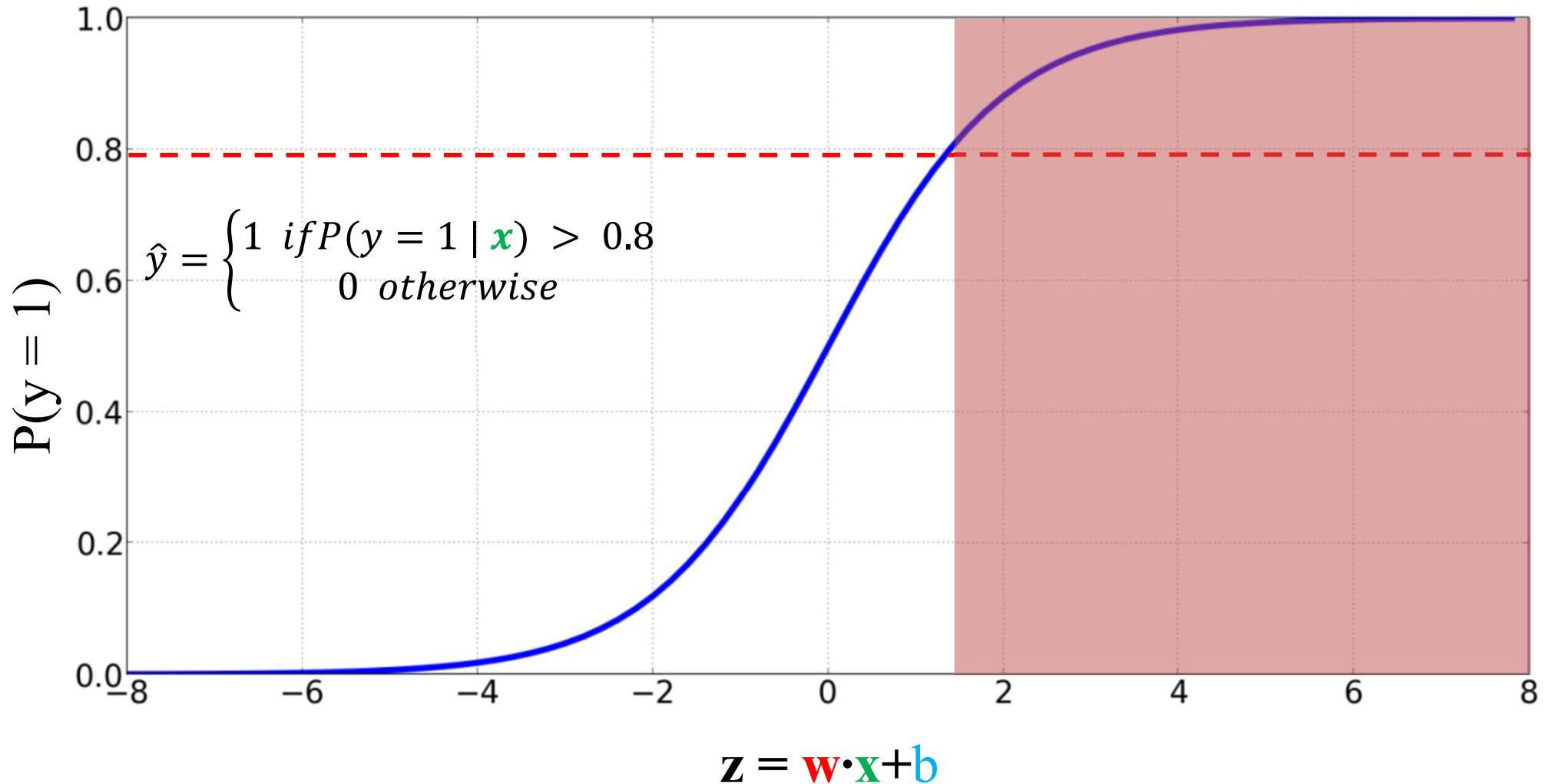
# Logistic Regression: Threshold 0.5



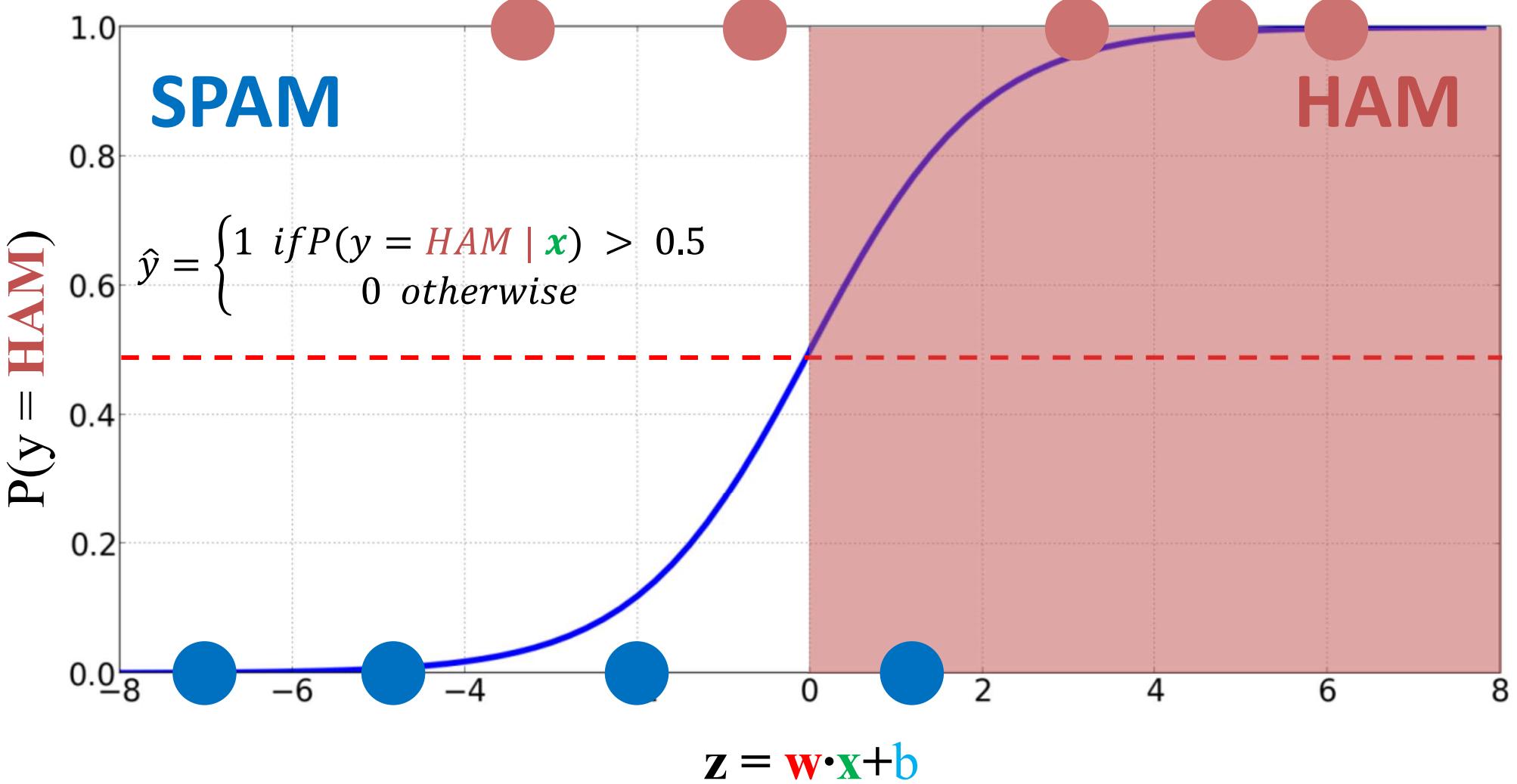
# Logistic Regression: Threshold 0.2



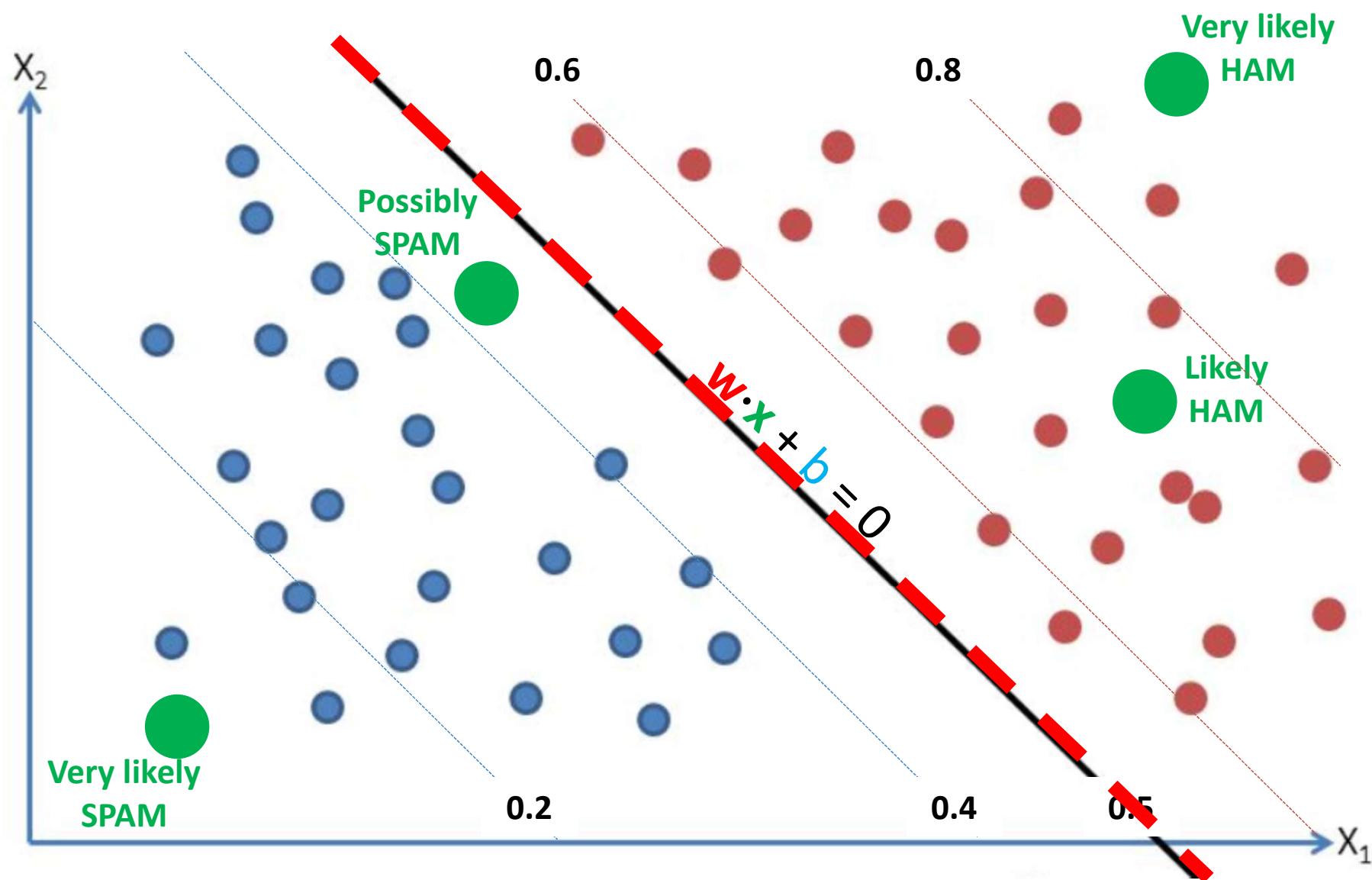
# Logistic Regression: Threshold 0.8



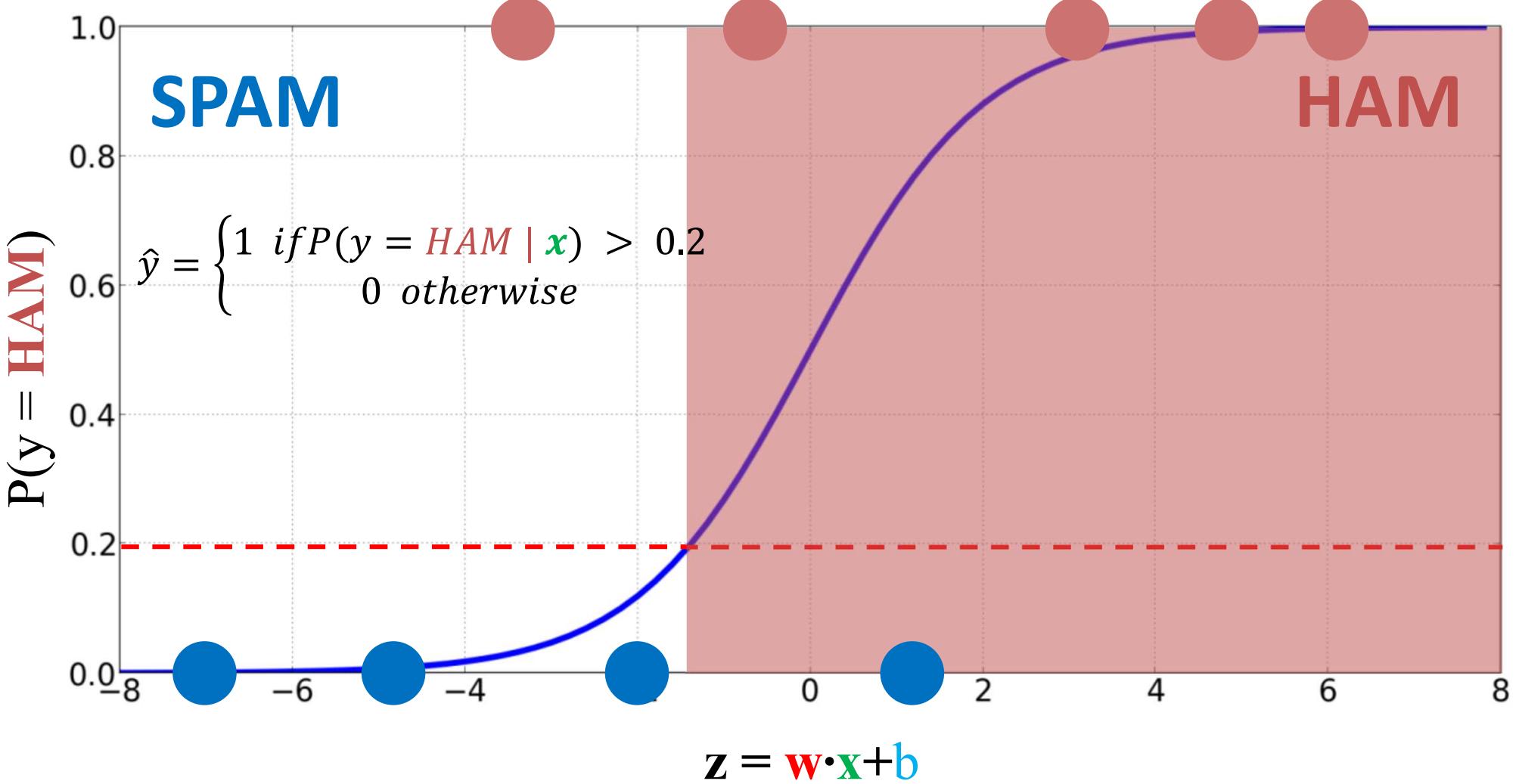
# Logistic Regression: Threshold 0.5



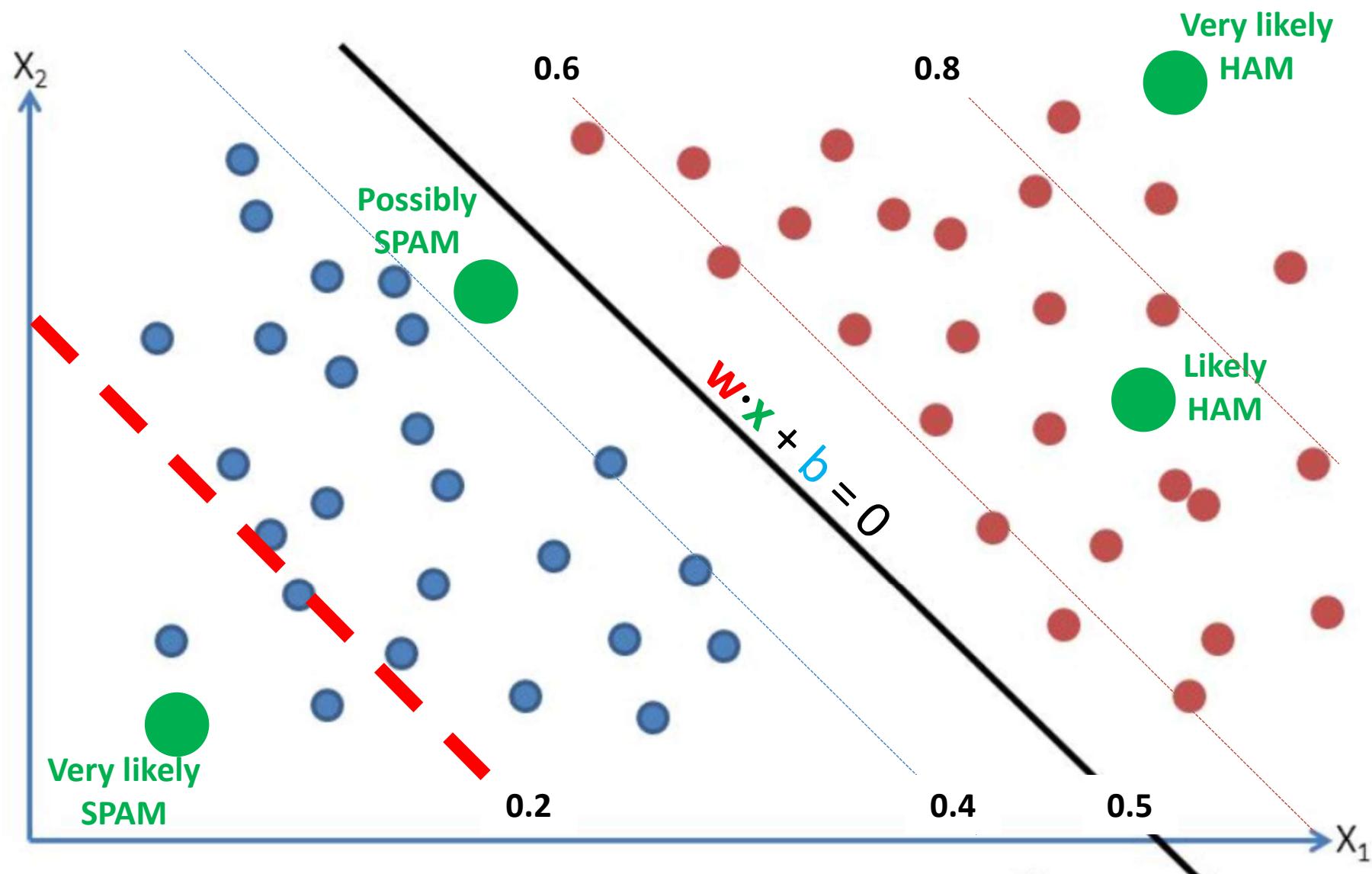
# Text Classification: Separator



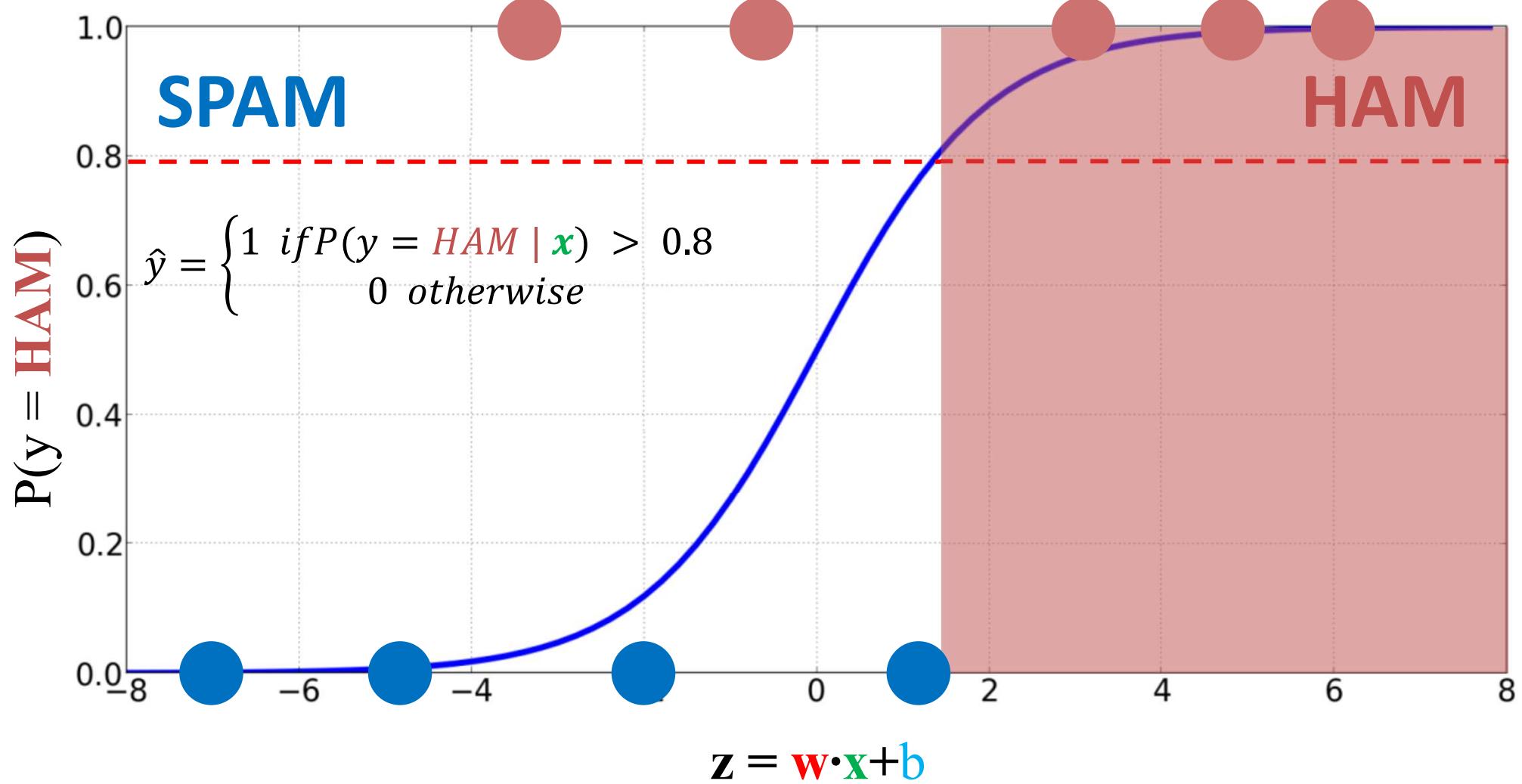
# Logistic Regression: Threshold 0.2



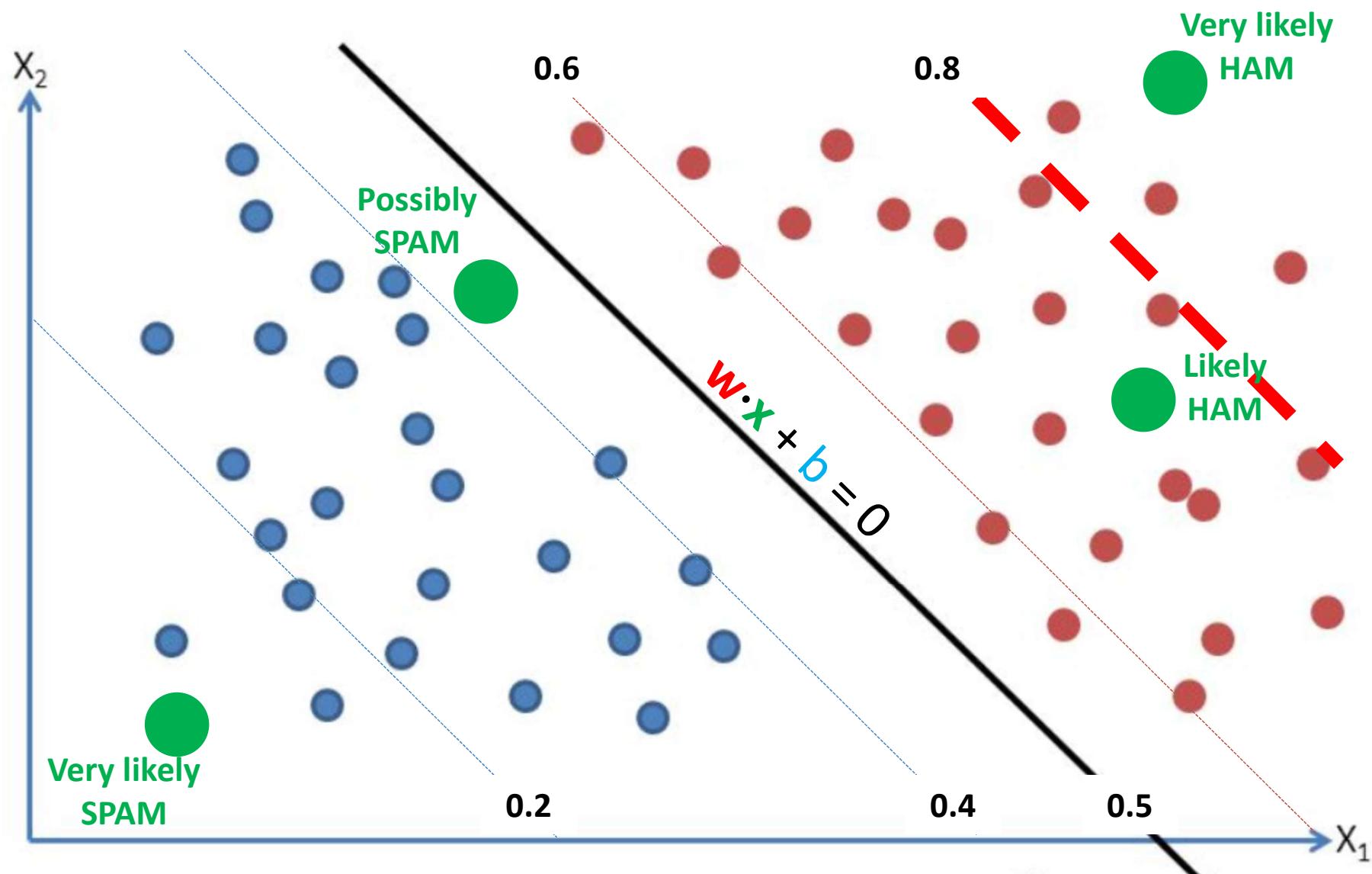
# Text Classification: Separator



# Logistic Regression: Threshold 0.8



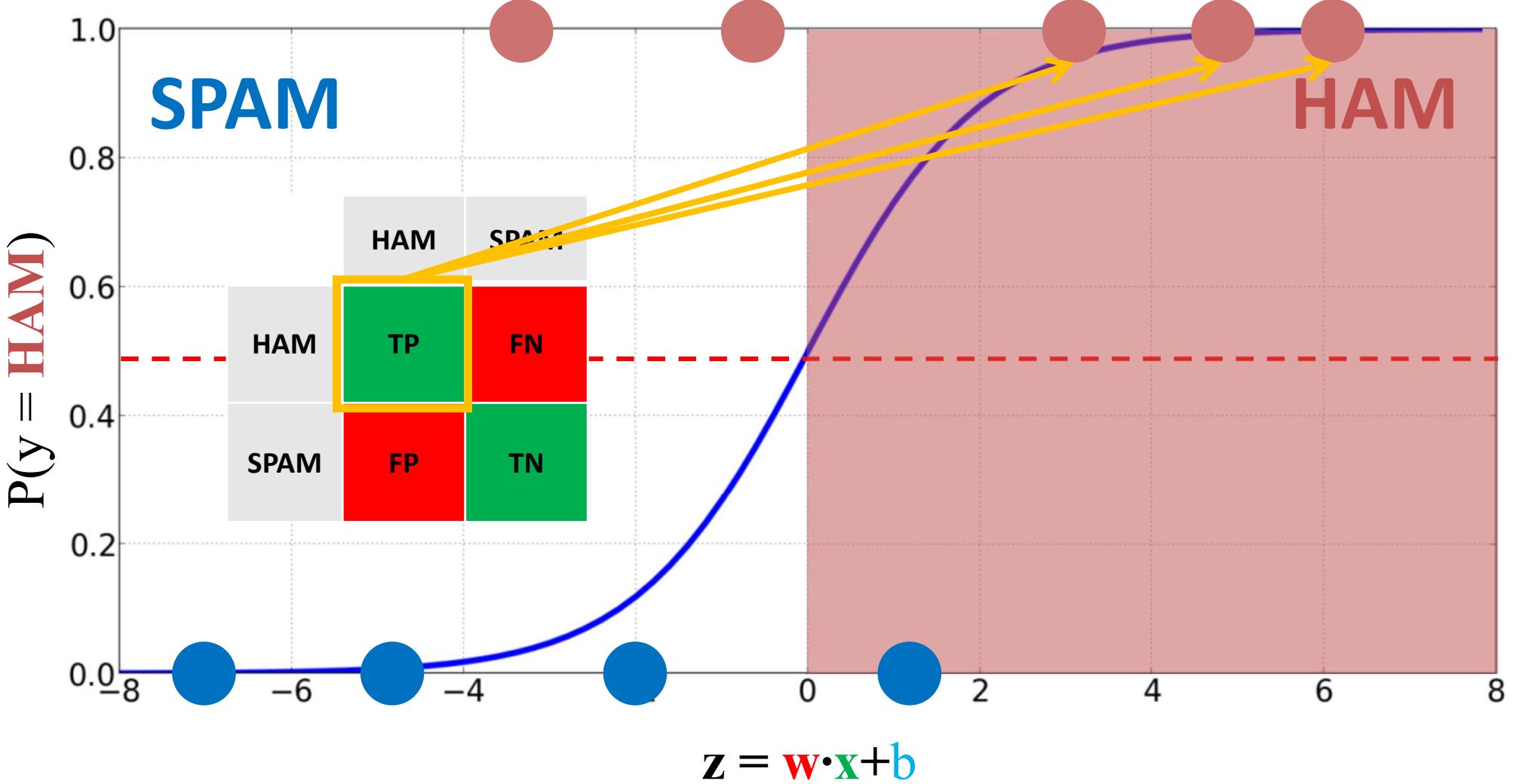
# Text Classification: Separator



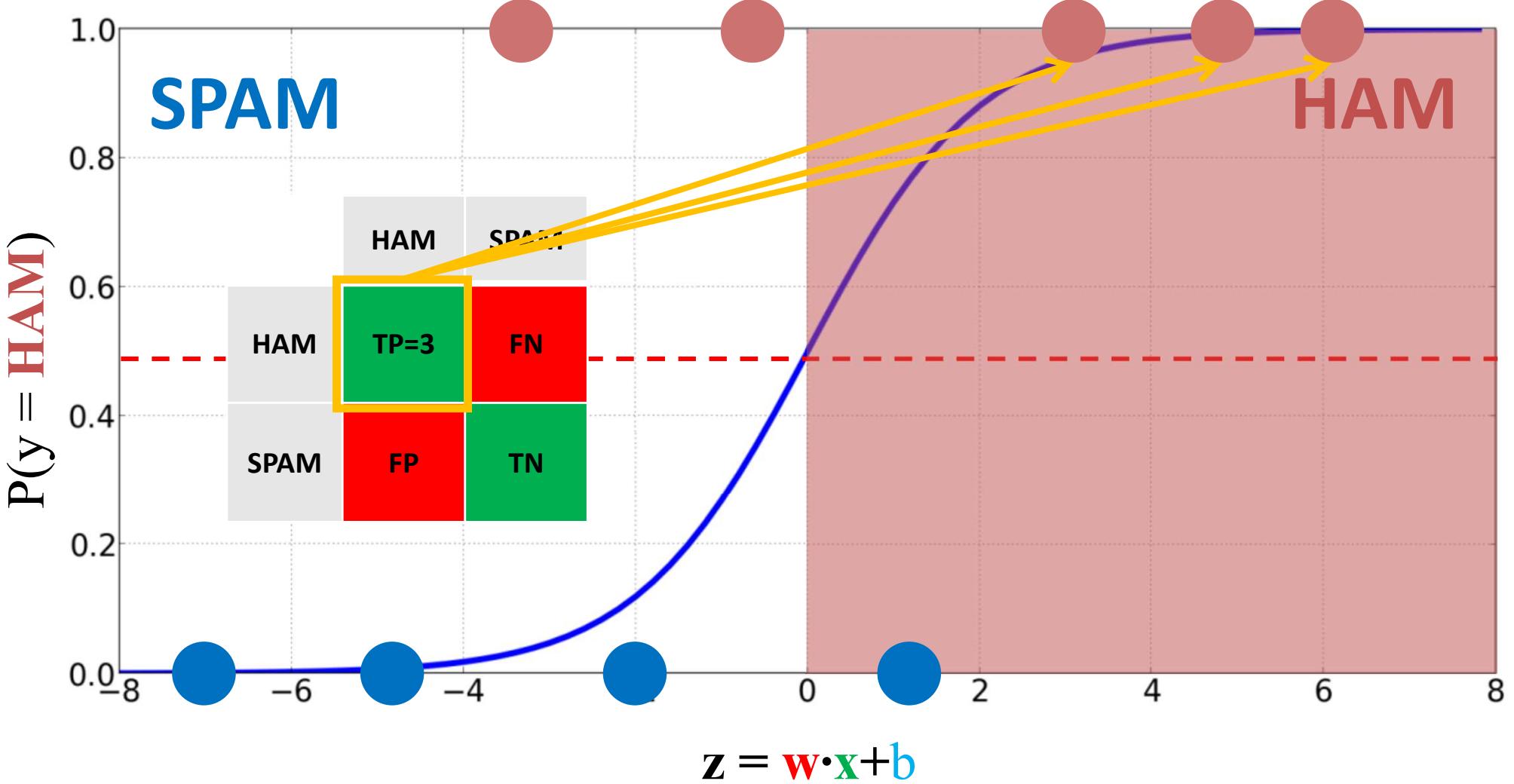
# Classifier Evaluation: Confusion Matrix

		Predicted class		
		Positive	Negative	
Actual class	Positive	True Positive (TP)	False Negative (FN) Type II Error	Sensitivity (Recall) $\frac{TP}{TP+FN}$
	Negative	False Positive (FP) Type I Error	True Negative (TN)	Specificity $\frac{TN}{TN+FP}$
		Precision $\frac{TP}{TP+FP}$	Negative Predictive Value $\frac{TN}{TN+FN}$	Accuracy $\frac{TP+TN}{TP+TN+FP+FN}$

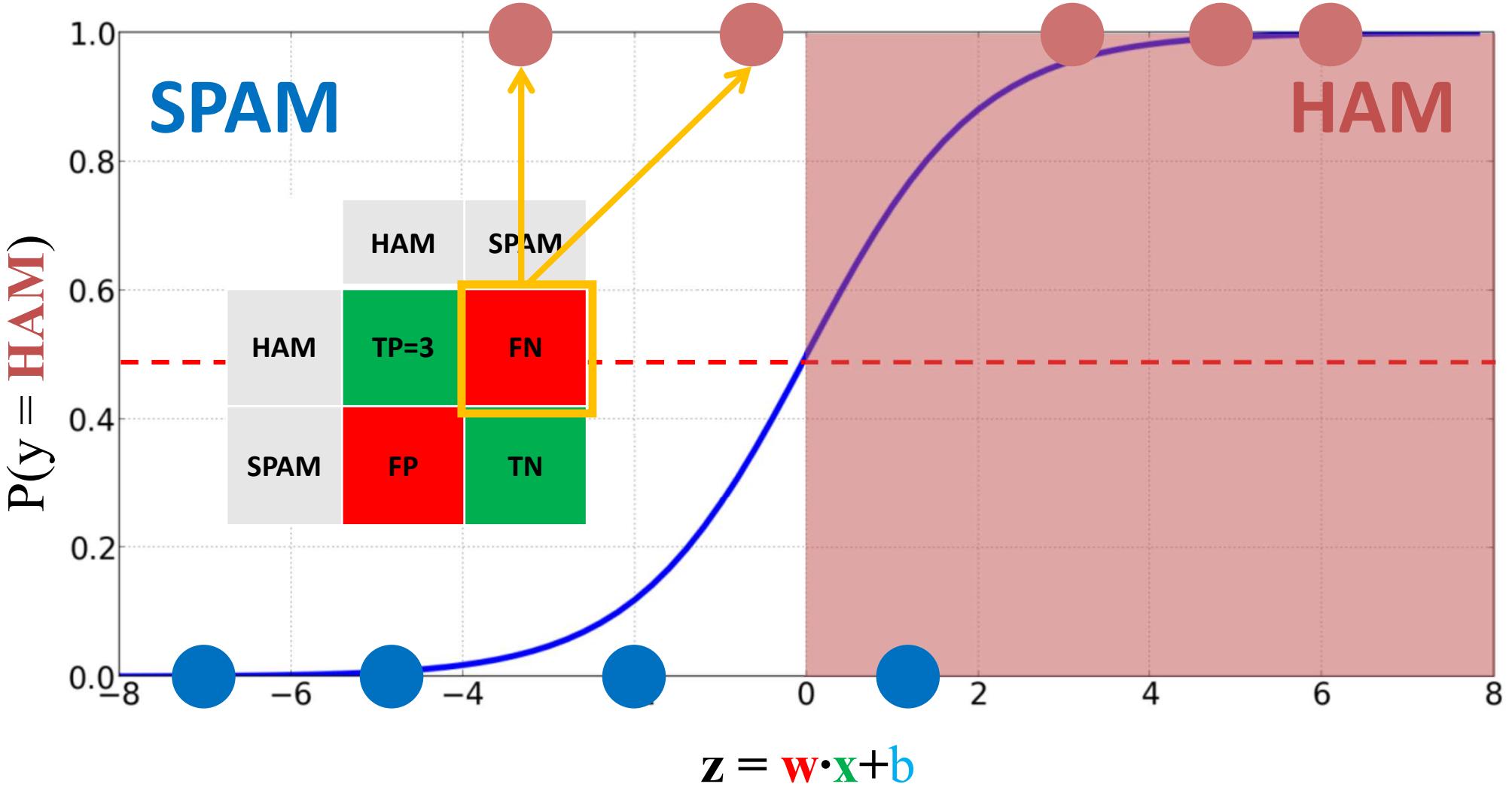
# Logistic Regression: Threshold 0.5



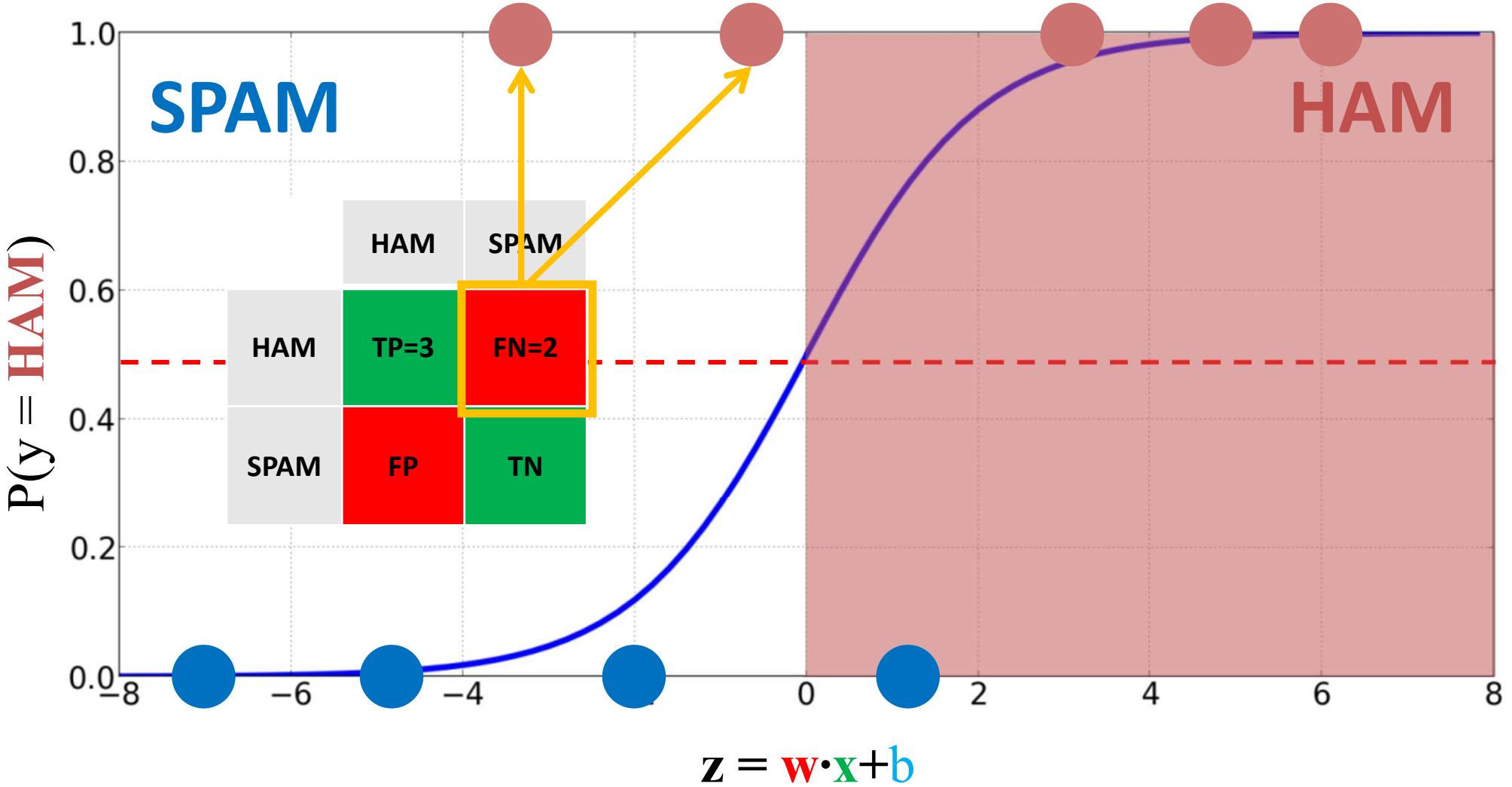
# Logistic Regression: Threshold 0.5



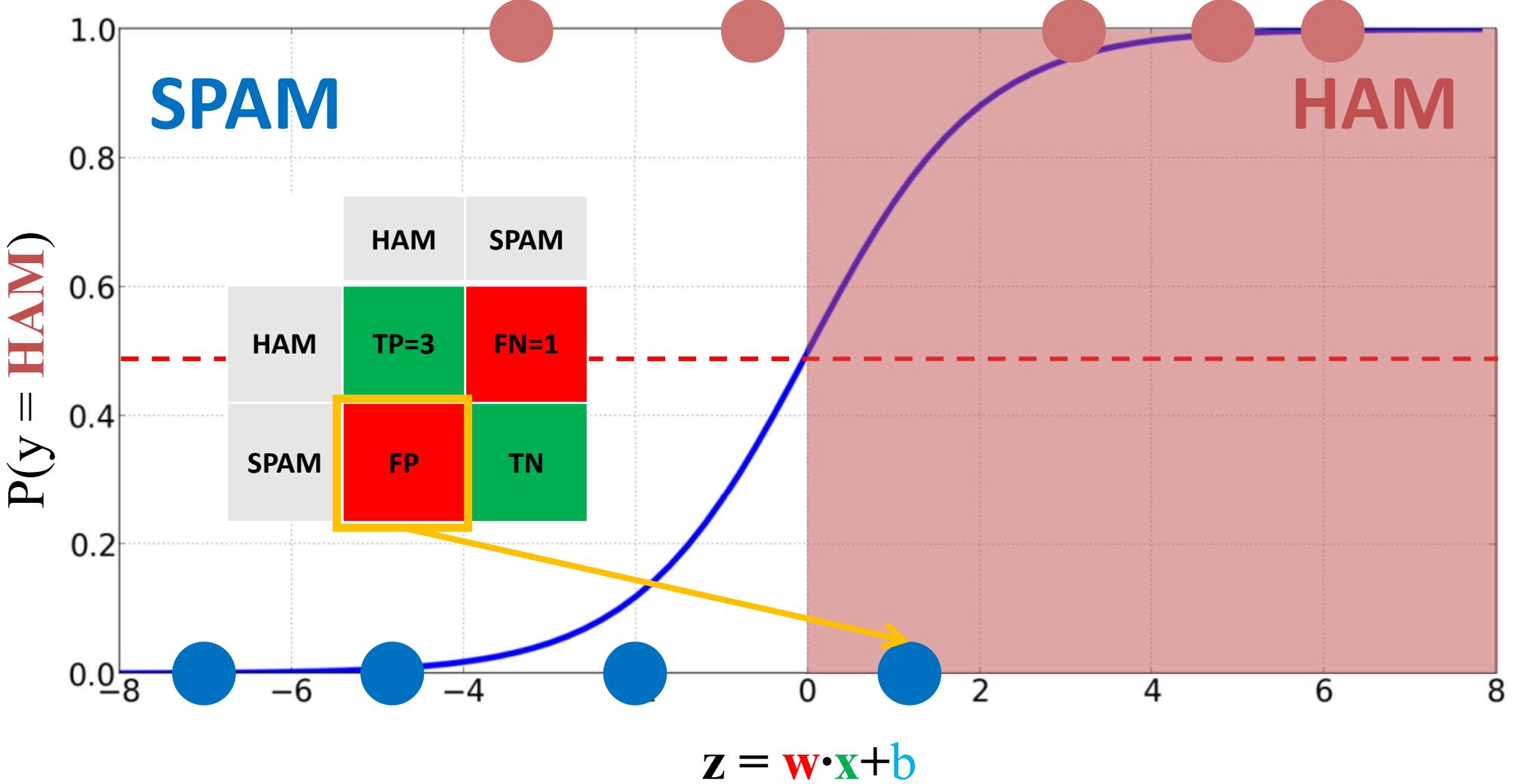
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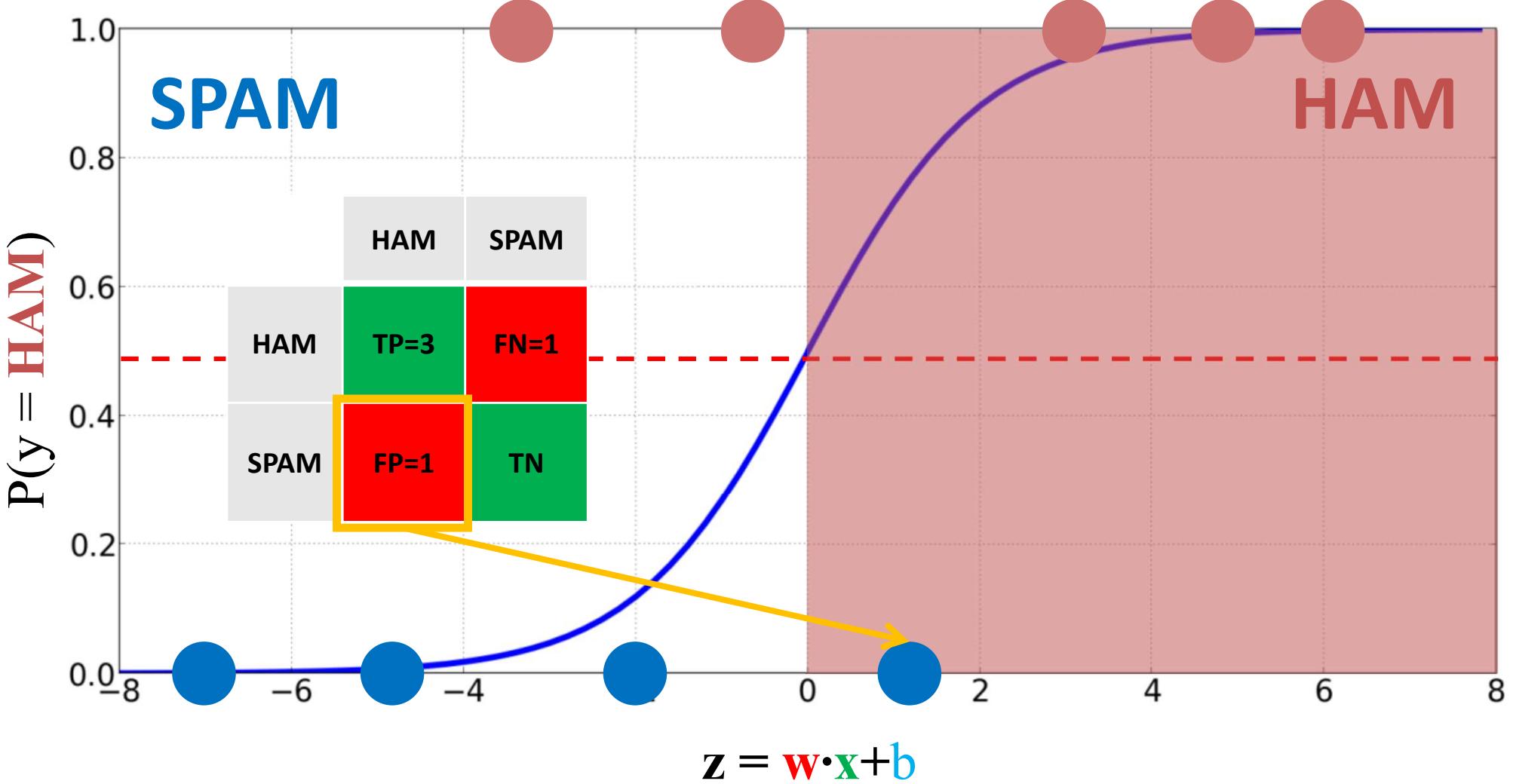
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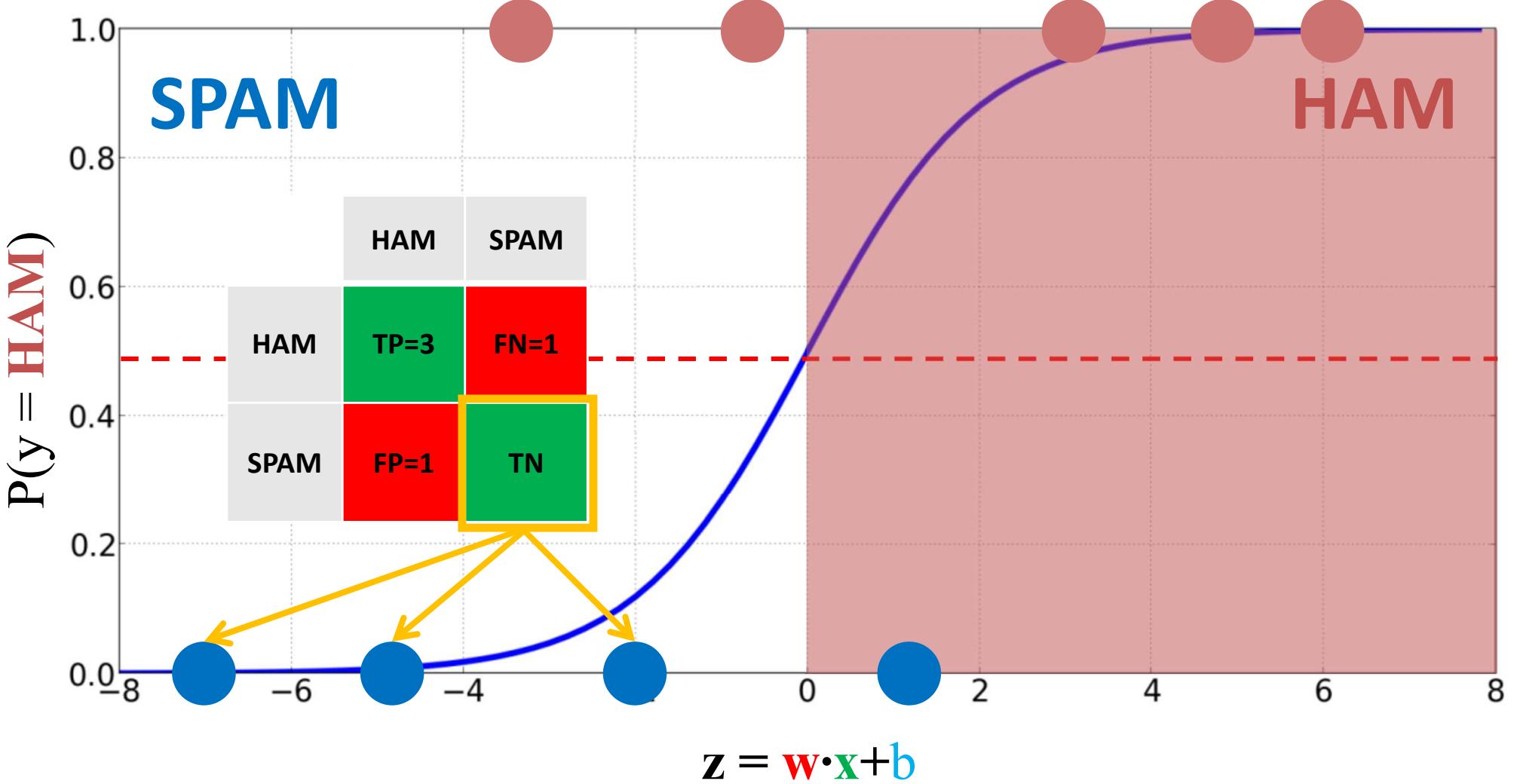
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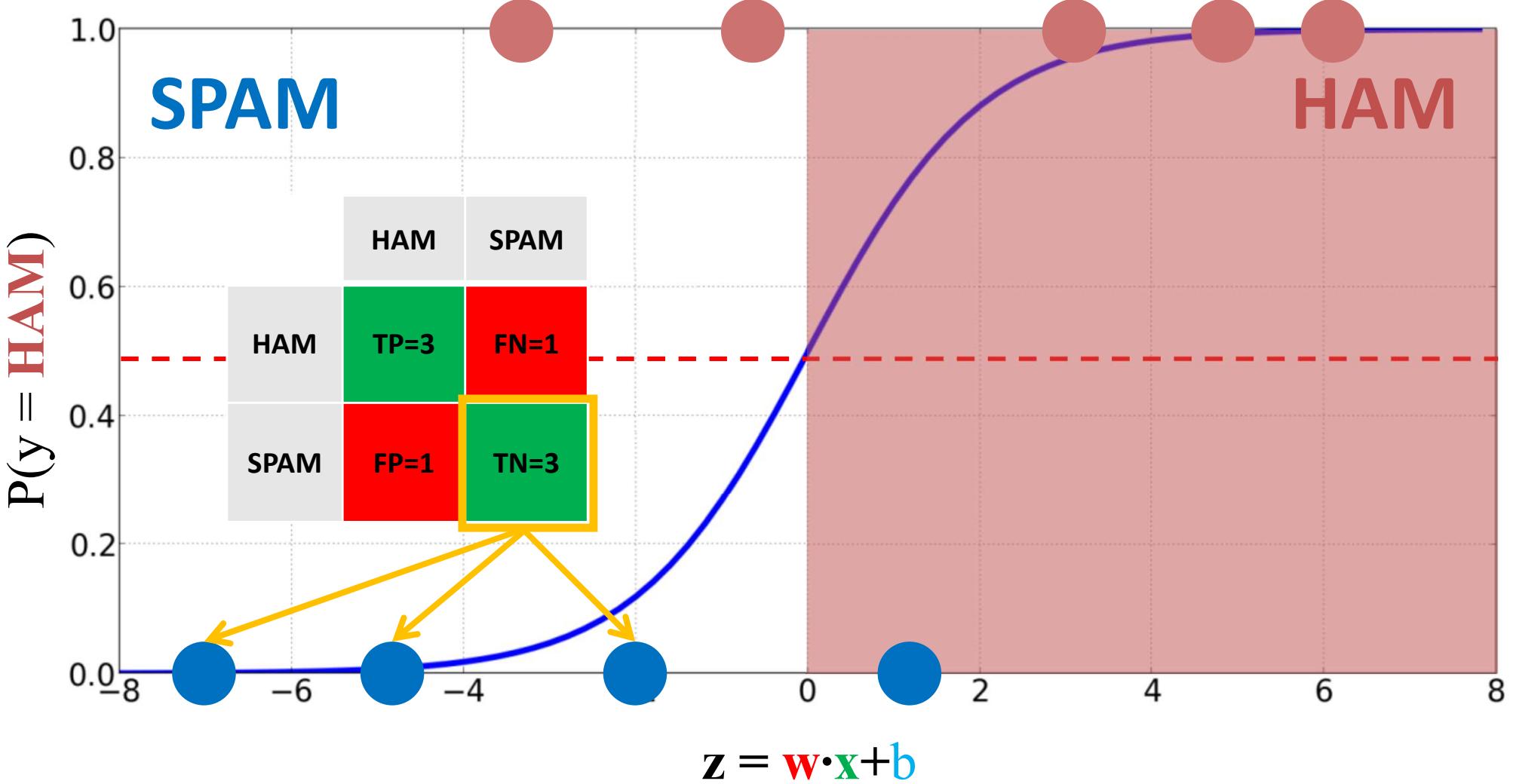
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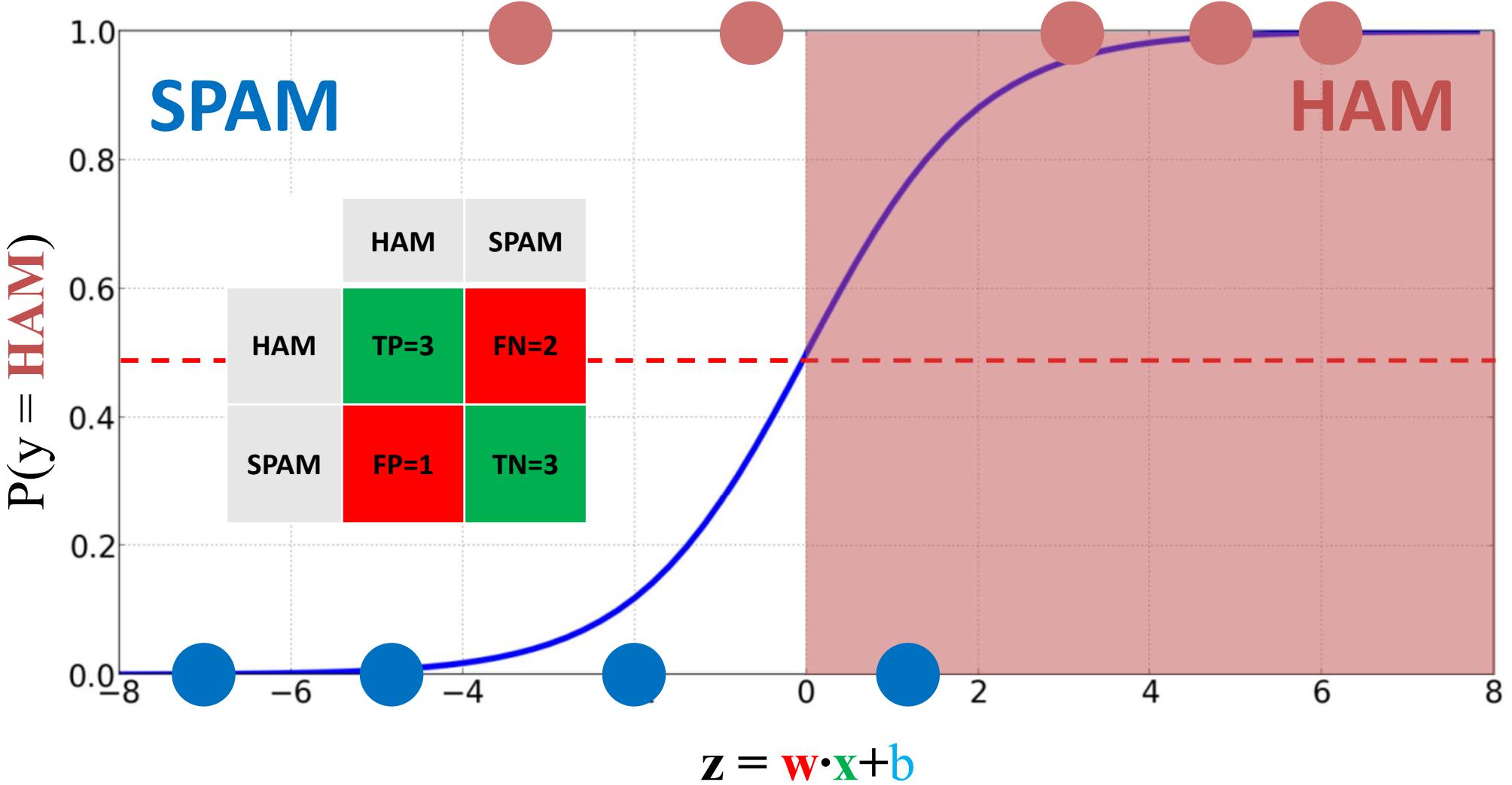
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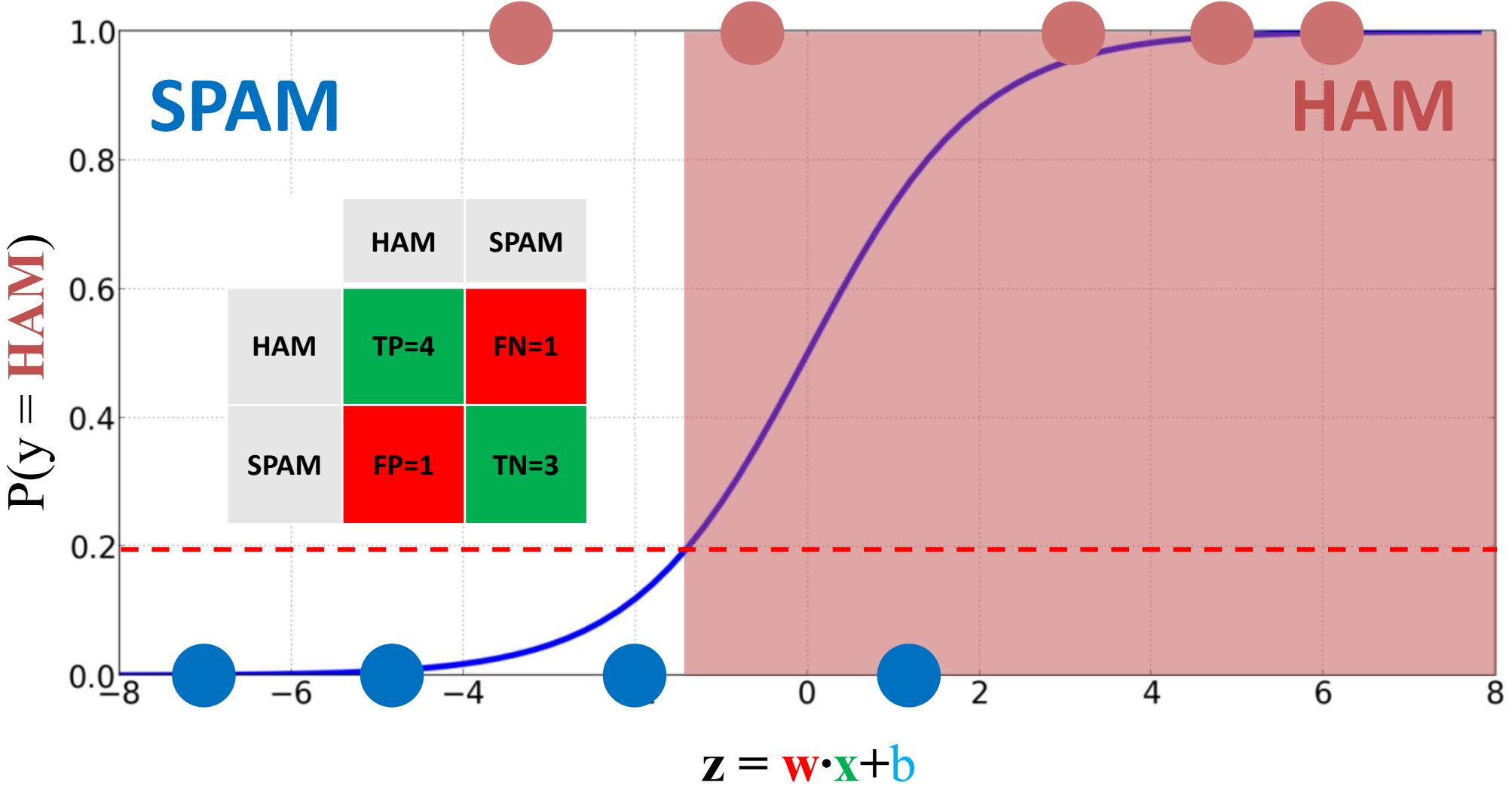
# Logistic Regression: Threshold 0.5



# Confusion Matrix: Threshold 0.5

		Predicted class			
		HAM	SPAM		
Actual class	HAM	True Positive (TP) 3	False Negative (FN) 2	Sensitivity (Recall)	$\frac{TP}{TP+FN} = \frac{3}{5}$
	SPAM	False Positive (FP) 1	True Negative (TN) 3	Specificity	$\frac{TN}{TN+FP} = \frac{3}{4}$
		Precision $\frac{TP}{TP+FP} = \frac{3}{4}$	Negative Predictive Value $\frac{TN}{TN+FN} = \frac{3}{5}$	Accuracy	$\frac{TP+TN}{TP+TN+FP+FN} = \frac{6}{9}$

# Logistic Regression: Threshold 0.2



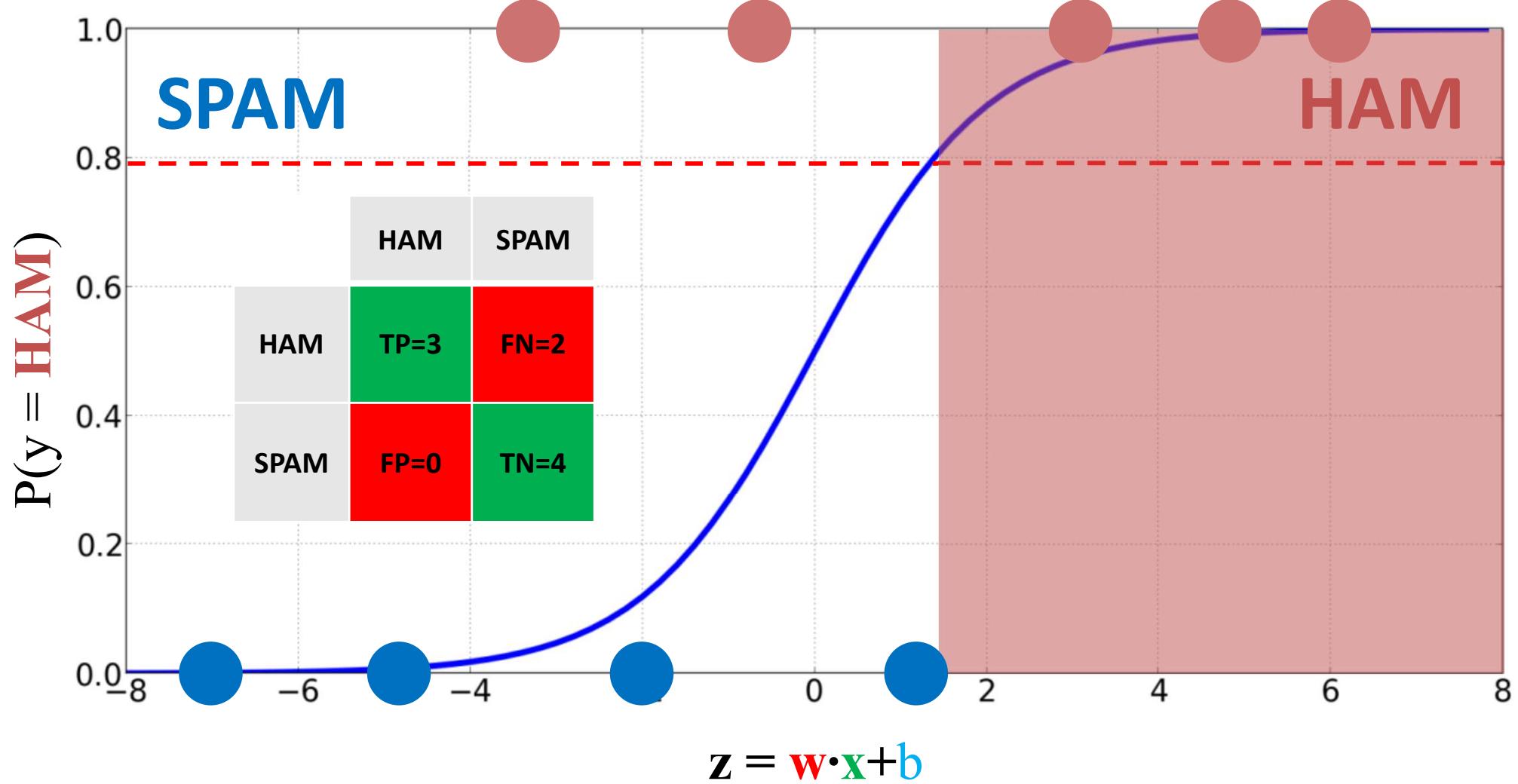
# Confusion Matrix: Threshold 0.2

		Predicted class			
		HAM	SPAM		
Actual class	HAM	True Positive (TP) 4	False Negative (FN) 1	Sensitivity (Recall)	$\frac{TP}{TP+FN} = \frac{4}{5}$
	SPAM	False Positive (FP) 1	True Negative (TN) 3	Specificity	$\frac{TN}{TN+FP} = \frac{3}{4}$
		Precision $\frac{TP}{TP+FP} = \frac{4}{5}$	Negative Predictive Value $\frac{TN}{TN+FN} = \frac{3}{4}$	Accuracy	$\frac{TP+TN}{TP+TN+FP+FN} = \frac{7}{9}$

# Confusion Matrix: Threshold 0.2

		Predicted class		
		Positive	Negative	
Actual class	Positive	True Positive (TP) 4	False Negative (FN) 1	Sensitivity (Recall) $\frac{TP}{TP+FN} = \frac{4}{5}$
	Negative	False Positive (FP) 1	True Negative (TN) 3	Specificity $\frac{TN}{TN+FP} = \frac{3}{4}$
Lower threshold Less False Negatives (Ex: Covid tests)	Precision $\frac{TP}{TP+FP} = \frac{4}{5}$	Negative Predictive Value $\frac{TN}{TN+FN} = \frac{3}{4}$	Accuracy $\frac{TP+TN}{TP+TN+FP+FN} = \frac{7}{9}$	

# Logistic Regression: Threshold 0.8



# Confusion Matrix: Threshold 0.8

		Predicted class		
		HAM	SPAM	
Actual class	HAM	True Positive (TP) 3	False Negative (FN) 2	Sensitivity (Recall) $\frac{TP}{TP+FN} = \frac{3}{5}$
	SPAM	False Positive (FP) 0	True Negative (TN) 4	Specificity $\frac{TN}{TN+FP} = \frac{4}{4}$
		Precision $\frac{TP}{TP+FP} = \frac{3}{3}$	Negative Predictive Value $\frac{TN}{TN+FN} = \frac{4}{6}$	Accuracy $\frac{TP+TN}{TP+TN+FP+FN} = \frac{7}{9}$

# Confusion Matrix: Threshold 0.8

		Predicted class		
		Positive	Negative	
Actual class	Positive	True Positive (TP) 3	False Negative (FN) 2	Sensitivity (Recall) $\frac{TP}{TP+FN} = \frac{3}{5}$
	Negative	False Positive (FP) 0	True Negative (TN) 4	Specificity $\frac{TN}{TN+FP} = \frac{4}{4}$
Higher threshold Less False Positives (Ex: crime convictions)	Precision $\frac{TP}{TP+FP} = \frac{3}{3}$	Negative Predictive Value $\frac{TN}{TN+FN} = \frac{4}{6}$	Accuracy $\frac{TP+TN}{TP+TN+FP+FN} = \frac{7}{9}$	

# Classifier Evaluation: Confusion Matrix

		Predicted class		
		Positive	Negative	
Actual class	Positive	True Positive (TP)	False Negative (FN) Type II Error	Sensitivity (Recall) $\frac{TP}{TP+FN}$
	Negative	False Positive (FP) Type I Error	True Negative (TN)	Specificity $\frac{TN}{TN+FP}$
		Precision $\frac{TP}{TP+FP}$	Negative Predictive Value $\frac{TN}{TN+FN}$	Accuracy $\frac{TP+TN}{TP+TN+FP+FN}$

# Classifier Performance Metrics

- Precision and recall provide two ways to summarize the errors made for the positive class (FP, FN).
- F-measure provides a single score that summarizes the precision and recall.
- Accuracy summarizes the correct predictions for both positive and negative classes.

# Receiver Operating Characteristic

Threshold: 0.5

		HAM	SPAM
		TP=3	FN=2
		FP=1	TN=3
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$

$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.2

		HAM	SPAM
		TP=4	FN=1
		FP=1	TN=3
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{4}{5}$$

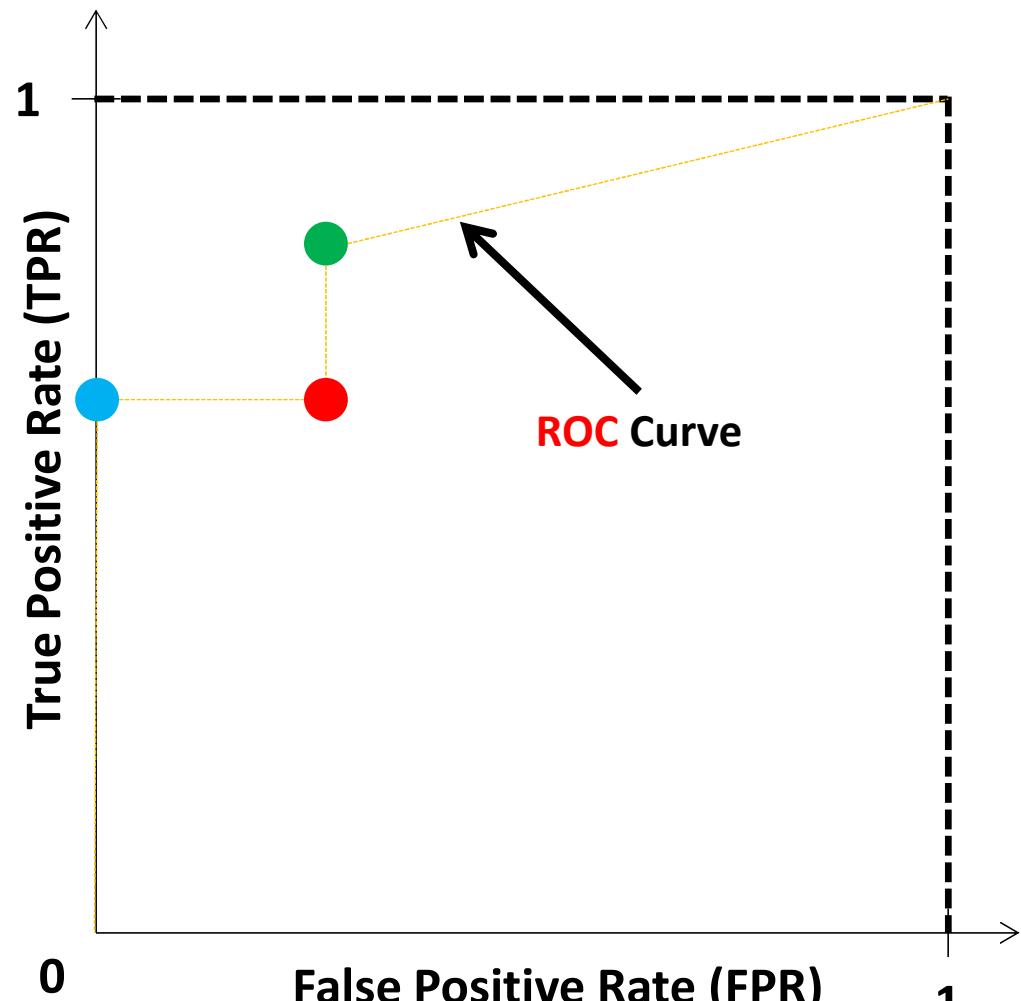
$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.8

		HAM	SPAM
		TP=3	FN=2
		FP=0	TN=4
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$

$$FPR = \frac{FP}{FP + TN} = \frac{0}{4}$$



TPR: Sensitivity | FPR: 1 - Specificity

# ROC Area Under the Curve

Threshold: 0.5

	HAM	SPAM
HAM	TP=3	FN=2
SPAM	FP=1	TN=3

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$

$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.2

	HAM	SPAM
HAM	TP=4	FN=1
SPAM	FP=1	TN=3

$$TPR = \frac{TP}{TP + FN} = \frac{4}{5}$$

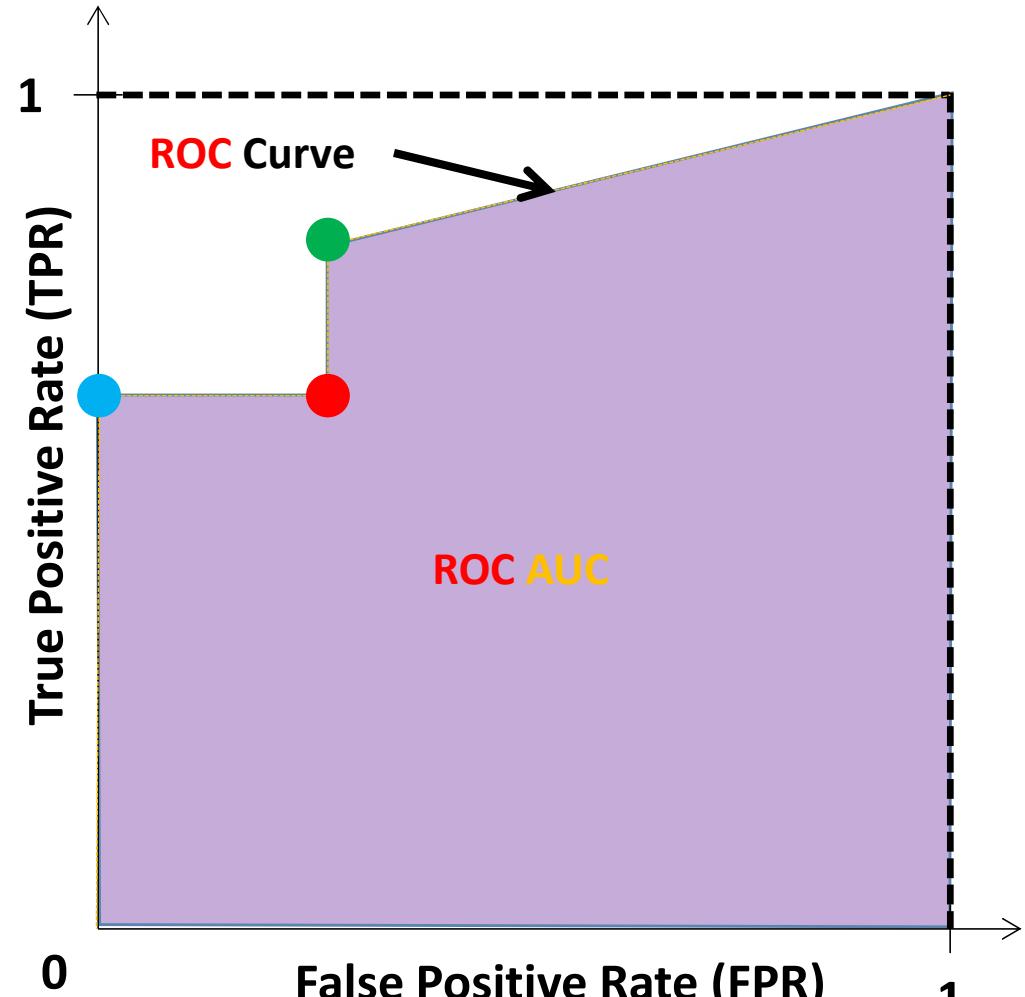
$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.8

	HAM	SPAM
HAM	TP=3	FN=2
SPAM	FP=0	TN=4

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$

$$FPR = \frac{FP}{FP + TN} = \frac{0}{4}$$



TPR: Sensitivity | FPR: 1 - Specificity

# Receiver Operating Characteristic

Threshold: 0.5

		HAM	SPAM
		TP=3	FN=2
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HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$

$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.2

		HAM	SPAM
		TP=4	FN=1
		FP=1	TN=3
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{4}{5}$$

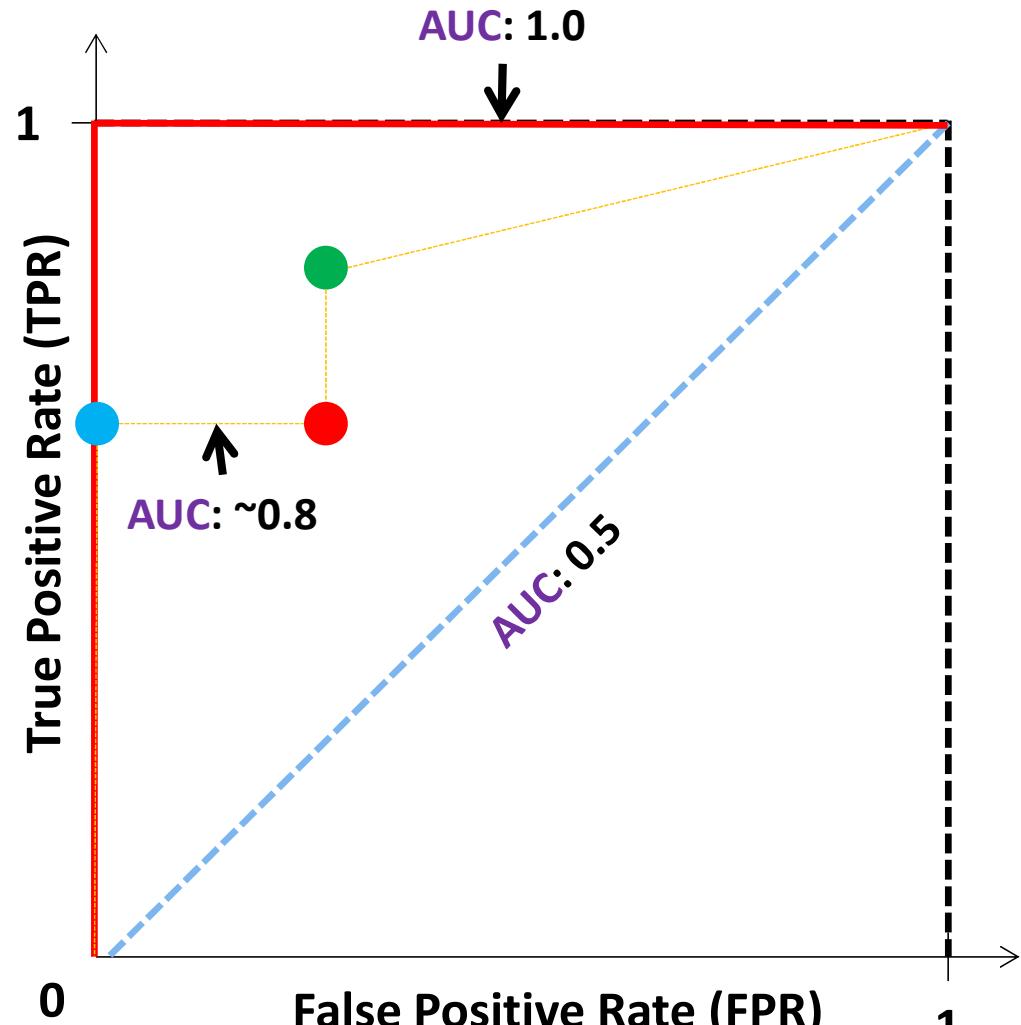
$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.8

		HAM	SPAM
		TP=3	FN=2
		FP=0	TN=4
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$

$$FPR = \frac{FP}{FP + TN} = \frac{0}{4}$$



TPR: Sensitivity | FPR: 1 - Specificity

# Receiver Operating Characteristic

Threshold: 0.5

		HAM	SPAM
		TP=3	FN=2
		FP=1	TN=3
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$
$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.2

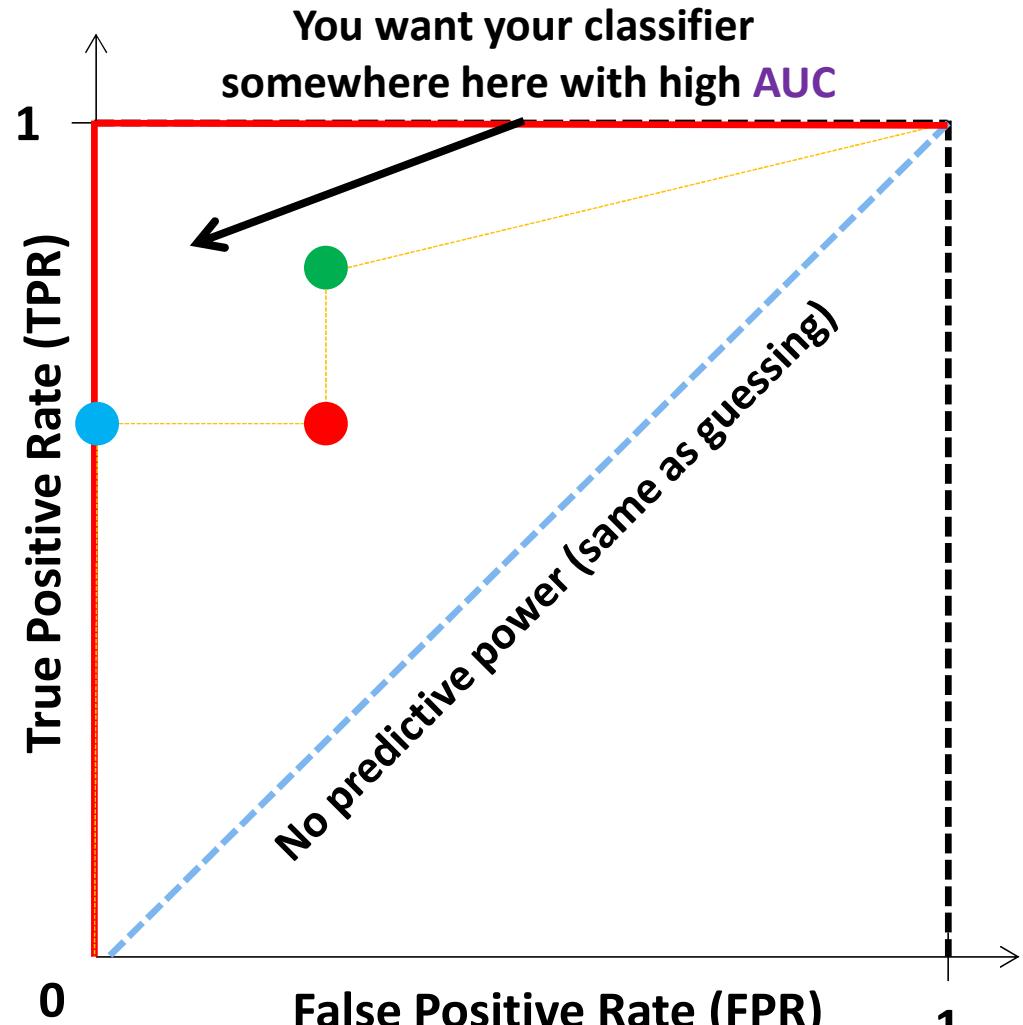
		HAM	SPAM
		TP=4	FN=1
		FP=1	TN=3
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{4}{5}$$
$$FPR = \frac{FP}{FP + TN} = \frac{1}{4}$$

Threshold: 0.8

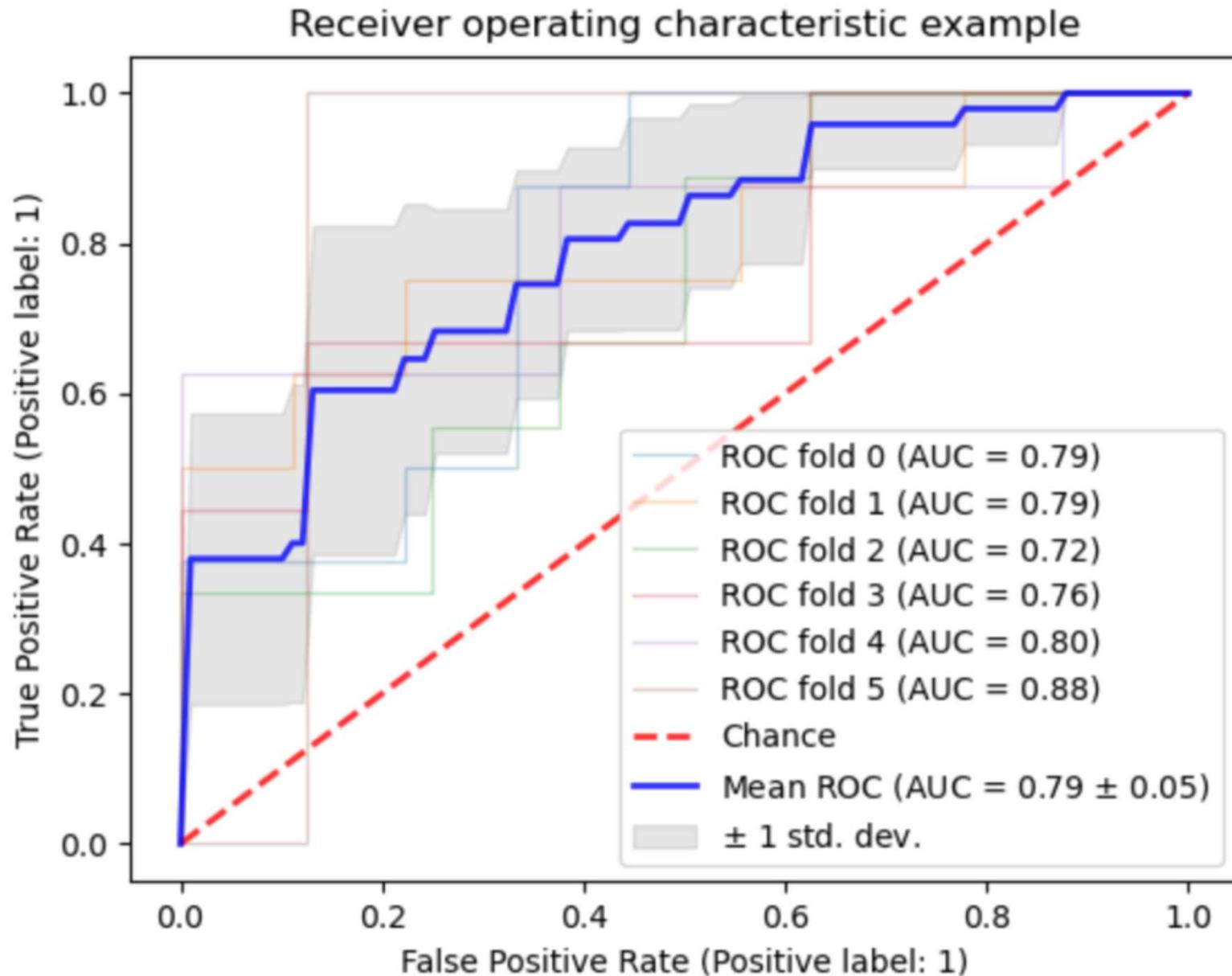
		HAM	SPAM
		TP=3	FN=2
		FP=0	TN=4
HAM			
SPAM			

$$TPR = \frac{TP}{TP + FN} = \frac{3}{5}$$
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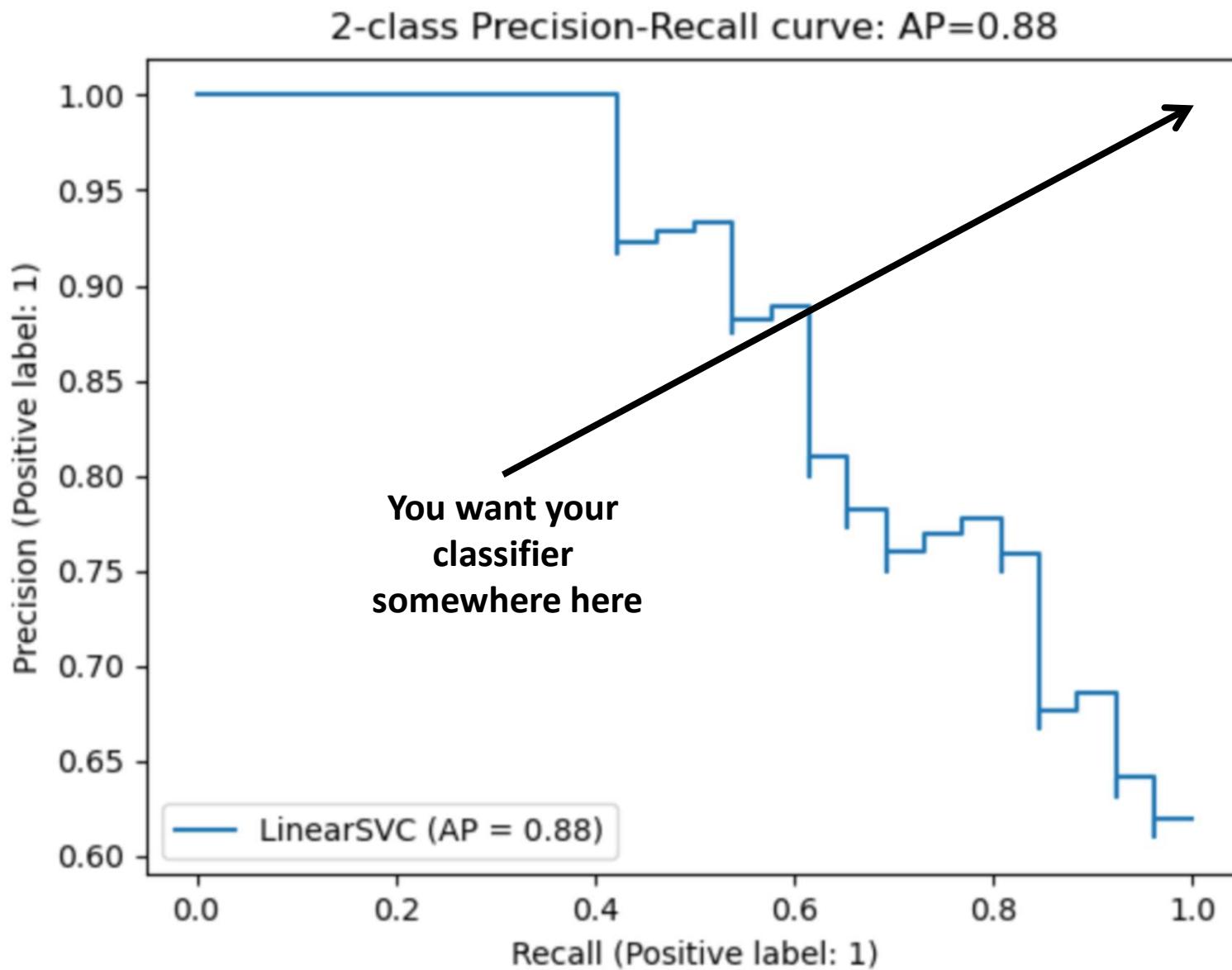


TPR: Sensitivity | FPR: 1 - Specificity

# Receiver Operating Characteristic



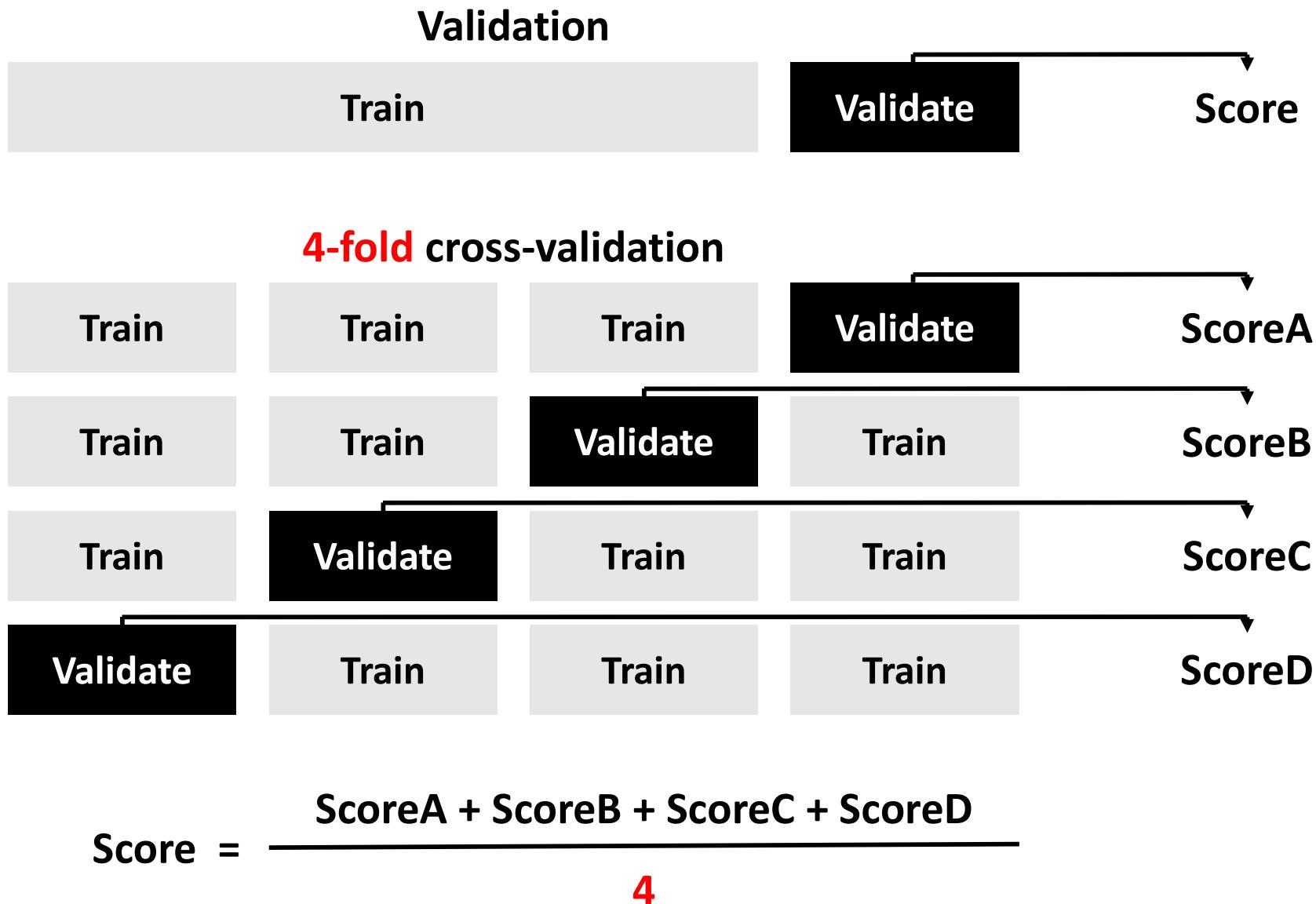
# Precision - Recall Curve



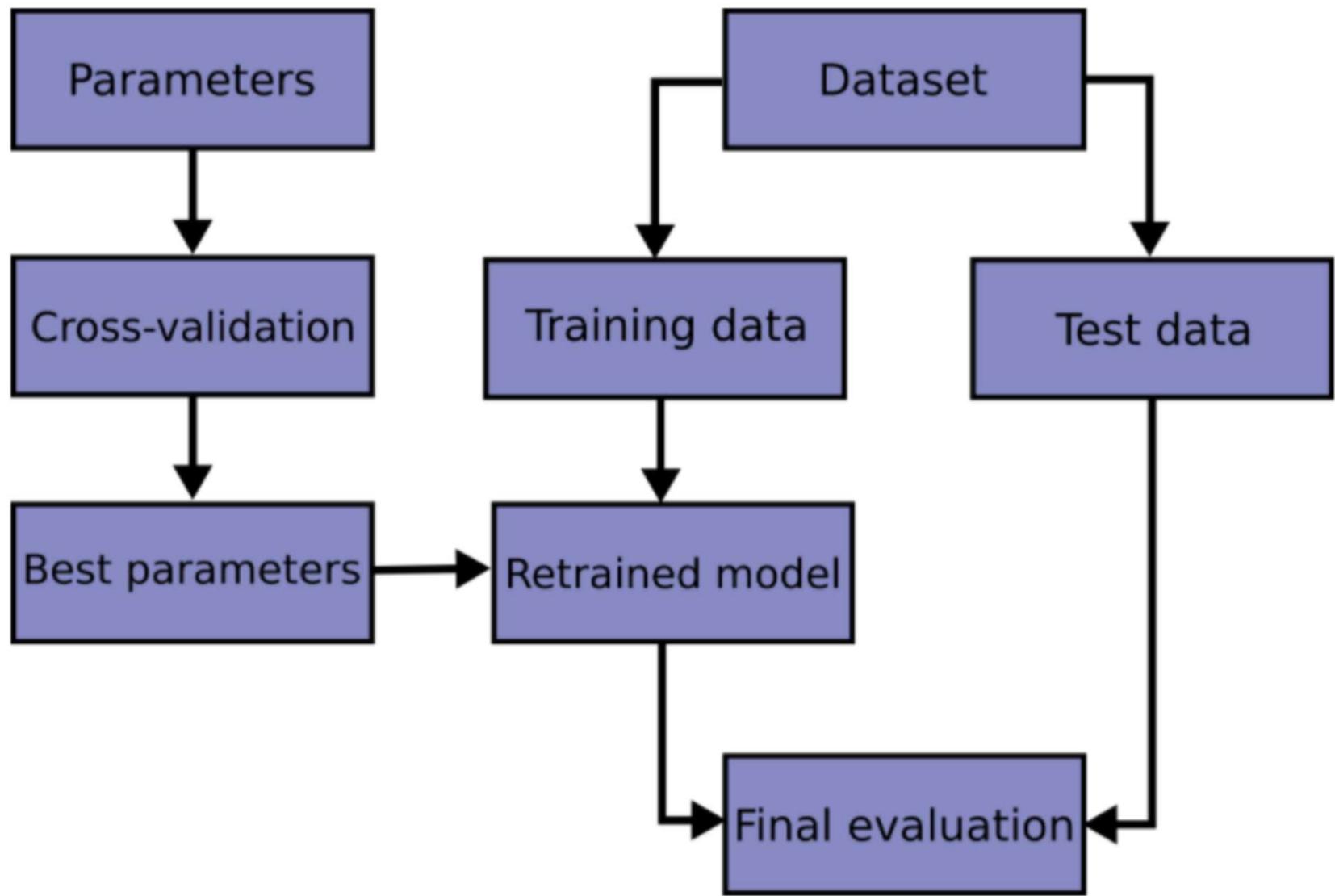
# ROC vs. Precision-Recall Curves

- Both summarize model performance using different probability thresholds
- **ROC curves** should be used when there are roughly equal numbers of observations for each class
- **Precision-Recall curves** should be used when there is a **moderate to large class imbalance** (when we are interested in the positive class and there's only a few positive samples)

# K-Fold Cross-Validation



# Parameter Tuning



# 3-class Confusion Matrix

		<i>gold labels</i>		
		urgent	normal	spam
<i>system output</i>	urgent	8	10	1
	normal	5	60	50
	spam	3	30	200

**precision<sub>u</sub>**=  $\frac{8}{8+10+1}$

**precision<sub>n</sub>**=  $\frac{60}{5+60+50}$

**precision<sub>s</sub>**=  $\frac{200}{3+30+200}$

**recall<sub>u</sub>**=  $\frac{8}{8+5+3}$

**recall<sub>n</sub>**=  $\frac{60}{10+60+30}$

**recall<sub>s</sub>**=  $\frac{200}{1+50+200}$

# **Macroaveraging and Microaveraging**

## **Macroaveraging:**

- compute the performance for each class, and then average over classes**

## **Microaveraging:**

- collect decisions for all classes into one confusion matrix**
- compute precision and recall from that table.**

# Macroaveraging and Microaveraging

Class 1: Urgent		Class 2: Normal		Class 3: Spam		Pooled	
true	true	true	true	true	true	true	true
urgent	not	normal	not	spam	not	yes	no
system	8	11	60	55	200	33	268
urgent	8	340	40	212	51	83	99
system							635

$$\text{precision} = \frac{8}{8+11} = .42$$

$$\text{precision} = \frac{60}{60+55} = .52$$

$$\text{precision} = \frac{200}{200+33} = .86$$

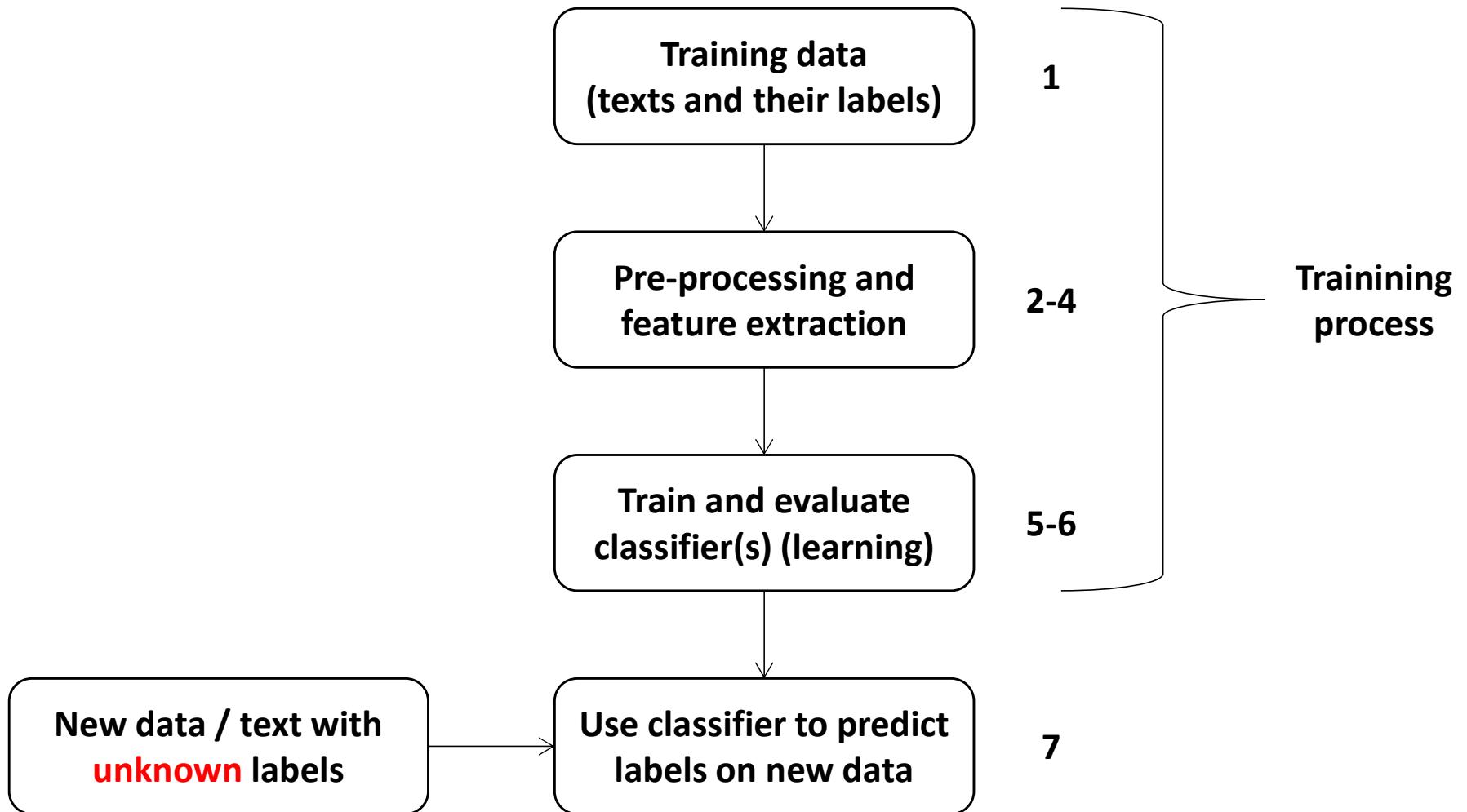
$$\text{microaverage precision} = \frac{268}{268+99} = .73$$

$$\text{macroaverage precision} = \frac{.42+.52+.86}{3} = .60$$

# Text Classification System Pipeline

1. Obtain / collect / create **labeled data set** suitable for the task
2. Split the data set into:
  - two (**training** and **test** sets) parts OR
  - three (**training**, **validation**, and **test** sets) parts
3. Choose **evaluation metric**
4. Transform raw text into **feature vectors**:
  - bag of words
  - other types
5. Using **feature vectors and labels** from the **training set**, **train the classifier / create a model**
6. Using **evaluation metric** from (3) **benchmark the classifier / model performance using the test set**
7. Deploy the classifier / model to serve a real world application and monitor its performance

# Text Classification System Pipeline



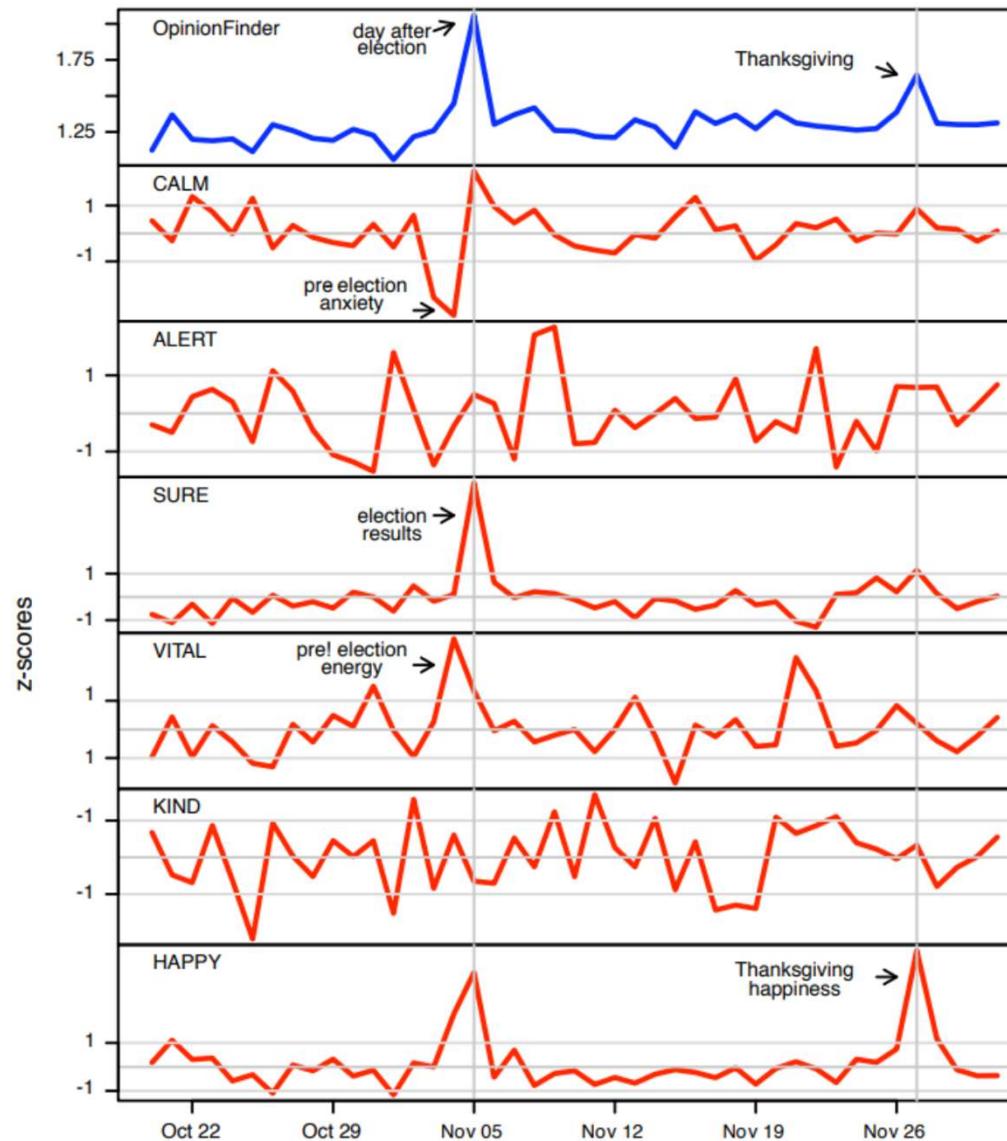
# Poor Classifier Performance: Reasons

1. With all possible features extracted, we ended up with a sparse feature vector (some features are too rare and end up being noise) → makes training hard
2. Few (~20%) relevant samples compared to non-relevant (~80%) samples in the data set → skews learning towards non-relevant data
3. Need better learning algorithm
4. Need better pre-processing / feature extraction
5. Classifier parameters / hyperparameters need tuning

# **Sentiment Analysis: Motivation**

- **Movie:** is this review positive or negative?
- **Products:** what do people think about the new iPhone?
- **Public sentiment:** what is consumer confidence?
- **Politics:** what do people think about this candidate or issue?
- **Prediction:** predict election outcomes or market trends from sentiment

# Sentiment Analysis: Twitter Mood



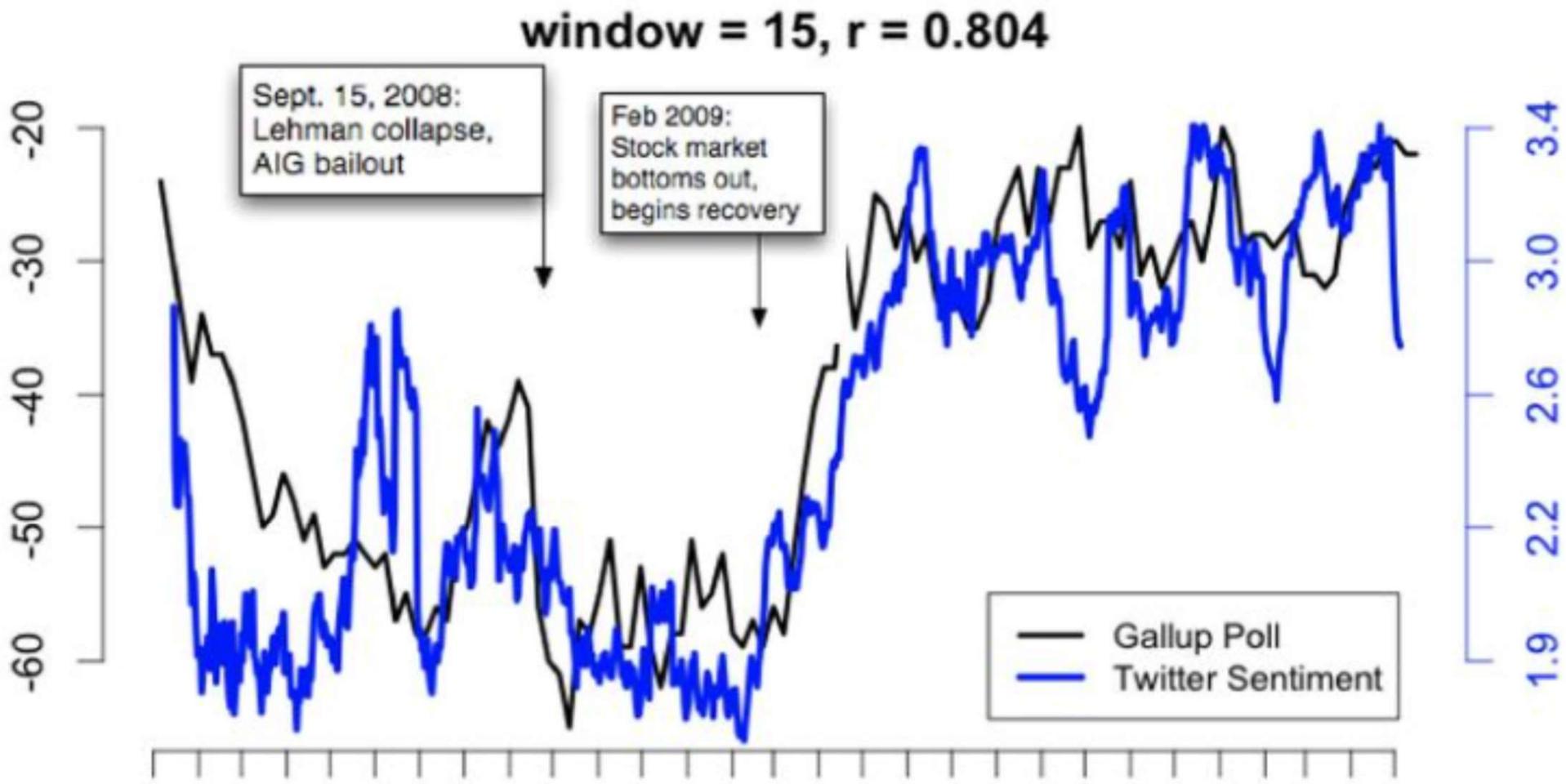
source: <https://arxiv.org/pdf/1010.3003.pdf>

# Sentiment Analysis: Tweets



source: [https://www.csc2.ncsu.edu/faculty/healey/tweet\\_viz/tweet\\_app/](https://www.csc2.ncsu.edu/faculty/healey/tweet_viz/tweet_app/)

# Sentiment Analysis: Text and Polls



source: <https://www.aaai.org/ocs/index.php/ICWSM/ICWSM10/paper/viewFile/1536/1842>

# Affective State

**Affective state:** any kind of **sentimental condition**, often in which someone's feelings control their consciousness.

# Scherer Typology of Affective States

- Emotion: brief organically synchronized ... evaluation of a major event
  - angry, sad, joyful, fearful, ashamed, proud, elated
- Mood: diffuse non-caused low-intensity long-duration change in subjective feeling
  - cheerful, gloomy, irritable, listless, depressed, buoyant
- Interpersonal stances: affective stance toward another person in a specific interaction
  - friendly, flirtatious, distant, cold, warm, supportive, contemptuous
- Attitudes: enduring, affectively colored beliefs, dispositions towards objects or persons
  - liking, loving, hating, valuing, desiring
- Personality traits: stable personality dispositions and typical behavior tendencies
  - nervous, anxious, reckless, morose, hostile, jealous

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# Sentiment Analysis: Detecting Attitude

Sentiment analysis deals with **detection of attitudes** (“enduring, affectively colored beliefs, dispositions towards objects or persons”). It involves four components:

1. Holder (**source**) of attitude
2. Target (**aspect**) of attitude
3. Type of attitude:
  - from a set of types: *like, love, hate, value, desire, etc.*
  - simple (**weighted**) polarity: *positive, negative, neutral (together with strength)*
4. Text / data containing attitude:
  - sentences,
  - entire documents, etc.

# **Sentiment Analysis: Other Names**

- Opinion extraction
- Opinion mining
- Sentiment mining
- Subjectivity analysis

# Sentiment Analysis: Complexity Levels

Sentiment analysis tasks can have different levels of complexity:

- Simple tasks:
  - decide if the attitude contained within text is positive or negative
- More complex / average complexity tasks:
  - rank that attitude on a scale from 1 to 5
- Advanced / complex tasks:
  - detect target (stance detection)
  - detect source
  - detect complex attitude types

# Sentiment Analysis: Baseline Algo

- Pre-processing: tokenization
- Feature extraction: bag of words, etc.
- Classification using a chosen classifier
  - Naive Bayes
  - Perceptron
  - Support Vector Machines
  - etc.

# Naive Bayes Classifier

category/class =  $\text{h}(\text{document})$

Finding model / hypothesis  $\text{h} \rightarrow$  Finding probabilities for  $y_{MAP}$

$$y_{MAP} \propto \underset{y \in Y}{\operatorname{argmax}} \left( P(y) * \prod_{i=1}^N P(x_i | y) \right)$$

Note: logarithms (to handle underflow) will be ignored in the following example

MAP: Maximum a posteriori (corresponds to the most likely class).

# Sentiment Analysis: Example

Training set	
$x_1$	just plain boring
$x_2$	entirely predictable and lacks energy
$x_3$	no surprises and very few laughs
$x_4$	very powerful
$x_5$	the most fun film of the summer
Test set	
$x_6$	predictable with no fun

$x_1, x_2, x_3, \dots, x_{N-2}, x_{N-1}, x_N$  - feature vectors (in **bold**) |  $y_1, y_2, y_3, \dots, y_{N-2}, y_{N-1}, y_N$  - labels

# Sentiment Analysis: Example

Training set		Learning
$x_1$	just plain boring	$y_1 = -$
$x_2$	entirely predictable and lacks energy	$y_2 = -$
$x_3$	no surprises and very few laughs	$y_3 = -$
$x_4$	very powerful	$y_4 = +$
$x_5$	the most fun film of the summer	$y_5 = +$
Test set		Note the add-1 smoothing!
$x_6$	predictable with no fun	$y_6 = ???$

Probability estimates:

Naive Bayes Classifier:

$$y_{MAP} \propto \underset{y \in Y}{\operatorname{argmax}} \left( P(y) * \prod_{i=1}^N P(x_i | y) \right)$$

Probability estimates (Maximum Likelihood estimation):

$$P(y = +) = \frac{N_{\text{samples labeled } +}}{N}$$

$$P(y = -) = \frac{N_{\text{samples labeled } -}}{N}$$

$$P(x_i = \text{word} | y = \text{CLASS}) = \frac{\text{count}(x_i = \text{word}, y = \text{CLASS}) + 1}{\sum_{x \in V} \text{count}(x, y = \text{CLASS}) + |V|}$$

$x_1, x_2, x_3, \dots, x_{N-2}, x_{N-1}, x_N$  - feature vectors (in **bold**) |  $y_1, y_2, y_3, \dots, y_{N-2}, y_{N-1}, y_N$  - labels

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Test set		
$x_6$	predictable with no fun	$y_6 = ???$

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# Sentiment Analysis: Example

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		<table border="1"><thead><tr><th>word</th><th>+</th><th>-</th></tr></thead><tbody><tr><td>just</td><td>0</td><td>1</td></tr><tr><td>plain</td><td>0</td><td>1</td></tr><tr><td>boring</td><td>0</td><td>1</td></tr><tr><td>entirely</td><td>0</td><td>1</td></tr><tr><td>predictable</td><td>0</td><td>1</td></tr><tr><td>and</td><td>0</td><td>2</td></tr><tr><td>lacks</td><td>0</td><td>1</td></tr><tr><td>energy</td><td>0</td><td>1</td></tr><tr><td>no</td><td>0</td><td>1</td></tr><tr><td>surprises</td><td>0</td><td>1</td></tr><tr><td>very</td><td>1</td><td>1</td></tr><tr><td>few</td><td>0</td><td>1</td></tr><tr><td>laughs</td><td>0</td><td>1</td></tr><tr><td>powerful</td><td>1</td><td>0</td></tr><tr><td>the</td><td>2</td><td>0</td></tr><tr><td>most</td><td>1</td><td>0</td></tr><tr><td>fun</td><td>1</td><td>0</td></tr><tr><td>film</td><td>1</td><td>0</td></tr><tr><td>of</td><td>1</td><td>0</td></tr><tr><td>summer</td><td>1</td><td>0</td></tr></tbody></table>	word	+	-	just	0	1	plain	0	1	boring	0	1	entirely	0	1	predictable	0	1	and	0	2	lacks	0	1	energy	0	1	no	0	1	surprises	0	1	very	1	1	few	0	1	laughs	0	1	powerful	1	0	the	2	0	most	1	0	fun	1	0	film	1	0	of	1	0	summer	1	0
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Test set		Other probabilities not shown
$x_6$	predictable <del>with</del> no fun	$y_6 = ???$
	unknown word (not in V) → ignore	

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# Sentiment Analysis: Example

Training set		Model
$x_1$	just plain boring	$y_1 = -$
$x_2$	entirely predictable and lacks energy	$y_2 = -$
$x_3$	no surprises and very few laughs	$y_3 = -$
$x_4$	very powerful	$y_4 = +$
$x_5$	the most fun film of the summer	$y_5 = +$
Test set		Other probabilities not shown
$x_6$	predictable <del>with</del> no fun	$y_6 = ???$
	unknown word (not in V) → ignore	

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# Sentiment Analysis: Example

Training set		Prediction	
$x_1$	just plain boring	$y_1 = -$	$P(y = +) = \frac{2}{5}$
$x_2$	entirely predictable and lacks energy	$y_2 = -$	$P(y = -) = \frac{3}{5}$
$x_3$	no surprises and very few laughs	$y_3 = -$	$P(x_i = \text{predictable}   y = +) = \frac{1}{29}$
$x_4$	very powerful	$y_4 = +$	$P(x_i = \text{no}   y = +) = \frac{1}{29}$
$x_5$	the most fun film of the summer	$y_5 = +$	$P(x_i = \text{fun}   y = +) = \frac{2}{29}$
Test set		$y_6 = ???$ predictable <del>with</del> no fun ↪ unknown word (not in V) → ignore	
$x_1, x_2, x_3, \dots, x_{N-2}, x_{N-1}, x_N$ - feature vectors (in <b>bold</b> )   $y_1, y_2, y_3, \dots, y_{N-2}, y_{N-1}, y_N$ - labels		<b>Label + case:</b> $P(y = +) * P(x_6   y = +) = \frac{2}{5} * \frac{1}{29} * \frac{1}{29} * \frac{2}{29}$ $= 3.2 * 10^{-5}$ <b>Label - case:</b> $P(y = -) * P(x_6   y = -) = \frac{3}{5} * \frac{2}{29} * \frac{2}{29} * \frac{1}{29}$ $= 6.1 * 10^{-5}$	

# Sentiment Analysis: Example

Training set		Model	
$x_1$	just plain boring	$y_1 = -$	$P(y = +) = \frac{2}{5}$
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$x_3$	no surprises and very few laughs	$y_3 = -$	$P(x_i = \text{predictable}   y = +) = \frac{1}{29}$
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# Sentiment Analysis: Feature Extraction

- What should we extract?
  - just **adjectives**?
  - or perhaps **all words**?
- Extracting **all words** is likely to work better

# Optimizing for Sentiment Analysis

- For tasks like sentiment, word **occurrence** seems to be **more important than word frequency**
  - the occurrence of the word *fantastic* tells us a lot
  - the fact that it occurs 5 times may not tell us much more.
- Use binary multinomial Naive Bayes, or binary NB
  - clip word counts at 1 (1 per document even if more)

# Sentiment Analysis: Binarization

## Four original documents:

- it was pathetic the worst part was the boxing scenes
- no plot twists or great scenes
- + and satire and great plot twists
- + great scenes great film

## After per-document binarization:

- it was pathetic the worst part boxing scenes
- no plot twists or great scenes
- + and satire great plot twists
- + great scenes film

	NB Counts		Binary Counts	
	+	-	+	-
and	2	0	1	0
boxing	0	1	0	1
film	1	0	1	0
great	3	1	2	1
it	0	1	0	1
no	0	1	0	1
or	0	1	0	1
part	0	1	0	1
pathetic	0	1	0	1
plot	1	1	1	1
satire	1	0	1	0
scenes	1	2	1	2
the	0	2	0	1
twists	1	1	1	1
was	0	2	0	1
worst	0	1	0	1

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duplicate words removed

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and	2	0	1	0
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scenes	1	2	1	2	
the	0	2	0	1	
twists	1	1	1	1	
was	0	2	0	1	
worst	0	1	0	1	

great and scenes appear in multiple documents

# Sentiment Analysis: Negations

Consider the following sentences / documents:

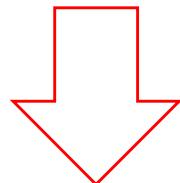
- *I really like this movie*
- *I really don't like this movie*
- **Negation changes the meaning of "like" to negative.**
- **Negation can also change negative to positive-ish**
  - *Don't dismiss this film*
  - *Doesn't let us get bored*

# Sentiment Analysis: Negations

Simple baseline method solution:

- Add **NOT\_** prefix to every word **between negation and following punctuation:**

*didn't like this movie , but I*



*didn't NOT\_like NOT\_this NOT\_movie , but I*

# Sentiment Analysis: Lexicons

What if we don't have enough labeled training data?

- In that case, we can make use of pre-built word lists → **lexicons**

There are various publicly available lexicons

# Sentiment Analysis: Lexicons

Add a **feature that gets a count whenever a word from the lexicon occurs:**

- for example: a feature called "this word occurs in the positive lexicon" or "this word occurs in the negative lexicon"
- all positive words (good, great, beautiful, wonderful) or negative words count for that feature.

Using 1-2 features isn't as good as using all the words.

But when training data is sparse or not representative of the test set, dense lexicon features can help

# MPQA Subjectivity Cues Lexicon

Home page:

[https://mpqa.cs.pitt.edu/lexicons/subj\\_lexicon/](https://mpqa.cs.pitt.edu/lexicons/subj_lexicon/)

6885 words from 8221 lemmas, annotated for intensity  
(strong/weak)

2718 positive

4912 negative

+ : admirable, beautiful, confident, dazzling, ecstatic, favor, glee, great

- : awful, bad, bias, catastrophe, cheat, deny, envious, foul, harsh, hate

# The General Inquirer

Home page:

<http://www.wjh.harvard.edu/~inquirer>

List of Categories:

<http://www.wjh.harvard.edu/~inquirer/homecat.htm>

Categories:

- Positive (1915 words) and Negative (2291 words)
- Strong vs Weak, Active vs Passive, Overstated versus Understated
- Pleasure, Pain, Virtue, Vice, Motivation, Cognitive Orientation, etc

Free for Research Use!

# Sentiment Analysis: Lexicons

What if there is no lexicon for a given domain?

- In that case, we can learn it:
  - start with a few labeled examples and hand-built patterns
  - build lexicon using the procedure below:

```
function BUILDSENTIMENTLEXICON(posseeds,negseeds) returns poslex,neglex
  poslex  $\leftarrow$  posseeds
  neglex  $\leftarrow$  negseeds
  Until done
    poslex  $\leftarrow$  poslex + FINDSIMILARWORDS(poslex)
    neglex  $\leftarrow$  neglex + FINDSIMILARWORDS(neglex)
  poslex,neglex  $\leftarrow$  POSTPROCESS(poslex,neglex)
```

# Identifying Word Polarity

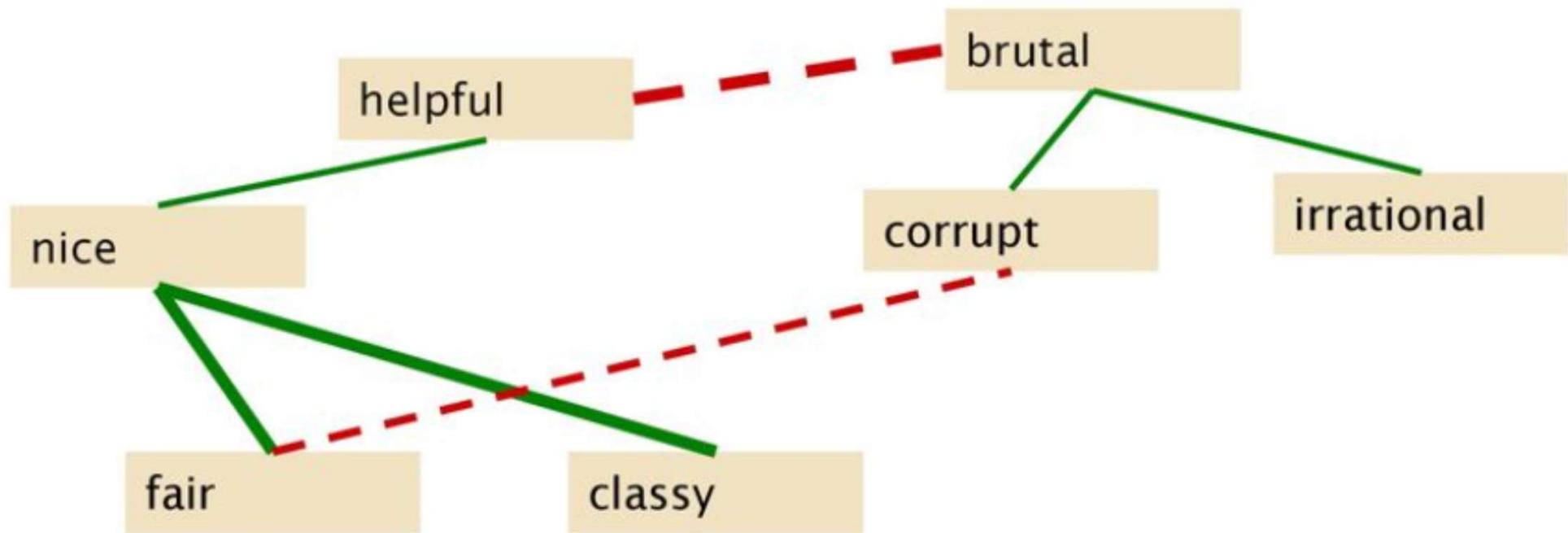
## Intuition:

- words joined by “*and*” have the same polarity:
  - *fair and legitimate, corrupt and brutal*
- words joined by “*but*” do not:
  - *fair, but brutal*

# Sentiment Analysis: Learning Lexicons

- Motivation:
  - learn a domain-specific lexicon
  - more words (more robust) than off-the-shelf lexicon
- Intuition:
  - start with “seed” words (*good*, *poor*)
  - find other words with similar polarity:
    - use “*and*” and “*but*”
    - use nearby words in the same document
    - add them to lexicon

# Identifying Word Polarity: Graph



# Sentiment Analysis: Challenges

## Subtlety:

- Perfume review in Perfumes: The Guide:
  - *If you are reading this because it is your darling fragrance, please wear it at home exclusively and tape the windows shut*
- Dorothy Parker (writer) on Katherine Hepburn (actress):
  - *She runs the gamut of emotions from A to B*

# Sentiment Analysis: Challenges

## Thwarted expectations:

- “*This film should be brilliant. It sounds like a great plot, the actors are first grade, and the supporting cast is good as well, and Stallone is attempting to deliver a good performance. However it can't hold up.*”

# Sentiment Analysis: Challenges

## Ordering effect:

- “Well as usual Keanu Reeves is nothing special, but surprisingly, the **very talented** Laurence Fishbourne **not so good** either. I was surprised.”

# Sentiment Analysis: Example

It's **hokey**. There are virtually **no** surprises , and the writing is **second-rate**.  
So why was it so **enjoyable**? For one thing , the cast is  
**great**. Another **nice** touch is the music **I** was overcome with the urge to get off  
the couch and start dancing . It sucked **me** in , and it'll do the same to **you** .

$x_1=3$        $x_5=0$        $x_6=4.19$        $x_2=2$        $x_3=1$        $x_4=3$

## Feature vector:

Var	Definition	Value
$x_1$	count(positive lexicon) $\in$ doc	3
$x_2$	count(negative lexicon) $\in$ doc)	2
$x_3$	$\begin{cases} 1 & \text{if "no" } \in \text{doc} \\ 0 & \text{otherwise} \end{cases}$	1
$x_4$	count(1st and 2nd pronouns $\in$ doc)	3
$x_5$	$\begin{cases} 1 & \text{if "!" } \in \text{doc} \\ 0 & \text{otherwise} \end{cases}$	0
$x_6$	$\log(\text{word count of doc})$	$\ln(66) = 4.19$

# Sentiment Analysis: Example

Feature vector  $\mathbf{x}$ :

Var	Definition	Value
$x_1$	$\text{count}(\text{positive lexicon}) \in \text{doc}$	3
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$x_4$	$\text{count}(1\text{st and 2nd pronouns } \in \text{doc})$	3
$x_5$	$\begin{cases} 1 & \text{if "!" } \in \text{doc} \\ 0 & \text{otherwise} \end{cases}$	0
$x_6$	$\ln(66) = 4.19$	

What is  $\mathbf{w} \cdot \mathbf{x} + b$  ???

Suppose:  $\mathbf{w} = [2.5, 5.0, 1.2, 0.5, 2.0, 0.7]$   
and  $b = 0.1$

# Sentiment Analysis: Example

$$\begin{aligned} p(+|x) = P(Y = 1|x) &= \sigma(w \cdot x + b) \\ &= \sigma([2.5, -5.0, -1.2, 0.5, 2.0, 0.7] \cdot [3, 2, 1, 3, 0, 4.19] + 0.1) \\ &= \sigma(.833) \\ &= 0.70 \end{aligned}$$

$$\begin{aligned} p(-|x) = P(Y = 0|x) &= 1 - \sigma(w \cdot x + b) \\ &= 0.30 \end{aligned}$$

Positive sentiment

# Period Disambiguation: Example

This ends in a period.

The house at 465 Main St. is new.

End of sentence  
Not end

Feature vector 

$$x_1 = \begin{cases} 1 & \text{if } \text{"Case}(w_i) = \text{Lower"} \\ 0 & \text{otherwise} \end{cases}$$

$$x_2 = \begin{cases} 1 & \text{if } w_i \in \text{AcronymDict} \\ 0 & \text{otherwise} \end{cases}$$

$$x_3 = \begin{cases} 1 & \text{if } w_i = \text{St.} \& \text{Case}(w_{i-1}) = \text{Cap"} \\ 0 & \text{otherwise} \end{cases}$$

# What do Words Mean?

In methods (N-grams, text classification, etc.) we've seen:

- words are just strings
- **meaning** is not considered

**Meaning** in logic:

- The meaning of "dog" is DOG (predicates and symbols)  
$$\forall x \text{ DOG}(x) \rightarrow \text{MAMMAL}(x)$$

Old linguistics joke by Barbara Partee in 1967:

- Q: What's the **meaning** of life?
- A: LIFE

That is not very helpful.

# Words: Lemmas and Senses

**lemma**

**mouse** (Noun)

1. any of numerous small rodents...
2. a hand-operated device that controls a cursor...

**senses**

from the online thesaurus WordNet

# Words: Lemmas and Senses

lemma

mouse (Noun)

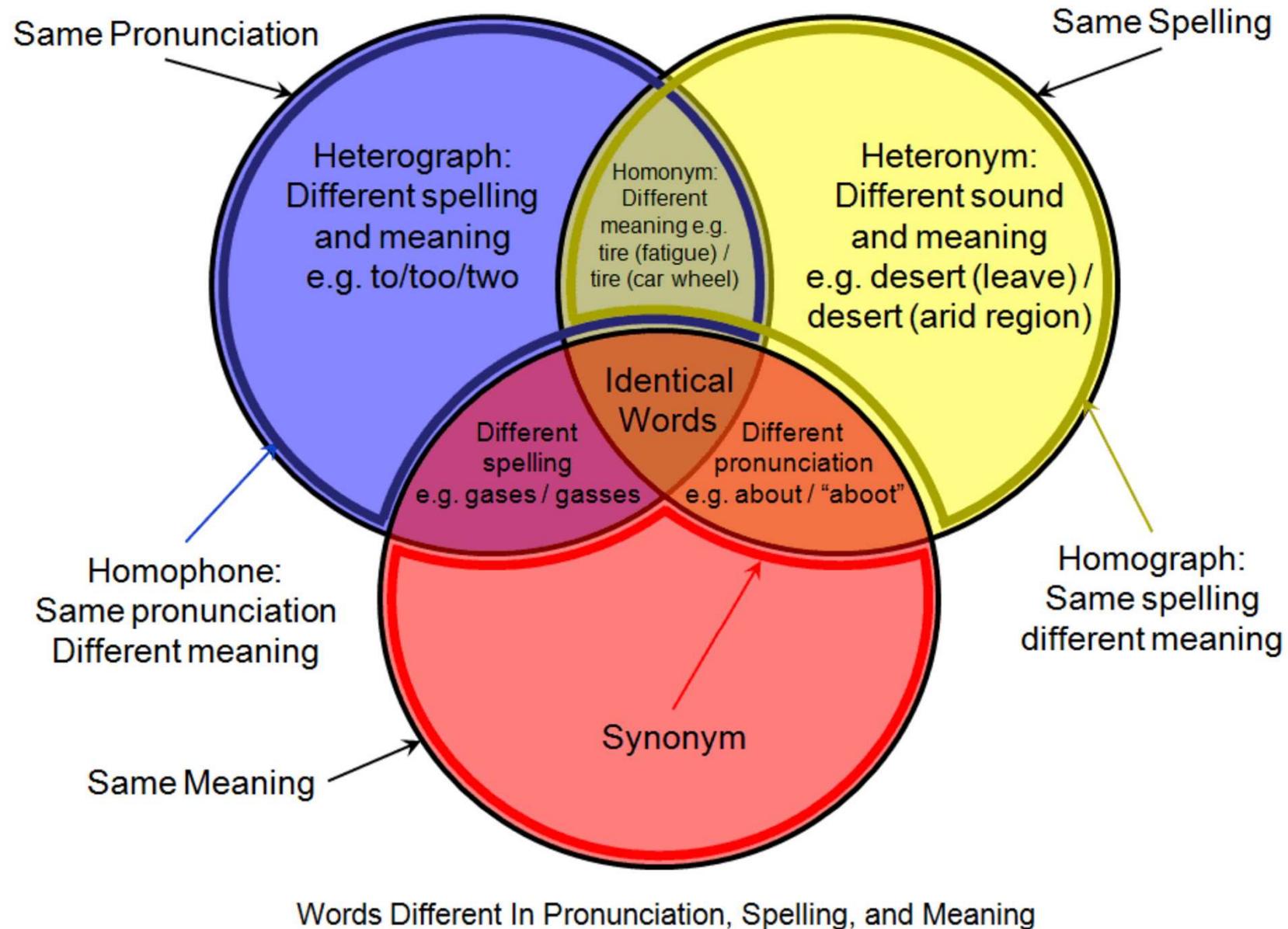
1. any of numerous small rodents...
2. a hand-operated device that controls a cursor...

senses

from the online thesaurus WordNet

- A **sense** or “concept” is the meaning component of a word
- **Lemmas** can be **polysemous** (have multiple **senses**)

# Relationships Between Words



Source: <https://owlcation.com/humanities/Lexical-Relations-Describing-Similarities-In-The-English-Language>

# Lexical Relationships

Lexical relationships are the connections established between one word and another:

- **Synonymy** is the idea that some words have the same meaning as others
  - *quick* is similar to *fast*
- **Antonymy** is precisely the opposite of synonymy
  - *good* is the opposite *bad*
- **Hyponymy** is similar to the notion of embeddedness
  - *Human* ← *Female* (*Female* is a more specific concept than *Human*)
- **Holonomy** and **Meronymy** describe relationships between an object and its parts:
  - *tree* is a holonym of *bark* (*tree* has bark)
  - *bark* is a meronym of *tree* (*bark* is a part of *tree*)

# Lexical Semantics: Definition

## Lexical semantics:

*the branch of linguistics and logic concerned with **meaning**.*

*There are a number of branches and subbranches of semantics, including:*

- **formal semantics**, which studies the logical aspects of **meaning**, such as **sense**, **reference**, **implication**, and **logical form**,
- **lexical semantics**, which studies **word meanings** and **word relations**, and **conceptual semantics**, which studies the **cognitive structure of meaning**.

from Oxford Dictionary

# Sense Relationships: Synonymy

- **Synonyms have the **same meaning** in some or all contexts:**
  - *filbert / hazelnut*
  - *couch / sofa*
  - *big / large*
  - *automobile / car*
  - *vomit / throw up*
  - *water / H<sub>2</sub>O*

# Sense Relationships: Synonymy

- There are probably **no examples of perfect synonymy:**
  - many aspects of meaning maybe identical, but not necessarily all aspects
- words may differ based on:
  - politeness
  - slang
  - register,
  - genre, etc.

# Sense Relationships: Synonymy?

- Some examples:

- *water / H<sub>2</sub>O*

- Would "H<sub>2</sub>O" be used in a surfing guide?

- *car / automobile*

- *big / large*

- *my big sister* is NOT always going to be synonymous with *my large sister*

# The Linguistic Principle of Contrast

- Substitutions between some pairs of words like *car / automobile* or *water / H<sub>2</sub>O* are **truth preserving**, the words are still not identical in meaning
- The Linguistic Principle of Contrast difference in form → difference in meaning

# Sense Relationships: Similarity

- Words with similar meanings.
- Not synonyms, but sharing some element of meaning
- Some examples:
  - *cow / horse*
  - *car / bicycle*

# Sense Relationships: Similarity

- Knowing **how similar two words** are can:
  - help in computing **how similar the meaning of two phrases or sentences** are
  - assist in **higher level tasks**:
    - question answering
    - paraphrasing
    - summarization

# Sense Relationships: Similarity

Human-evaluated word similarity:

Word 1	Word 2	Similarity [0-10]
<i>vanish</i>	<i>disappear</i>	9.8
<i>behave</i>	<i>obey</i>	7.3
<i>belief</i>	<i>impression</i>	5.95
<i>muscle</i>	<i>bone</i>	3.65
<i>modest</i>	<i>flexible</i>	0.98
<i>hole</i>	<i>agreement</i>	0.3

Source: SimLex-999 dataset (Hill et al., 2015) | <https://fh295.github.io/simlex.html>

# Sense Relationships: Relatedness

- Also called "**word association**"
- Words can be **related** in any way, for example via a semantic frame or field
- Some examples:
  - *coffee, tea:* **similar**
  - *coffee, cup:* **related, not similar**

# Semantic Frame: Definition

## Semantic Frame:

*a semantic frame is defined as a **coherent structure of concepts that are related** such that **without knowledge of all of them, one does not have complete knowledge of one** of the either*

**from** [https://cogling.fandom.com/wiki/Semantic\\_frame](https://cogling.fandom.com/wiki/Semantic_frame)

# Semantic Field: Definition

## Semantic Field:

*a **lexical set** of semantically **related items***

from Oxford Dictionary

# Semantic Field

Words that

- cover a particular semantic domain
- bear structured relations with each other.

hospitals

*surgeon, scalpel, nurse, anaesthetic, hospital*

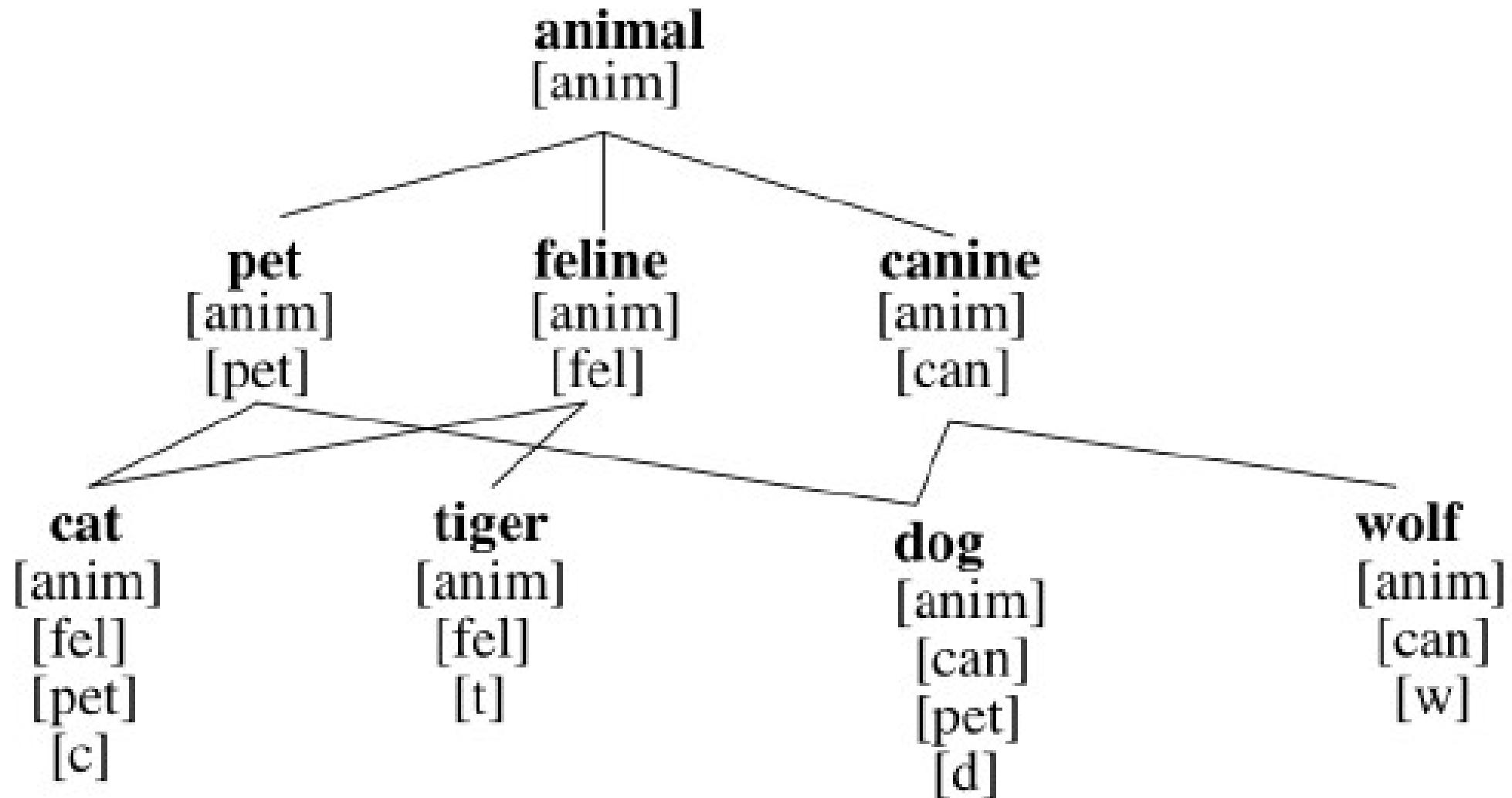
restaurants

*waiter, menu, plate, food, menu, chef*

houses

*door, roof, kitchen, family, bed*

# Semantic Field



Source: Helge Dyvik - "Translations as a semantic knowledge source"

# Sense Relationships: Antonymy

- Senses that are **opposites with respect to only one feature of meaning**
- Otherwise, they are **very similar (sharing some element of meaning):**
  - *dark/light short/long fast/slow*
  - *hot/cold up/down in/out*

# Sense Relationships: Antonymy

- More formally, **antonyms** can
  - define a **binary opposition** or be at **opposite ends of a scale**:
    - *long / short, fast / slow*
  - **be reversives**:
    - *rise/fall, up/down*

# Words and Meaning: Connotations

- Words have **affective** meanings
  - positive connotations (*happy*)
  - negative connotations (*sad*)
- Connotations can be **subtle**:
  - positive connotation: *copy, replica, reproduction*
  - negative connotation: *fake, knockoff, forgery*
- Evaluation (sentiment):
  - positive evaluation (*great, love*)
  - negative evaluation (*terrible, hate*)

# Words and Meaning: Connotations

- Words seem to vary along **three affective dimensions:**
  - **valence:** the pleasantness of the stimulus
  - **arousal:** the intensity of emotion provoked by the stimulus
  - **dominance:** the degree of control exerted by the stimulus

	Word	Score		Word	Score
valence	love	1.000		toxic	0.008
	happy	1.000		nightmare	0.005
arousal	elated	0.960		mellow	0.069
	frenzy	0.965		napping	0.046
dominance	powerful	0.991		weak	0.045
	leadership	0.983		empty	0.081

Source: NRC VAD Lexicon (<https://saifmohammad.com/WebPages/nrc-vad.html>)

# Words and Meaning: Summary

- Concepts or word **senses**
  - have a complex many-to-many association with words (homonymy, multiple **senses**)
- Have **relations** with each other
  - **synonymy**
  - **antonymy**
  - **similarity**
  - **relatedness**
  - **connotation**

# WordNet

**WordNet® is a large lexical database of English.**  
**Nouns, verbs, adjectives and adverbs are grouped into sets of cognitive synonyms (synsets), each expressing a distinct concept.**

**Synsets are interlinked by means of conceptual-semantic and lexical relations.**

**Link: <https://wordnet.princeton.edu/>**

# Challenge

- We know word relationships exist
- How can we quantify them in a automated fashion?
- How do we represent them in numerical way?
- How can we use them in computational models and processes?