

1. The length of a side of a cube is chosen at random from the uniform distribution on the interval $[4, 8]$. Calculate i) The probability that the length of the side is between 5 and 6 ii) The probability that the volume of the cube is between 27 and 216. iii) The expected volume of the cube.
2. The density function of the random variable X is given by $f(x)=cx^2$ for $x \in [3,6]$, otherwise $f(x)=0$. Calculate i) the value of the constant c ii) $P(4 \leq X \leq 5)$ iii) $E(X)$, $Var(X)$ and the k -th moment of X . iv) the cumulative distribution function of X , $F_X(x)$. v) find the median and upper quartile of this distribution.