

## 0.1 Application to MCS

Let  $\hat{\beta}$  denote the least square estimate of  $\beta$  based upon the full set of observations, and let  $\hat{\beta}^{(k)}$  denoted the estimate with the  $k^{th}$  case excluded.

## 0.2 Grubbs' Data

For the Grubbs data the  $\hat{\beta}$  estimated are  $\hat{\beta}_0$  and  $\hat{\beta}_1$  respectively. Leaving the fourth case out, i.e.  $k = 4$  the corresponding estimates are  $\hat{\beta}_0^{-4}$  and  $\hat{\beta}_1^{-4}$

$$Y^{-Q} = \hat{\beta}^{-Q} X^{-Q} \tag{1}$$

When considering the regression of case-wise differences and averages, we write  $D^{-Q} = \hat{\beta}^{-Q} A^{-Q}$

	F	C	D	A
1	793.80	794.60	-0.80	794.20
2	793.10	793.90	-0.80	793.50
3	792.40	793.20	-0.80	792.80
4	794.00	794.00	0.00	794.00
5	791.40	792.20	-0.80	791.80
6	792.40	793.10	-0.70	792.75
7	791.70	792.40	-0.70	792.05
8	792.30	792.80	-0.50	792.55
9	789.60	790.20	-0.60	789.90
10	794.40	795.00	-0.60	794.70
11	790.90	791.60	-0.70	791.25
12	793.50	793.80	-0.30	793.65

$$Y^{(k)} = \hat{\beta}^{(k)} X^{(k)} \quad (2)$$

Consider two sets of measurements , in this case F and C , with the vectors of case-wise averages  $A$  and case-wise differences  $D$  respectively. A regression model of differences on averages can be fitted with the view to exploring some characteristics of the data.

When considering the regression of case-wise differences and averages, we write

$$D^{-Q} = \hat{\beta}^{-Q} A^{-Q} \quad (3)$$

Let  $\hat{\beta}$  denote the least square estimate of  $\beta$  based upon the full set of observations, and let  $\hat{\beta}^{(k)}$  denoted the estimate with the  $k^{th}$  case excluded.

For the Grubbs data the  $\hat{\beta}$  estimated are  $\hat{\beta}_0$  and  $\hat{\beta}_1$  respectively. Leaving the fourth case out, i.e.  $k = 4$  the corresponding estimates are  $\hat{\beta}_0^{-4}$  and  $\hat{\beta}_1^{-4}$

$$Y^{(k)} = \hat{\beta}^{(k)} X^{(k)} \quad (4)$$

Consider two sets of measurements , in this case F and C , with the vectors of case-wise averages  $A$  and case-wise differences  $D$  respectively. A regression model of differences on averages can be fitted with the view to exploring some characteristics of the data.

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Call: lm(formula = D ~ A)
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Coefficients: (Intercept)          A
-37.51896      0.04656
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When considering the regression of case-wise differences and averages, we write

$$D^{-Q} = \hat{\beta}^{-Q} A^{-Q} \tag{5}$$

# Bibliography