0.1 CPJ's Three Propositions

0.2 The CPJ Paper

0.2.1 Case-Deletion results for Variance components

? examines case deletion results for estimates of the variance components, proposing the use of one-step estimates of variance components for examining case influence. The method describes focuses on REML estimation, but can easily be adapted to ML or other methods.

This paper develops their global influences for the deletion of single observations in two steps: a one-step estimate for the REML (or ML) estimate of the variance components, and an ordinary case-deletion diagnostic for a weighted regression problem (conditional on the estimated covariance matrix) for fixed effects.

0.2.2 CPJ Notation

$$\boldsymbol{C} = \boldsymbol{H}^{-1} = \begin{bmatrix} c_{ii} & \boldsymbol{c}_i' \\ \boldsymbol{c}_i & \boldsymbol{C}_{[i]} \end{bmatrix}$$

? noted the following identity:

$$\boldsymbol{H}_{[i]}^{-1} = \boldsymbol{C}_{[i]} - \frac{1}{c_{ii}} \boldsymbol{c}_{[i]} \boldsymbol{c}_{[i]}'$$

? use the following as building blocks for case deletion statistics.

- $\breve{x}_i$
- $\breve{z}_i$
- $\breve{z}_i j$
- $\breve{y}_i$
- $p_i i$
- m_i

All of these terms are a function of a row (or column) of $\boldsymbol{H}$ and $\boldsymbol{H}_{[i]}^{-1}$

0.3 Matrix Notation for Case Deletion

0.3.1 Case deletion notation

For notational simplicity, $\boldsymbol{A}(i)$ denotes an $n \times m$ matrix $\boldsymbol{A}$ with the i-th row removed, a_i denotes the i-th row of $\boldsymbol{A}$, and a_{ij} denotes the $(i, j)-$th element of $\boldsymbol{A}$.

0.3.2 Partitioning Matrices

Without loss of generality, matrices can be partitioned as if the $i-$th omitted observation is the first row; i.e. $i = 1$.

0.4 CPJ's Three Propositions

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.4.1 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.4.2 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.4.3 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.4.4 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.

0.5 The CPJ Paper

0.5.1 Case-Deletion results for Variance components

? examines case deletion results for estimates of the variance components, proposing the use of one-step estimates of variance components for examining case influence. The method describes focuses on REML estimation, but can easily be adapted to ML or other methods.

This paper develops their global influences for the deletion of single observations in two steps: a one-step estimate for the REML (or ML) estimate of the variance components, and an ordinary case-deletion diagnostic for a weighted regression problem (conditional on the estimated covariance matrix) for fixed effects.

0.5.2 CPJ Notation

$$\boldsymbol{C} = \boldsymbol{H}^{-1} = \begin{bmatrix} c_{ii} & \boldsymbol{c}_i' \\ \boldsymbol{c}_i & \boldsymbol{C}_{[i]} \end{bmatrix}$$

? noted the following identity:

$$\boldsymbol{H}_{[i]}^{-1} = \boldsymbol{C}_{[i]} - \frac{1}{c_{ii}} \boldsymbol{c}_{[i]} \boldsymbol{c}_{[i]}'$$

? use the following as building blocks for case deletion statistics.

- $\breve{x}_i$
- $\breve{z}_i$
- $\breve{z}_i j$
- $\breve{y}_i$
- $p_i i$
- m_i

All of these terms are a function of a row (or column) of $\boldsymbol{H}$ and $\boldsymbol{H}_{[i]}^{-1}$

0.6 The CPJ Paper

0.6.1 Case-Deletion results for Variance components

? examines case deletion results for estimates of the variance components, proposing the use of one-step estimates of variance components for examining case influence. The method describes focuses on REML estimation, but can easily be adapted to ML or other methods.

This paper develops their global influences for the deletion of single observations in two steps: a one-step estimate for the REML (or ML) estimate of the variance components, and an ordinary case-deletion diagnostic for a weighted regression problem (conditional on the estimated covariance matrix) for fixed effects.

0.6.2 CPJ Notation

$$\boldsymbol{C} = \boldsymbol{H}^{-1} = \begin{bmatrix} c_{ii} & \boldsymbol{c}'_i \\ \boldsymbol{c}_i & \boldsymbol{C}_{[i]} \end{bmatrix}$$

? noted the following identity:

$$\boldsymbol{H}^{-1}_{[i]} = \boldsymbol{C}_{[i]} - \frac{1}{c_{ii}} \boldsymbol{c}_{[i]} \boldsymbol{c}'_{[i]}$$

? use the following as building blocks for case deletion statistics.

- $\breve{x}_i$
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- $\breve{z}_i j$
- $\breve{y}_i$
- $p_i i$
- m_i

All of these terms are a function of a row (or column) of $\boldsymbol{H}$ and $\boldsymbol{H}^{-1}_{[i]}$

0.7 Matrix Notation for Case Deletion

0.7.1 Case deletion notation

For notational simplicity, $\boldsymbol{A}(i)$ denotes an $n \times m$ matrix $\boldsymbol{A}$ with the i-th row removed, a_i denotes the i-th row of $\boldsymbol{A}$, and a_{ij} denotes the $(i, j)-$th element of $\boldsymbol{A}$.

0.7.2 Partitioning Matrices

Without loss of generality, matrices can be partitioned as if the $i-$th omitted observation is the first row; i.e. $i = 1$.

0.8 CPJ's Three Propositions

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.8.1 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.8.2 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.

0.9 The CPJ Paper

0.9.1 Case-Deletion results for Variance components

? examines case deletion results for estimates of the variance components, proposing the use of one-step estimates of variance components for examining case influence. The method describes focuses on REML estimation, but can easily be adapted to ML or other methods.

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0.9.2 CPJ Notation

$$\boldsymbol{C} = \boldsymbol{H}^{-1} = \begin{bmatrix} c_{ii} & \boldsymbol{c}'_i \\ \boldsymbol{c}_i & \boldsymbol{C}_{[i]} \end{bmatrix}$$

? noted the following identity:

$$\boldsymbol{H}^{-1}_{[i]} = \boldsymbol{C}_{[i]} - \frac{1}{c_{ii}} \boldsymbol{c}_{[i]} \boldsymbol{c}'_{[i]}$$

? use the following as building blocks for case deletion statistics.

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- $\breve{y}_i$
- $p_i i$
- m_i

All of these terms are a function of a row (or column) of $\boldsymbol{H}$ and $\boldsymbol{H}^{-1}_{[i]}$

0.10 CPJ's Three Propositions

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.10.1 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.10.2 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.

0.11 The CPJ Paper

0.11.1 Case-Deletion results for Variance components

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0.11.2 CPJ Notation

$$\boldsymbol{C} = \boldsymbol{H}^{-1} = \begin{bmatrix} c_{ii} & \boldsymbol{c}_i' \\ \boldsymbol{c}_i & \boldsymbol{C}_{[i]} \end{bmatrix}$$

? noted the following identity:

$$\boldsymbol{H}^{-1}_{[i]} = \boldsymbol{C}_{[i]} - \frac{1}{c_{ii}} \boldsymbol{c}_{[i]} \boldsymbol{c}'_{[i]}$$

? use the following as building blocks for case deletion statistics.

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- $\breve{z}_i$
- $\breve{z}_i j$
- $\breve{y}_i$
- $p_i i$
- m_i

All of these terms are a function of a row (or column) of $\boldsymbol{H}$ and $\boldsymbol{H}^{-1}_{[i]}$

0.12 CPJ's Three Propositions

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.12.1 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.12.2 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.

0.13 CPJ's Three Propositions

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.13.1 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.13.2 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.

0.14 The CPJ Paper

0.14.1 Case-Deletion results for Variance components

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0.14.2 CPJ Notation

$$\boldsymbol{C} = \boldsymbol{H}^{-1} = \begin{bmatrix} c_{ii} & \boldsymbol{c}_i' \\ \boldsymbol{c}_i & \boldsymbol{C}_{[i]} \end{bmatrix}$$

? noted the following identity:

$$\boldsymbol{H}^{-1}_{[i]} = \boldsymbol{C}_{[i]} - \frac{1}{c_{ii}} \boldsymbol{c}_{[i]} \boldsymbol{c}'_{[i]}$$

? use the following as building blocks for case deletion statistics.

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- m_i

All of these terms are a function of a row (or column) of $\boldsymbol{H}$ and $\boldsymbol{H}^{-1}_{[i]}$

0.15 Matrix Notation for Case Deletion

0.15.1 Case deletion notation

For notational simplicity, $\boldsymbol{A}(i)$ denotes an $n \times m$ matrix $\boldsymbol{A}$ with the i-th row removed, a_i denotes the i-th row of $\boldsymbol{A}$, and a_{ij} denotes the $(i, j)-$th element of $\boldsymbol{A}$.

0.15.2 Partitioning Matrices

Without loss of generality, matrices can be partitioned as if the $i-$th omitted observation is the first row; i.e. $i = 1$.

0.16 CPJ's Three Propositions

Proposition 1

$$\boldsymbol{V}^{-1} = \begin{bmatrix} \nu^{ii} & \lambda_i' \\ \lambda_i & \Lambda_{[i]} \end{bmatrix}$$

$$\boldsymbol{V}_{[i]}^{-1} = \boldsymbol{\Lambda}_{[i]} - \frac{\lambda_i \lambda_i'}{\lambda_i}$$

0.16.1 Proposition 2

(i) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{X}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{X}$

(ii) $= (\boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y})^{-1}$

(iii) $\boldsymbol{X}_{[i]}^T \boldsymbol{V}_{[i]}^{-1} \boldsymbol{Y}_{[i]} = \boldsymbol{X}' \boldsymbol{V}^{-1} \boldsymbol{Y}$

0.16.2 Proposition 3

This proposition is similar to the formula for the one-step Newtown Raphson estimate of the logistic regression coefficients given by Pregibon (1981) and discussed in Cook Weisberg.