

Normal Distribution

(1)

 X : gestation periods

$$X \sim N(275, 4^2)$$

VARIANCE = 16 = 4²

Questions

i) $P(X \geq 280)$

Z score

$$Z_0 = \frac{x_0 - \mu}{\sigma} = \frac{280 - 275}{4} = \frac{5}{4} = 1.25$$

From table $P(Z \geq 1.25) = 0.1056$

$$\therefore P(X \geq 280) = \underline{\underline{0.1056}}$$

ii) $P(X \leq 268)$

$$\begin{aligned} \text{Z score} &= \frac{x_0 - \mu}{\sigma} = \frac{268 - 275}{4} \\ &= -7/4 = -1.75 \end{aligned}$$

$$P(Z \leq -1.75) = P(Z \geq 1.75)$$

Symmetry Rule

$$P(X \leq 268) = P(Z \geq 1.75) \\ = \underline{\underline{0.0401}}$$

from MUKOOCH BARNES table 3

iii) $P(272 \leq X \leq 283)$ interval

$$= 1 - \left[\underset{\text{Too Low}}{P(X \leq 272)} + \underset{\text{Too High}}{P(X \geq 283)} \right]$$

$$P(X \leq 272)$$

$$\begin{aligned} \text{Z score : } Z_0 &= \frac{x_0 - \mu}{\sigma} = \frac{272 - 275}{4} \\ &= -0.75 \end{aligned}$$

$$P(Z \leq -0.75) = P(Z \geq 0.75)$$

Symmetry Rule.

$$P(X \leq 272) = P(Z \geq 0.75) \quad (3)$$

$$= \underline{\underline{0.2266}}$$

(From tables).

• $P(X \geq 283)$

Z score ≈ 2 .

workings

Skipped here

$$P(Z \geq 2) = 0.02275$$

$$\therefore P(X \geq 283) = \underline{\underline{0.02275}}$$

Put it Altogether

$$P(272 \leq X \leq 283)$$

$$= 1 - [0.2266 + 0.02275]$$

$$= 1 - 0.2494 \quad (\text{Rounded})$$

$$= 0.7506$$

iv) Find a value x_0 such that (4)

$$P(X \geq x_0) = 0.025$$

Check murdoch barnes tables

to find z_0 such that

$$P(Z \geq z_0) = 0.025$$

[or as close as you can get]

	0.06
1.9	0.0250

$$\underline{\underline{z_0 = 1.96}}$$

$$1.96 = \frac{x_0 - 275}{4} \quad \leftarrow \text{Z score formula}$$

$$7.84 = x_0 - 275$$

$$x_0 = \underline{\underline{282.84}}$$