

We can also get confidence intervals for the parameter estimates. These can be obtained either by profiling the likelihood function or by using the standard errors and assuming a normal distribution. Note that profiled CIs are not symmetric (although they are usually close to symmetric). If the 95% CI does not cross 0, the parameter estimate is statistically significant.

```
(ci <- confint(m))  
# default method gives profiled CIs  
Waiting for profiling to be done...  
      2.5 % 97.5 %  
pared    0.5282 1.5722  
public -0.6522 0.5191  
gpa       0.1076 1.1309  
confint.default(m) # CIs assuming normality  
      2.5 % 97.5 %  
pared    0.5268 1.569  
public -0.6426 0.525  
gpa       0.1051 1.127
```

Confidence Intervals

- ▶ The CIs for both `pared` and `gpa` do not include 0; `public` does.
- ▶ The estimates in the output are given in units of ordered logits, or ordered log odds.
- ▶ So for `pared`, we would say that for a one unit increase in `pared` (i.e., going from 0 to 1), we expect a 1.05 increase in the expected value of `apply` on the log odds scale, given all of the other variables in the model are held constant.

Confidence Intervals

- ▶ For gpa, we would say that for a one unit increase in gpa, we would expect a 0.62 increase in the expected value of apply in the log odds scale, given that all of the other variables in the model are held constant.

- ▶ The coefficients from the model can be somewhat difficult to interpret because they are scaled in terms of logs.
- ▶ Another way to interpret logistic regression models is to convert the coefficients into odds ratios.
- ▶ To get the Odds Ratios and confidence intervals, we just exponentiate the estimates and confidence intervals.

Odds Ratios

```
exp(coef(m))
  pared public    gpa
2.8511 0.9429 1.8514
# Odds Ratios and CIs
exp(cbind(OR = coef(m), ci))
      OR  2.5 % 97.5 %
pared  2.8511 1.6958  4.817
public 0.9429 0.5209  1.681
gpa    1.8514 1.1136  3.098
```

- ▶ These coefficients are called **proportional odds ratios** and we would interpret these pretty much as we would odds ratios from a binary logistic regression.
- ▶ For pared, we would say that for a one unit increase in parental education, i.e., going from 0 (Low) to 1 (High), the odds of "very likely" applying versus "somewhat likely" or "unlikely" applying combined are 2.85 greater, given that all of the other variables in the model are held constant.

- ▶ Similarly, the odds "very likely" or "somewhat likely" applying versus "unlikely" applying is 2.85 times greater, given that all of the other variables in the model are held constant.
- ▶ For gpa (and other continuous variables), the interpretation is that when a student's gpa moves 1 unit, the odds of moving from "unlikely" applying to "somewhat likely" or "very likely" applying (or from the lower and middle categories to the high category) are multiplied by 1.85.