Consider a binary decision problem with the following conditional p.d.fs.

The Bayes costs are given by

Coo = 0	Co1 = 2
C10 = 1	$C_{II} = D$

- · Determine the Bayes test y P(Ho) = 3.
- · Compute the associated Bayes' Risk.

1) compute the likelihood natro.

$$A(x) = \frac{f(x)H.}{f(x)Ho} = \frac{e^{-2|x|}}{\frac{1}{2}e^{-1|x|}}$$

$$A(x) = \frac{\left[e^{-|x|}\right]^2}{2\left[e^{-|x|}\right]}$$

$$\frac{C_{10} - C_{00}) P(H_0)}{(C_{01} - C_{11}) P(H_1)}$$

Therefore we need to compute 12

Logarithm of both side then negate

In [e-1x1] \$ In [/2]

|x| \$ - en[1/2]

therefore

| x 1 \$ 0.693

CAREFUL Operator Switches Direction

.. 0.693 is our threshold. The decision

Regions are

· Ro: 5 x: |x| > 0,693 }

· R: 2 x: 1x/< 0.693 }

P(D/Ho) = 50.693 1 e - 1×1 dx

 $= 2 \int_{0.2}^{0.693} e^{-x} dx = \int_{0}^{0.693} e^{-x} dx.$

e note of 1

See note about integration of absolute value functions.

$$P(D_0|H_1) = \int_{-\infty}^{-0.693} e^{2x} dx + \int_{0.693}^{\infty} e^{-2x} dx$$

$$= 2 \int_{0.693}^{\infty} e^{-2x} dx = 0.25.$$

Bayes Risk:

$$E = P(D_1 | H_0) P(H_0) \leftarrow cost = 1$$

$$+ 2 P(D_0 | H_1) P(H_1) \leftarrow cost = 2$$

$$= (0.5) \frac{2}{3} + 2(0.25) \frac{1}{3}$$

$$= 0.5$$
(see workings page 7)

Consider a binary decision problem with the following conditional Pdfs.

· Determine the Dayes test y P(Ho) = 1/2

· Compute the associated Bayes RISK.

$$A(x) = \frac{f(x|H_0)}{f(x|H_0)} = 2e^{-|x|}$$

$$\frac{1}{(2-0)^{1/2}} = \frac{1}{2}$$

decision operator Switches Direction The Decision Regions Are therefore

$$P(D_1|H_0) = 2 \int_0^{1.386} dx = 0.75$$

see note about integration of functions with absolute values.

$$P(H_a|D_i) = 2 \int_{1.386}^{\infty} e^{-2x} dx = 0.0625$$

Bayes Risk

$$C = (0.75 \times \frac{1}{2}) + 2(0.0625)(1/2) = 0.4375$$

* WORKINGS from Page 3

$$\int e^{-x} dx = -1 \cdot e^{-x}$$

$$2\int_{0.2}^{0.693} dx = \frac{2}{2} \left[-0.693 - -0.693 \right]$$

=
$$\frac{2}{2}\left[-\frac{1}{2}+1\right]$$
. dable regative

Workings from Page 4

$$\int e^{-2x} dx = \frac{e^{-2x}}{-2}$$

$$2\int_{0.693}^{\infty} e^{-2x} dx = 2\left[e^{-\infty} - \left(-\frac{e}{2}\right)\right]$$

$$= 2 \left[0 + 0.25 \right]$$