## Solving ODEs using Laplace tRANSforms

Solve

$$\frac{dy}{dt^2} + 2\frac{dy}{dt} + y = 1 + t$$

REMARK: THESE Boundary Condutions may be non-zero.

$$y''(t) + 2y'(t) + y = 1 + t$$

$$L(y') = S^2 Y(s) - S y(o) - y(o)$$

$$= S^2 Y(s)$$

• 
$$L(y') = 5Y(s) - y(o)$$
  
=  $SY(s)$  (x2)

$$(5^2 + 25 + 1) Y(s)$$

## RHS:

$$\int \left[1+t\right] = \frac{1}{s} + \frac{1}{s^2}$$

$$= \frac{s+1}{s^2}$$

$$Y(s)(s^2+2s+1) = \frac{5+1}{s^2}$$

$$\Upsilon(s) = \frac{(s+1)}{(s+1)^2(s^2)}$$

$$= \frac{1}{(S+1)(S)}$$

$$Y(s) = \frac{1}{(s+1)(s^2)} = \frac{A}{s+1} + \frac{Bs+c}{s^2}$$

$$= \frac{AS^{2} + BS^{2} + BS + CS + C}{(S+1)(S^{2})}$$

$$= \frac{(A+B)S^{2} + (B+C)S + C}{(S+1)(S^{2})}$$

$$Y(s) = \frac{1}{S+1} - \frac{1}{S} + \frac{1}{S^2}$$

$$y(t) = e^{-t} - 1 + t$$