

```
> Conc=c( 0, 5, 10, 15, 20, 25, 30)
> Abso=c( 0.003, 0.127, 0.251, 0.390, 0.498, 0.625, 0.763)
>
> length(Abso)
[1] 7
>
> mean(Abso)
[1] 0.3795714
```

```
> Conc=c( 0, 5, 10, 15, 20, 25, 30)
> Abso=c( 0.003, 0.127, 0.251, 0.390, 0.498, 0.625, 0.763)
> plot(Conc,Abso)
> length(Abso)
[1] 7
> mean(Abso)
[1] 0.3795714
> FitA=lm(Abso~Conc)
> summary(FitA)
```

```
Call:
lm(formula = Abso ~ Conc)

Residuals:
    1         2         3         4         5         6         7
0.0008929 -0.0009286 -0.0027500  0.0104286 -0.0073929 -0.0062143
0.0059643

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  0.0021071  0.0047874   0.44   0.678
Conc         0.0251643  0.0002656  94.76 2.48e-09 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.007026 on 5 degrees of freedom
Multiple R-squared:  0.9994,    Adjusted R-squared:  0.9993
F-statistic: 8980 on 1 and 5 DF,  p-value: 2.481e-09
```

Regression Equation

$$\mathbf{Abso.fitted = 0.0021 + 0.251 Conc}$$

Remarks

- Number of Independent (Predictor) variables : $k = 1$
- Number of paired observations : $n=7$
- Degrees of freedom :
 - $df_1 = k = 1$
 - $df_2 = n - k - 1 = 5$

Regression Equation for FitA

Abso.fitted = 0.0021+ 0.0251 conc

TSS= 0.4435157

Mean (Abso)= 0.3795714

SSR=0.4432689

SSE=0.0002468214

TSS = SSR + SSE

0.4435157 = 0.4432689 + 0.0002468214

Notice that TSS is the sum of SSR and SSE

```
> anova(FitA)
Analysis of Variance Table

Response: Abso
      Df Sum Sq Mean Sq F value    Pr(>F)    
Conc    1 0.44327  0.44327   8979.5 2.481e-09 ***
Residuals 5 0.00025 0.00005
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
>
```

Remark : The Total Sums of Squares is not included in the output.

MSR = SSR/(k)

MSE = SSE/(n-k-1)

The test statistic is $F_{ts} = MSR/MSE$

(I have added a subscript “ts” to emphasis the term’s purpose as a Test Statistic for a hypothesis test)

MSE = SSE/n-k-1 = 4.936429e-05

MSR= SSR/k = 0.4432689

Test statistic = 36.64

The associated p-value

The null hypothesis is the independent variables used in the model jointly describes the response of the fitted model.

- $H_0: \beta_1 = \beta_2 = \dots = \beta_n = 0$
- H_1 : At least one of the β values for the independent variables is not zero.

We have a very low p-value. So we reject the null hypothesis. The independent variables can indeed be used to build a model for the response variable