

# Integration

## Basic Integration:

- A. An integral is basically the exact opposite of a derivative.
- B. An integral gives the area under a curve from the x-axis to the curve from a specified range. An integral is expressed by the symbol:  $\int$ .
- C. Below are some basic rules for computing integrals:

# Integration

1. The integral of a constant,  $c$ , is  $cx$ .

# Integration

2. The integral of  $x^n$  is .

# Integration

3. The integral of  $a \cdot f(x)$ , where  $a$  is a constant, is equal to  $a$  times the integral of  $f(x)$ . (\*Basically, you can factor out the constant\*)

# Integration

4. The integral of  $f(x) g(x) =$  .
- a. In this problem, we can take each term separate.
  - b. The integral of  $3x^2 = x^3$ ; of  $2x = x^2$ ; of  $1 = x$ .
  - c. The answer is  $x^3+x^2+x+C$
  - d. We usually add a  $C$  on the end because the integral of 0 is a constant.

# Integration

D. You should notice, that if you take the derivative of the new function, you will end up with the original function.

# Integration

## E. Common Integrals:

1. The integral of  $\sin(ax) = -1/a \cos(ax)$
2. The integral of  $\cos(ax) = 1/a \sin(ax)$
3. The integral of  $\sec^2 x = \tan(x)$
4. The integral of  $e(ax) = 1/a e(ax)$ .
5. The integral of  $1/ax = 1/a \ln(ax)$

F. These are just some of the common integrals. There are lots of integrals in many different forms, which can be found on the front or back cover of most calculus books.

G. When calculating an integral in a specified range:

# Integration

- a. To compute this integral take each term separate and get:  $x^3/3 - x^2$ .
- b. To find the value from 0 to 3, first plug in 3. Doing so gives:  
 $3^3/3 - 3^2 = 9 - 9 = 0$ .
- c. Next find the value for 0. This gives:  $0^3/3 - 0^2 = 0$ .
- d. The answer is  $0 - 0 = 0$ .



# Integration

- a. The integral of  $\cos 4x$  is  $\sin 4x/4$ .
- b. To find the value from 0 to we must first use .  
Doing so gives:

$$\sin(3/2)/3 = \sin(3/2)/3 = -1/3.$$

- c. Next, find the value for 0. This is  $\sin 0/4 = 0$ .
- d. The answer is  $-1/3 - 0 = -1/3$ .

# Integration

- a. The integral of  $x^2 - 2$  is  $x^3/3 - 2x$ .
- b. Plug in 4 and get  $64/3 - 8 = 40/3$ .
- c. Plug in 1 and get  $1/3 - 2 = -5/3$ .
- d. The answer is

$$40/3 - (-5/3) = 45/3 = 15.$$