

Operations Research 2 - 2015 Question 6

Maximize $p = 7x + 6y$

subject to

$$8x + 12y \leq 125$$

$$9x - 4y \leq 45$$

$$y \leq 9$$

$$x \leq 7$$

$$x, y \geq 0$$

$$x, y \text{ integers}$$

- An IP is to be solved using the tabular Branch and Bound method.
- Use the solution grids below to solve the problem. Each node is referenced by its tree level, ordered from left to right so that the annotation Node XY is the node at level X at position Y where Y = 1 is the left-most position in level X.

	Node 0		Node 1A		Node 1B
(i)	$X = 6.50, Y = 7.50$	(i)	$X = 6.00, Y = 5.00$	(i)	$X = 5.75, Y = 7.00$
(ii)	$X = 7.50, Y = 6.00$	(ii)	$X = 6.00, Y = 6.00$	(ii)	$X = 6.625, Y = 6.00$
(iii)	$X = 7.20, Y = 5.40$	(iii)	$X = 4.50, Y = 5.50$	(iii)	$X = 5.625, Y = 6.875$
(iv)	$X = 6.00, Y = 9.00$	(iv)	$X = 7.00, Y = 5.00$	(iv)	$X = 7.50, Y = 4.125$
(v)	$X = 7.00, Y = 5.75$	(v)	$X = 7.00, Y = 3.00$	(v)	$X = 7.00, Y = 5.75$
	Node 2A		Node 2B		Node 2C
(i)	$X = 6.50, Y = 4.50$	(i)	$X = 7.25, Y = 5.75$	(i)	$X = 6.00, Y = 5.00$
(ii)	$X = 6.25, Y = 5.50$	(ii)	$X = 6.25, Y = 5.50$	(ii)	$X = 6.625, Y = 5.75$
(iii)	$X = 5.625, Y = 5.00$	(iii)	$X = 7.25, Y = 5.25$	(iii)	$X = 5.625, Y = 6.75$
(iv)	$X = 7.50, Y = 4.75$	(iv)	$X = 7.00, Y = 4.00$	(iv)	$X = 6.00, Y = 6.00$
(v)	$X = 7.25, Y = 5.25$	(v)	$X = 7.50, Y = 4.50$	(v)	$X = 6.00, Y = 6.416$
	Node 2D		Node 3A		Node 3B
(i)	$X = 5.75, Y = 7.00$	(i)	$X = 6.125, Y = 2.50$	(i)	$X = 6.75, Y = 3.50$
(ii)	$X = 7.00, Y = 7.00$	(ii)	$X = 6.75, Y = 3.50$	(ii)	$X = 6.25, Y = 5.50$
(iii)	$X = 5.625, Y = 6.75$	(iii)	$X = 6.8, Y = 3.666$	(iii)	$X = 6.125, Y = 2.50$
(iv)	$X = 7.50, Y = 4.00$	(iv)	$X = 7.2, Y = 2.9$	(iv)	$X = 6.00, Y = 4.50$
(v)	$X = 7.00, Y = 6.00$	(v)	$X = 7.00, Y = 3.875$	(v)	$X = 7.00, Y = 3.875$

	Node 3C		Node 3D		Node 3E
(i)	$X = 5.75, Y = 6.75$	(i)	$X = 7.25, Y = 3.333$	(i)	$X = 6.00, Y = 6.00$
(ii)	$X = 5.625, Y = 7.333$	(ii)	$X = 4.833, Y = 6.5$	(ii)	$X = 6.125, Y = 5.75$
(iii)	$X = 7.50, Y = 7.125$	(iii)	$X = 3.75, Y = 8.666$	(iii)	$X = 6.00, Y = 6.75$
(iv)	$X = 7.125, Y = 7.00$	(iv)	$X = 5.25, Y = 4.33$	(iv)	$X = 5.75, Y = 5.00$
(v)	$X = 7.00, Y = 8.00$	(v)	$X = 5, Y = 5.50$	(v)	$X = 7.00, Y = 6.00$
	Node 3F		Node 3G		Node 3H
(i)	$X = 5.75, Y = 7.00$	(i)	$X = 5.00, Y = 6.00$	(i)	$X = 6.75, Y = 3.50$
(ii)	$X = 7.00, Y = 7.00$	(ii)	$X = 6.75, Y = 3.50$	(ii)	$X = 6.75, Y = 2.10$
(iii)	$X = 5.125, Y = 7.00$	(iii)	$X = 6.75, Y = 4.50$	(iii)	$X = 6.75, Y = 3.50$
(iv)	$X = 6.00, Y = 6.00$	(iv)	$X = 6.75, Y = 4.50$	(iv)	$X = 6.00, Y = 4.00$
(v)	$X = 7.25, Y = 5.00$	(v)	$X = 3.666, Y = 8.50$	(v)	$X = 7.00, Y = 3.50$