Revision of Differentiations

Part A: Revision of Differentiations

$$1 f(x) = x^2$$

$$2 f(x) = 2x + 2$$

$$3 f(x) = \frac{1}{2}x^2$$

$$4 f(x) = 2x^2 + 4x + 4$$

$$5 f(x) = \sqrt{x+2}$$

$$6 f(x) = \frac{1}{x}$$

$$7 f(x) = \frac{3}{x+1}$$

$$8 f(x) = \frac{1}{\sqrt{x+1}}$$

$$9 f(x) = \frac{x}{x+2}$$

Selected Solutions

$$4$$
 $4x + 4$

$$4x + 4$$

$$\frac{1}{2\sqrt{x+2}}$$

$$6 - \frac{1}{x}$$

7

$$\frac{-3}{(x+1)^2}$$

8

$$\frac{-1}{2(x+1)^{3/2}}$$

9

$$\frac{2}{(x+2)^2}$$

Part B: Using the Power Rule

10
$$f(x) = x^5 + x^3$$

11
$$f(x) = 2x^2 + 4$$

$$12 \ f(x) = 3\sqrt[3]{x}$$

$$13 \ f(x) = 2x^5 + 8x^2 + x - 78$$

14
$$f(x) = 7x^7 + 8x^5 + x^3 + x^2 - x$$
 19 $f(x) = \frac{1}{\sqrt[3]{x}} + \sqrt{x}$

$$15 f(x) = \frac{1}{x^2} + 3x^{\frac{1}{3}}$$

$$16 f(x) = 3x^{15} + \frac{1}{17}x^2 + \frac{2}{\sqrt{x}}$$

17
$$f(x) = \frac{3}{x^4} - \sqrt[4]{x} + x$$

$$18 \ f(x) = 6x^{1/3} - x^{0.4} + \frac{9}{x^2}$$

$$19 f(x) = \frac{1}{\sqrt[3]{x}} + \sqrt{x}$$

Part C: Using the Product Rule

$$20 f(x) = (x^4 + 4x + 2)(2x + 3)$$

$$21 f(x) = (2x - 1)(3x^2 + 2)$$

20
$$f(x) = (x^4 + 4x + 2)(2x + 3)$$
 22 $f(x) = (x^3 - 12x)(3x^2 + 2x)$

23
$$f(x) = (2x^5 - x)(3x + 1)$$

Part D: Using the Quotient Rule

$$24 \ f(x) = \frac{2x+1}{x+5}$$

$$25 \ f(x) = \frac{3x^4 + 2x + 2}{3x^2 + 1}$$

$$26 \ f(x) = \frac{x^{\frac{3}{2}+1}}{x+2}$$

$$27 \ f(u) = \frac{u^3 + 2}{u^3}$$

$$28 \ f(x) = \frac{x^2 + x}{2x - 1}$$

$$29 \ g(x) = \frac{x+1}{2x^2 + 2x + 3}$$

$$30 \ h(x) = \frac{16x^4 + 2x^2}{x}$$

Part E: Using the Chain Rule

$$31 \ f(x) = (x+5)^2$$

$$32 \ f(x) = (x^3 - 2x + 5)^2$$

33
$$f(x) = \sqrt{1 - x^2}$$

$$34 \ f(x) = \frac{(2x+4)^3}{4x^3+1}$$

$$35 \ f(x) = (2x+1)\sqrt{2x+2}$$

$$36 \ f(x) = \frac{2x+1}{\sqrt{2x+2}}$$

$$37 \ f(x) = \sqrt{2x^2 + 1}(3x^4 + 2x)^2$$

$$38 \ f(x) = \frac{2x+3}{(x^4+4x+2)^2}$$

39
$$f(x) = \sqrt{x^3 + 1}(x^2 - 1)$$

Part F: Differentiation of Exponentials

$$40 f(x) = ((2x+3)^4 + 4(2x+3) + 2)^2$$

41
$$f(x) = \sqrt{1+x^2}$$

$$42 \ f(x) = (3x^2 + e)e^{2x}$$

43
$$f(x) = e^{2x^2 + 3x}$$

$$44 \ f(x) = e^{e^{2x^2 + 1}}$$

$$45 \ f(x) = 4^x$$

Part G: Logarithms

$$46 \ f(x) = 2^{x-3} \cdot 3\sqrt{x^3 - 2} + \ln x$$

$$47 \ f(x) = \ln x - 2e^x + \sqrt{x}$$

48
$$f(x) = \ln(\ln(x^3(x+1)))$$

$$49 \ f(x) = \ln(2x^2 + 3x)$$

$$50 \ f(x) = \log_4 x + 2\ln x$$

Part H: Trigonometric functions

$$51 f(x) = \sin(x) + \cos(x)$$

$$52 \ f(x) = \sin(4x)$$

$$53 \ f(x) = \cos(4x)$$

$$54 \ f(x) = \sin(3x) + \cos(5x)$$

$$55 \ f(x) = e^{\frac{x}{2}} + \tan(2x)$$