

# Information Criteria

## Information Criteria

- ▶ We define two types of information criterion: the Bayesian Information Criterion (BIC) and the Akaike Information Criterion (AIC).
- ▶ In AIC and BIC, we choose the model that has the minimum value.
- ▶ *(Remark, a difference of less than two is considered negligible).*

# Information Criteria

## Formulae

$$AIC = 2 \log(L) + 2p,$$

$$BIC = 2 \log(L) + p \log n$$

where

- ▶  $L$  is the likelihood of the data with a certain model,
- ▶  $n$  is the number of observations and
- ▶  $p$  is the number of parameters in the model.

## Information Criteria

However, which criterion should we choose?

- ▶ AIC is well-known for overestimating the correct number of segments
- ▶ BIC has a slight tendency to underestimate this number.
- ▶ However analyses usually renders concordant results.

- ▶ The Akaike information criterion is a measure of the relative **goodness of fit** of a statistical model.
- ▶ When using the AIC for selecting the parametric model class, choose the model for which the AIC value is lowest.

## Akaike Information Criterion

### Akaike Information Criterion (AIC)

- ▶ Akaike's information criterion is a measure of the goodness of fit of an estimated statistical model.
- ▶ The AIC is a **model selection** tool, i.e. a method of comparing two or more candidate regression models.
- ▶ The AIC methodology attempts to find the model that best explains the data with a minimum of parameters. (i.e. in keeping with the law of parsimony)

# Akaike Information Criterion

## **Akaike Information Criterion (AIC)**

- ▶ The AIC is calculated using the "likelihood function" and the number of parameters
- ▶ Given a data set, several competing models may be ranked according to their AIC, with the one having the lowest AIC being the best.

# Akaike Information Criterion

## Akaike Information Criterion (AIC)

$$AIC = 2p - 2\ln(L)$$

- ▶  $p$  is the number of free model parameters.
- ▶  $L$  is the value of the Likelihood function for the model in question.
- ▶ For AIC to be optimal,  $n$  must be large compared to  $p$ .

# Schwarz's Bayesian Information Criterion

An alternative to the AIC is the Schwarz BIC, which additionally takes into account the sample size  $n$ .

$$\text{BIC} = p \ln n - 2 \ln(L)$$



- ▶ These are relative measures of goodness-of-fit and are used to compare different solutions with different numbers of segments.
- ▶ (“Relative” means that these criteria are not scaled on a range of, for example, 0 to 1 but can generally take any value.)
- ▶ **Important:** Compared to an alternative solution with a different number of segments, smaller values in AIC or BIC indicate an increased fit.