

# Set Theory Introduction

- ▶ A set is simply a collection of things or objects, of any kind.
- ▶ These objects are called elements or members of the set. We refer to the set as an entity in its own right and often denote it by  $A$ ,  $B$ ,  $C$  or  $D$ , etc.
- ▶ If  $A$  is a set and  $x$  a member of the set, then we say  $x \in A$  i.e.  $x$  belongs to  $A$ . The symbol  $\notin$  denotes the negation of *in* i.e.  $x \notin A$  means  $x$  does not belong to  $A$ .

# Set Theory Introduction

- ▶ The elements of a set, and hence the set itself, are characterised by having one or more properties that distinguish the elements of the set from those not in the set.
- ▶ For example, if  $C$  is the set of non-negative real numbers, then we might use the notation

$$C = \{x/x \text{ is a real number and } x \neq 0\}$$

- ▶ We would verbalise this as *the set of all  $x$  such that  $x$  is a real number and non-negative.*

## Differences and complements

- ▶ If  $A$  and  $B$  are sets then the difference set  $A \setminus B$  is the set of all elements of  $A$  which do not belong to  $B$ .
- ▶ If  $B$  is a sub-set of  $A$ , then  $A \setminus B$  is sometimes called the complement of  $B$  in  $A$ . When  $A$  is the universal set one may simply refer to the complement of  $B$  to denote all things not in  $B$ .
- ▶ The complement of a set  $A$  is denoted as  $A^c$  or  $A'$ .