#### **Table 1 Cumulative Binomial Probabilities**

p = probability of success in a single trial; n = number of trials. The table gives the probability of obtaining r or more successes in n independent trials. That is

$$\sum_{x=r}^{n} \binom{n}{x} p^{x} (1-p)^{n-x}$$

When there is no entry for a particular pair of values of r and p, this indicates that the appropriate probability is less than 0.000 05. Similarly, except for the case r = 0, when the entry is exact, a tabulated value of 1.0000 represents a probability greater than 0.999 95.

and the second s	<i>p</i> =	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
n = 2	r = 0 $1$ $2$	1.0000 .0199 .0001	1.0000 .0396 .0004	1.0000 .0591 .0009	1.0000 .0784 .0016	1.0000 .0975 .0025	1.0000 .1164 .0036	1.0000 .1351 .0049	1.0000 .1536 .0064	1.0000 .1719 .0081
<i>n</i> = 5	r = 0 $1$ $2$ $3$ $4$	1.0000 .0490 .0010	1.0000 .0961 .0038 .0001	1.0000 .1413 .0085 .0003	1.0000 .1846 .0148 .0006	1.0000 .2262 .0226 .0012	1.0000 .2661 .0319 .0020 .0001	1.0000 .3043 .0425 .0031 .0001	1.0000 .3409 .0544 .0045 .0002	1.0000 .3760 .0674 .0063 .0003
<i>n</i> = 10	r = 0 $1$ $2$ $3$ $4$ $5$ $6$	1.0000 .0956 .0043 .0001	1.0000 .1829 .0162 .0009	1.0000 .2626 .0345 .0028 .0001	1.0000 .3352 .0582 .0062 .0004	1.0000 .4013 .0861 .0115 .0010	1.0000 .4614 .1176 .0188 .0020	1.0000 .5160 .1517 .0283 .0036	1.0000 .5656 .1879 .0401 .0058	1.0000 .6106 .2254 .0540 .0088 .0010 .0001
n = 20	r = 0 $1$ $2$ $3$ $4$	1.0000 .1821 .0169 .0010	1.0000 .3324 .0599 .0071 .0006	1.0000 .4562 .1198 .0210 .0027	1.0000 .5580 .1897 .0439 .0074	1.0000 .6415 .2642 .0755 .0159	1.0000 .7099 .3395 .1150 .0290	1.0000 .7658 .4131 .1610 .0471	1.0000 .8113 .4831 .2121 .0706	1.0000 .8484 .5484 .2666 .0993
	5 6 7 8			.0003	.0010	.0026	.0056 .0009 .0001	.0107 .0019 .0003	.0183 .0038 .0006 .0001	.0290 .0068 .0013 .0002
n = 50	r = 0 $1$ $2$ $3$ $4$	1.0000 .3950 .0894 .0138 .0016	1.0000 .6358 .2642 .0784 .0178	1.0000 .7819 .4447 .1892 .0628	1.0000 .8701 .5995 .3233 .1391	1.0000 .9231 .7206 .4595 .2396	1.0000 .9547 .8100 .5838 .3527	1.0000 .9734 .8735 .6892 .4673	1.0000 .9845 .9173 .7740 .5747	1.0000 .9910 .9468 .8395 .6697
	5 6 7 8 9	.0001	.0032 .0005 .0001	.0168 .0037 .0007 .0001	.0490 .0144 .0036 .0008	.1036 .0378 .0118 .0032 .0008	.1794 .0776 .0289 .0094 .0027	.2710 .1350 .0583 .0220 .0073	.3710 .2081 .1019 .0438 .0167	.4723 .2928 .1596 .0768 .0328
	10 11 12 13 14					.0002	.0007	.0022 .0006 .0001	.0056 .0017 .0005 .0001	.0125 .0043 .0013 .0004 .0001

Table 1 Cumulative Binomial Probabilities – continued

	<i>p</i> =	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
n = 100	r = 0 $1$ $2$ $3$ $4$	1.0000 .6340 .2642 .0794 .0184	1.0000 .8674 .5967 .3233 .1410	1.0000 .9524 .8054 .5802 .3528	1.0000 .9831 .9128 .7679 .5705	1.0000 .9941 .9629 .8817 .7422	1.0000 .9979 .9848 .9434 .8570	1.0000 9993 9940 9742 .9256	1.0000 .9998 .9977 .9887 .9633	1.0000 .9999 .9991 .9952 .9827
	5 6 7 8	.0034 .0005 .0001	.0508 .0155 .0041 .0009	.1821 .0808 .0312 .0106 .0032	.3711 .2116 .1064 .0475 .0190	.5640 .3840 .2340 .1280 .0631	.7232 .5593 .3936 .2517 .1463	.8368 .7086 .5557 .4012 .2660	.9097 .8201 .6968 .5529 .4074	.9526 .8955 .8060 .6872 .5506
	10 11 12 13 14			.0009	.0068 .0022 .0007 .0002	.0282 .0115 .0043 .0015 .0005	.0775 .0376 .0168 .0069 .0026	.1620 .0908 .0469 .0224 .0099	.2780 .1757 .1028 .0559 .0282	.4125 .2882 .1876 .1138 .0645
	15 16 17 18 19		,			.0001	.0009 .0003 .0001	.0041 .0016 .0006 .0002 .0001	.0133 .0058 .0024 .0009 .0003	.0341 .0169 .0078 .0034 .0014
	20 21 22								.0001	.0005 .0002 .0001
	p =	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50
n = 2	r = 0 $1$ $2$	1.0000 .1900 .0100	1.0000 .2775 .0225	1.0000 .3600 .0400	1.0000 .4375 .0625	1.0000 .5100 .0900	1.0000 .5775 .1225	1.0000 .6400 .1600	1.0000 .6975 .2025	1.0000 .7500 .2500
<i>n</i> = 5	r = 0 $1$ $2$ $3$ $4$	1.0000 .4095 .0815 .0086	1.0000 .5563 .1648 .0266 .0022	1.0000 .6723 .2627 .0579 .0067	1.0000 .7627 .3672 .1035 .0156	1.0000 .8319 .4718 .1631 .0308	1.0000 .8840 .5716 .2352 .0540	1.0000 .9222 .6630 .3174 .0870	1.0000 .9497 .7438 .4069 .1312	1.0000 .9688 .8125 .5000 .1875
	5		.0001	.0003	.0010	.0024	.0053	.0102	.0185	.0313
n = 10	r = 0 $1$ $2$ $3$ $4$	1.0000 .6513 .2639 .0702 .0128	1.0000 .8031 .4557 .1798 .0500	1.0000 .8926 .6242 .3222 .1209	1.0000 .9437 .7560 .4744 .2241	1.0000 .9718 .8507 .6172 .3504	1.0000 .9865 .9140 .7384 .4862	1.0000 .9940 .9536 .8327 .6177	1.0000 .9975 .9767 .9004 .7430	1.0000 .9990 .9893 .9453 .8281
	5 6 7 8 9	.0016	.0099 .0014 .0001	.0328 .0064 .0009 .0001	.0781 .0197 .0035 .0004	.1503 .0473 .0106 .0016 .0001	.2485 .0949 .0260 .0048 .0005	.3669 .1662 .0548 .0123 .0017	.4956 .2616 .1020 .0274 .0045	.6230 .3770 .1719 .0547 .0107
	10					1,0000	1,0000	.0001	1,0000	.0010
n = 20	r = 0 $1$ $2$ $3$ $4$	1.0000 .8784 .6083 .3231 .1330	1.0000 .9612 .8244 .5951 .3523	1.0000 .9885 .9308 .7939 .5886	1.0000 .9968 .9757 .9087 .7748	1.0000 .9992 .9924 .9645 .8929	1.0000 .9998 .9979 .9879 .9556	1.0000 1.0000 .9995 .9964 .9840	1.0000 1.0000 .9999 .9991 .9951	1.0000 1.0000 1.0000 .9998
	5 6 7 8 9	.0432 .0113 .0024 .0004	.1702 .0673 .0219 .0059	.3704 .1958 .0867 .0321 .0100	.5852 .3828 .2142 .1018 .0409	.7625 .5836 .3920 .2277 .1133	.8818 .7546 .5834 .3990 .2376	.5841	.9811 .9447 .8701 .7480 .5857	.9941 .9793 .9423 .8684 .7483
	10 11 12 13	.0001	.0002	.0026 .0006 .0001	.0139 .0039 .0009 .0002	.0480 .0171 .0051 .0013 .0003	.1218 .0532 .0196 .0060	.2447 .1275 .0565 .0210	.4086 .2493 .1308 .0580 .0214	.588 .411 .251 .131 .057
	14 15 16 17 18					,000	.0003		.0064 .0015 .0003	.020 .005 .001 .000

Table 1 Cumulative Binomial Probabilites – continued

	p =	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50
		1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
= 50	r = 0	1.0000		1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
	1	.9948	.9997	.9998	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
	2	.9662	.9971	.9987	.9999	1.0000	1.0000	1.0000	1.0000	1.0000
	. 3	.8883	.9858 .9540	.9987	.9995	1.0000	1.0000	1.0000	1.0000	1.0000
	4	.7497				.9998	1.0000	1.0000	1.0000	1.0000
	. 5	.5688	.8879	.9815	.9979	.9993	.9999	1.0000	1.0000	1.0000
	. 6	.3839	.7806	.9520	.9930		.9998	1.0000	1.0000	1.0000
	7	.2298	.6387	.8966	.9806	.9975	.9992	.9999	1.0000	1.0000
	8	.1221	.4812	.8096	.9547	.9927		.9998	1.0000	1.0000
	9	.0579	.3319	.6927	.9084	.9817	.9975			
	10	.0245	.2089	.5563	.8363	.9598	.9933	.9992	.9999	1.0000 1.0000
	11	.0094	.1199	.4164	.7378	.9211	.9840	.9978	.9998	1.0000
	12	.0032	.0628	.2893	.6184	.8610	.9658	.9943	.9994	
	13	.0010	.0301	.1861	.4890	.7771	.9339	.9867	.9982	.9998
	13		.0132	, .1106	.3630	.6721	.8837	.9720	.9955	.9995
			.0053	.0607	.2519	.5532	.8122	.9460	.9896	.9987
	15		.0033	.0308	.1631	.4308	.7199	.9045	.9780	.9967
	_ 16		.0019	.0144	.0983	.3161	.6111	.8439	.9573	.9923
	17		.0007	.0063	.0551	.2178	.4940	.7631	.9235	.9836
	18 19		.0002	.0003	.0287	1406	.3784	.6644	.8727	.9675
			.0001	.0009	.0139	.0848	.2736	.5535	.8026	.9405
	20				,0063	.0478	.1861	.4390	.7138	.8987
	21			.0003	.0026	.0251	.1187	.3299	.6100	.8389
	22			.0001		.0123	.0710	.2340	.4981	.7601
	23				.0010	.0125	.0396	.1562	.3866	.6641
	24	1					.0207	.0978	.2840	.5561
	2.5	5			.0001	.0024		.0573	.1966	.4439
	20					.0009	.0100	.0373	.1279	3359
	2					.0003	.0045	.0160	.0780	.2399
	2					.0001	.0019	.0076	.0444	.1611
	2	9								.1013
	3	0					.0003	.0034	.0235 .0116	.0595
	3						.0001		.0053	.0325
	3							.0005		.0164
		3						.0002		.0077
		4						.0001		
		35							.0003	.0033
									.0001	.0013
		36								.0005
		37 38								.0002

Table 1 gives binomial probabilities only for a limited range of values of n and p since, in practice, either the more compact tabulation of the Poisson distribution (Table 2) or that of the Normal distribution (Table 3) can usually be used to give an adequate approximation.

As a reasonable working rule:

- (i) use the Poisson approximation if p < 0.1, putting m = np
- (ii) use the Normal approximation if  $0.1 \le p \le 0.9$  and np > 5, putting  $\mu = np$  and  $\sigma = \sqrt{np(1-p)}$ .
- (iii) use the Poisson approximation if p > 0.9, putting m = n(1 p) and working in terms of 'failures'.

*Note*: For values of p > 0.5, work in terms of 'failures' which will have probability q = (1 - p).

Example: What is the probability that 40 or more seeds will germinate out of 50 if the germination rate is 70%? Since the probability of 'success' is greater than 0.5, the table can not be used directly; however, 40 or more successes is the same as 10 or fewer 'failures'. The probability of 10 or fewer 'failures' = 1 - probability of 11 or more 'failures' = 1 - 0.9211 = 0.0789.

Table 1 Cumulative Binomial Probabilities – continued

****	p =	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50
n = 100	r = 0 1 2 3 4	1.0000 1.0000 .9997 .9981 .9922	1.0000 1.0000 1.0000 1.0000 .9999	1.0000 1.0000 1.0000 1.0000 1.0000						
	5 6 7 8 9	.9763 .9424 .8828 .7939 .6791	.9996 .9984 .9953 .9878 .9725	1.0000 1.0000 .9999 .9997 .9991	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000
	10 11 12 13 14	.5487 .4168 .2970 1982 .1239	.9449 .9006 .8365 .7527 .6526	.9977 .9943 .9874 .9747 .9531	1.0000 .9999 .9996 .9990 .9975	1.0000 1.0000 1.0000 1.0000 .9999	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000
	15 16 17 18 19	.0726 .0399 .0206 .0100 .0046	.5428 .4317 .3275 .2367 .1628	.9196 .8715 .8077 .7288 .6379	.9946 .9889 .9789 .9624 .9370	.9998 .9996 .9990 .9978 .9955	1.0000 1.0000 1.0000 .9999 .9999	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000
	20 21 22 23 24	.0020 .0008 .0003 .0001	.1065 .0663 .0393 .0221 .0119	.5398 .4405 .3460 .2611 .1891	.9005 .8512 .7886 .7136 .6289	.9911 .9835 .9712 .9521 .9245	.9997 .9992 .9983 .9966 .9934	1.0000 1.0000 1.0000 .9999 .9997	1.0000 1.0000 1.0000 1.0000 1.0000	1.0000 1.0000 1.0000 1.0000 1.0000
	25 26 27 28 29		.0061 .0030 .0014 .0006	.1314 .0875 .0558 .0342 .0200	.5383 .4465 .3583 .2776 .2075	.8864 .8369 .7756 .7036 .6232	.9879 .9789 .9649 .9442 .9152	.9994 .9988 .9976 .9954 .9916	1.0000 1.0000 .9999 .9998 .9996	1.0000 1.0000 1.0000 1.0000
	30 31 32 33 34		.0001	.0112 .0061 .0031 .0016 .0007	.1495 .1038 .0693 .0446 .0276	.5377 .4509 .3669 .2893 .2207	.8764 .8270 .7669 .6971 .6197	.9852 .9752 .9602 .9385 .9087	.9992 .9985 .9970 .9945 .9902	1.000 1.000 .999 .999
	35 36 37 38 39			.0003 .0001 .0001	.0164 .0094 .0052 .0027 .0014	.1629 .1161 .0799 .0530 .0340	.5376 .4542 .3731 .2976 .2301	.8697 .8205 .7614 .6932 .6178	.9834 .9728 .9571 .9349 .9049	.999 .998 .996 .994 .989
	40 41 42 43 44				.0007 .0003 .0001 .0001	.0210 .0125 .0072 .0040 .0021	.1724 .1250 .0877 .0594 .0389	.5379 .4567 .3775 .3033 .2365	.8657 .8169 .7585 .6913 .6172	.982 .971 .955 .933 .903
	45 46 47 48 49					.0011 .0005 .0003 .0001	.0246 .0150 .0088 .0050 .0027	.1789 .1311 .0930 .0638 .0423	.5387 .4587 .3804 .3069 .2404	.864 .815 .757 .69
	50 51 52 53 54						.0015 .0007 .0004 .0002 .0001	.0271 .0168 .0100 .0058 .0032	.1827 .1346 .0960 .0662 .0441	.539 .469 .389 .30 .24
	55 56 57 58 59							.0017 .0009 .0004 .0002 .0001	.0284 .0176 .0106 .0061 .0034	.18 .13 .09 .06
	60 61 62 63 64								.0018 .0009 .0005 .0002	.02 .01 .01 .00
	65 66 67 68 69									00. 00. 00. 00.

### **Table 2 Cumulative Poisson Probabilities**

The table gives the probability that r or more random events are contained in an interval when the average number of such events per interval is m, i.e.

$$\sum_{x=r}^{\infty} e^{-m} \, \frac{m^x}{x!}$$

Where there is no entry for a particular pair of values of r and m, this indicates that the appropriate probability is less than 0.000 05. Similarly, except for the case r = 0 when the entry is exact, a tabulated value of 1.0000 represents a probability greater than 0.999 95.

m =	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
r = 0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
r - 0	0952	.1813	.2592	.3297	.3935	.4512	.5034	.5507	.5934	.6321
2	.0047	.0175	.0369	.0616	.0902	.1219	.1558	.1912	.2275	.2642
3	.0002	.0011	.0036	.0079	.0144	.0231	.0341	.0474	.0629	.0803
4.	.0002	.0001	.0003 ·	.0008	.0018	.0034	.0058	.0091	.0135	.0190
				.0001	.0002	.0004	.0008	.0014	.0023	.0037
5 6				• • • • • •			.0001	.0002	.0003	-000
7										.000.
m =	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9	2.0
	1 0000	1 0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
r = 0	1.0000	1.0000 .6988	.7275	.7534	.7769	.7981	.8173	.8347	.8504	.864
1	.6671	.3374	.3732	.4082	.4422	.4751	.5068	.5372	.5663	.594
2	.3010	.1205	.1429	.1665	.1912	.2166	.2428	2694	.2963	.323
3 4	.0996 .0257	.0338	.0431	.0537	.0656	.0788	.0932	.1087	.1253	.142
				.0143	.0186	.0237	.0296	.0364	.0441	.052
5	.0054	.0077	.0107	.0032	.0045	.0060	.0080	.0104	0132	.016
6	.0010	.0015	.0022	.0032	.00043	.0013	.0019	.0026	.0034	.004
7	.0001	.0003	.0004	.0001	.0002	.0003	.0004	.0006	.0008	.001
8			.0001	.0001	.0002	.000	.0001	.0001	.0002	.000
9								acting angle and a state in the state of the	AND THE PROPERTY OF THE PROPER	e-temposer-taken en e
m =	2.1	2.2	2.3	2.4	2.5	2.6	2.7	2.8	2.9	3.0
r = 0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.000
1	.8775	.8892	.8997	.9093	.9179	.9257	.9328	.9392	.9450	.950
2	.6204	.6454	.6691	.6916	.7127	.7326	.7513	.7689	.7854	.800
3	.3504	.3773	4040	.4303	.4562	.4816	.5064	.5305	.5540	.576
4	.1614	.1806	.2007	.2213	.2424	.2640	2859	.3081	.3304	.352
5	.0621	.0725	.0838	.0959	.1088	.1226	.1371	.1523	.1682	.184
6	.0204	.0249	.0300	.0357	.0420	.0490	.0567	.0651	.0742	.08
7	.0059	.0075	.0094	.0116	.0142	.0172	.0206	.0244	.0287	.03
8	.0015	.0020	.0026	.0033	.0042	.0053	.0066	.0081	.0099	.01
9	.0003	.0005	.0006	.0009	.0011	.0015	.0019	.0024	.0031	.00
10	.0001	.0001	.0001	.0002	.0003	.0004	.0005	.0007	.0009	.00
11	1000.	.0001	.0001		.0001	.0001	.0001	.0002	.0002	.00
									.0001	.00

Table 2 Cumulative Poisson Probabilities – continued

m =	3.1	3.2	3.3	3.4	3.5	3.6	3.7	3.8	3.9	4.0
= 0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
	.9550	.9592	.9631	.9666	.9698	.9727	.9753	.9776	.9798	.9817
1		.8288	.8414	.8532	.8641	.8743	.8838	.8926	.9008	.9084
2	.8153 .5988	.6201	.6406	.6603	.6792	.6973	.7146	.7311	.7469	.7619
3 4	.3752	.3975	.4197	.4416	.4634	.4848	.5058	.5265	.5468	.5665
5	.2018	.2194	.2374	.2558	.2746	.2936	.3128	.3322	.3516	.3712
6	.0943	1054	.1171	.1295	.1424	.1559	.1699	.1844	.1994	.2149
	.0388	.0446	.0510	.0579	.0653	.0733	.0818	.0909	.1005	.1107
7	.0142	.0168	.0198	.0231	.0267	.0308	.0352	.0401	.0454	.0511
8	.0047	.0057	.0069	.0083	.0099	.0117	.0137	.0160	.0185	.0214
10	.0014	.0018	.0022	.0027	.0033	.0040	.0048	.0058	.0069 ـ	.0081
11	.0004	.0005	.0006	.0008	.0010	.0013	.0016	.0019	.0023	.0028
	.0004	.0001	.0002	.0002	.0003	.0004	.0005	.0006	.0007	.0009
12	.0001	.0001	.0002	.0001	.0001	.0001	.0001	.0002	.0002	.0003
13 14									.0001	.0001
n =	4.1	4.2	4.3	4.4	4.5	4.6	4.7	4.8	4.9	5.0
		1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
= 0	1.0000	1.0000	1.0000	.9877	.9889	.9899	.9909	.9918	.9926	.9933
1	.9834	.9850	.9864		.9389	.9437-	.9482	.9523	.9561	.959
2	.9155	.9220	.9281	.9337	.9389 .8264	.8374	.8477	.8575	.8667	.875
3	.7762	.7898	.8026	.8149 .6406	.6577	.6743	.6903	.7058	.7207	.7350
4	.5858	.6046	.6228						.5418	.559:
5	.3907	.4102	.4296	.4488	.4679	.4868	.5054	.5237	.3665	.384
6	.2307	.2469	.2633	.2801	.2971	.3142	.3316	.3490	.2233	.237
7	.1214	.1325	.1442	.1564	.1689	.1820	.1954	.2092	.1233	.133
8	.0573	.0639	.0710	.0786	.0866	.0951	.1040	.1133		.068
9	.0245	.0279	.0317	.0358	.0403	.0451	.0503	.0558	.0618	
10	.0095	.0111	.0129	.0149	.0171	.0195	.0222	.0251	.0283	.031
11	.0034	.0041	.0048	.0057	.0067	.0078	.0090	.0104	.0120	.013
12	.0011	.0014	.0017	.0020	.0024	.0029	.0034	.0040	.0047	.005
13	.0003	.0004	.0005	.0007	.0008	.0010	.0012	.0014	.0017	.002
14	.0001	.0001	.0002	.0002	.0003	.0003	.0004	.0005	.0006	.000
15				.0001	.0001	.0001	.0001	.0001	.0002	.000
16							ang and a gradual control of the state of th		.0001	.000
n =	5.2	5.4	5.6	5.8	6.0	6.2	6.4	6.6	6.8	7.0
= ()	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.000
1	.9945	.9955	.9963	.9970	.9975	.9980	.9983	.9986	.9989	.999
2	.9658	.9711	.9756	.9794	.9826	.9854	.9877	.9897	.9913	.992
3	.8912	.9052	.9176	.9285	.9380	.9464	.9537	.9600	.9656	.970
4	.7619	.7867	.8094	.8300	.8488	.8658	.8811	.8948	.9072	.918
5	.5939	.6267	.6579	.6873	.7149	.7408	.7649	.7873	.8080	.827
6	.4191	.4539	.4881	.5217	.5543	.5859	.6163	.6453	.6730	.699
7	.2676	.2983	.3297	.3616	.3937	.4258	.4577	.4892	.5201	.550
8	.1551	.1783	.2030	.2290	.2560	.2840	.3127	.3419	.3715	.40
9	.0819	.0974	.1143	.1328	.1528	.1741	.1967	.2204	.2452	.270
10	.0397	.0488	.0591	.0708	.0839	.0984	.1142	.1314	.1498	.16 .09
11	.0177	.0225	.0282	.0349	.0426	.0514	.0614	.0726	.0849	.09
12	.0073	.0096	.0125	.0160	.0201	.0250	.0307	.0373	.0448	.03
13	.0028	.0038	.0051	.0068	.0088	.0113	.0143	.0179 .0080	.0221	.02
14	.0010	.0014	.0020	.0027	.0036				.0044	.00
15	.0003	.0005	.0007	.0010	.0014	.0019	.0026	.0034 .0014	.0044	00. 00.
16	.0001	.0002	.0002	.0004	.0005	.0007	.0010		.0018	.00.
17		.0001	.0001	.0001	.0002	.0003	.0004	.0005 .0002	.0007	.00.
18					.0001	.0001	.0001	.0002	.0003	.00

Table 2 Cumulative Poisson Probabilities – continued

	7.2	7.4	7.6	7.8	8.0	8.2	8.4	8.6	8.8	9.0
m = 0 $1$	1.0000 .9993 .9939	1.0000 .9994 .9949	1.0000 .9995 .9957	.9996 .9964	1.0000 .9997 .9970	.9997 .9975	1.0000 .9998 .9979 .9900	1.0000 .9998 .9982 .9914	1.0000 .9998 .9985 .9927	1.0000 .9999 .9988 .9938
2 3	.9745 .9281	.9781 .9368	.9812 .9446	.9839 .9515	.9862 .9576	.9882 .9630	.9677	.9719	.9756	.9788
5	.8445 .7241 .5796	.8605 .7474 .6080	.8751 .7693 .6354	.8883 .7897 .6616	.9004 .8088 .6866	.9113 .8264 .7104	.9211 .8427 .7330	.9299 .8578 .7543 .6272	.9379 .8716 .7744 .6522	.9450 .8843 .7932 .6761
7 8 9	.4311	.4607	.4900 .3518	.5188 .3796	.5470 .4075	.5746 .4353	.6013 .4631	.4906	.5177	.5443 .4126
10 11 12 13	.1904 .1133 .0629 .0327 .0159	.2123 .1293 .0735 .0391 .0195	.2351 .1465 .0852 .0464 .0238	.2589 .1648 .0980 .0546 .0286	.2834 .1841 .1119 .0638 .0342	.3085 .2045 .1269 .0739 .0405	.3341 .2257 .1429 .0850 .0476	.3600 .2478 .1600 .0971 .0555	.3863 .2706 .1780 .1102 .0642	.2940 .1970 .1242 .0739
14 15 16 17 18	.0139 .0073 .0031 .0013 .0005	.0092 .0041 .0017 .0007 .0003	.0114 .0052 .0022 .0009 .0004	.0141 .0066 .0029 .0012 .0005	.0173 .0082 .0037 .0016 .0006	.0209 .0102 .0047 .0021 .0009	.0251 .0125 .0059 .0027 .0011	.0299 .0152 .0074 .0034 .0015	.0353 .0184 .0091 .0043 .0019	.0415 .0220 .0111 .0053 .0024
19 20 21 22 23	0001	.0001	.0001	.0002	.0003	.0003	.0005 .0002 .0001	.0006 .0002 .0001	.0008 .0003 .0001	.0011 .0004 .0002 .0001
m =	9.2	9.4	9.6	9.8	10.0	11.0	12.0	13.0	14.0	15.0
r = 0 $1$ $2$ $3$ $4$	1.0000 .9999 .9990 .9947 .9816	1.0000 .9999 .9991 .9955 .9840	1.0000 .9999 .9993 .9962 .9862	1.0000 .9999 .9994 .9967 .9880	1.0000 1.0000 .9995 .9972 .9897	1.0000 1.0000 .9998 .9988 .9951	1.0000 1.0000 .9999 .9995 .9977	1.0000 1.0000 1.0000 .9998 .9990	1.0000 1.0000 1.0000 .9999 .9995	1.0000 1.0000 1.0000 1.0000 .9998
5 6 7 8 9	.9514 .8959 .8108 .6990 .5704	.9571 .9065 .8273 .7208 .5958	.9622 .9162 .8426 .7416 .6204	.9667 .9250 .8567 .7612 .6442	.9707 .9329 .8699 .7798 .6672	.9849 .9625 .9214 .8568 .7680	.9924 .9797 .9542 .9105 .8450	.9893 .9741 .9460 .9002	.9945 .9858 .9684 .9379	.9972 .9924 .9820 .9626
10 11 12 13 14	.4389 .3180 .2168 .1393 .0844	.4651 .3424 .2374 .1552 .0958	.4911 .3671 .2588 .1721 .1081	.5168 .3920 .2807 .1899 .1214	.5421 .4170 .3032 .2084 .1355	.6595 .5401 .4207 .3113 .2187		.7483 .6468 .5369 .4270	.8243 .7400 .6415 .5356	.8815 .8152 .7324 .6368
15 16 17 18 19	.0483 .0262 .0135 .0066	.0309 .0162 .0081	.0194	.0735 .0421 .0230 .0119 .0059	.0835 .0487 .0270 .0143 .0072	.1460 .0926 .0559 .0322 .0177	.1556 .1013 .0630 .0374	.2364 .1645 .1095 .0698	.3306 .2441 .1728 .1174	.431 .335 .251 .180
20 21 22 23	.0014 .0006 .0002 .0001	.0017	.0010	.0028 .0012 .0005 .0002 .0001	.0003	.0093 .0047 .0023 .0010	7 .0116 3 .0061 0 .0030	.0250 .0141 .0076	.0479 .0288 .0167 .0093	.083 .053 .032 .019
24 25 26 27 28						.000		3 .0010 1 .0005	.0026	5 .000 3 .000 5 .00
29 30 31				,	,				.000.	

Table 2 Cumulative Poisson Probabilities – continued

m =	16.0	17.0	18.0	19.0	20.0	21.0	22.0	23.0	24.0	25.0
r = 0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
1	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
4	.9999	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
5	.9996	.9998	.9999	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
6	.9986	.9993	.9997	.9998	.9999	1.0000	1.0000	1.0000	1.0000	1.0000
7	.9960	.9979	.9990	.9995	.9997	.9999	.9999	1.0000	1.0000	1.0000
8	.9900	9946	.9971	.9985	.9992	.9996	.9998	.9999	1.0000	1.0000
9	.9780	.9874	.9929	.9961	.9979	.9989	.9994	.9997	.9998	.9999
10	.9567	.9739	.9846	.9911	.9950	.9972	.9985	.9992	.9996	.9998
11	.9226	.9509	.9696	.9817	.9892	.9937	.9965	.9980	.9989	.9994
12	.8730	.9153	.9451	.9653	.9786	.9871	.9924	.9956	.9975	.9986
13	.8069	.8650	.9083	.9394	.9610	.9755	.9849	.9909	.9946	.9969
14	.7255	.7991	.8574	.9016	.9339	.9566	.9722	.9826	.9893	.9935
15	.6325	.7192	.7919	.8503	.8951	.9284	.9523	.9689	.9802	.9876
16	.5333	.6285	.7133	.7852	.8435	.8889	.9231	.9480	.9656	.9777
17	.4340	.5323	.6249	.7080	.7789	.8371	.8830	.9179	.9437	.9623
18	.3407	.4360	.5314	.6216	.7030	.7730	.8310	.8772	.9129	.9395
19	.2577	.3450	.4378	.5305	.6186	.6983	.7675	.8252	.8717	.9080
20	.1878	.2637	.3491	.4394	.5297	.6157	.6940	.7623	.8197	.8664
21	.1318	.1945	.2693	.3528	.4409	.5290	.6131	.6899	.7574	.8145
22	.0892	.1385	.2009	.2745	.3563	.4423	.5284	.6106	.6861	.7527
23	.0582	.0953	.1449	.2069	.2794	.3595	.4436	.5277	.6083	.6825
24	.0367	.0633	.1011	.1510	.2125	.2840	.3626	.4449	.5272	.6061
25	.0223	.0406	.0683	.1067	.1568	.2178	.2883	.3654	.4460	.5266
26	.0131	.0252	.0446	.0731	.1122	.1623	.2229	.2923	.3681	.4471
27	.0075	.0152	.0282	.0486	.0779	.1174	.1676	.2277	.2962	.3706
28	.0041	.0088	.0173	.0313	.0525	.0825	.1225	.1726	.2323	.2998
29	.0022	.0050	.0103	.0195	.0343	.0564	.0871	.1274	.1775	.2366
30	.0011	.0027	.0059	.0118	.0218	.0374	.0602	.0915	.1321	.1821
31	.0006	.0014	.0033	.0070	.0135	.0242	.0405	.0640	.0958	.1367
32	.0003	.0007	.0018	.0040	.0081	.0152	.0265	.0436	.0678	.1001
33	.0001	.0004	.0010	.0022	.0047	.0093	.0169	.0289	.0467	.0715
34	.0001	.0002	.0005	.0012	.0027	.0055	.0105	.0187	.0314	.0498
35		.0001	.0002	.0006	.0015	.0032	.0064	.0118	.0206	.0338
36			.0001	.0003	.0008	.0018	.0038	.0073	.0132	.0225
37			.0001	.0002	.0004	.0010	.0022	.0044	.0082	.0146
38				.0001	.0002	.0005	.0012	.0026	.0050	.0092
39					.0001	.0003	.0007	.0015	.0030	.0057
40					.0001	.0001	.0004	.0008	.0017	.0034
41						.0001	.0002	.0004	.0010	.0020
42							.0001	.0002	.0005	.0012
43								.0001	.0003	.0007
44								.0001	.0002	.0004
45									.0001	.0002
46										.0001

Table 2 Cumulative Poisson Probabilities – continued

m =	==	26.0	27.0	28.0	29.0	30.0	32.0	34.0	36.0	38.0	40.0
r =	- 0	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
	10	.9999	.9999	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
	11	.9997	.9998	.9999	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
	12	.9992	.9996	.9998	.9999	.9999	1.0000	1.0000	1.0000	1.0000	1.0000
	13	.9982	.9990	.9994	.9997	.9998	1.0000	1.0000	1.0000	1.0000	1.0000
	14	.9962	.9978	.9987	.9993	.9996	.9999	1.0000	1.0000	1.0000	1.0000
	15	.9924	.9954	.9973	.9984	.9991	.9997	.9999	1.0000	1.0000	1.0000
	16	.9858	.9912	.9946	.9967	.9981	.9993	.9998	.9999	1.0000	1.0000
	17	.9752	.9840	.9899	.9937	.9961	.9986	.9995	.9998	1.0000	1.0000
	18	.9580	.9726	.9821	.9885	.9927	.9972	.9990	.9997	.9999	1.0000
	19	.9354	.9555	.9700	.9801	.9871	.9948	.9980	.9993	.9998	.9999
	20	.9032	.9313	.9522	.9674	.9781	.9907	.9963	.9986	.9995	.9998
			.8985	.9273	.9489	.9647	.9841	.9932	.9973	.9990	.9996
	21	.8613	.8564	.8940	.9233	.9456	.9740	.9884	.9951	.9981	.9993
	22	.8095		.8517	.8896	.9194	.9594	.9809	.9915	.9965	.9986
	23 24	.7483 .6791	.8048 .7441	.8002	.8471	.8854	.9390	.9698	.9859	.9938	.9974
				.7401	.7958	.8428	.9119	.9540	.9776	.9897	.995
	25	.6041	.6758		.7363	.7916	.8772	.9326	.9655	.9834	.9924
	26	.5261	.6021	.6728 .	.6699	.7327	.8344	.9047	.9487	.9741	.987
	27	.4481	.5256	.6003	.5986	.6671	.7838	.8694	.9264	.9611	.980
	28	.3730 .3033 —	.4491 3753	.5251 .4500	.5247	.5969	.7259	.8267	.8977	.9435	.970
	29				.4508	.5243	.6620	.7765	.8621	.9204	.956
	30	.2407	.3065	.3774		.4516	.5939	.7196	.8194	.8911	.938
	31	.1866	.2447	.3097	.3794	.3814	.5235	.6573	.7697	.8552	.914
	32	.1411	.1908	.2485	.3126			.5911	.7139	.8125	.884
	33 34	.1/042 .0751	.1454 .1082	.1949 .1495	.2521 .1989	.3155 .2556	.4532 .3850	.5228	.6530	.7635	.848
		7.			.1535	.2027	.3208	.4546	.5885	.7086	.806
	35	0528	.0787	.1121 .0822	.1333	.1574	.2621	.3883	.5222	.6490	.757
	36	.0363	.0559		.0856	.1196	.2099	.3256	.4558	.5862	.703
	37	.0244	.0388	.0589		.0890	.1648	.2681	.3913	.5216	.645
	38 39	.0160	.0263	.0413 .0 <u>2</u> 83	.0619 .0438	.0648	.1268	.2166	.3301	.4570	584
				-0190	.0303	.0463	.0956	.1717	.2737	.3941	.521
	.40	.0064	.0113	0190	.0205	.0323	.0707	.1336	.2229	.3343	.458
	41	.0039	.0072	£.0125		.0323	.0512	1019	.1783	.2789	.39€
		.0024	.0045	.0080			.0364	.0763	.1401	.2288	.338
	43	.0014	.0027 .0016	<_0050 √0031	.0089 .0056	.0148 .0097	.0253	.0561	.1081	.1845	.283
	44	.0008		Ý.		.0063	.0173	.0404	.0819	.1462	.234
	45	.0004	.0009	.0019	.0035		.0116	.0286	.0609	.1139	.190
	46	.0002	.0005	.0011	.0022	.0040	.0076	.0199	.0445	.0872	.15
	47	.0001	.0003	.0006	.0013	.0025	.0070	.0136	.0320	.0657	.11
	48	.0001	.0002 .0001	.0004 .0002	.0008	.0015	.0049	.0091	.0225	.0486	.09
	49		.0001				.0019	.0060	.0156	.0353	.07
	50			.0001	.0002	.0005	.0013	.0039	.0106	.0253	.05
	51			.0001	.0001	.0003		.0033	.0071	.0178	.03
	52				.0001	.0002	.0007	.0024	.0047	.0123	.02
	53					.0001 .0001	.0004	.0013	.0030	.0084	.02
	54					.0001		.0006	.0019	.0056	.01
	55						.0001	.0003	.0012	.0037	.00
	56	*					.0001		.0012	.0024	.00
	57							.0002		.0024	00.
	58							.0001	.0005		.00
	59				4			.0001	.0003	.0010	
٠.	60								.0002	.0006	.00.
									.0001	.0004	.00
	61								.0001	.0002	.00
	62									.0001	.00
	63 64				•					.0001	.00
											.00.
	65 66										.00
	46										.00

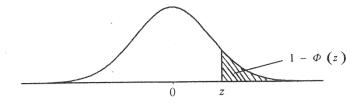
For values of m greater than 30, use the table of areas under the Normal curve (Table 3) to obtain approximate Poisson probabilities, putting  $\mu=m$  and  $\sigma=\sqrt{m}$ .

### Table 3 Areas in Upper Tail of the Normal Distribution

The function tabulated is  $1 - \Phi(z)$  where  $\Phi(z)$  is the cumulative distribution function of a standardised Normal variable, z.

Thus  $1 - \Phi(z) = \frac{1}{\sqrt{2\pi}} \int_{z}^{\infty} e^{-z^2/2}$  is the probability that a standardised Normal variate selected at random will be greater than a

value of  $z \left( = \frac{x - \mu}{\sigma} \right)$ 



			*						-	
$\frac{x-\mu}{\sigma}$	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0 0.1 0.2 0.3 0.4	.5000 .4602 .4207 .3821	.4960 .4562 .4168 .3783 .3409	.4920 .4522 .4129 .3745 .3372	.4880 .4483 .4090 .3707 .3336	.4840 .4443 .4052 .3669 .3300	.4801 .4404 .4013 .3632-	.4761 .4364 .3974 .3594 .3228	.4721 .4325 .3936 .3557 .3192	.4681 .4286 .3897 .3520 .3156	.4641 .4247 .3859 .3483 .3121
0.5 0.6 0.7 0.8 0.9	.3085 .2743 .2420 .2119 .1841	.3050 .2709 .2389 .2090 .1814	.3015 .2676 .2358 .2061 .1788	.2981 .2643 .2327 .2033 .1762	.2946 .2611 .2296 .2005 .1736	.2912 .2578 .2266 .1977 .1711	.2877 .2546 .2236 .1949 .1685	.2843 .2514 .2206 .1922 .1660	.2810 .2483 .2177 .1894 .1635	.2776 .2451 .2148 .1867 .1611
1.0 1.1 1.2 1.3 1.4	.1587 .1357 .1151 .0968 .0808	.1562 .1335 .1131 .0951 .0793	.1539 .1314 .1112 .0934 .0778	1515 .1292 .1093 .0918 .0764	.1492 .1271 .1075 .0901 .0749	.1469 .1251 .1056 .0885 .0735	.1446 .1230 .1038 .0869 .0721	.1423 .1210 .1020 .0853 .0708	.1401 .1190 .1003 .0838 .0694	.1379 .1170 .0985 .0823 .0681
1.5 1.6 1.7 1.8	.0668 .0548 .0446 .0359 .0287	.0655 .0537 .0436 .0351 .0281	.0643 .0526 .0427 .0344 .0274	.0630 .0516 .0418 .0336 .0268	.0618 .0505 .0409 .0329 .0262	.0606 .0495 .0401 .0322 .0256	.0594 .0485 .0392 .0314 .0250	.0582 .0475 .0384 .0307 .0244	.0571 .0465 .0375 .0301 .0239	.0559 .0455 .0367 .0294 .0233
2.0 2.1 2.2 2.3 2.4	.02275 .01786 .01390 .01072 .00820	.02222 .01743 .01355 .01044 .00798	.02169 .01700 .01321 .01017 .00776	.02118 .01659 .01287 .00990 .00755	.02068 .01618 .01255 .00964 .00734	.02018 .01578 .01222 .00939 .00714	.01970 .01539 .01191 .00914 .00695	.01923 .01500 .01160 .00889 .00676	.01876 .01463 .01130 .00866 .00657	.01831 .01426 .01101 .00842 .00639
2.5 2.6 2.7 2.8 2.9	.00621 .00466 .00347 .00256 .00187	.00604 .00453 .00336 .00248 .00181	.00587 .00440 .00326 .00240 .00175	.00570 .00427 .00317 .00233 .00169	.00554 .00415 .00307 .00226 .00164	.00539 .00402 .00298 .00219 .00159	.00523 .00391 .00289 .00212 .00154	.00508 .00379 .00280 .00205 .00149	.00494 .00368 .00272 .00199 .00144	.00480 .00357 .00264 .00193 .00139
3.0 3.1 3.2 3.3 3.4	.00135 .00097 .00069 .00048 .00034	.00131 .00094 .00066 .00047 .00032	.00126 .00090 .00064 .00045 .00031	.00122 .00087 .00062 .00043 .00030	.00118 .00084 .00060 .00042 .00029	.00114 .00082 .00058 .00040 .00028	.00111 .00079 .00056 .00039 .00027	.00107 .00076 .00054 .00038 .00026	.00104 .00074 .00052 .00036 .00025	.00100 .00071 .00050 .00035 .00024
3.5 3.6 3.7 3.8 3.9	.00023 .00016 .000108 .000072 .000048	.00022 .00015 .000104 .000069 .000046	.00022 .00015 .000100 .000067 .000044	.00021 .00014 .000096 .000064 .000042	.00020 .00014 .000092 .000062 .000041	.00019 .00013 .000088 .000059 .000039	.00019 .00013 .000085 .000057	.00018 .00012 .000082 .000054 .000036	.00017 .00012 .000078 .000052 .000034	.00017 .00011 .000075 .000050 .000033
4.0	.000032									

#### Table 7 Percentage Points of the t Distribution

The table gives the value of  $t_{\alpha \nu}$  – the  $100\alpha$  percentage point of the t distribution for  $\nu$  degrees of freedom.

The values of t are obtained by solution of the equation:

$$\alpha = \Gamma[\frac{1}{2}(\nu+1)][\Gamma(\frac{1}{2}\nu)]^{-1} (\nu\pi)^{-1/2} \int_{t}^{\infty} (1+x^{2}/\nu)^{-(\nu+1)/2} dx$$

Note: The tabulation is for one tail only, that is, for positive values of t.

For |t| the column headings for  $\alpha$  should be doubled.

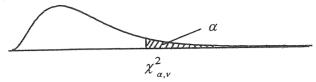
	a Military
Ó	$t_{\alpha,\nu}$

						0	$l_{\alpha,\nu}$
$\alpha =$	0.10	0.05	0.025	0.01	0.005	0.001	0.0005
v = 1	3.078	6.314	12.706	31.821	63,657	318.31	636.62
2	1.886	2.920	4.303	6.965	9.925	22.326	31.598
3	1.638	2.353	3.182	4.541	5.841	10.213	12.924
. 4	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	1.321	1.717	2.074	2.508	2.819	3.505	3.792
23	1.319	1.714	2.069	2.500	2.807	3.485	3.767
24	1.318	1.711	2.064	2.492	2.797	3.467	3.745
25	1.316	1.708	2.060	2.485	2.787	3.450	3.725
26	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	1.310	1.697	2.042	2.457	2.750	3.385	3.646
40	1.303	1.684	2.021	2.423	2.704	3.307	3.551
60	1.296	1.671	2.000	2.390	2.660	3.232	3.460
120	1.289	1.658	1.980	2.358	2.617	3.160	3.373
$\infty$	1.282	1.645	1.960	2.326	2.576	3.090	3.291

This table is taken from Table III of Fisher & Yates: Statistical Tables for Biological, Agricultural and Medical Research, reprinted by permission of Addison Wesley Longman Ltd. Also from Table 12 of Biometrika Tables for Statisticians, Volume 1, by permission of Oxford University Press and the Biometrika Trustees.

# Table 8 Percentage Points of the $\chi^2$ Distribution

Table of  $\chi^2_{\alpha\nu}$  – the  $100\alpha$  percentage point of the  $\chi^2$  distribution for  $\nu$  degrees of freedom.



$\alpha =$	.995	.99	.98	.975	.95	.90	.80	.75	.70	.50
			$.0^{3}628$	$.0^{3}982$	.00393	.0158	.0642	.102	.148	.455
y=1	$.0^{4}393$	$.0^{3}157$		.0506	.103	.211	.446	.575	.713	1.386
2	.0100	.0201	.0404	.216	.352	.584	1.005	1.213	1.424	2.366
3	.0717	.115	.185	.484	.711	1.064	1.649	1.923	2.195	3.357
4	.207	.297	.429	.831	1.145	1.610	2.343	2.675	3.000	4.351
5	.412	.554	.752					3.455	3.828	5.348
6	.676	.872	1.134	1.237	1.635	2.204	3.070		4.671	6.346
7	.989	1.239	1.564	1.690	2.167	2.833	3.822	4.255	5.527	7.344
8	1.344	1.646	2.032	2.180	2.733	3.490	4.594	5.071	6.393	8.343
9	1.735	2.088	2.532	2.700	3.325	4.168	5.380	5.899	7.267	9.342
10	2.156	2.558	3.059	3.247	3.940	4.865	6.179	6.737	1.207	
			3.609	3.816	4.575	5.578	6.989	7.584	8.148	10.341
11	2.603	3.053	4.178	4.404	5.226	6.304	7.807	8.438	9.034	11.340
12	3.074	3.571	4.1765	5.009	5.892	7.042	8.634	9.299	9.926	12.340
13	3.565	4.107	5.368	5.629	6.571	7.790	9.467	10.165	10.821	13.339
14	4.075	4.660	5.985	6.262	7.261	8.547	10.307	11.036	11.721	14.33
15	4.601	5.229	3.963				11 150	11.912	12.624	15.33
16	5.142	5.812	6.614	6.908	7.962	9.312	11.152		13.531	16.33
17	5.697	6.408	7.255	7.564	8.672	10.085	12.002	12.792	14.440	17.33
18	6.265	7.015	7.906	8.231	9.390	10.865	12.857	13.675	15.352	18.33
19	6.844	7.633	8.567	8.907	10.117	11.651	13.716	14.562	16.266	19.33
20	7.434	8.260	9.237	9.591	10.851	12.443	14.578	15.452		
			0.016	10.283	11.591	13.240	15.445	16.344	17.182	20.33
21	8.034	8.897	9.915	10.283	12.338	14.041	16.314	17.240	18.101	21.33
22	8.643	9.542	10.600	11.688	13.091	14.848	17.187	18.137	19.021	22.33
23	9.260	10.196	11.293	12.401	13.848	15.659	18.062	19.037	19.943	23.33
24	9.886	10.856	11.992	13.120	14.611	16.473	18.940	19.939	20.867	24.33
25	10.520	11.524	12.697				10.000	20.843	21.792	25.33
26	11.160	12.198	13.409	13.844	15.379	17.292	19.820	20.843	22.719	26.33
27	11.808	12.879	14.125	14.573	16.151	18.114	20.703	22.657	23.647	27.3
28	12.461	13.565	14.847	15.308	16.928	18.939	21.588	23.567	24.577	28.3
29	13.121	14.256	15.574	16.047	17.708	19.768	22.475	24.478	25.508	29.3
30	13.787	14.953	16.306	16.791	18.493	20.599	23.364	24.470		
		22.164	23.838	24.433	26.509	29.051	32.345	33.660	34.872	39.3
40	20.706	22.164		32.357	34.764	37.689	41.449	42.942	44.313	49.3
50	27.991	29.707	31.664 39.699	40.482	43.188	46.459	50.641	52.294	53.809	59.3
60	35.535	37.485		48.758	51.739	55.329	59.898	61.698	63.346	69.3
70	43.275	45.442	47.893 56.213	57.153	60.391	64.278	69.207	71.145	72.915	79.3
80	51.171	53.539	56.213					80.625	82.511	89.3
90	59.196	61.754	64.634	65.646	69.126	73.291	78.558	90.133	92.129	
100	67.327	70.065	73.142	74.222	77.929	82.358	87.945	90.133	74.147	<i>ال</i>

For values of v > 30, approximate values of  $\chi^2$  may be obtained from the expression  $v \left[1 - \frac{2}{9v} \pm \frac{x}{\sigma} \sqrt{\frac{2}{9v}}\right]^3$  where  $\frac{x}{\sigma}$  is the

normal deviate cutting off the corresponding tails of a normal distribution. If  $\frac{x}{\sigma}$  is taken at the 0.02 level, so that 0.01 of the normal distribution is in each tail, the expression yields  $\chi^2$  at the 0.99 and 0.01 points.

For very large values of  $\nu$ , it is sufficiently accurate to compute  $\sqrt{2\chi^2}$ , the distribution of which is approximately normal around a mean of  $\sqrt{2\nu-1}$  and with a standard deviation of 1.

Table taken from Table IV of Fisher and Yates: Statistical Tables for Biological, Agricultural and Medical Research, reprinted by permission of Addison Wesley Longman Ltd, and from Table 8 of Biometrika Tables for Statisticians, Vol. 1, by permission of Oxford University Press and the Biometrika Trustees.

Table 8 Percentage Points of the  $\chi^2$  Distribution – continued

The second secon			10	.05	.025	.02	.01	.005	.001	$= \alpha$
.30	.25	.20	.10	.03	and the second		THE PARTY OF THE P	7.879	10.827	v=1
1:074	1.323	1.642	2.706	3.841	5.024	5.412	6.635		13.815	2
1.074	2.773	3.219	4.605	5.991	7.378	7.824	9.210	10.597	16.268	3
2.408		4.642	6.251	7.815	9.348	9.837	11.345	12.838	18.465	4
3.665	4.108	5.989	7.779	9.488	11.143	11.668	13.277	14.860	20.517	5
4.878	5.385	7.289	9.236	11.070	12.832	13.388	15.086	16.750	20.517	
6.064	6.626		-	10 500	14.449	15.033	16.812	18.548	22.457	6
7.231	7.841	8.558	10.645	12.592	16.013	16.622	18.475	20.278	24.322	7
8.383	9.037	9.803	12.017	14.067		18.168	20.090	21.955	26.125	8
9.524	10.219	11.030	13.362	15.507	17.535	19.679	21.666	23.589	27.877	9
10.656	11.389	12.242	14.684	16.919	19.023	21.161	23.209	25.188	29.588	10
11.781	12.549	13.442	15.987	18.307	20.483	21.101			01.064	11
		14 621	17.275	19.675	21.920	22.618	24.725	26.757	31.264	12
12.899	13.701	14.631	18.549	21.026	23.337	24.054	26.217	28.300	32.909	13
14.011	14.845	15.812	19.812	22.362	24.736	25.472	27.688	29.819	34.528	
15.119	. 15.984	16.985	21.064	23.685	26.119	26.873	29.141	31.319	36.123	14
16.222	17.117	18.151	22.307	24.996	27.488	28.259	30.578	32.801	37.697	15
17.322	18.245	19.311	22.307			20.622	32.000	34.267	39.252	16
18.418	19.369	20.465	23.542	26.296	28.845	29.633		35.718	40.790	17
19.511	20.489	21.615	24.769	27.587	30.191	30.995	33.409	37.156	42.312	18
20.601	21.605	22.760	25.989	28.869	31.526	32.346	34.805	38.582	43.820	19
	22.718	23.900	27.204	30.144	32.852	33.687	36.191	39.997	45.315	20
21.689	23.828	25.038	28.412	31.410	34.170	35.020	37.566	39.931		
22.775	23.626			22 (71)	35.479	36.343	38.932	41.401	46.797	21
23.858	24.935	26.171	29.615	32.671	36.781	37.659	40.289	42.796	48.268	22
24.939	26.039	27.301	30.813	33.924	38.076	38.968	41.638	44.181	49.728	23
26.018	27.141	28.429	32.007	35.172	39.364	40.270	42.980	45.558	51.179	24
27.096	28.241	29.553	33.196	36.415	40.646	41.566	44.314	46.928	52.620	2:
28.172	29.339	30.675	34.382	37.652	40.040			40.000	54.052	2
	20.424	31.795	35.563	38.885	41.923	42.856	45.642	48.290	55.476	2
29.246	30.434	32.912	36.741	40.113	43.194	44.140	46.963	49.645		2
30.319	31.528	34.027	37.916	41.337	44.461	45.419	48.278	50.993	56.893	2
31.391	32.620		39.087	42.557	45.722	46.693	49.588	52.336	58.302	3
32.461	33.711	35.139	40.256	43.773	46.979	47.962	50.892	53.672	59.703	ر
33.530	34.800	36.250				(0.426	63.691	66.766	73.402	4
44.165	45.616	47.269	51.805	55.759	59.342	60.436	76.154	79.490	86.661	4
54.723	56.334	58.164	63.167	67.505	71.420	72.613	88.379	91.952	99.607	$\epsilon$
65.227	66.981	68.972	74.397	79.082	83.298	84.580	100.425	104.215	112.317	7
75.689	77.577	79.715	85.527	90.531	95.023	96.388	112.329	116.321	124.839	8
86.120	88.130	90.405	96.578	101.880	106.629	108.069	112.329			
			107 565	113.145	118.136	119.648	124.116	128.299	137.208	
96.524	98.650	101.054	107.565	124.342	129.561	131.142	135.807	140.170	149.449	10
106.906	109.141	111.667	118.498	124.342	127.501					

# Table 9 Percentage Points of the F Distribution

The table gives the values of  $F_{\alpha;\nu_1,\nu_2}$  the  $100\alpha$  percentage point of the F distribution having  $\nu_1$  degrees of freedom in the numerator and  $\nu_2$  degrees of freedom in the denominator. For each pair of values of  $\nu_1$  and  $\nu_2$ ,  $F_{\alpha;\nu_1,\nu_2}$  is tabulated for  $\alpha = 0.05$ ,

0.025, 0.01, 0.001, the 0.025 values being bracketed.

The lower percentage points of the distribution may be obtained from the relation:

-α:V1 V0	$=$ <sup>1</sup> $/F_{\alpha;\nu_2}$	$v_1$									IRIT	
	$F_{.95,12,8} = \frac{1}{2}$		$/_{2.85} = 0.3$	<u>51</u>					And the second	F	$\alpha; \nu_1, \nu_2$	
$ u_{ m l}$	1	2	3	4	5	6	7	8	10	12	24	. ∞
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	241.9	243.9	249.0	254.3 (1018)
1	(648) 4052 4053*	(800)	(864) 5403	(900) 5625	(922) 5764 5764*	(937) 5859 5859*	(948) 5928 5929*	(957) 5981 5981*	(969) 6056 6056*	(977) 6106 6107*	(997) 6235 6235*	6366 6366*
2	18.5	19.0	19.2	19.2	19.3	19.3	19.4	19.4	19.4	19.4 (39.4)	19.5 (39.5)	19.5 (39.5)
2	(38.5)	(39.0)	(39.2)	(39.2)	(39.3)	(39.3)	(39.4)	(39.4) 99.4	(39.4) 99.4	99.4	99.5	99.5
	98.5	99.0	99.2 999.2	99.2· 999.2	99.3 999.3	99.3 999.3	99.4 999.4	99.4	999.4	999.4	999.5	999.5
	998.5	999.0		9.12	9.01	8.94	8.89	8.85	8.79	8.74	8.64	8.53
3	10.13	9.55 (16.0)	9.28 (15.4)	(15.1)	(14.9)	(14.7)	(14.6)	(14.5)	(14.4)	(14.3)	(14.1)	(13.9)
	(17.4) 34.1	30.8	29.5	28.7	28.2	27.9	27.7	27.5	27.2	27.1	26.6	26.1
	167.0	148.5	141.1	137.1	134.6	132.8	131.5	130.6	129.2	128.3	125.9	123.5
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	5.96	5.91	5.77	5.63 (8.26)
4	(12.22)	(10.65)	(9.98)	(9.60)	(9.36)	(9.20)	(9.07)	(8.98)	(8.84)	(8.75)	(8.51) 13.9	13.5
	21.2	18.0	16.7	16.0	15.5	15.2	15.0	14.8	14.5	14.4 47.41	45.77	44.05
	74.14	61.25	56.18	53.44	51.71	50.53	49.66	49.00	48.05			4.36
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.74	4.68	4.53 (6.28)	(6.02)
3	(10.01)	(8.43)	(7.76)	(7.39)	(7.15)	(6.98)	(6.85)	(6.76)	(6.62)	(6.52) 9.89	9.47	9.02
	16.26	13.27	12.06	11.39	10.97	10.67	10.46	10.29 27.65	10.05 26.92	26.42	25.14	23.79
	47.18	37.12	33.20	31.09	29.75	28.83	28.16				3.84	3.67
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.06	4.00 (5.37)	(5.12)	(4.85)
, 0	(8.81)	(7.26)	(6.60)	(6.23)	(5.99)	(5.82)	(5.70)	(5.60) 8.10	(5.46) 7.87	7.72	7.31	6.88
	13.74	10.92	9.78	9.15	8.75	8.47 20.03	8.26 19.46	19.03	18.41	17.99	16.90	15.75
	35.51	27.00	23.70	21.92	20.80				3.64	3.57	3.41	3.23
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73 (4.90)	(4.76)	(4.67)	(4.42)	(4.14)
	(8.07	(6.54)	(5.89)	(5.52)	(5.29)	(5.12)	(4.99) 6.99	6.84	6.62	6.47	6.07	5.65
	12.25	9.55	8.45	7.85	7.46 16.21	7.19 15.52	15.02	14.63	14.08	13.71	12.73	11.70
	29.25	21.69	18.77	17.20			•		3.35	3.28	3.12	2.93
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50 (4.53)	3.44 (4.43)				
	(7.57)		(5.42)	(5.05)	(4.82) 6.63	(4.65) 6.37	6.18	6.03	5.81	5.67	5.28	4.86
	11.26	8.65 18.49	7.59 15.83	7.01 14.39	13.48	12.86	12.40	12.05	11.54	11.19	10.30	9.34
	25.42					3.37	3.29	3.23	3.14	3.07	2.90	2.71
9	5.12	4.26	3.86	3.63	3.48 (4.48)						(3.61)	
	(7.21)		(5.08) 6.99	(4.72) 6.42	6.06	5.80		5.47	5.26	5.11	4.73	4.31
	10.56 22.86	8.02 16.39	13.90	12.56	11.71	11.13	10.69	10.37	9.87	9.57	8.72	7.8
				3.48	3.33	3.22	3.14	3.07	2.98	2.91	2.74	2.5
10		4.10	3.71									
	(6.94)		(4.83) 6.55	5.99	5.64			, .	4.85			
	10.04 21.04		12.55	11.28	10.48			9.20	8.74	8.44	7.64	
			3.59	3.36			3.01	2.95				
11								(3.66				
	(6.72 9.65	,	6.22	5.67		5.07	4.89	4.74				
	9.63 19.69		11.56				8.66	8.35	7.92			
10					3.11	3.00	2.91					
12	2 4.75 (6.55						3) (3.61					
	9.33	,		,	5.0€	4.82						
	18.64					8.3	8.00	7.73	7.29	7.00	) 0.2.	ر ر

<sup>\*</sup> Entries marked thus must be multiplied by 100

Table 9 Percentage Points of the F Distribution - continued

$\nu_{ m l}$	1	2	3	4	5	6	7	8	10	12	24	∞
						2.02	2.02	277	2.67	2.60	2.42	2.21
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.67		(2.89)	(2.60)
	(6.41)	(4.97)	(4.35)	(4.00)	(3.77)	(3.60)	(3.48)	(3.39)	(3.25)	(3.15)		3.17
	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.10	3.96	3.59	
	17.82	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.80	6.52	5.78	4.97
		3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.60	2.53	2.35	2.13
14	4.60		(4.24)	(3.89)	(3.66)	(3.50)	(3.38)	(3.29)	(3.15)	(3.05)	(2.79)	(2.49)
	(6.30)	(4.86)		5.04	4.70	4.46	4.28	4.14	3.94	3.80	3.43	3.00
	8.86	6.51	5.56	8.62	7.92	7.44	7.08	6.80	6.40	6.13	5.41	4.60
	17.14	11.78	9.73								2.24	2.01
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.49	2.42	(2.63)	(2.32
	(6.12)	(4.69)	(4.08)	(3.73)	(3.50)	(3.34)	(3.22)	(3.12)	(2.99)	(2.89)		
	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.69	3.55	3.18	2.75
	16.12	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.81	5.55	4.85	4.06
				2.02	2.77	2.66	2.58	2.51	2.41	2.34	2.15	1.92
18	4.41	3.55	3.16	2.93		(3.22)	(3.10)	(3.01)	(2.87)	(2.77)	(2.50)	(2.19)
	(5.98)	(4.56)	(3.95)	(3.61)	(3.38)		3.84	3.71	3.51	3.37	3.00	2.57
	8.29	6.01	5.09	4.58	4.25	4.01		5.76	5.39	5.13	4.45	3.67
	15.38	10.39	8.49	7.46	6.81	6.35	6.02					
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.35	2.28	2.08	1.84
20		(4.46)	(3.86)	(3.51)	(3.29)	(3.13)	(3.01)	(2.91)	(2.77)	(2.68)	(2.41)	(2.09)
	(5.87)		4.94	4.43	4.10	3.87	3.70	3.56	3.37	3.23	2.86	2.42
	8.10 14.82	5.85 9.95	8.10	7.10	6.46	6.02	5.69	5.44	5.08	4.82	4.15	3.3
							2.46	2.40	2.30	2.23	2.03	1.7
22	4.30	3.44	3.05	2.82	2.66	2.55		(2.84)	(2.70)	(2.60)	(2.33)	(2.0
	(5.79)	(4.38)	(3.78)	(3.44)	(3.22)	(3.05)	(2.93)		3.26	3.12	2.75	2.3
	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45		4.58	3.92	3.1
	14.38	9.61	7.80	6.81	6.19	5.76	5.44	5.19	4.83			
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.25	2.18	1.98	1.7
24		(4.32)	(3.72	(3.38)	(3.15)	(2.99)	(2.87)	(2.78)	(2.64)	(2.54)	(2.27)	(1.9
	(5.72)		4.72	4.22	3.90	3.67	3.50	3.36	3.17	3.03	2.66	2.2
	7.82	5.61 9.34	7.55	6.59	5.98	5.55	5.23	4.99	4.64	4.39	3.74	2.9
	14.03					0.47	2.39	2.32	2.22	2.15	1.95	1.6
.26	4.23	3.37	2.98	2.74	2.59	2.47		(2.73)	(2.59)	(2.49)	(2.22)	(1.8
	(5.66)	(4.27)	(3.67)	(3.33)	(3.10)	(2.94)	(2.82)		3.09	2.96	2.58	2.1
	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	4.48	4.24	3.59	2.8
	13.74	9.12	7.36	6.41	5.80	5.38	5.07	4.83	4.40	4.24		
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.19	2.12	1.91	1.6
28	(5.61)	(4.22)	(3.63)	(3.29)	(3.06)	(2.90)	(2.78)	(2.69)	(2.55)	(2.45)	(2.17)	(1.8
	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.03	2.90	2.52	2.0
	13.50	8.93	7.19	6.25	5.66	5.24	4.93	4.69	4.35	4.11	3.46	2.6
							2.33	2.27	2.16	2.09	1.89	1.0
30	4.17	3.32	2.92	2.69	2.53	2.42	(2.75)	(2.65)	(2.51)	(2.41)	(2.14)	(1.
	(5.57)	(4.18)	(3.59)	(3.25)	(3.03)	(2.87)		3.17	2.98	2.84	2.47	2.0
	7.56	5.39	4.51	4.02	3.70	3.47	3.30	4.58	4.24	4.00	3.36	2.
	13.29	8.77	7.05	6.12	5.53	5.12	4.82					
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.08	2.00	1.79	1.
40	(5.42)	(4.05)	(3.46)	(3.13)	(2.90)	(2.74)	(2.62)	(2.53)	(2.39)	(2.29)	(2.01)	(1.
	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.80	2.66	2.29	1.
	12.61	8.25	6.59	5.70	5.13	4.73	4.44	4.21	3.87	3.64	3.01	2.
						2.25	2.17	2.10	1.99	1.92	1.70	1.
60	4.00	3.15	2.76	2.53	2.37	2.25	(2.51)	(2.41)	(2.27)	(2.17)	(1.88)	(1.
	(5.29)	(3.93)	(3.34)	(3.01)	(2.79)	(2.63)	2.95	2.82	2.63	2.50	2.12	1.
	7.08	4.98	4.13	3.65	3.34	3.12	2.93 4.09	3.86	3.54	3.32	2.69	1
	11.97	7.77	6.17	5.31	4.76	4.37						
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.91	1.83	1.61	1
120	(5.15)	(3.80)	(3.23)	(2.89)	(2.67)	(2.52)	(2.39)	(2.30)	(2.16)	(2.05)		(1
	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66	2.47	2.34	1.95	1
	11.38	7.32	5.78	4.95	4.42	4.04	3.77	3.55	3.24	3.02	2.40	1
						2.10	2.01	1.94	1.83	1.75	1.52	1
$\infty$	3.84	3.00	2.60	2.37	2.21		(2.29)					(1
	(5.02)	(3.69)	(3.12)	(2.79)	(2.57)	(2.41)	2.64	2.51	2.32	2.18	1.79	ì
	6.63	4.61	3.78	3.32 4.62	3.02 4.10	2.80 3.74	3.47	3.27	2.96	2.74	2.13	1
	10.83	6.91	5.42									

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