Kraft inequality

- Let X be a DMS with alphabet $(x_i = \{1, 2, ..., m\})$. Assume that the length of the assigned binary code word corresponding to x, is n.
- A necessary and sufficient condition for the existence of an instantaneous binary code is

$$K = \sum_{i=1}^{m} 2^{-n_i} \le 1$$

which is known as the **Kraft inequality**.

Note that the Kraft inequality assures us of the existence of an
instantaneously decodable code with code word lengths that satisfy the
inequality. But it does not show us how to obtain these code words, nor
does it say that any code that satisfies the inequality is automatically
uniquely decodable



Kevin O'Brien MA4413 Autumn 2011 1/3