Laplace Transforms: Tutorial Sheet 1

For all of the questions on this worksheet, you may assume t > 0. You may need to state this assumption in a written examination.

1. Using the tables, state the Laplace Transform of the following expressions:

(a)
$$f(t) = t^6$$

(c)
$$f(t) = e^{3t} + e^{-2t}$$

(b)
$$f(t) = e^{2t}$$

(d)
$$f(t) = \sinh(t)$$

2. Using the tables write down the transforms of the following functions

(a)
$$2t^2$$

(c)
$$3\sin(2t)$$

(b)
$$2t + 1$$

(d)
$$3e^{-t}$$

3. Using the tables write down the transforms of the following functions

(a)
$$(t-2)^2$$

(c)
$$e^{2t-2}$$

(b)
$$2t - 2$$

(d)
$$t + \sinh(t)$$

4. Using the tables write down the transforms of the following functions

(a)
$$t^2 - 3t + 4$$

(e)
$$2\cos tt$$

(b)
$$2\cos(t) + 3\sin(2t)$$

(f)
$$e^{-t}(e^{2t} + 2et)^2$$

(c)
$$4e^t - e^{-2t}$$

(g)
$$4 \sin t \cos t$$

(d)
$$(t^2-3)^2$$

(h)
$$1 - 4\sin(t)$$

5. Calculate the Laplace transform of the following functions directly from the definig formula.

(a)
$$2t^2$$

(c)
$$3e^{-t}$$

(b)
$$3\sin(2t)$$

(d)
$$\sinh(3t)$$