

1. Cars enter a car wash at an average rate of 4 per half hour.
  - (a) Compute the probability that the 3 cars arrive in a half hour period.
  - (b) Compute the probability that the 3 cars arrive in a 15 minute period.
2. Consider an  $M/M/1$  system with arrivals  $X_a \sim \text{Poisson}(\lambda_a = 3 / \text{minute})$  and service time  $T_s \sim \text{Exponential}(\lambda_s = 4 / \text{minute})$ . Calculate the following:
  - (a) The expected time spent in the system.
  - (b) The expected time spent in the queue component.
  - (c) The expected number of individuals in the system.
  - (d) The expected number of individuals in the queue component.
  - (e) The utilisation factor.
  - (f) The probability that an individual spends more than 2 minutes in the system.
  - (g) The probability that less than 3 individuals exit the system in a 1 minute period.
3. Assume that potholes arise on a road at a rate of  $\frac{1}{300}$  per metre according to a Poisson distribution. Calculate the following:
  - (a) The probability that there are no potholes in 1km.
  - (b) The probability that there are at least 15 potholes in 6km.
  - (c) The probability that there are between 10 and 12 potholes in 3km.
  - (d) The value of  $x$  such that  $x$  or more potholes in 3km is approximately 10%, i.e.,  $\Pr(X \geq x) \approx 0.1$ .
  - (e) The probability that the next pothole appears within 100 metres.
  - (f) The probability that the next pothole is more than 1km away.
  - (g) The probability that the next pothole is between 300 and 1200 metres from here. **(h)** The average distance between potholes and the corresponding standard deviation.
4. A life insurance salesman sells on the average 3 life insurance policies per week. Use Poisson's law to calculate the probability that in a given week he will sell
  - (a) some policies
  - (b) 2 or more policies but less than 5 policies.
  - (c) Assuming that there are 5 working days per week, what is the probability that in a given day he will sell one policy?