Question 1 (Sample Variant 1)[25 marks]

(a) Probability (6 Marks)

An IT consultant is responsible for three software engineering projects X, Y and Z. He knows that the probability of completing project X in time is 0.99, for project Y this probability is 0.95 and for project Z it is 0.80.

- (i) (1 marks) What assumption do you need to make in order to calculate the probability of completing all three projects in time, from the information given?
- (ii) (3 marks) Calculate the probability of completing all three projects in time.
- (iii) (2 marks) Calculate the probability that only projects X and Y will be completed on time.

(b) Probability (8 Marks)

The following contingency table illustrates the number of 400 students in different departments according to gender.

	Computer Science	Statistics	Equine Science	
Males	140	100	20	
Females	30	80	30	

- (i) (2 marks) What is the probability that a randomly chosen person from the sample is a computer science student?
- (ii) (2 marks) What is the probability that a randomly chosen person from the sample is both female and studying statistics?
- (iii) (2 marks) What is the probability that a randomly chosen person from the sample is male?
- (iv) (2 marks) Given that a student studies statistics, what is the probability that the student is female?

(c) Discrete Random Variables (6 Marks)

The probability distribution of discrete random variable X is tabulated below. There are 6 possible outcome of X, i.e. 1, 2, 3, 4,5 and 6.

x_i	1	2	3	4	5	6
$P(x_i)$	0.16	0.14	k	0.17	0.21	0.19

- i (1 marks) Compute the value for k.
- ii (2 marks) Determine the expected value E(X).
- iii (2 marks) Evaluate $E(X^2)$.
- iv (1 marks) Compute the variance of random variable X.

(d) Descriptive Statistics (5 Marks)

Consider the following data set of seven numbers:

For this sample, compute the following descriptive statistics:

- (i) (1 Mark) The mean,
- (ii) (1 Mark) The median,
- (iii) (2 Marks) The variance,
- (iv) (1 Mark) The standard deviation.