Introductory example

look at the following problem:

Input: a string w consisting of 0s and 1s

Question: Are these requirements fullfilled?

- 1 is not a sub-word
- w is divisible by 3 in binary

Examples: 0101, 1001, 00110, 0101010

We want:

A program that takes w as argument and returns 0 or 1

A possible solution (cryptic C code)

```
int F[] = { 1, 0, 0, 0, 1, 0, 0 };
int delta[][2] = { { 0, 1 }, { 3, 6 }, { 3, 4 }, { 2, 5 }, { 0, 6 }, { 2, 6 }, { 6, 6 } };
int three_not_11(char *w)
{
   int q = 0;
   while( *w ) q = delta[ q ][ *w++ - '0' ];
   return F[q];
}
```

Finite Automaton

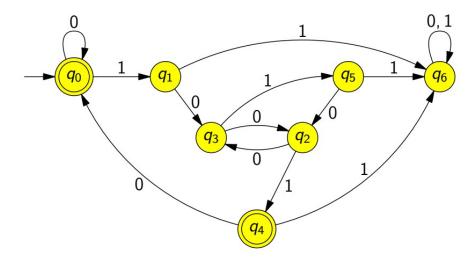


Figure 1: "Finite Automaton"

 ${\bf q}0$ is start ${\bf q}6$ is default false (11 is sub-word) q1-q5 are possible paths ${\bf q}0$ & q4 are true paths