

FoSAP Exercise 1

Group 3

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Introduction

Welcome To this special endeavour, where I write every single thing in \LaTeX How is any of this gonna work?

Simple: With patience and a format definition. Therefore, please let me define the format of this.

THE FORMAT

- Every file will be named similar to the sections in here, so `2.1-stack_exercise.c` is Exercise 2, section 1.
- Every Solution **WILL** be in this pdf along with everything predefined by the exercise.
- Any explanation will be both in this PDF as well as in each file.
- This explanation will be in each PDF, in case someone who doesn't know the format tries to correct the exercises

1 H1

Exercise: Let $v, w \in \Sigma^*$ with $vw = w^Rv$ and $|w| \geq |v|$. Prove $(vw)^R = vw$.
 Because $(vw)^R = vw \Leftrightarrow vw$ is a palindrome, we only have to show that vw is a palindrome when $vw = w^Rv$. Now we have the following cases:

$|v| = |w|$: $v = w^R \wedge w = v$
 $\Rightarrow w = v \wedge w = w^R$
 Therefore w and v must be a palindrome, and thus vw is a palindrome as well

$|v| = 0$: then $vw = w^R = w$ because $v = \epsilon$, therefore vw is a palindrome

$1 \leq |v| < |w|$:

let $v = v_1, \dots, v_n$
 then $w^R = v_1, \dots, v_n, w'_n, \dots, w'_1$
 and $w = w'_1, \dots, w'_n, v_n, \dots, v_1$
 $\Rightarrow vw = v_1, \dots, v_n, w'_1, \dots, w'_n, v_n, \dots, v_1$
 therefore: $w^Rv = v_1, \dots, v_n, w'_n, \dots, w'_1, v_n, \dots, v_1$

Because $vw = w^Rv$, $w'_1, \dots, w'_n = w'_n, \dots, w'_1$ applies and therefore w'_1, \dots, w'_n must be a palindrome. Furthermore, $v_1, \dots, v_n = v_n, \dots, v_1$, making v a palindrome as well. Since w' and v , which can be found on both sides of w' , are both palindromes, vw must be a palindrome as well, Proving the statement $vw = w^Rv$.

2 H2

Solution: $((((AB)^+A)((((CB)^+ + (C(BA)^+)^+)^+ + ((CA^+) + (C(AB)^+)^+)^+)*C))^+$

Explanation:

$((AB)^+A)$: Every option before a C
 $((CB)^+ + (C(BA)^+)^+)^+$: Every transition $C \rightarrow B$
 $((CA^+) + (C(AB)^+)^+)^+$: Every transition $C \rightarrow A$
 C : Makes sure that we always go through before ending

3 H3