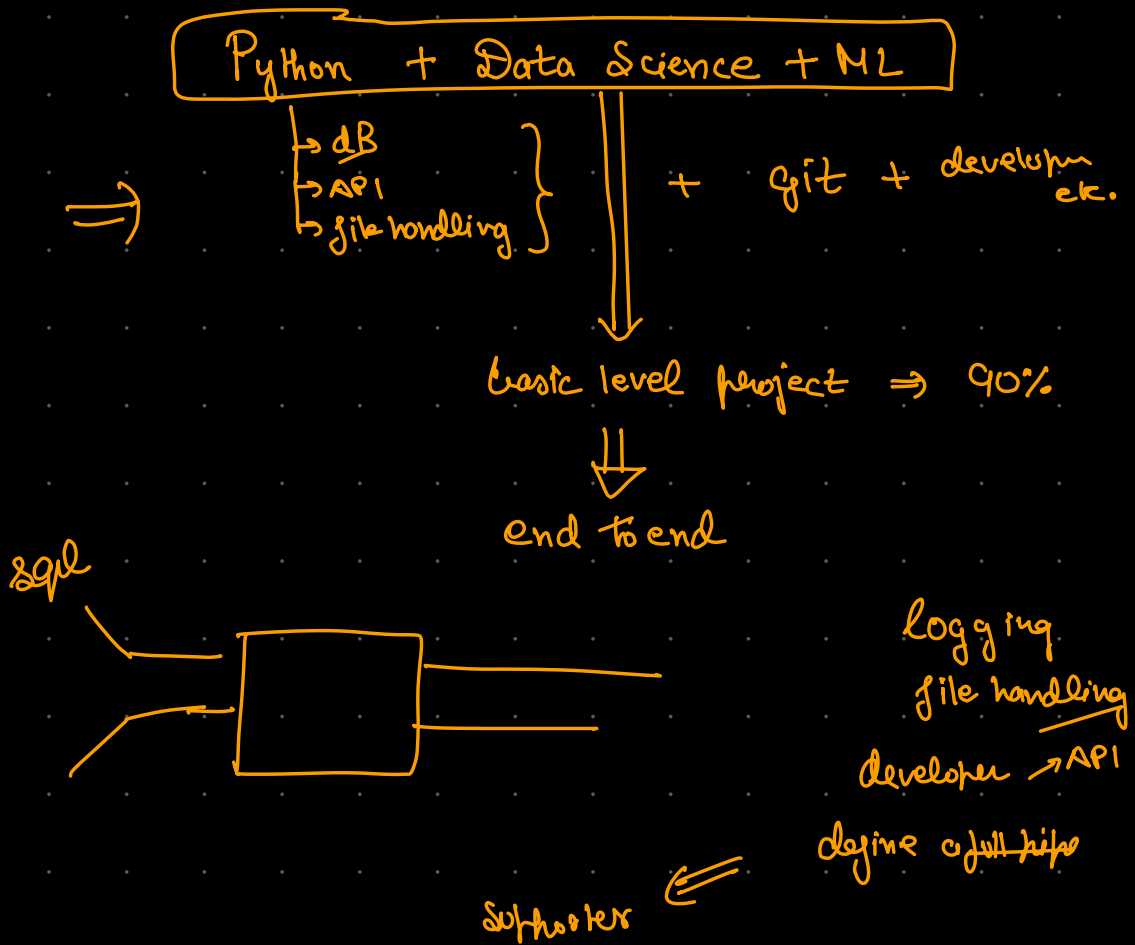
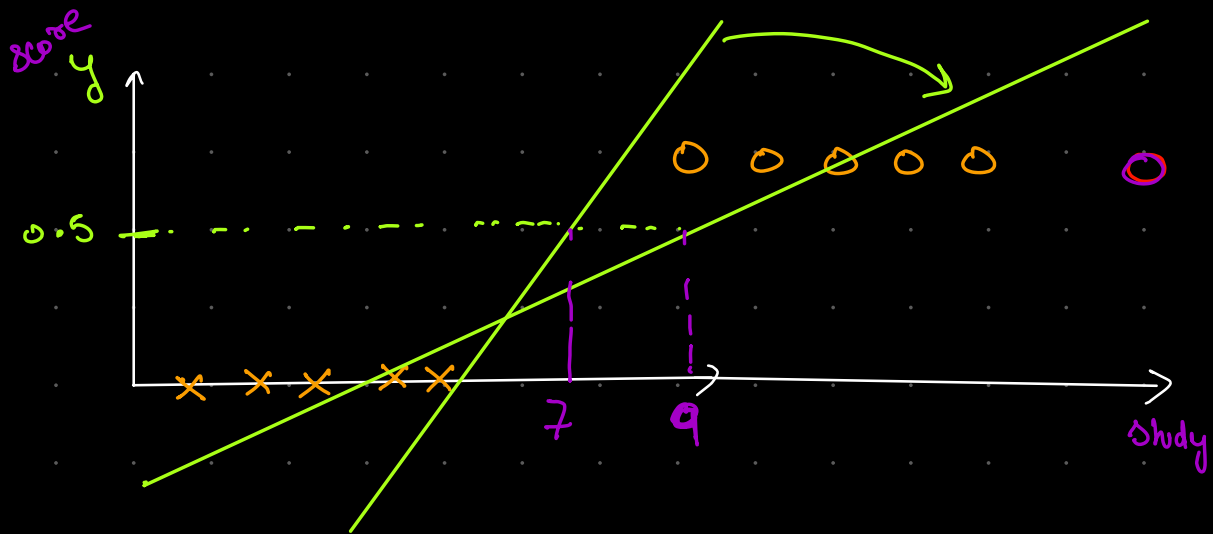


# Machine Learning

## Logistic Regression

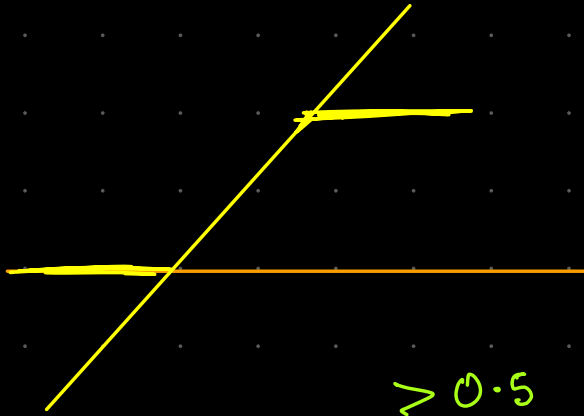


1. LoR
2. Practical + Code logistic + L1 / L2
3. Naive Bayes
4. Tree Based (DT, RF)  $\Rightarrow$
5. SVM / SVD
6. Boosting,
7. Unsupervised learning.



$$f(m,c) = y = mx + c$$

$$f(m, c) = g(mx + c)$$

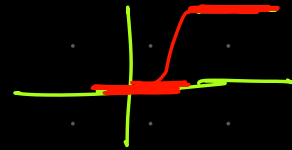


sigmoid/activation

$\Downarrow$

$$\left( \frac{1}{1 + e^{-x}} \right) =$$

$$\begin{aligned} &> 0.5 \rightarrow 1 \\ &< 0.5 \rightarrow 0 \end{aligned}$$



$$f(m, c) = \frac{1}{1 + e^{-mx + c}}$$

We are again going to train on train data

$$\{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\}$$

study	score
5	0
7	1
8	1

Aim  $\Rightarrow$  find value of  $m, c$  such that we can predict/classify  $y$  properly.

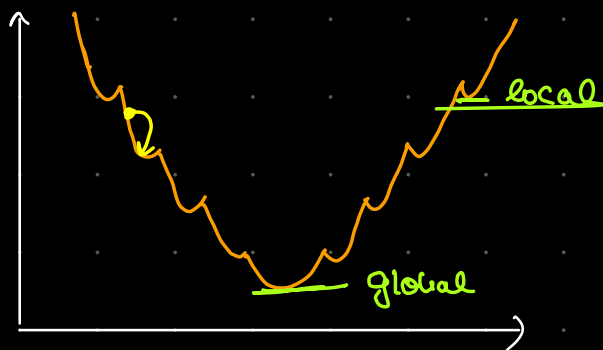
Cost fn

$$\mathcal{E} = \frac{1}{2m} \sum_{i=1}^N (y_i - \hat{y}_i)^2 \rightarrow (mx+c)$$

Now,  $y = \frac{1}{1 + e^{-(mx+c)}}$

say  $c=0$  (for easy explanation)

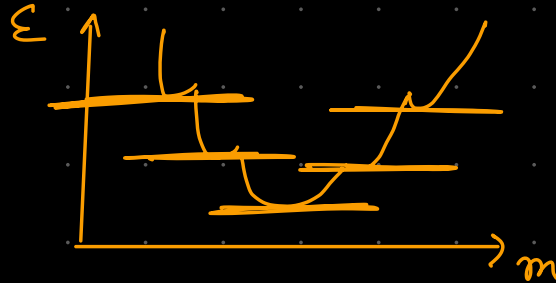
$$y = \frac{1}{1 + e^{-mx}}$$



non-convex

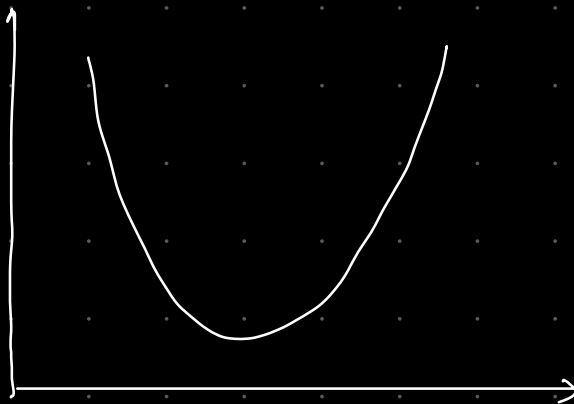
$$\frac{d\mathcal{E}}{dm} = 0$$

$$\underline{E} = \left( 0 - \frac{1}{1+e^{-m5}} \right) + \left( 1 - \frac{1}{1+e^{-7m}} \right)$$



log loss cost fn

$$E(m) = \begin{cases} -\log(\hat{y}) & y=1 \\ -\log(1-\hat{y}) & y=0 \end{cases}$$



Cost  $f^n$  / Error  $f^n$

$$= \underbrace{-y \log \hat{y}}_{\substack{\downarrow \\ 0}} - \underbrace{(1-y) \log (1-\hat{y})}_{\substack{\downarrow \\ 0}}$$

$y=0$   $-\log (1-\hat{y})$

$y=1 \Rightarrow -\log \hat{y} - 0$

$$\text{Cost} / \text{Error} = \mathcal{E}(m, c)$$

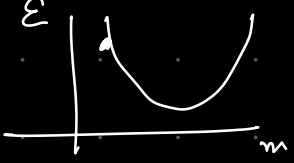
$$= -y \log \hat{y} - (1-y) \log (1-\hat{y})$$

$$\hat{y} = \frac{1}{1 + e^{-(mx+c)}}$$

$y=1$

error =  $-\log \hat{y}$   $\rightarrow \frac{1}{1 + e^{-mx+c}}$

We are gonna apply gradient descent.

$$\left\{ \begin{array}{l} m_{\text{new}} = m_{\text{old}} - \alpha \frac{\partial E}{\partial m} \\ c_{\text{new}} = c_{\text{old}} - \alpha \frac{\partial E}{\partial c} \end{array} \right.$$


$$E(m, c) = -y \log \hat{y} - (1-y) \log(1-\hat{y})$$

$$\hat{y} = \frac{1}{1 + e^{-(mx+c)}}$$

study

result

5

6

7

8

9

0  
0  
1  
1  
0

y

$$\hat{y} = \frac{1}{1 + e^{-mx}}$$

for  $x=5$ ,  $m=2$

$$\hat{y} = \frac{1}{1 + e^{-2 \cdot 5}}$$

$$= 0.99 \rightarrow 1$$

## Confusion matrix

Predicted	pass	fail
Actual		
pass		
fail		

